

# Heavy baryonで探るdiquark相関

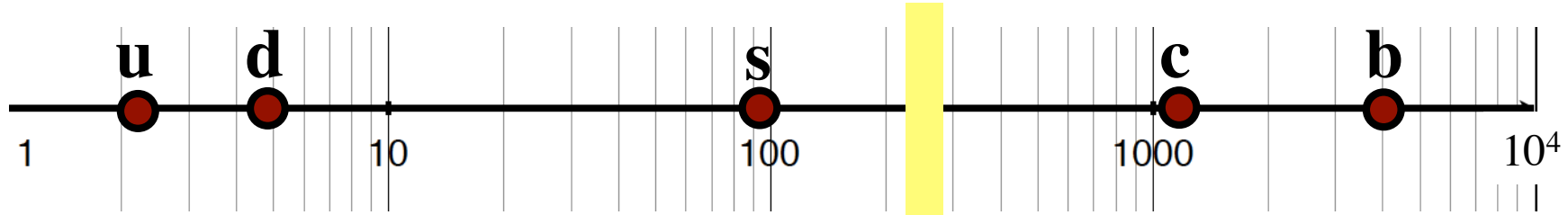
保坂 淳 (阪大RCNP)

- はじめに
- ダイクォーク相関
- バリオン分光

# はじめに

QCD, with *invisible color* and *variety of flavors*

Quarks: Masses in Log [MeV]



Light flavor

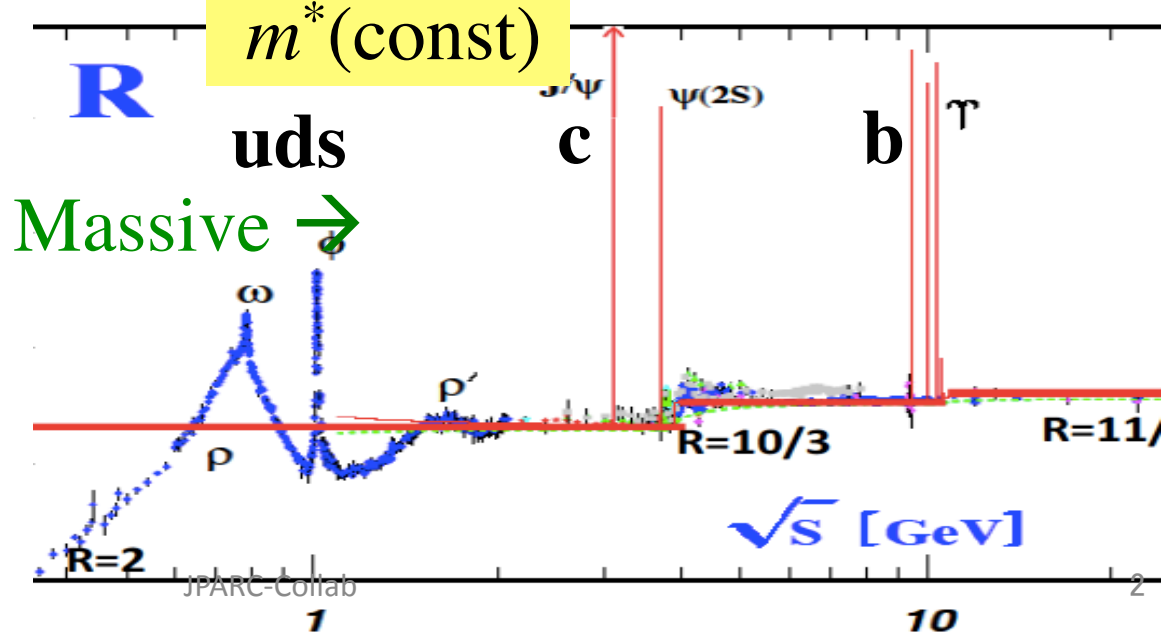
Heavy flavor

$\Lambda_{\text{QCD}}$

$m^*(\text{const})$

← Massless

Massive →



# Heavy flavors

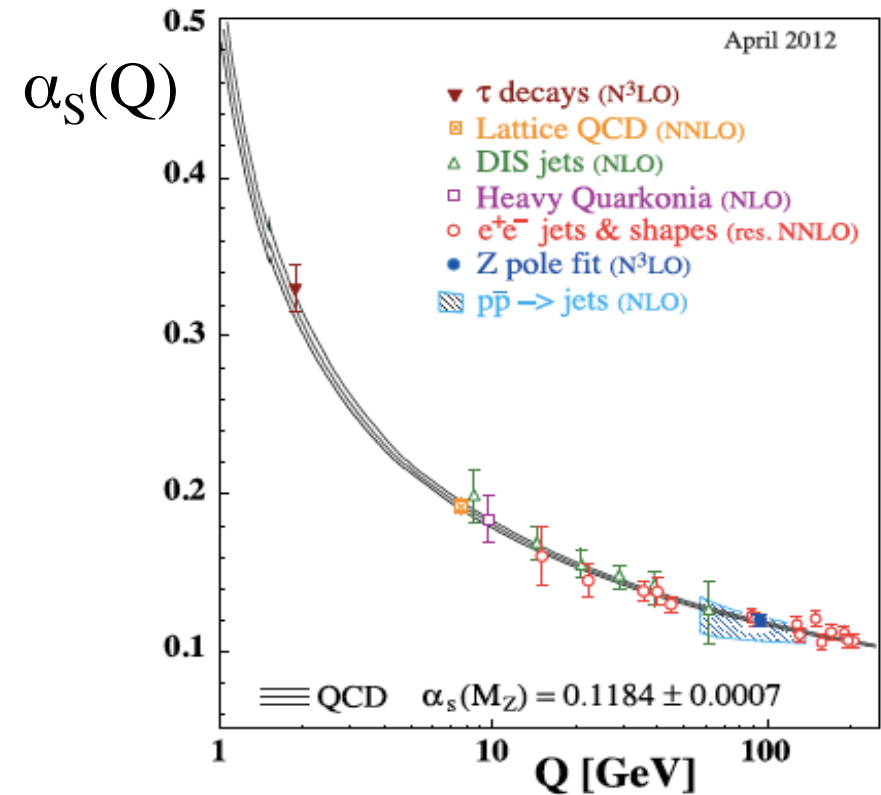
$$m_c \sim 1.3 \text{ GeV}, m_b \sim 4.6 \text{ GeV}$$

$$E_{\text{int}} \sim \Lambda_{\text{QCD}} \sim 300 \text{ MeV}$$



- $p \sim \sqrt{(2m_c E_{\text{int}})}$   
 $\sim 0.7 (\sim 1) \text{ GeV (charm)}$
- $V \sim \alpha_s/r \sim 0.5/(0.2*\sqrt{6}) \text{ [fm]}$   
 $\sim 200 \text{ MeV} \ll m_c$   
→  $\sim$  **Perturbative**
- $v \sim p/M \sim 0.5$   
→ **Nonrel.**

PDG 2012



# Light flavors

$$m_u \sim 2 \text{ MeV}, m_d \sim 4.8 \text{ MeV}, m_s \sim 95 \text{ MeV}$$

$$E_{\text{int}} \sim \Lambda_{\text{QCD}} \sim 300 \text{ MeV} \sim \textit{dynamically generated mass}$$

Quasiparticles for  $\Delta E(\text{excitations}) < 1 \text{ GeV}$

## Hierarchies

- Bare quarks  $\rightarrow$  Const. massive quarks  
 $\rightarrow$  Diquarks ...
- Hadrons  $\rightarrow$  Multihadrons (nuclei)

## Threshold

- Orbital excitations  $\sim qq^{\text{bar}}$  creation ( $\sim$  real)  
 $\rightarrow$  Multiquarks

## Pions

- Present around light quarks
- Source of interactions between const. quarks  
 $\rightarrow$  hadron interactions of light quarks

