

Nuclear effects in the extraction of oscillation parameters

Olga Lalakulich, Kai Gallmeister
and Ulrich Mosel



**Institut für
Theoretische Physik**



Motivation and Contents

- Neutrino energy and Q^2 needed for
 - Hadron physics, electroweak couplings to nucleons and resonances
 - Neutrino oscillations
- Neutrino beams are broad in energy
- Modern experiments use nuclear targets
- Nuclear effects affect cross section measurements, neutrino energy and Q^2 reconstruction and, consequently, oscillation parameters



Neutrino Oscillations

$$\begin{aligned}
 P(\nu_\mu \rightarrow \nu_e) &\simeq \sin^2 2\theta_{13} \sin^2 \theta_{23} \frac{\sin^2[(1 - \hat{A})\Delta]}{(1 - \hat{A})^2} \\
 &- \alpha \sin 2\theta_{13} \xi \sin \delta \sin(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha \sin 2\theta_{13} \xi \cos \delta \cos(\Delta) \frac{\sin(\hat{A}\Delta)}{\hat{A}} \frac{\sin[(1 - \hat{A})\Delta]}{(1 - \hat{A})} \\
 &+ \alpha^2 \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(\hat{A}\Delta)}{\hat{A}^2} \\
 &\equiv O_1 + O_2(\delta) + O_3(\delta) + O_4 .
 \end{aligned}$$

appearance probability

mass hierarchy

$$\Delta = \frac{\Delta m_{21}^2 L}{4E} \quad \alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \quad \xi = \cos \theta_{13} \sin(2\theta_{12}) \sin(2\theta_{23})$$

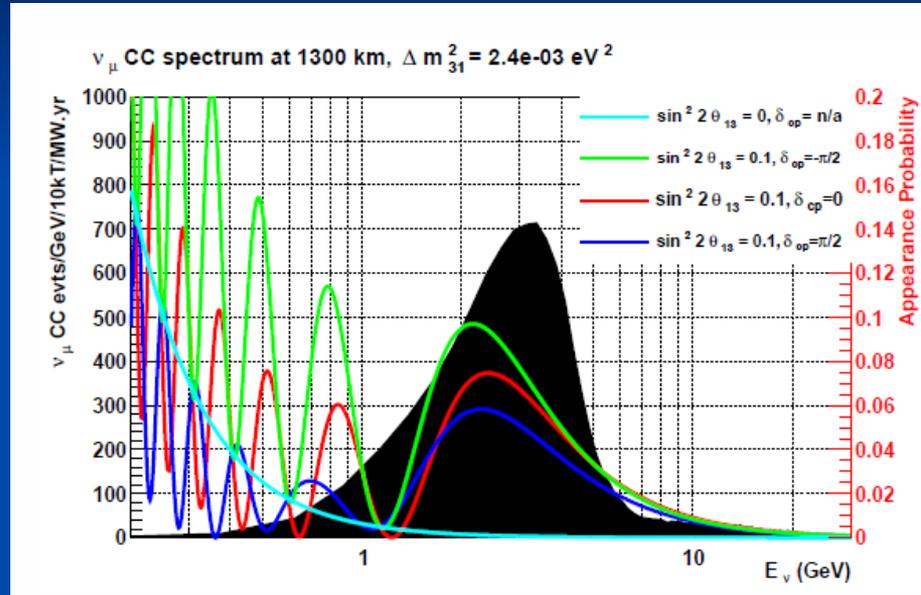
$$\hat{A} = \frac{2\sqrt{2}G_F n_e E}{\Delta m_{31}^2} \quad \delta = \text{CP violating phase}$$

Vacuum oscillation

Matter effects,
 n_e = electron density
 depends on sign of Δ_{31}



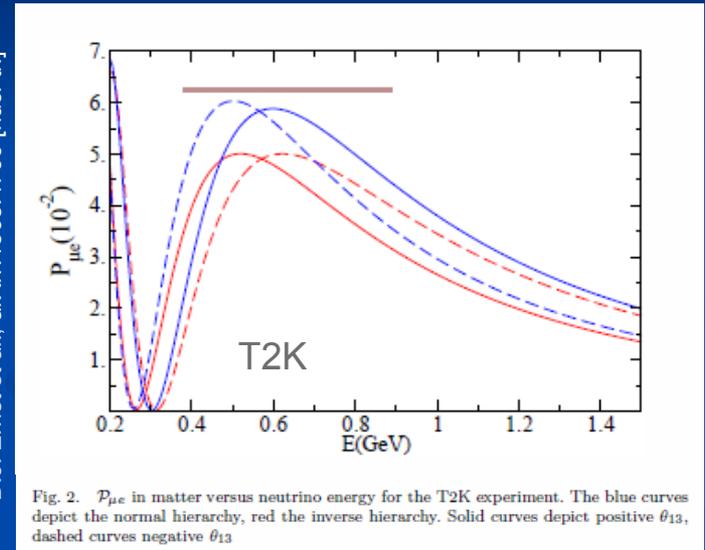
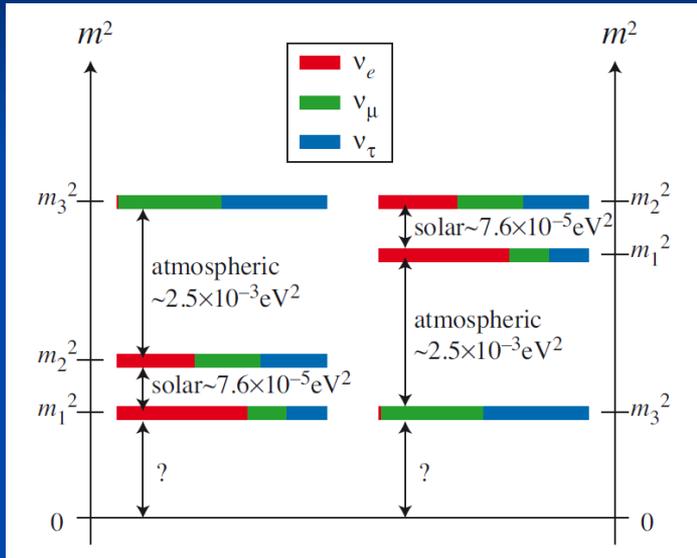
LBNE, δ_{CP} Sensitivity



Need to know neutrino energy to better than about 100 MeV

Need energy to distinguish between different δ_{CP}

Oscillation Signal Dependence on Hierarchy and Mixing Angle



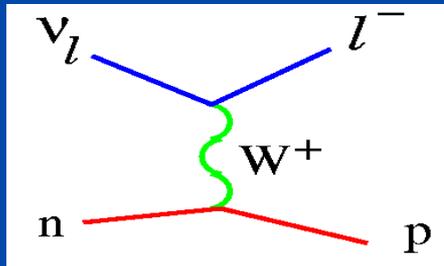
D. J. Ernst et al., arXiv:1303.4790 [nucl-th]

Fig. 2. $P_{\mu e}$ in matter versus neutrino energy for the T2K experiment. The blue curves depict the normal hierarchy, red the inverse hierarchy. Solid curves depict positive θ_{13} , dashed curves negative θ_{13} .