# ダイクォーク相関

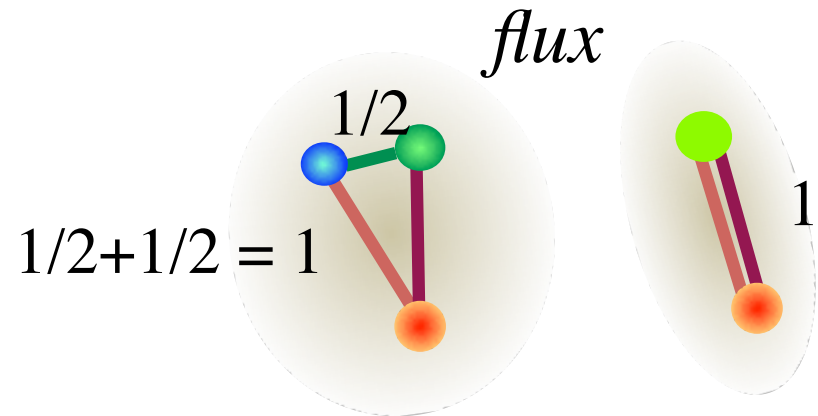
Selem-Wilczek: e-Print: [hep-ph/0602128](https://arxiv.org/abs/hep-ph/0602128)

- $ee$  は斥力
- $qq$  は引力を持つ
  - $SU(3)_c$  :  $qq^{\text{bar}}$  の半分
  - $SU(2)_c$  :  $qq^{\text{bar}}$  と同じ  $\rightarrow$  Pauli-Gursey symmetry
  - $q \sim q^{\text{bar}}$

$qq^{\text{bar}}$  力はカイラル対称性を破る

質量の生成、パイオンのゼロ質量

- $qq$  力は十分強い  $\sim$  数百 MeV



# スピン、フレーバー依存

Color magnetic int.

$qq$	$(\bar{3}_C, 0_S)$ -1/2	$(\bar{3}_C, 1_S)$ +1/6	$(6_C, 0_S)$ +1/4	$(6_C, 1_S)$ -1/12
$\bar{q}q$	$(1_C, 0_S)$ -1	$(1_C, 1_S)$ +1/3	$(8_C, 0_S)$ +1/8	$(8_C, 1_S)$ -1/24

Good diquark 

Bad diquark 

- $\Sigma$ - $\Lambda$  (80 MeV),  $\Sigma_c$ - $\Lambda_c$  (215 MeV) mass difference
- $\Lambda$ ,  $\Sigma$ の生成比 (e+e-@10 GeV)

$$\Lambda : \Sigma = 0.08:0.023, \quad \Lambda_c : \Sigma_c = 0.074:0.014$$

- $\Delta I = 1/2$  rule
- $F_2^n/F_2^p \rightarrow 1/4$
- Exoticsができにくい ← Good diquark間は斥力？

# Chew-Frautsch systematics

Regge trajectory in a relativistic string connecting q-qq of finite mass



$$\mu^{3/2} = \mu_1^{3/2} + \mu_2^{3/2}$$

$$E \approx \sqrt{\sigma L} + \kappa L^{-1/4} \mu^{3/2}$$

$$\kappa \equiv \frac{2}{3} \frac{\pi^{1/2}}{\sigma^{1/4}}$$

$$\sigma \sim 1.1 \text{ GeV}^2$$

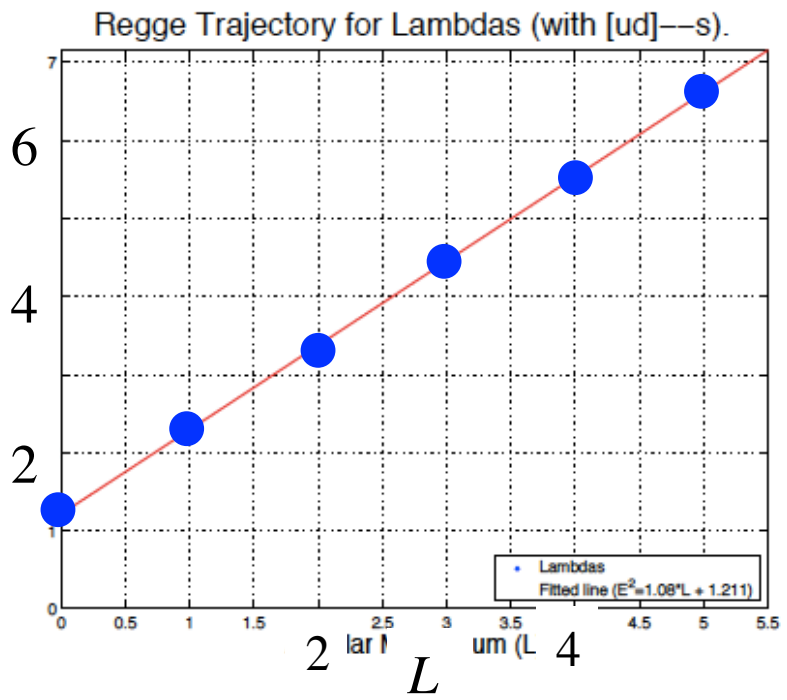
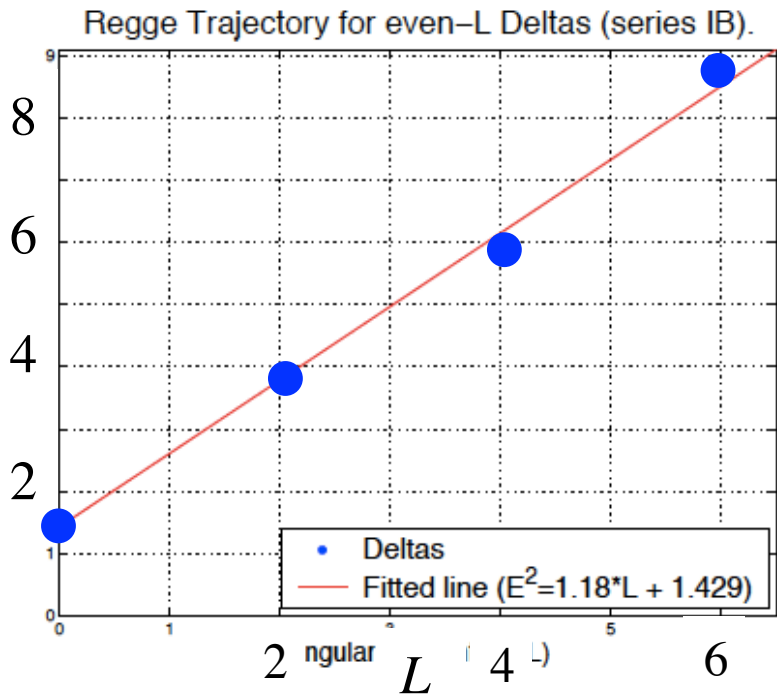
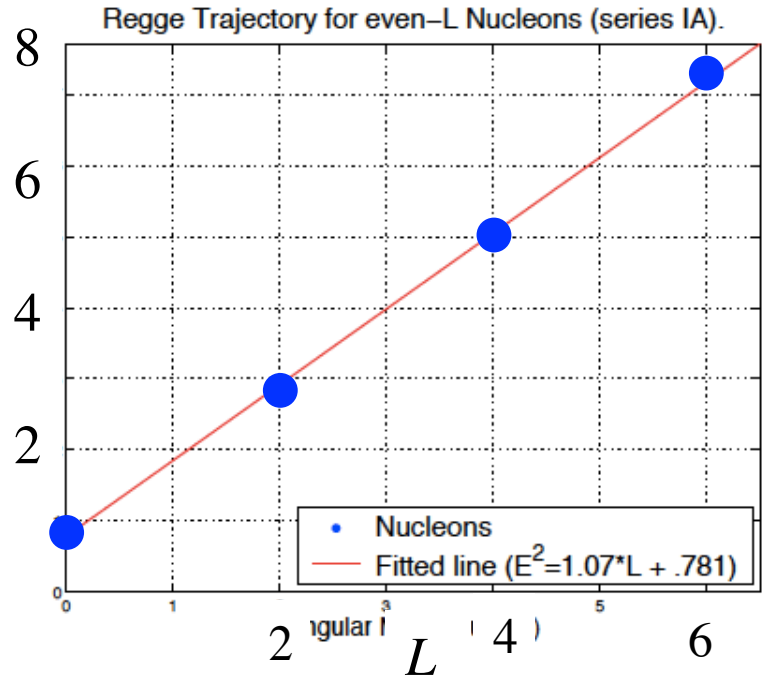
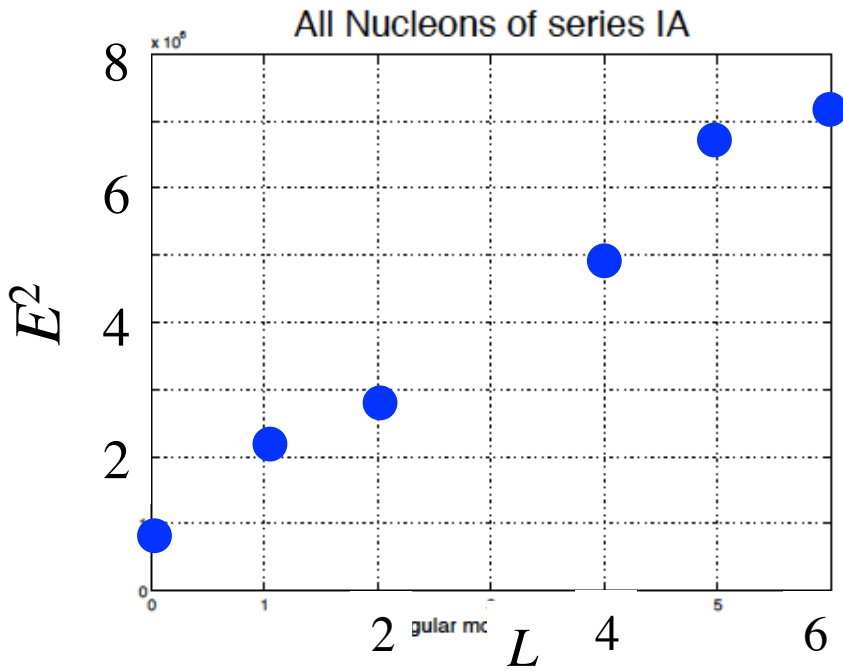


$$\mu \ll M$$

$$E - M = \sqrt{\frac{\sigma L}{2}} + 2^{1/4} \kappa L^{-1/4} \mu^{3/2}$$

$$\text{N}(1680)\text{-}\Delta(1950) \quad (ud)^{3/2} - [ud]^{3/2} = \frac{2^{1/4}}{\kappa} (1.950 - 1.680) = .28 \text{ GeV}^{3/2}$$

$$\Sigma(2030)\text{-}\Sigma(1915) \quad (us)^{3/2} - [us]^{3/2} = \frac{2^{1/4}}{\kappa} (2.030 - 1.915) = .12 \text{ GeV}^{3/2}$$





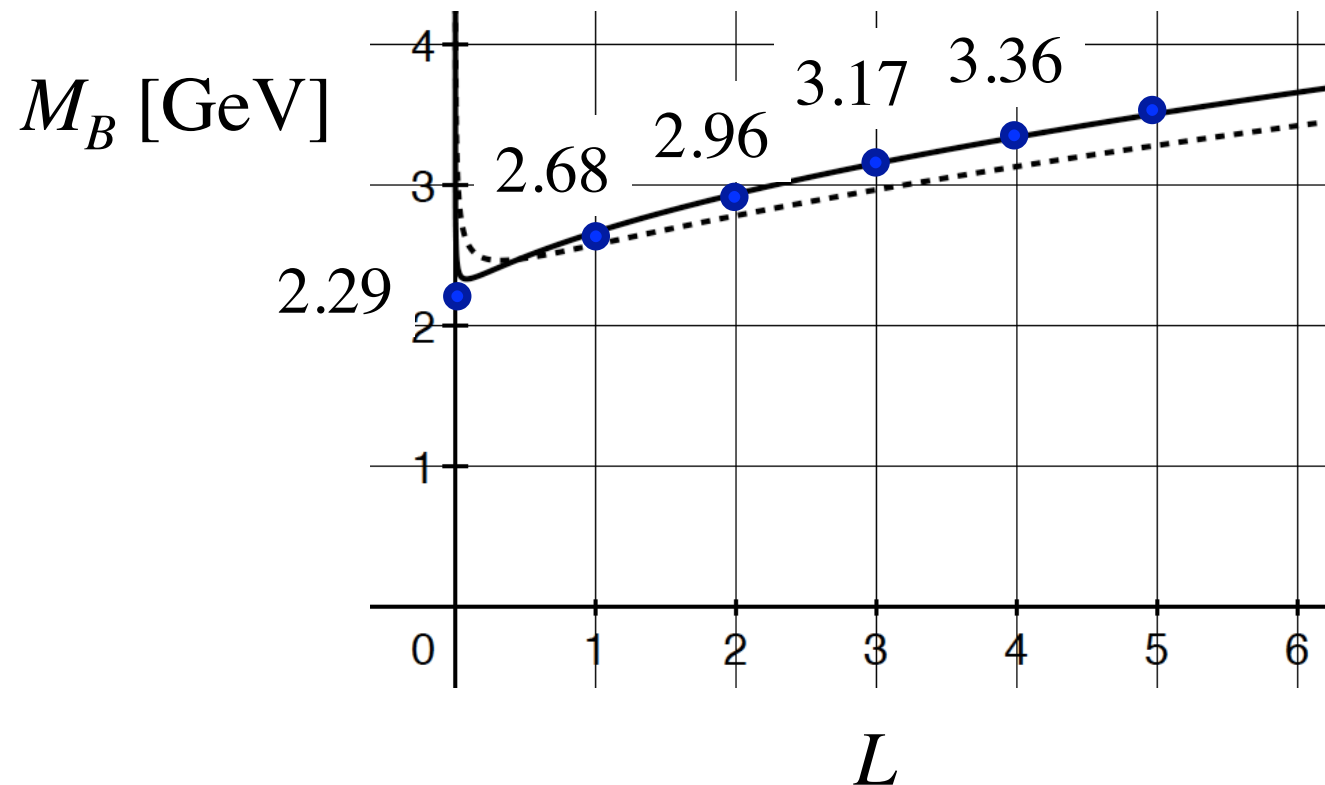
# Selem-Wilczek

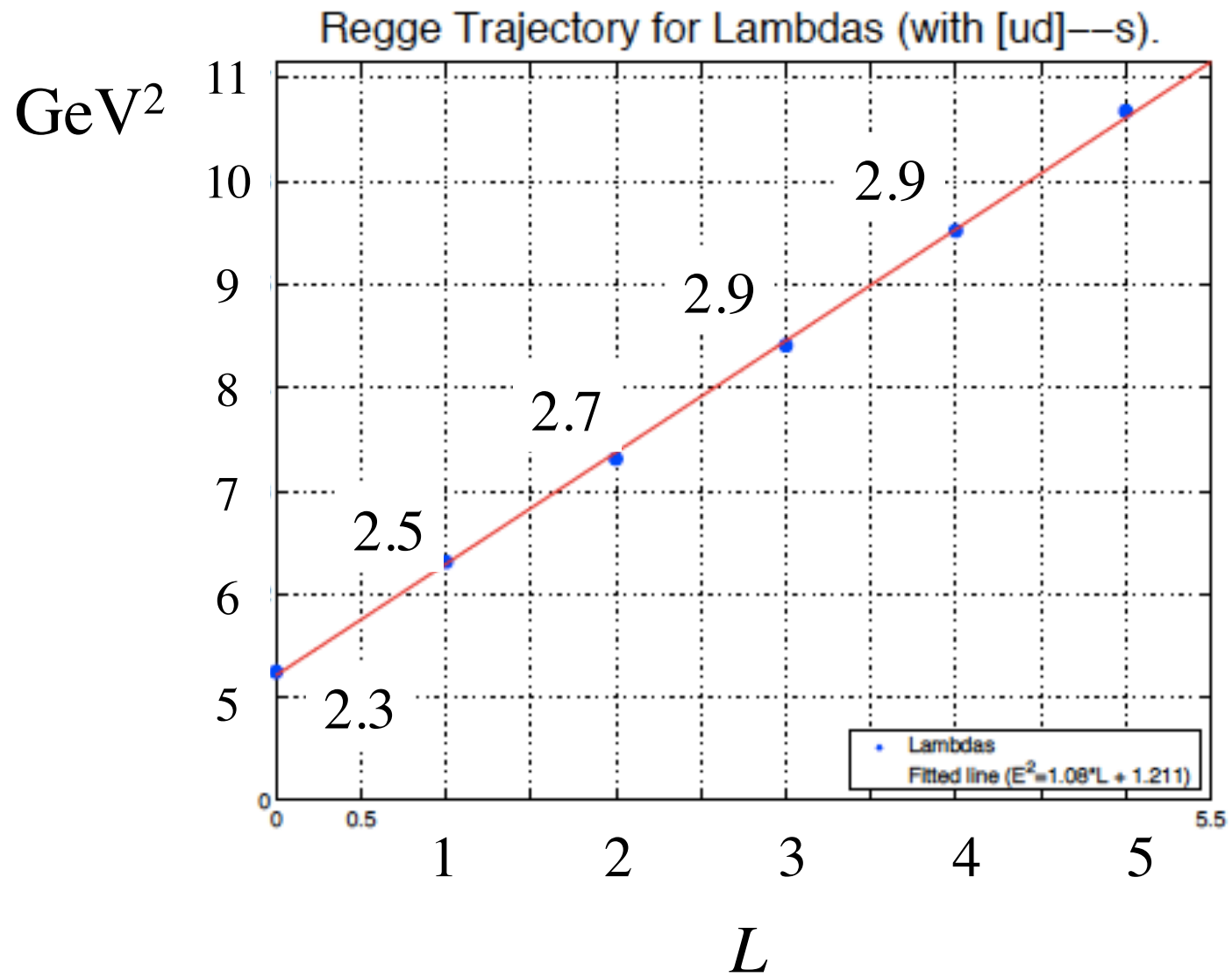
$$E - M = \sqrt{\frac{\sigma L}{2}} + 2^{\frac{1}{4}} \kappa L^{-\frac{1}{4}} \mu^{\frac{3}{2}}$$

$$\mu = 0.3, M = 1.7$$

$$\mu = 0.6, M = 1.2$$