Shape sensitive to hierarchy and sign of mixing angle
Energy resolution of about 50 MeV is needed

Energy Reconstruction by QE

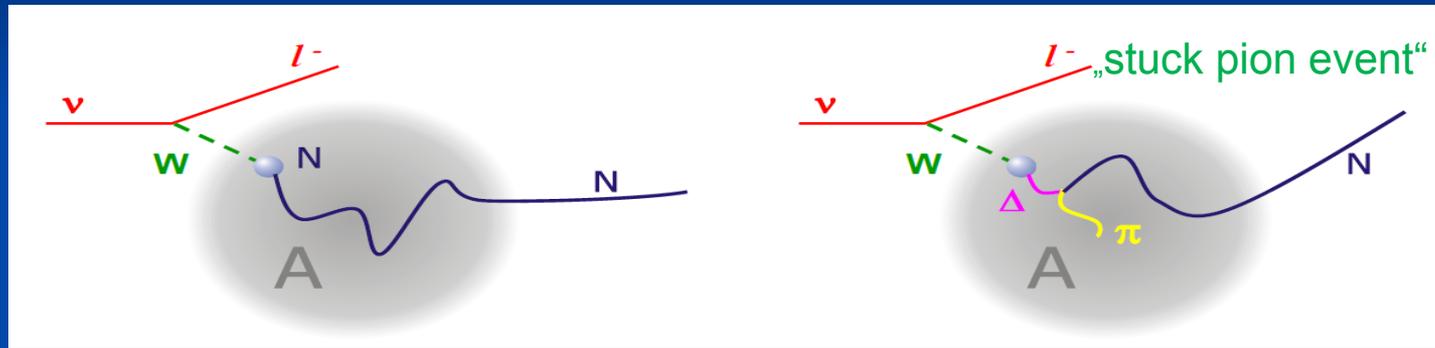
- In QE scattering on nucleon at rest, only $l + p$, **no** π , is outgoing. lepton determines neutrino energy:



$$E_\nu = \frac{2M_N E_\mu - m_\mu^2}{2(M_N - E_\mu + p_\mu \cos \theta_\mu)}$$

- **Trouble:** all presently running expts use nuclear targets
 1. Nucleons are Fermi-moving
 2. Final state interactions may hinder correct event identification

Final State Interactions in Nuclear Targets



Complication to identify QE, entangled with π production

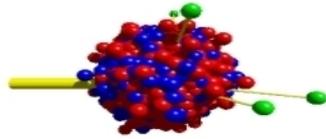
Both must be treated at the same time!

Nuclear Targets (K2K, MiniBooNE, T2K, MINOS, Minerva,)

Need for a Neutrino Generator

- Need final state for event reconstruction
- Inclusive cross sections are not enough, need semi-inclusive for event identification
- Must describe complete final state of $(\nu A \rightarrow l X)$ for 0 pion condition (incl. ‚stuck pions‘)
- Only practical theory: MC or transport code





- **GiBUU : Theory and Event Generator**
based on a BM solution of Kadanoff-Baym equations
- Physics content and details of num. implementation:
Buss et al, Phys. Rept. 512 (2012) 1- 124
- Code available from **gibuu.hepforge.org**

Mine of information on theoretical treatment of potentials, collision terms, spectral functions and cross sections, useful for any generator



Transport Equation

Collision term

$$\mathcal{D}F(x, p) + \text{tr} \left\{ \text{Re} \tilde{S}^{\text{ret}}(x, p), -i \tilde{\Sigma}^<(x, p) \right\}_{\text{pb}} = C(x, p).$$

Drift term

$$\left[\left(1 - \frac{\partial H}{\partial p_0} \right) \frac{\partial}{\partial t} + \frac{\partial H}{\partial \mathbf{p}} \frac{\partial}{\partial \mathbf{x}} - \frac{\partial H}{\partial \mathbf{x}} \frac{\partial}{\partial \mathbf{p}} + \frac{\partial H}{\partial t} \frac{\partial}{\partial p^0} + \text{KB term} \right] F(x, p) = - \text{loss term} + \text{gain term}$$

F: 8d-Spectral
phase space
density

Kadanoff-Baym equation

- LHS: drift term + backflow (KB) terms
- RHS: collision term = - loss + gain terms (detailed balance)



Collision term

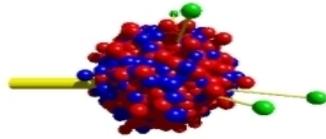
$$\begin{aligned} C^{(2)}(x, p_1) &= C_{\text{gain}}^{(2)}(x, p_1) - C_{\text{loss}}^{(2)}(x, p_1) = \frac{\mathcal{S}_{1'2'}}{2p_1^0 g_{1'} g_{2'}} \int \frac{d^4 p_2}{(2\pi)^4 2p_2^0} \int \frac{d^4 p_{1'}}{(2\pi)^4 2p_{1'}^0} \int \frac{d^4 p_{2'}}{(2\pi)^4 2p_{2'}^0} \\ &\times (2\pi)^4 \delta^{(4)}(p_1 + p_2 - p_{1'} - p_{2'}) |\overline{\mathcal{M}}_{12 \rightarrow 1'2'}|^2 [F_{1'}(x, p_{1'}) F_{2'}(x, p_{2'}) \overline{F}_1(x, p_1) \\ &\times \overline{F}_2(x, p_2) - F_1(x, p_1) F_2(x, p_2) \overline{F}_{1'}(x, p_{1'}) \overline{F}_{2'}(x, p_{2'})] \end{aligned}$$

For two-body collisions

with

$$\begin{aligned} F(x, p) &= 2\pi g A(x, p) f(x, p) \\ \overline{F}(x, p) &= 2\pi g A(x, p) [1 - f(x, p)] \end{aligned}$$





- **GiBUU** describes (within the same unified theory and code)
 - heavy ion reactions, particle production and flow
 - pion and proton induced reactions
 - low and high energy photon and electron induced reactions
 - **neutrino induced reactions**

using the **same physics input!** And the same **code!**
NO TUNING!



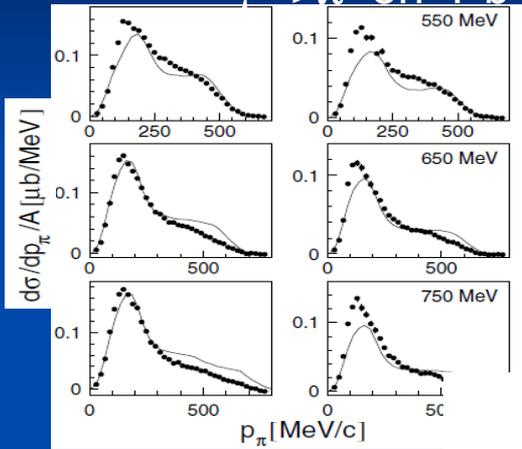
GiBUU Ingredients

- In-medium corrected primary interaction cross sections, nucleons bound and moving in local Fermigas
- Includes spectral functions for baryons and mesons (binding + collision broadening)
- *Vector* couplings taken from electro-production (MAID)
- *Axial* couplings modeled with PCAC
- *Hadronic* couplings for FSI taken from PDG
- Events for $W > 2$ GeV (DIS) from PYTHIA