$\Lambda_c$  trajectory





# 格子QCD

## ダイクォーク相関関数

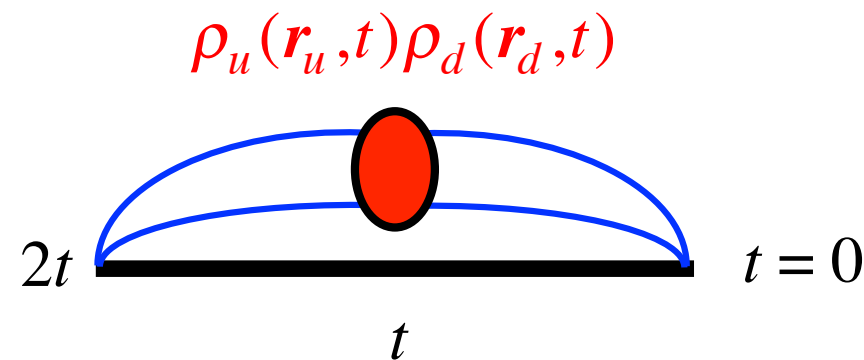
$$C(\mathbf{r}_u, \mathbf{r}_d; t) = \langle 0 | J_\Gamma(0, 2t) \rho_u(\mathbf{r}_u, t) \rho_d(\mathbf{r}_d, t) J_\Gamma^\dagger(0, 0) | 0 \rangle$$

$$\rho(\mathbf{r}, t) = \bar{q}_f \gamma_0 q_f, \quad f = u, d$$

$$J_\Gamma(x) = \varepsilon^{abc} [u_a^T(x) C \Gamma d_b(x) \pm d_a^T(x) C \Gamma u_b(x)] s_c(x)$$

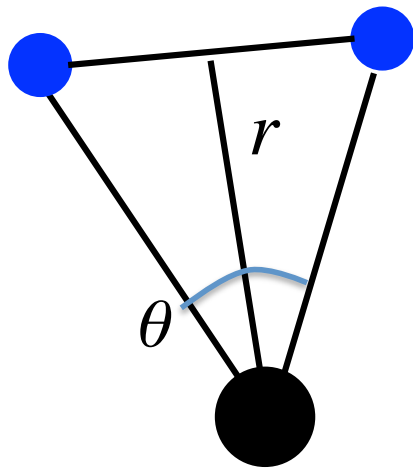
*ud*-diquark

Static heavy quark



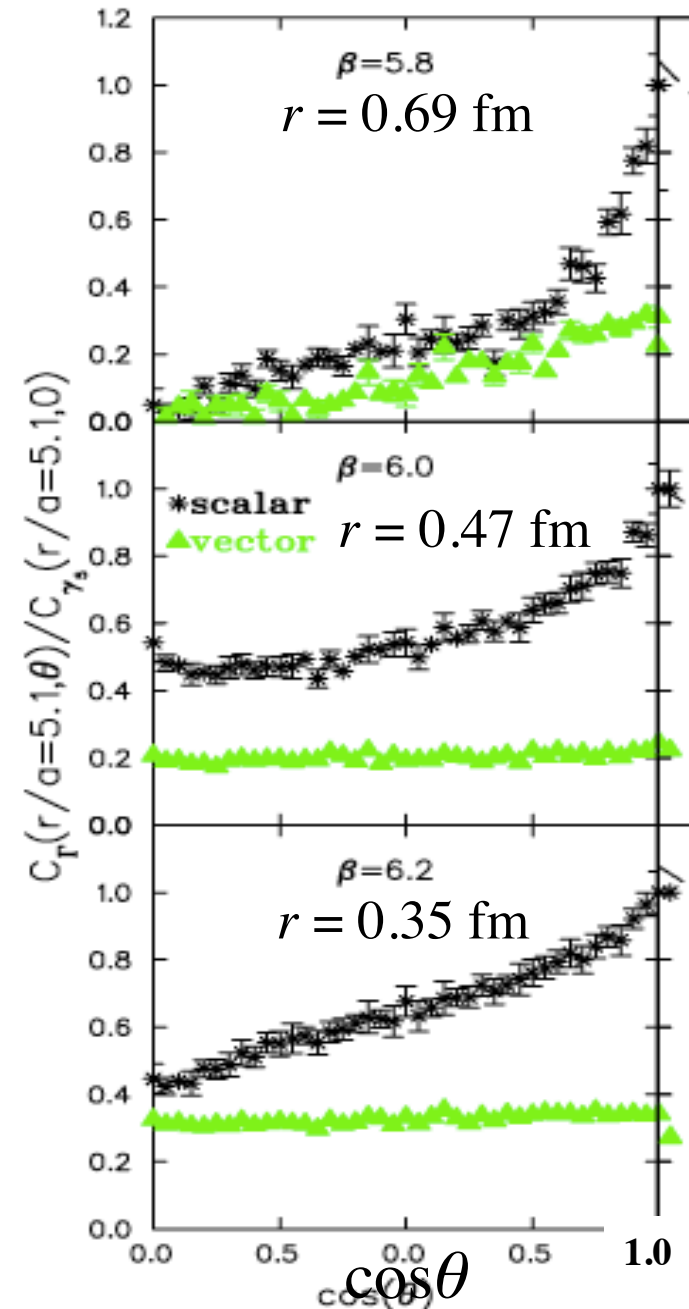
# Density correlations

Alexandrou, deForcrand, Lucini  
PRL 97, 222002 (2006)