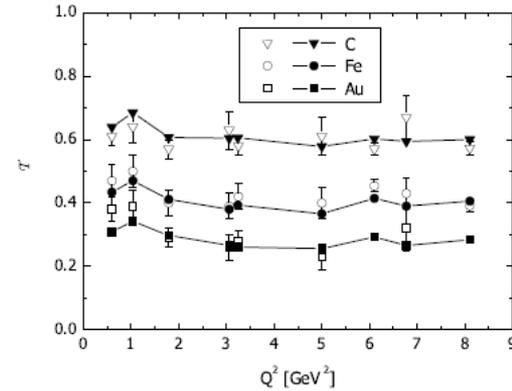


Check: pions, protons

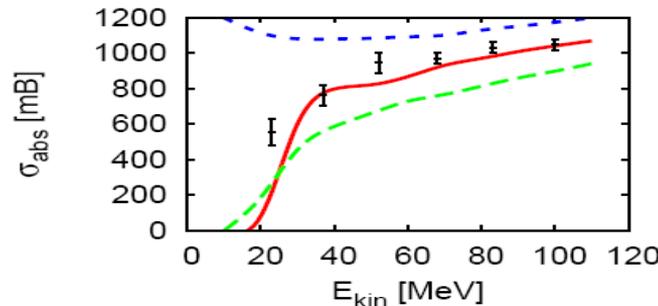
$\gamma \rightarrow \pi^0$ on Pb



Proton transparency



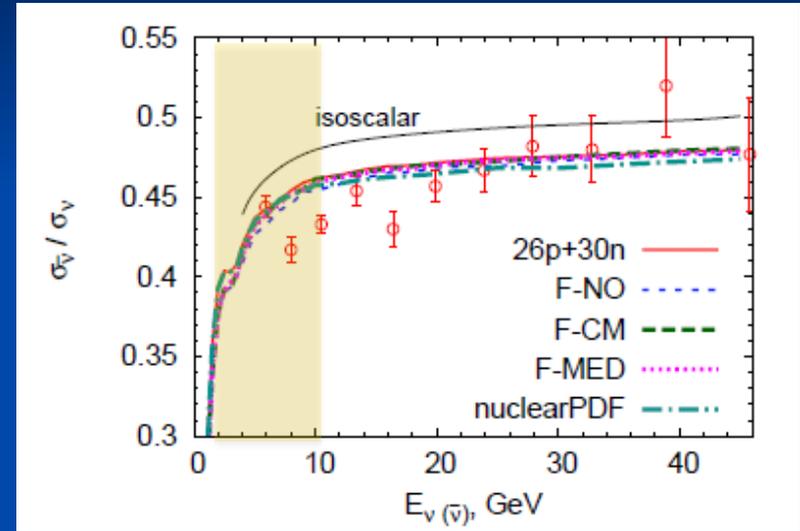
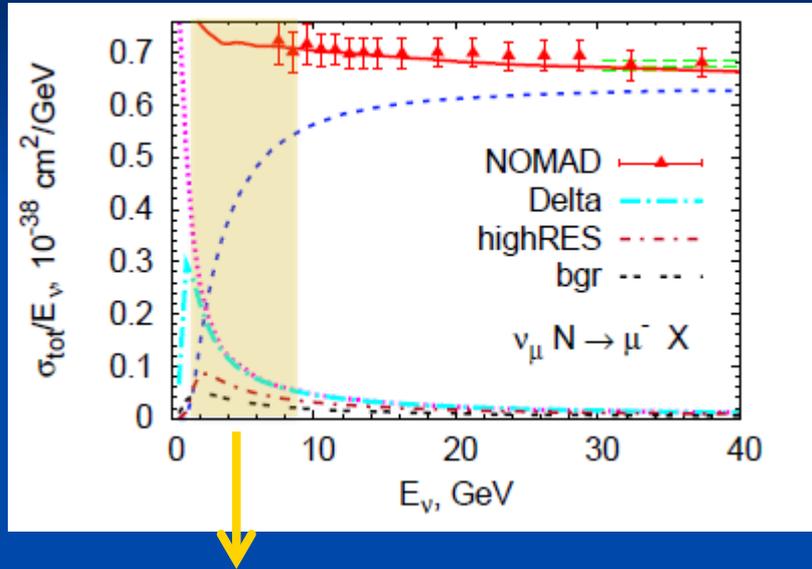
π^+ on Au



Pion reaction Xsect.



SIS - DIS



Shallow Inelastic Scattering,
interplay of different reaction mechanisms

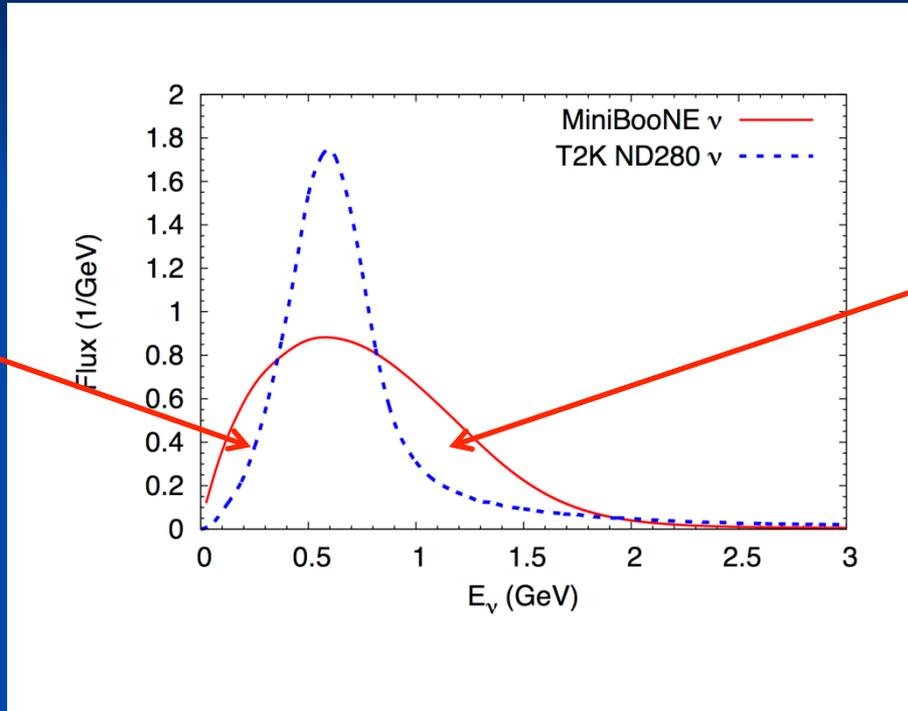
Curves: GiBUU

Reaction Types

- 3 major reaction types relevant:
 1. QE scattering
 - I. true QE (single particle interaction)
 - II. many-particle interactions (RPA + 2p2h + spectral functions)
 2. Pion production
 3. SIS and DIS (less important at T2K and MiniBooNE)
- All reaction types are entangled:
final states may look the same



T2K vs MB Flux



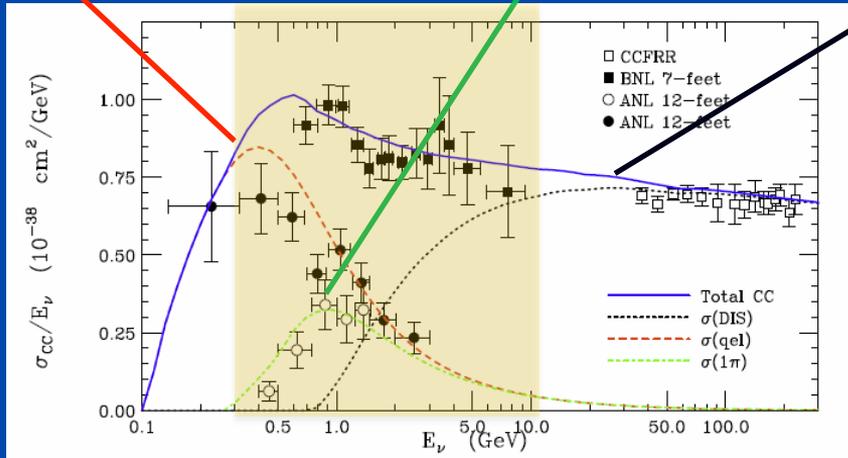
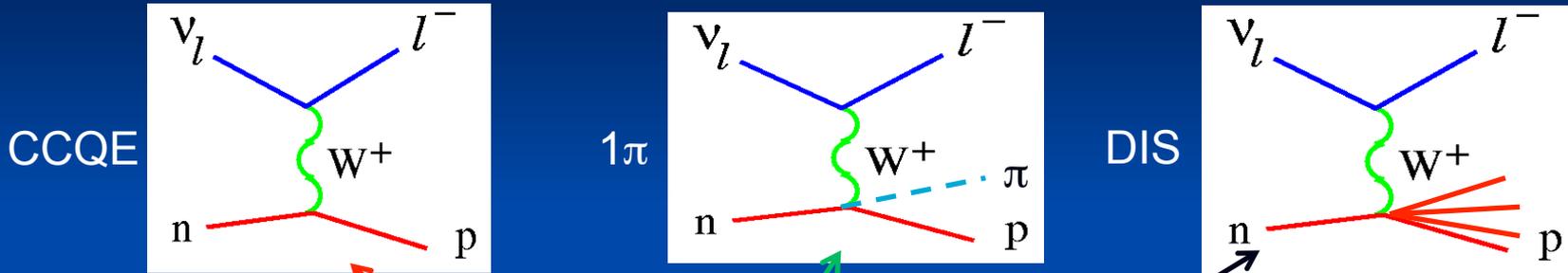
less RPA