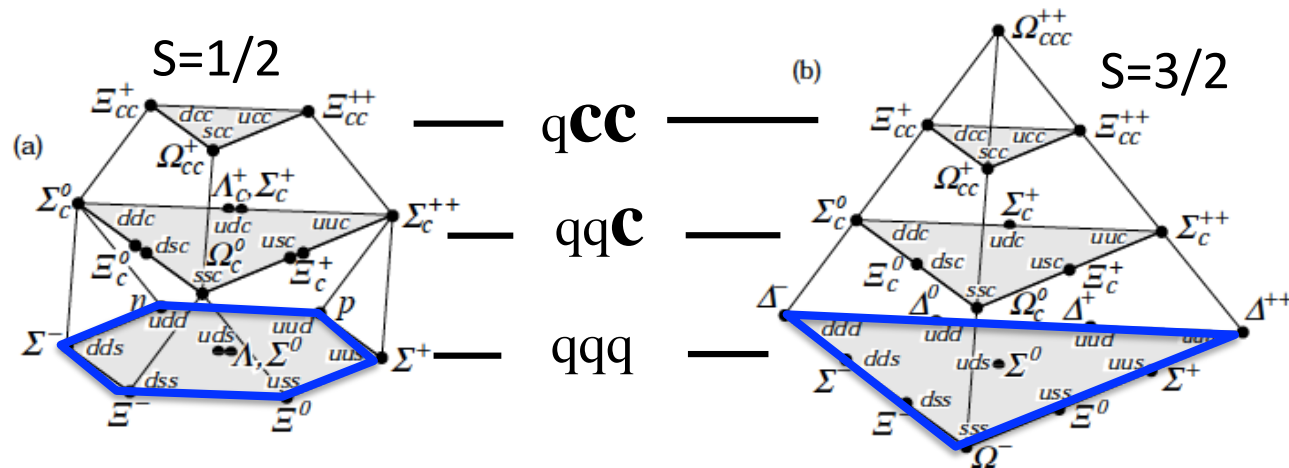
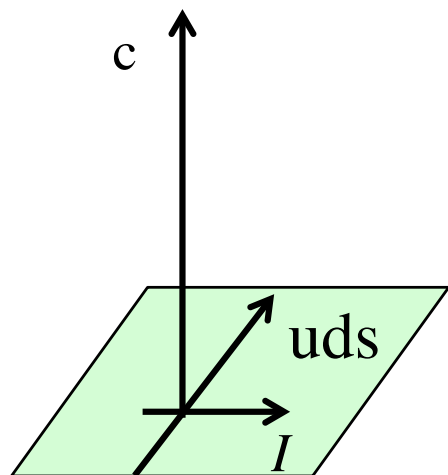
Good diquark  
Bad diquark