T2K ND280
205kA flux

less pions



Neutrino-nucleon cross section



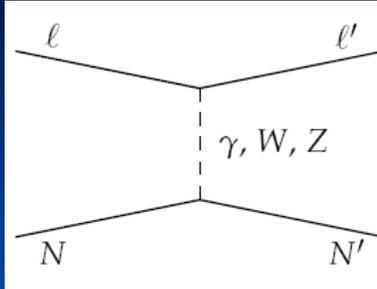
note:

$$10^{-38} \text{ cm}^2 = 10^{-11} \text{ mb}$$

In the region of modern experiments (0.5 – 10 GeV) all 3 mechanisms overlap



Quasielastic scattering



$$J_{QE}^\mu = \left(\gamma^\mu - \frac{\not{q} q^\mu}{q^2} \right) F_1^V + \frac{i}{2M_N} \sigma^{\mu\alpha} q_\alpha F_2^V + \gamma^\mu \gamma_5 F_A + \frac{q^\mu \gamma_5}{M_N} F_P$$

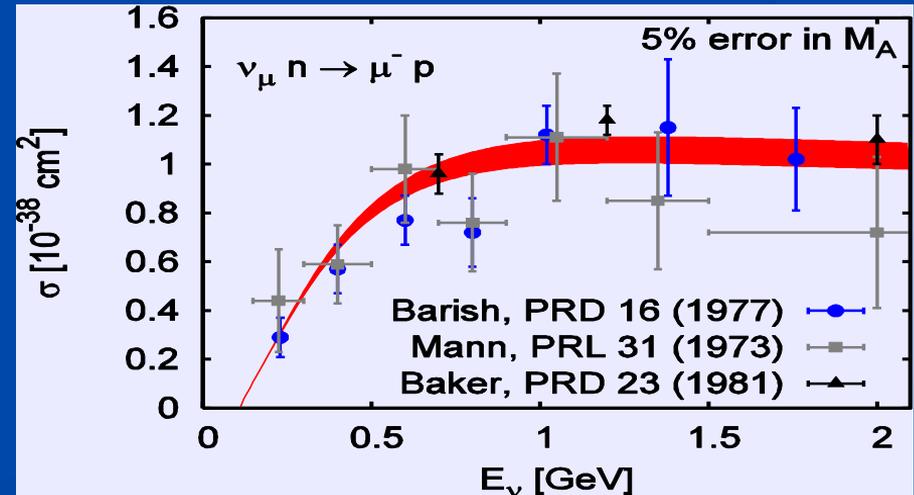
- Vector form factors from e -scattering
- axial form factors

$F_A \leftrightarrow F_P$ and $F_A(0)$ via **PCAC**

dipole ansatz for F_A with

$M_A = 1$ GeV:

$$F_A(Q^2) = \frac{g_A}{\left(1 + \frac{Q^2}{M_A^2}\right)^2}$$



2p-2h Processes

- Model for $\nu + p_1 + p_2 \rightarrow p_3 + p_4 + l$ (no recoil)

$$\frac{d^2\sigma}{dE_l' d(\cos\theta')} \propto \frac{k'}{k} \int_{NV} d^3r \int \prod_{j=1}^4 \frac{d^3p_j}{(2\pi)^3 2E_j} f_1 f_2 \overline{|M|^2} (1-f_3)(1-f_4) \delta^4(p)$$

with flux averaged matrixelement

$$\overline{|M|^2} = \int \Phi(E_\nu) L_{\mu\nu} W^{\mu\nu} dE_\nu$$

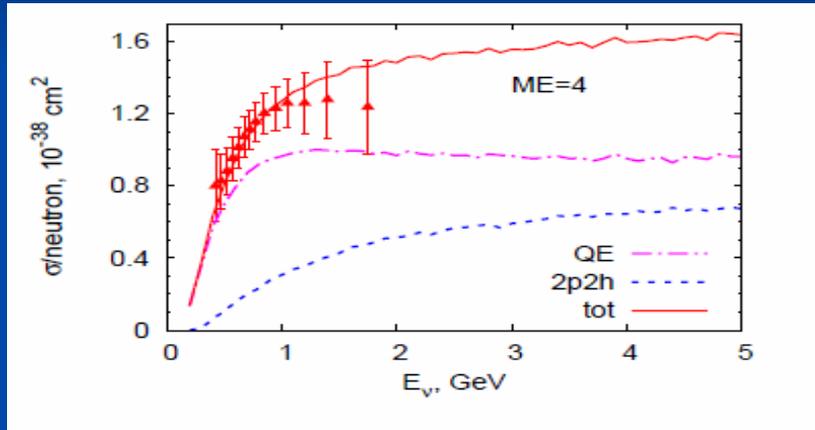
Flux smears out details in hadron tensor W

W contains 2p-2h and poss. RPA effects

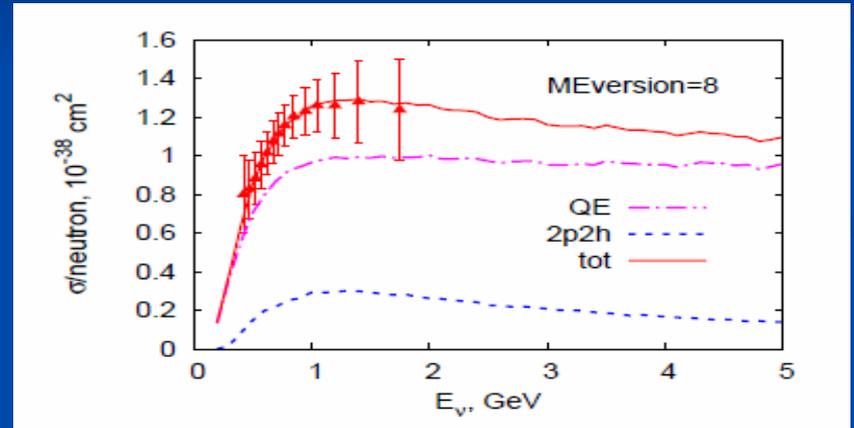
Ansatz for W : $W_{\mu\nu} = g_{\mu\nu} F(Q^2)$

The MiniBooNE QE Puzzle

$M = \text{const}$



$M = M(E, q), W^{\mu\nu} \sim P_T^{\mu\nu}(q)$



Phase-space model for 2p-2h
Absolute value fitted to data.

Pion Production

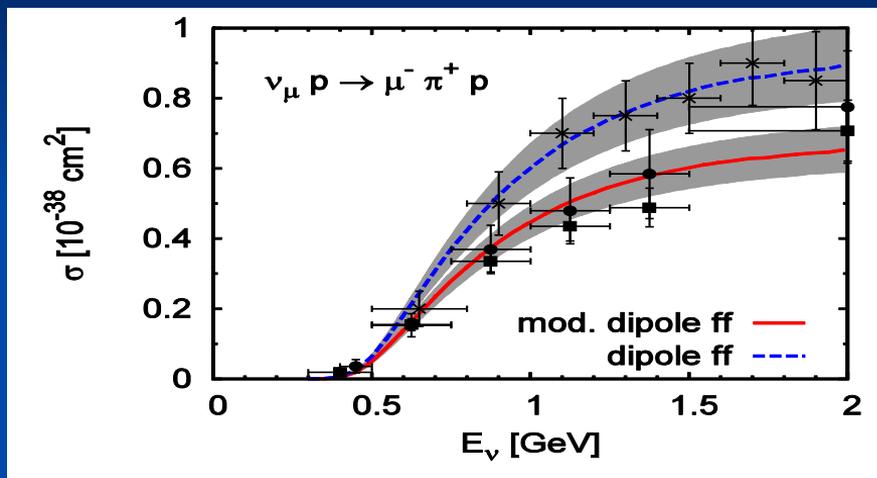
- Pion production dominated by **$P_{33}(1232)$ resonance (not just a heavier nucleon)**

$$J_{\Delta}^{\alpha\mu} = \left[\frac{C_3^V}{M_N} (g^{\alpha\mu} \not{q} - q^{\alpha} \gamma^{\mu}) + \frac{C_4^V}{M_N^2} (g^{\alpha\mu} q \cdot p' - q^{\alpha} p'^{\mu}) + \frac{C_5^V}{M_N^2} (g^{\alpha\mu} q \cdot p - q^{\alpha} p^{\mu}) \right] \gamma_5$$

$$+ \frac{C_3^A}{M_N} (g^{\alpha\mu} \not{q} - q^{\alpha} \gamma^{\mu}) + \frac{C_4^A}{M_N^2} (g^{\alpha\mu} q \cdot p' - q^{\alpha} p'^{\mu}) + C_5^A g^{\alpha\mu} + \frac{C_6^A}{M_N^2} q^{\alpha} q^{\mu}$$