Indicates significant attraction  
between quarks in good diquark pair

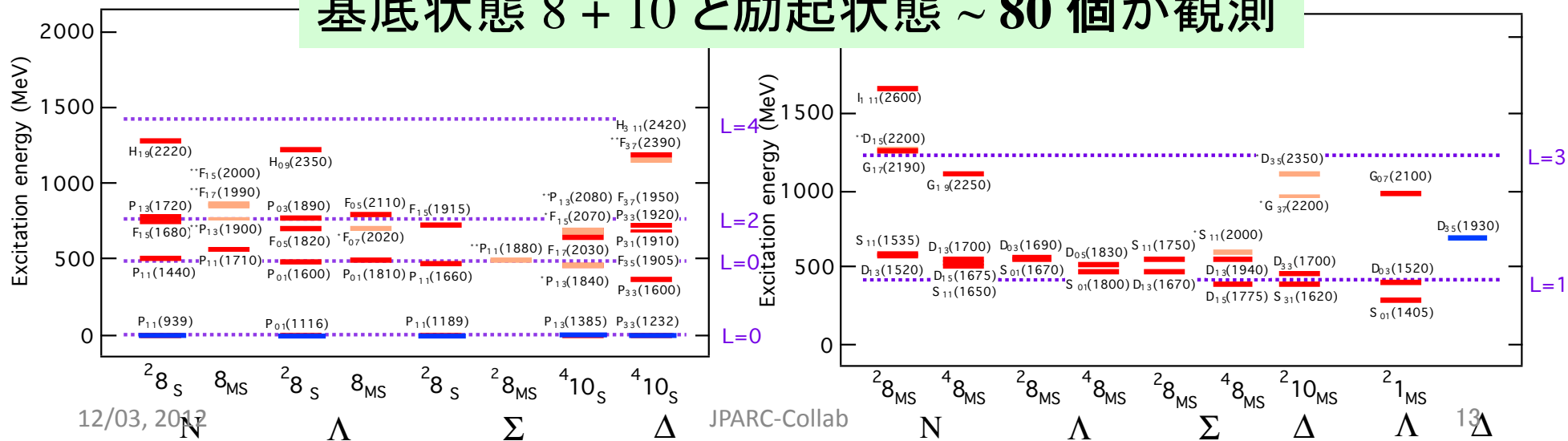


# バリオン分光

## 軽いクォーク(uds)のバリオン

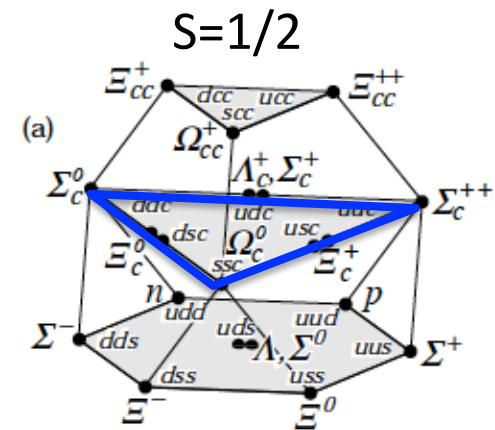
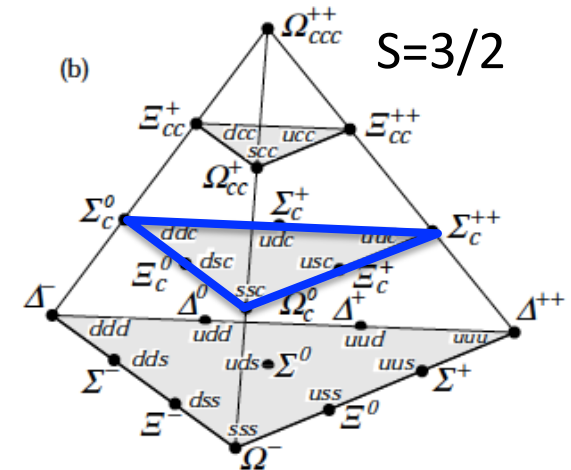
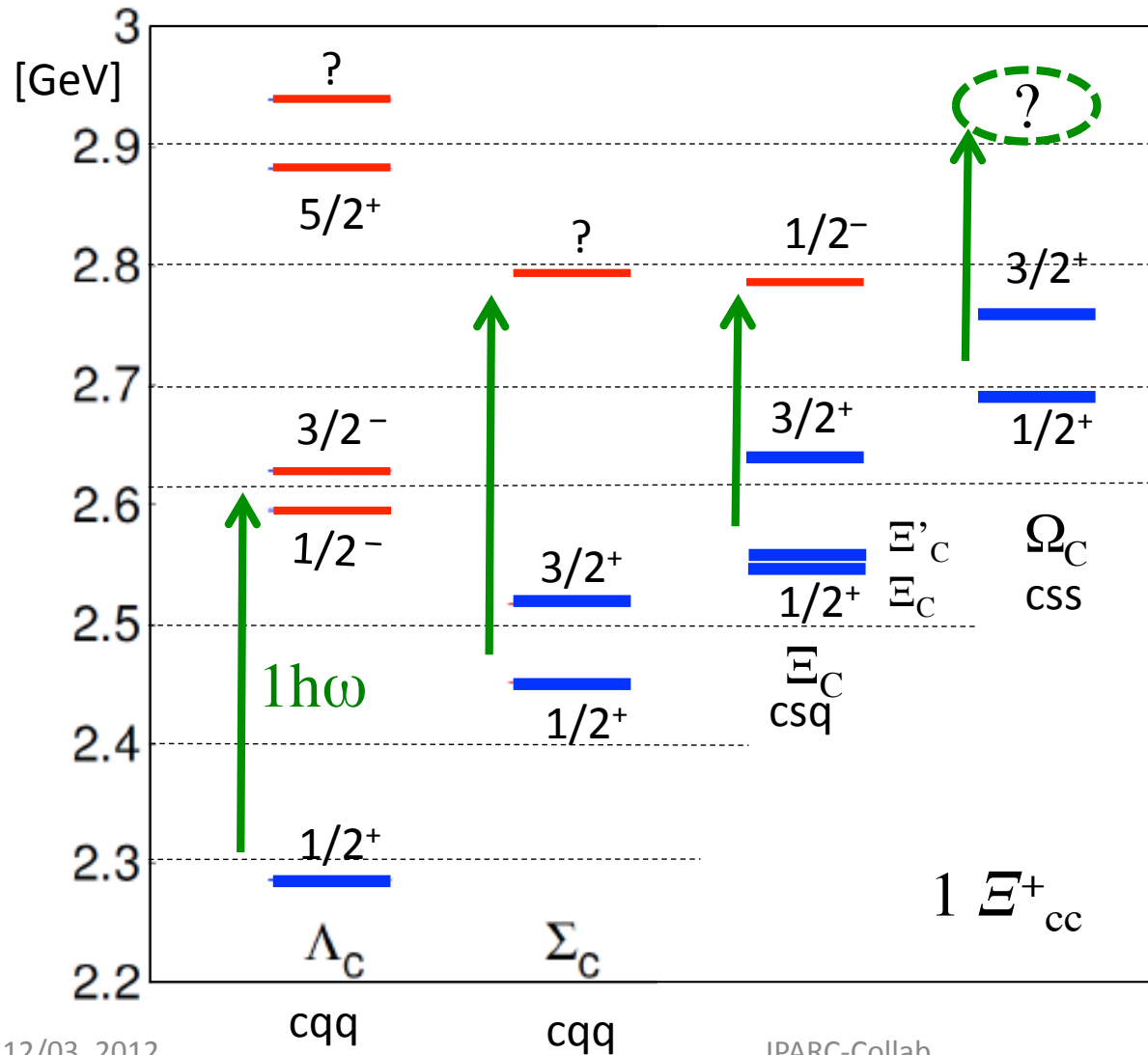


基底状態 8 + 10 と励起状態 ~ 80 個が観測



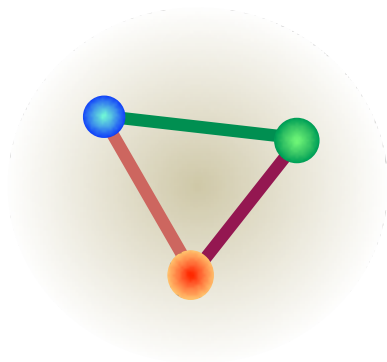
# Charmed baryons $14_c + 1_{cc} \lll 80_{uds}$ 個

(6<sub>excited</sub>)