- **$C^V(Q^2)$** from electron data (MAID analysis with CVC)
- **$C^A(Q^2)$** from fit to neutrino data (experiments on hydrogen/deuterium),
so far only **C_5^A determined**, for other axial FFs only educated guesses

Pion Production



10 % error in $C_5^A(0)$

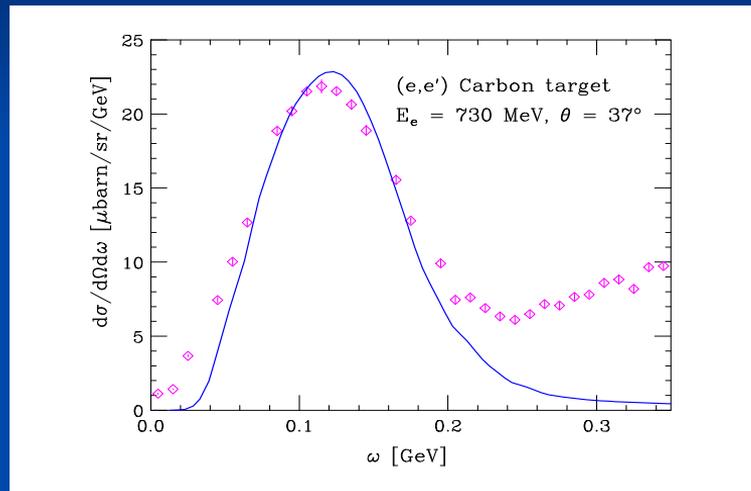
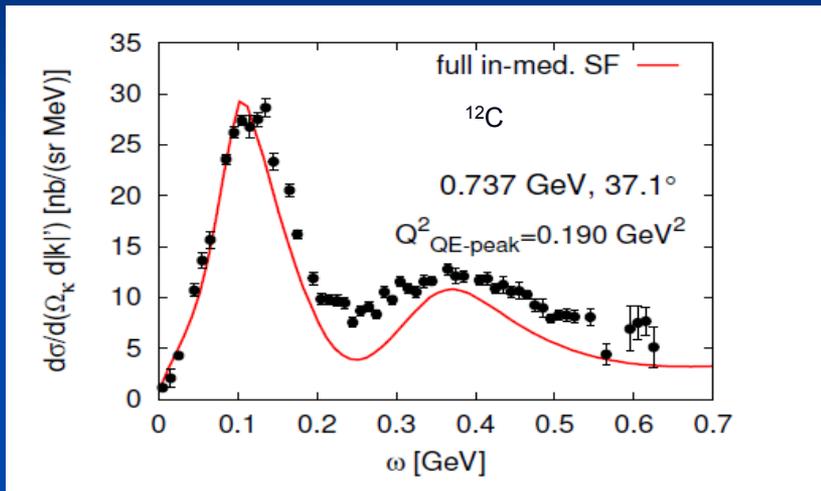
data:
PRD 25, 1161 (1982), PRD 34, 2554 (1986)

discrepancy between elementary data sets
→ impossible to determine 3 axial formfactors

New pion data on elementary target desperately needed!

Electrons as Benchmark for GiBUU

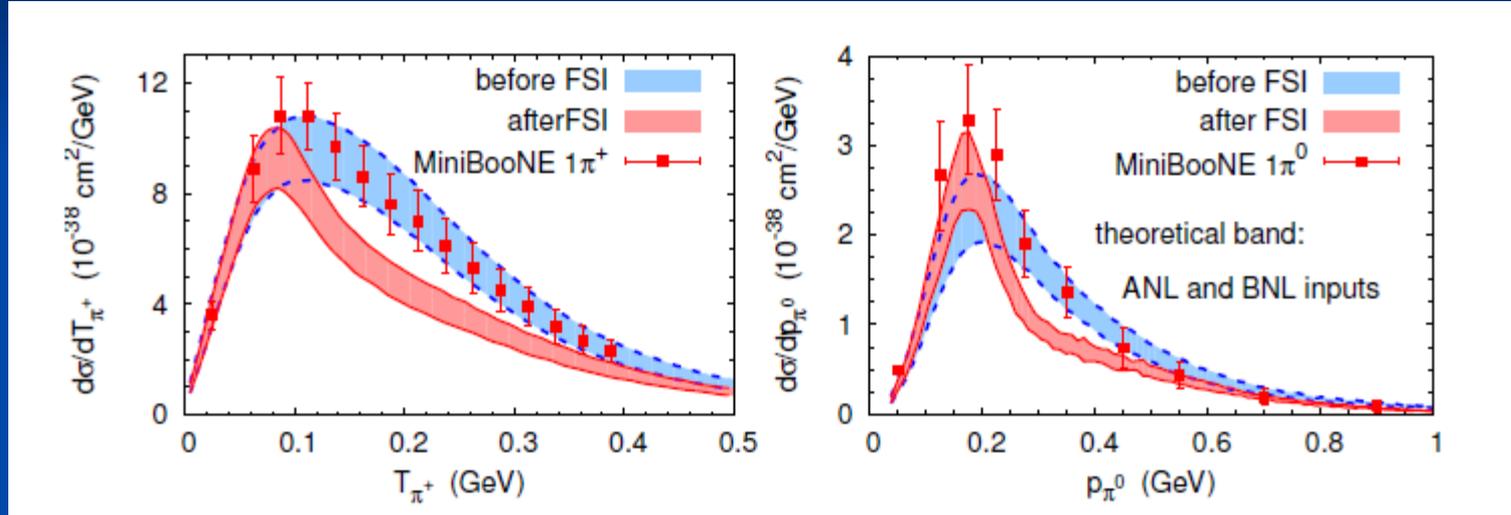
Trouble for neutrinos: ω must be reconstructed