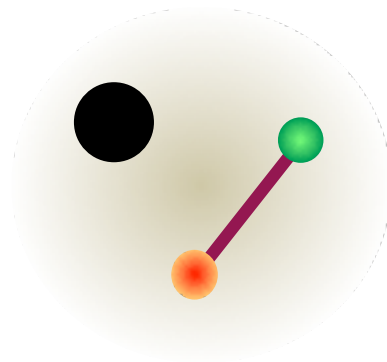


# 重いハドロンを使う利点

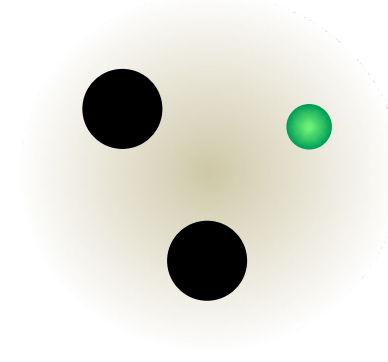
- モードを差別化する



バリオン



ダイクォーク  
重いクォーク

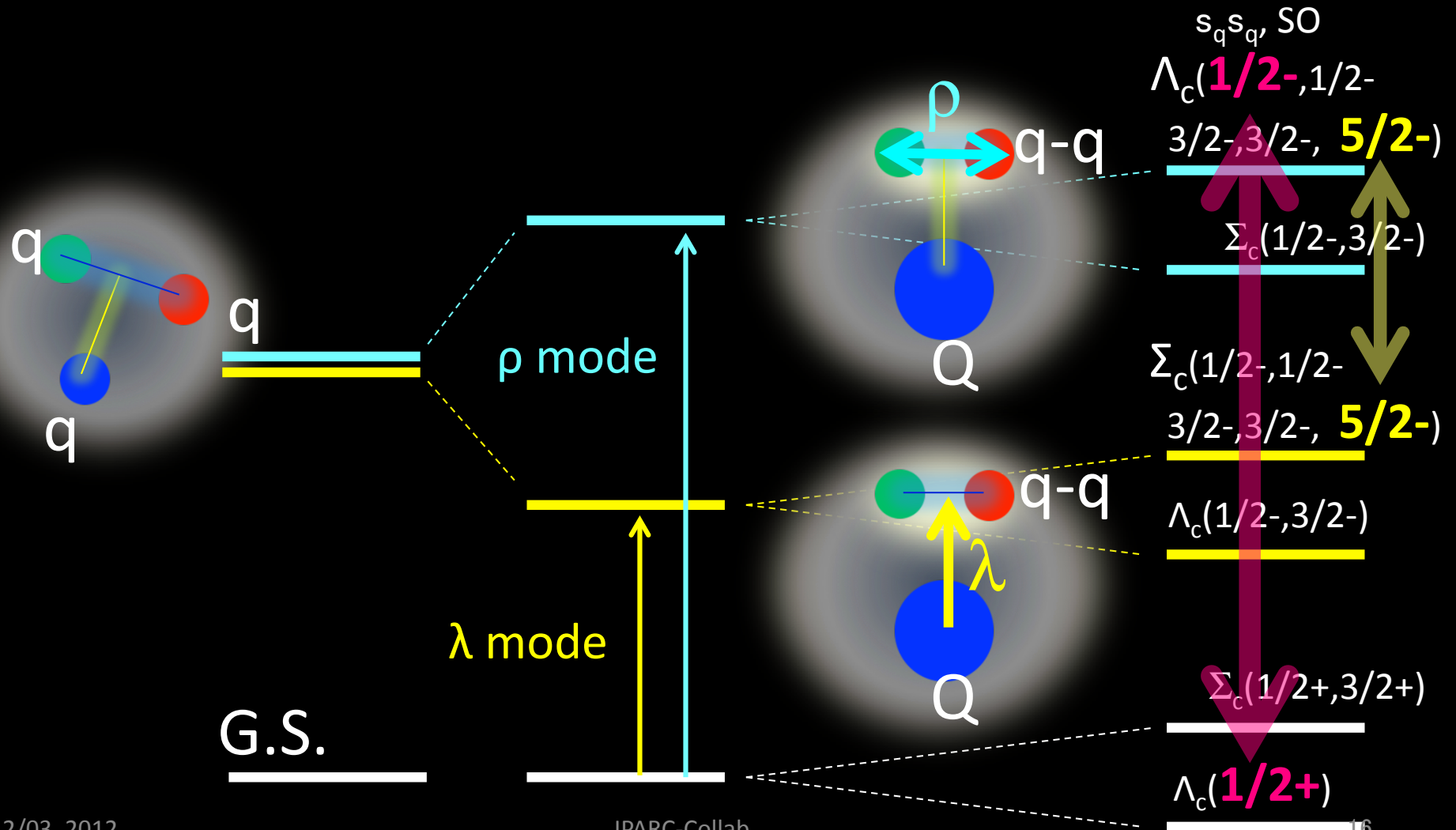


構成クォーク  
重いダイクォーク

- 予想されるスペクトラム、崩壊、生成比を実験で検証

# “Q” may isolate “qq”

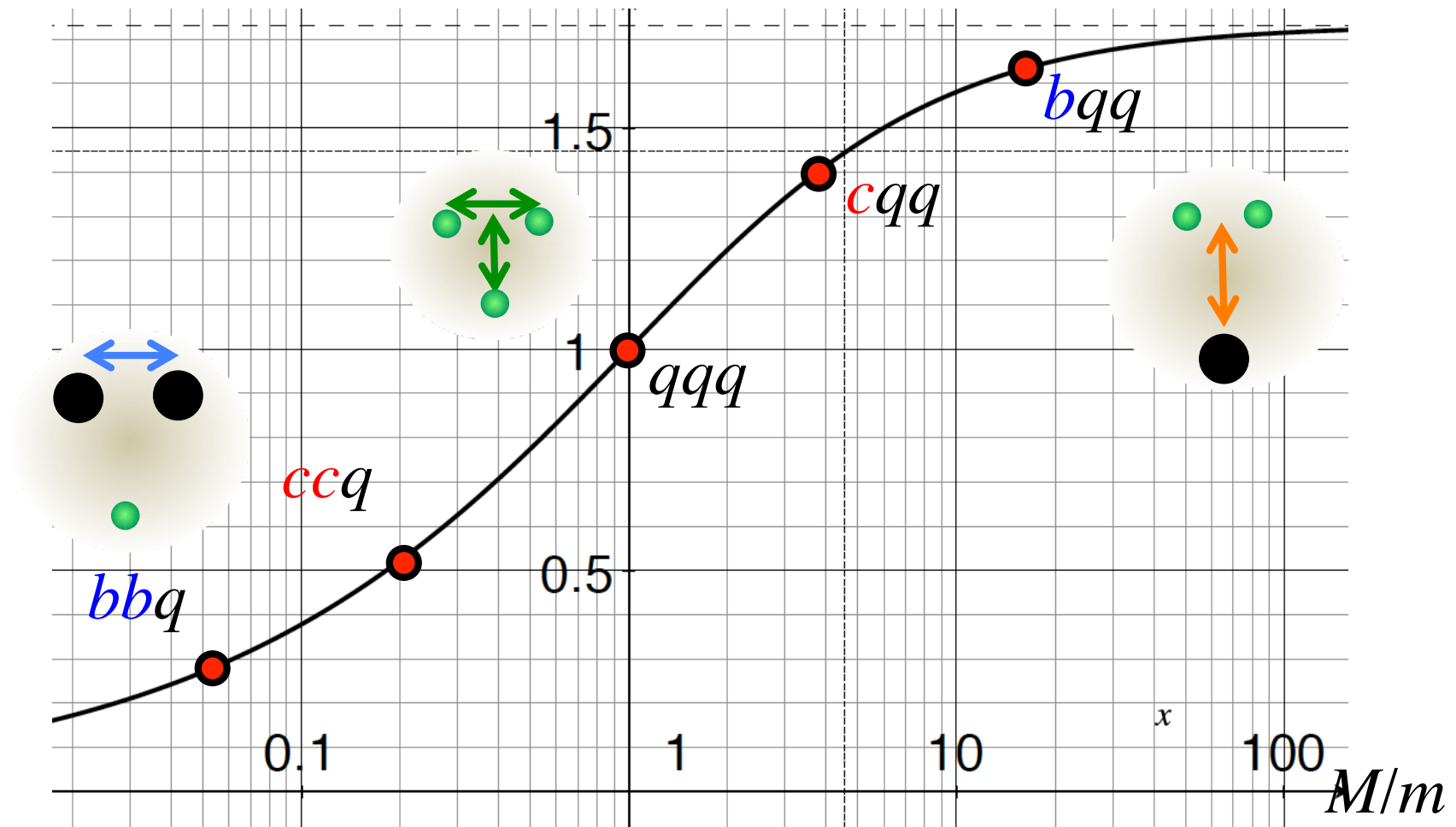
- $\lambda$  and  $\rho$  motions split  $\rightarrow$  known as **isotope shift**





# Spectrum

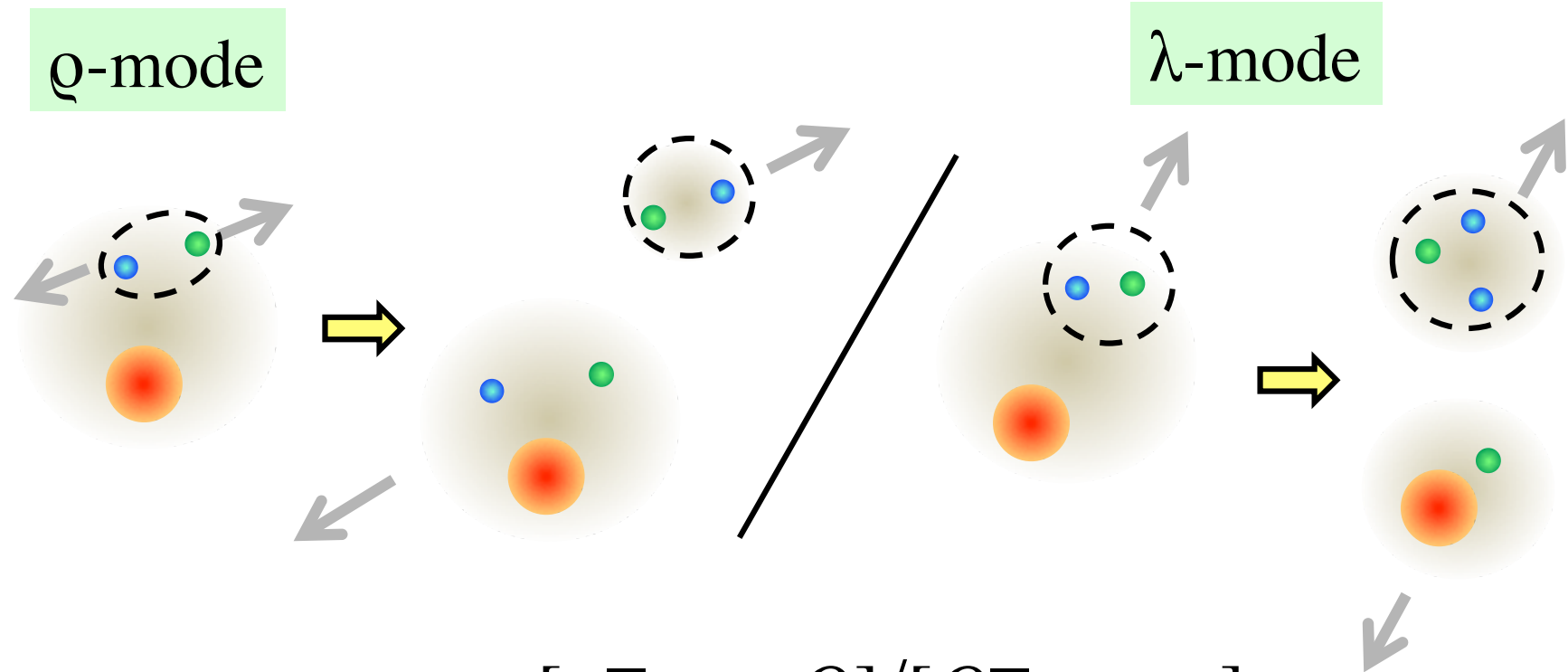
$$\frac{\omega_\lambda}{\omega_\rho} = \left[ \frac{1}{3} \left( 1 + \frac{2m}{M} \right) \right]^{1/2} = \left[ \frac{1}{3} (1 + 2x) \right]^{1/2}$$



$L=1$	$\rho$ mode	$\Lambda_c(\underline{1/2-}, 1/2-$ $\underline{3/2-, 3/2-}, \underline{5/2-})$ $\Sigma_c(1/2-, 3/2-)$	$S_D=1$ $S_D=0$
	$\lambda$ mode	$\Sigma_c(1/2-, 1/2-$ $\underline{3/2-, 3/2-}, \underline{5/2-})$ $\Lambda_c(\underline{1/2-, 3/2-})$	$S_D=1$ $S_D=0$
		$\Sigma_c(1/2+, 3/2+)$	
	GS	$\Lambda_c(\underline{1/2+})$	

- **Isotope shift**  
5/2- provides cleanest configuration  
– *Indication in strange baryons*  
 $\Lambda_{5/2-}(1830) > \Sigma_{5/2-}(1775)$   
( $\rho$ )                      ( $\lambda$ )
  
- **Chiral partner** of diquarks  
 $0^+(^1S_0)$  and  $0^-(^3P_0)$   
just as  
 $\pi$  and  $\sigma$

# Decays



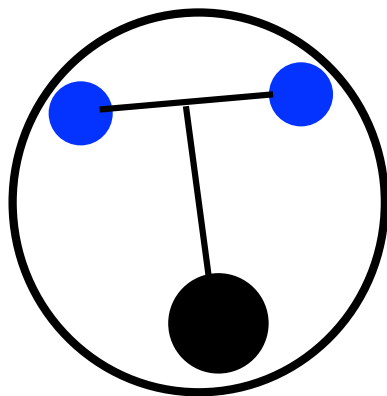
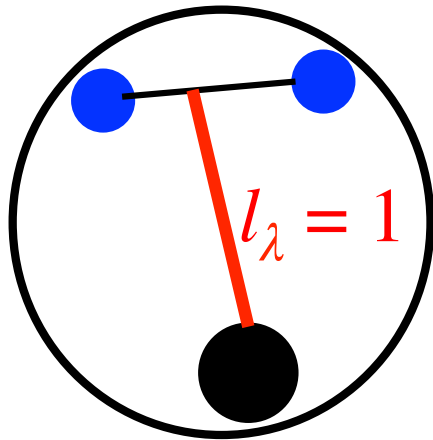
$$\text{Ratio: } [q\bar{q} + qqQ]/[Q\bar{q} + qqq]$$

q-modeバリオンは軽い中間子と重いバリオンに  
 λ-mode 重い 軽い に崩壊

# $1/2^- \rightarrow 1/2^+$ E1 transition

$\lambda$  mode

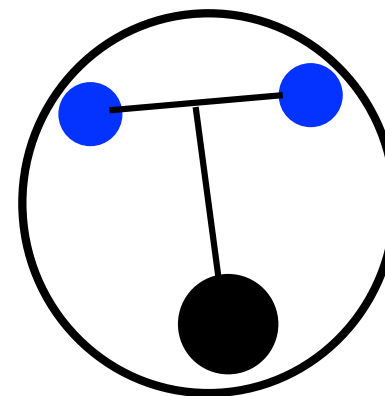
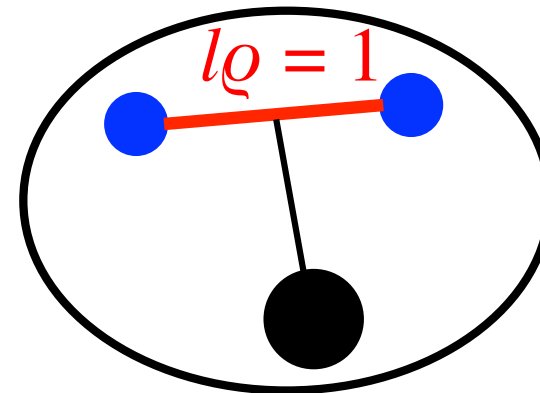
Good diquark  $0^+$



Good diquark  $0^+$

$\rho$  mode

3P0 diquark  $0^-$

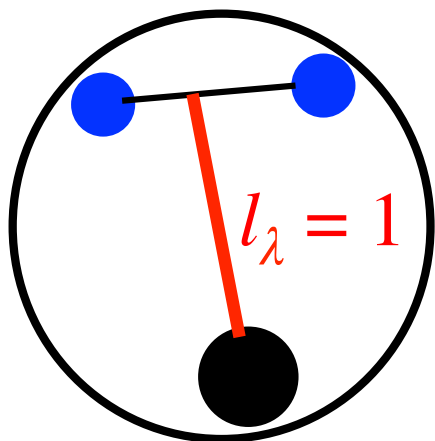


$0^- \rightarrow 0^+$  is forbidden

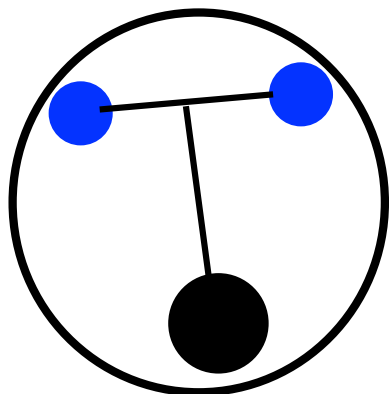
# $5/2^- \rightarrow 1/2^+$ M2, E3 transition

$\lambda$  mode

$^3S_1$  diquark  $1^+$



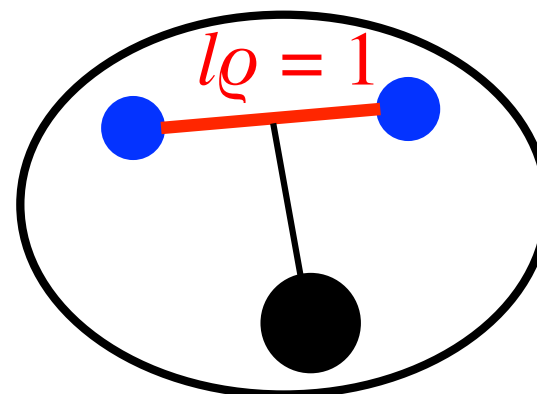
Both M2 E3



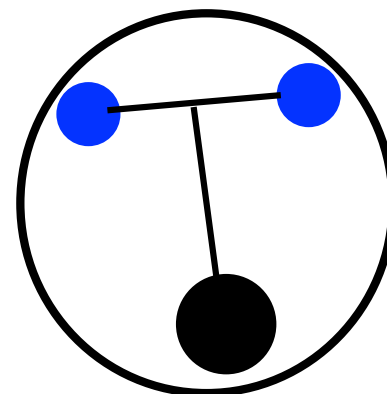
Good diquark  $0^+$

$\rho$  mode

$^3P_2$  diquark  $2^-$



$2^- \rightarrow 0^+$  is  
M2



# 重いクォークの役割

- 2体相関を見る
- スペクトラムの系統性  
     $\lambda$ - $q$ モードの分離、Good, bad diquark
- 崩壊パターン、ダイクォーク相関による選択則
- ダイクォークの分布