No free parameters!
no 2p-2h, contributes
in dip region and under Δ

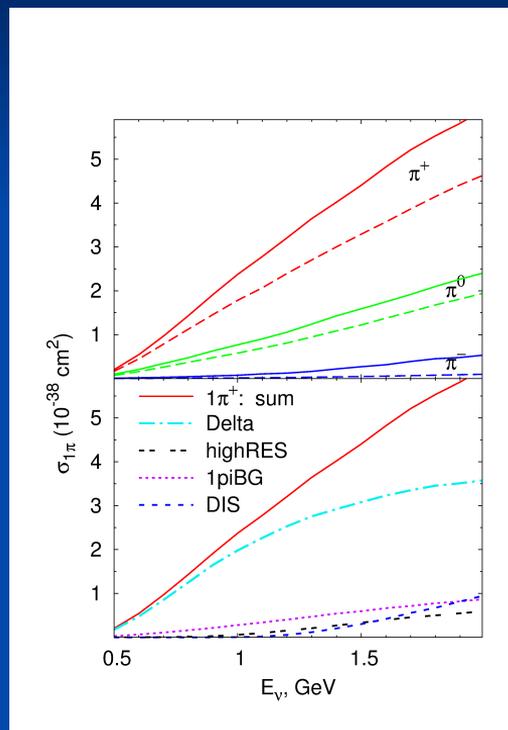
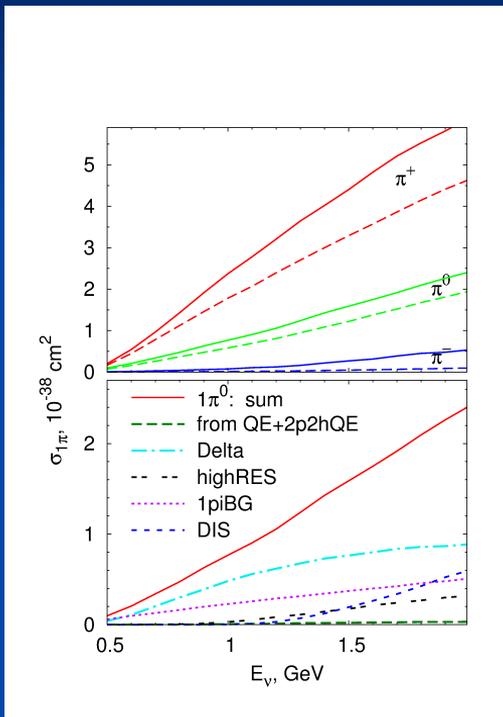
O. Benhar, spectral fctn

Pion Spectra in MB



Strong fsi effect ($\pi + N \rightarrow \Delta$, $\Delta + N \rightarrow NN$) not seen in data

Pion Production in T2K

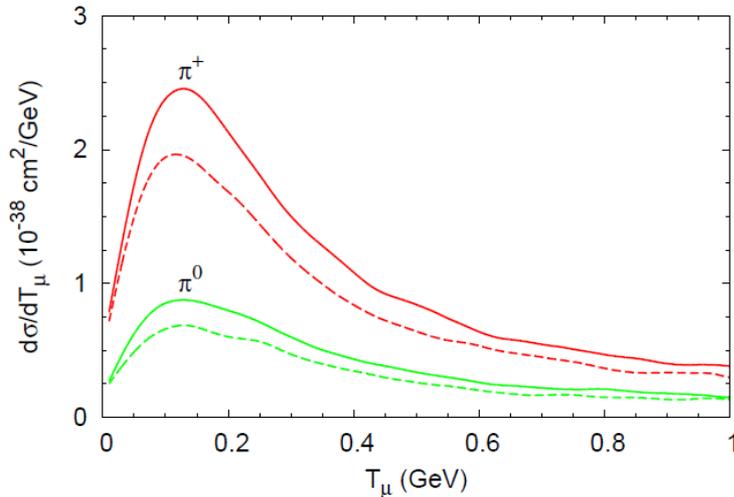
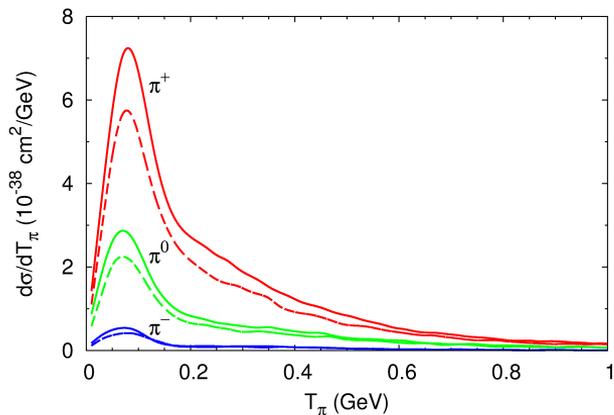


Δ dominant
only up to 0.8 GeV

*Measurement
of π^+ production
between about
0.5 and 0.8 GeV
would be clean probe
of Δ dynamics.*

Pion Production in T2K

O.L., U.M.: Phys.Rev. C88 (2013) 017601



Upper curve: BNL input, lower curve: ANL input

T2K pion data may help to distinguish between ANL and BNL input



Oscillation and Energy Reconstruction

- For nuclear targets QE reaction must be identified to use the reconstruction formula for E_ν
exp: 1 lepton, no pion, any number of other hadrons
- *But:* exp. definition of QE cannot distinguish between true QE (1p-1h), N^* and 2p-2h interactions
- Many different reaction mechanisms, besides true QE, can contribute to the same outgoing lepton kinematics



Energy Reconstruction by QE

- CCQE scattering on neutron at rest

- Energy

$$E_\nu^{\text{rec}} = \frac{2(M_n - E_B)E_\mu - (E_B^2 - 2M_n E_B + m_\mu^2 + \Delta M^2)}{2 \left[M_n - E_B - E_\mu + |\vec{k}_\mu| \cos \theta_\mu \right]}$$

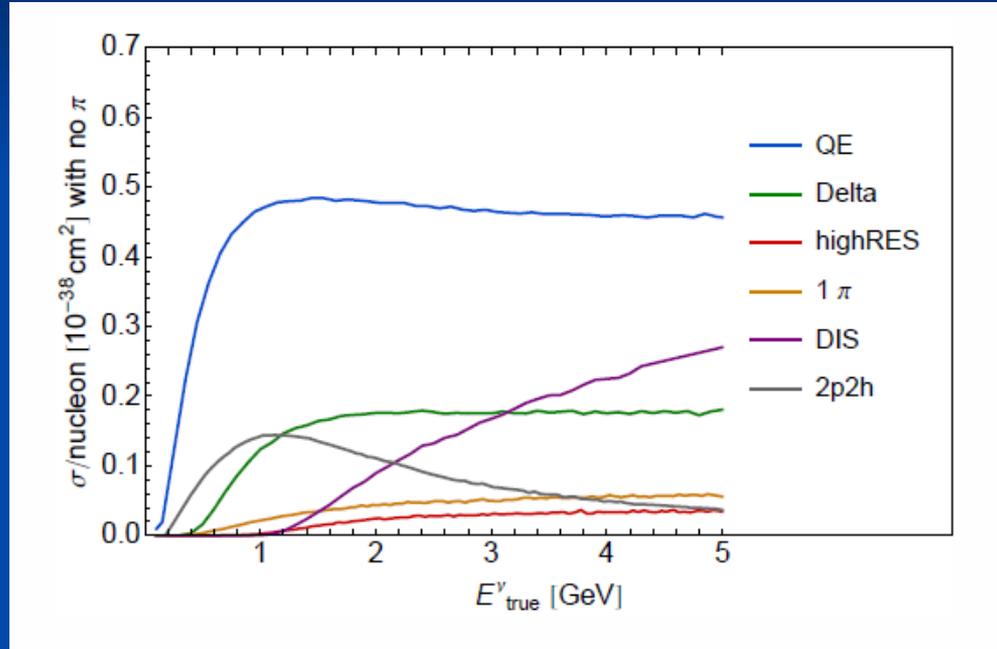
- Q^2

$$Q_{\text{rec}}^2 = -m_\mu^2 + 2E_\nu^{\text{rec}} (E_\mu - |\vec{k}_\mu| \cos \theta_\mu)$$

- Energy reconstruction tilts spectrum, affects Q^2 distribution at small Q^2

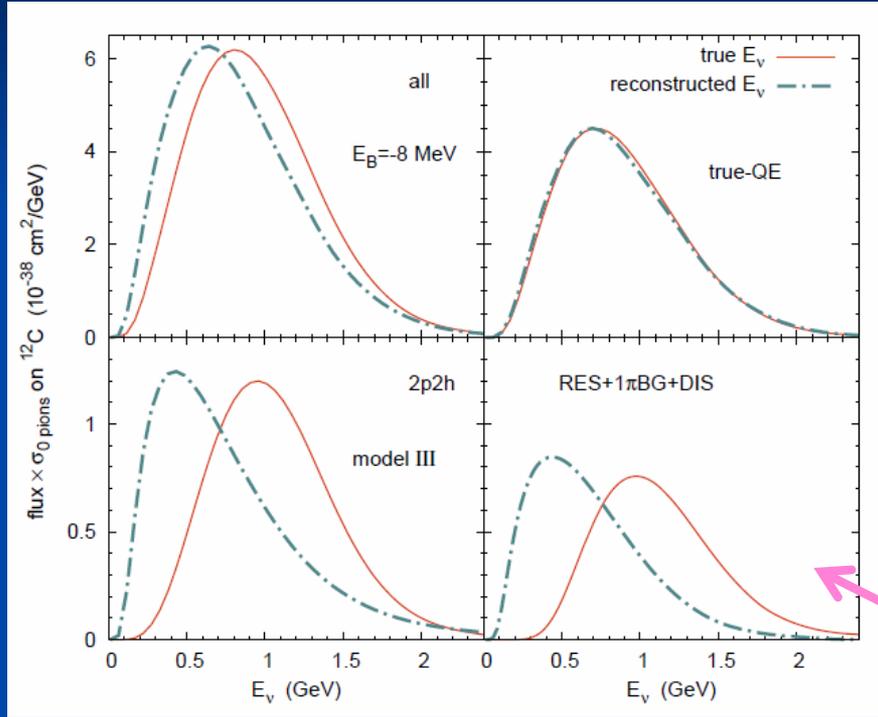
0 Pion Events from GiBUU

From Coloma & Huber: arXiv:1307.1243v1



Energy reconstruction in MB

Event rates = flux x crosssection



Reconstructed energy shifted to lower energies for all processes beyond QE
Reconstruction must be done for 0 pion events
Not only 2p-2h important

NOT contained in Nieves model

MiniBooNE flux

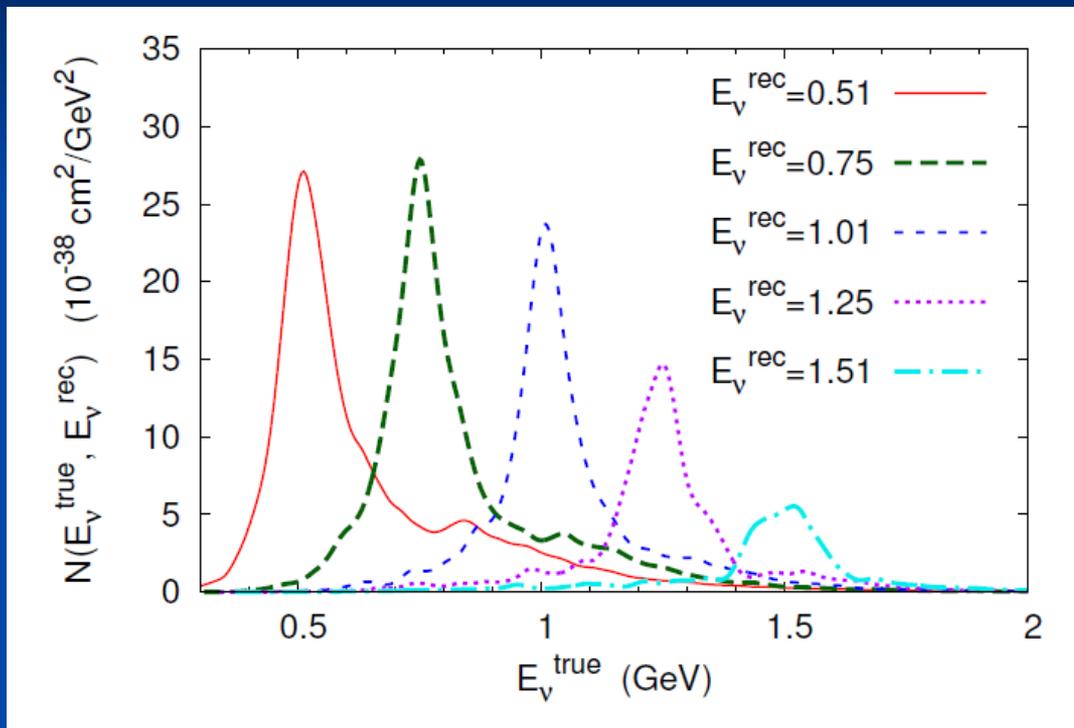
JPARC 02/2014



Institut für
Theoretische Physik



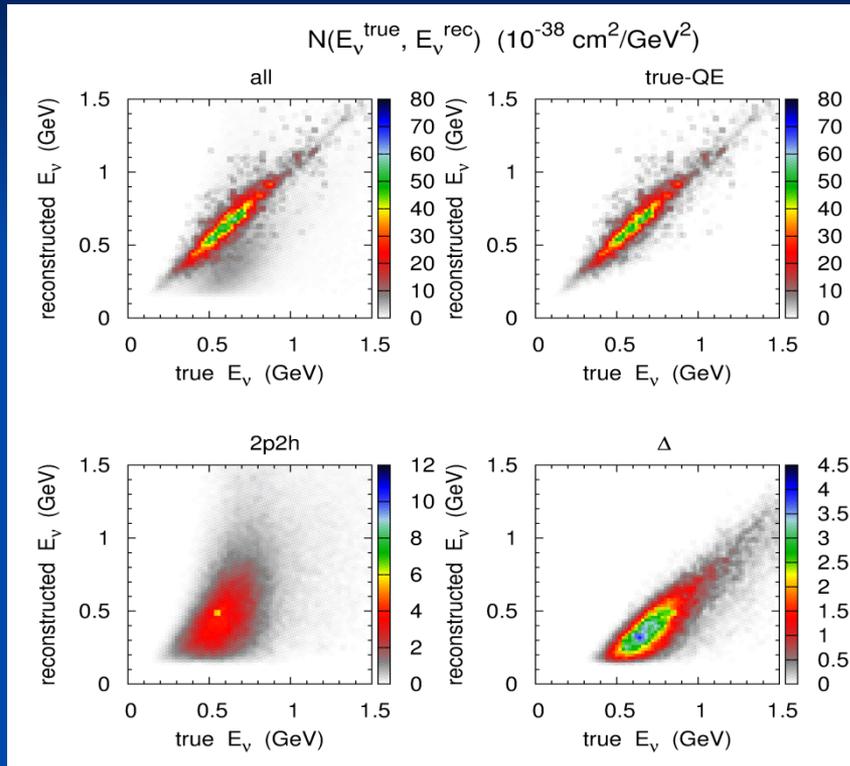
Energy-Reconstruction



Reconstr. energy contains a superposition of many true energies:

1. broadening due to Fermi motion
2. High energy tails due to reaction mechanisms other than QE

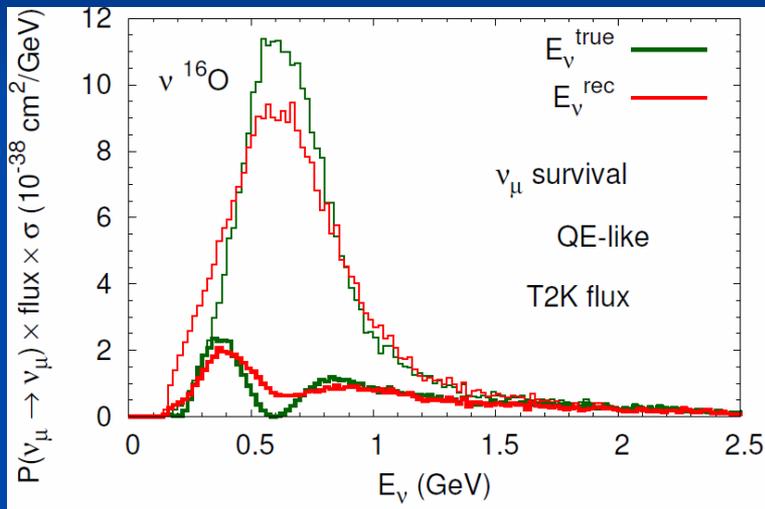
T2K migration matrix



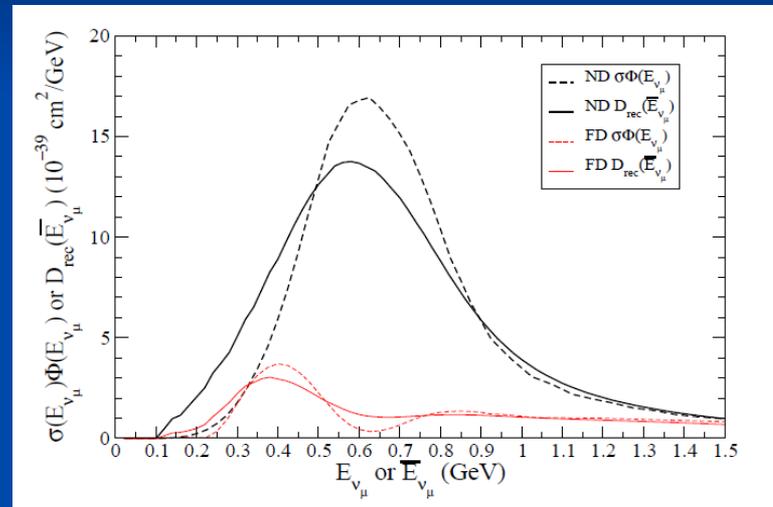
T2K Flux
Target: ^{16}O

Oscillation signal in T2K

ν_μ disappearance



GiBUU

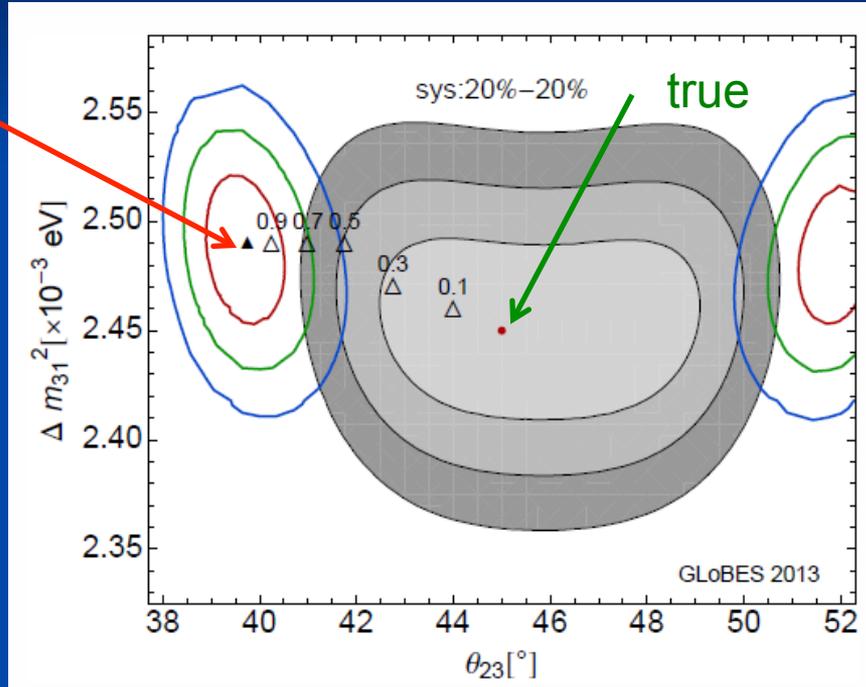


Martini



Sensitivity of oscillation parameters to nuclear model

reconstructed from naive QE dynamics

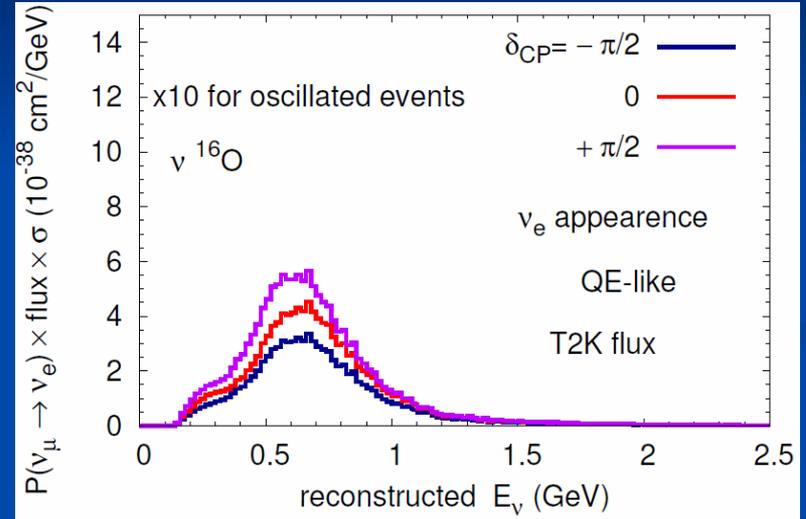
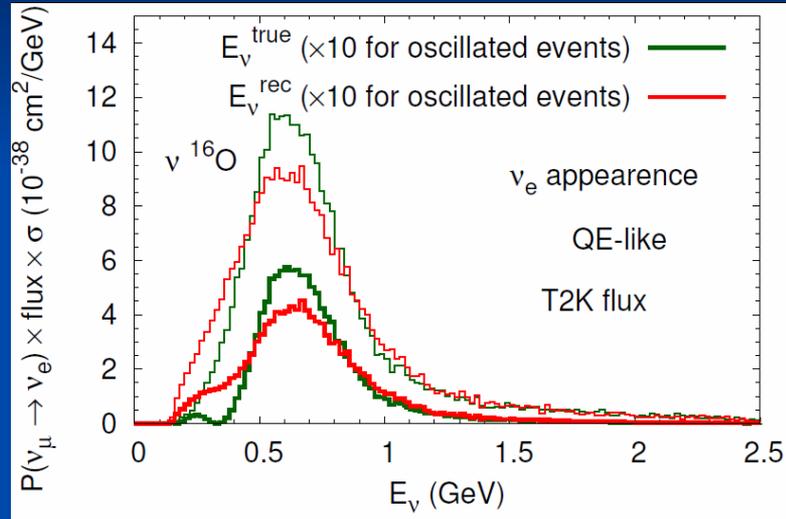


P. Coloma, P. Huber,
arXiv:1307.1243, July 2013
Analysis based on GiBUU

T2K

Oscillation signal in T2K

δ_{CP} sensitivity of appearance expts



Uncertainties due to energy reconstruction
as large as δ_{CP} dependence

Sensitivity of T2K to Energy Reconstruction

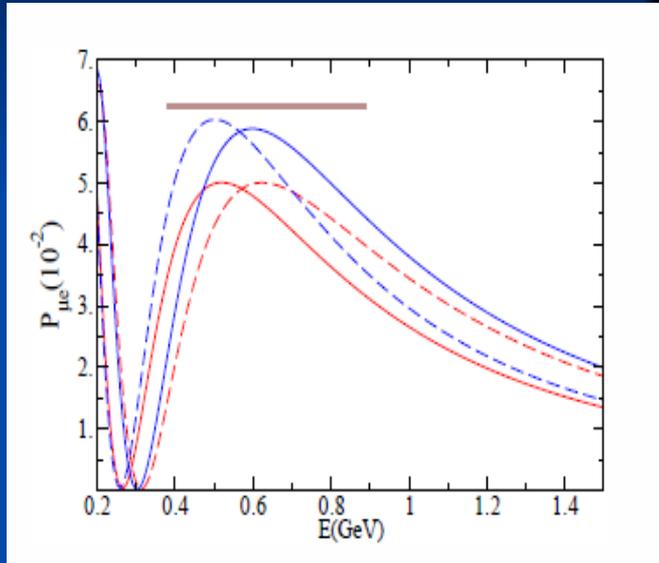
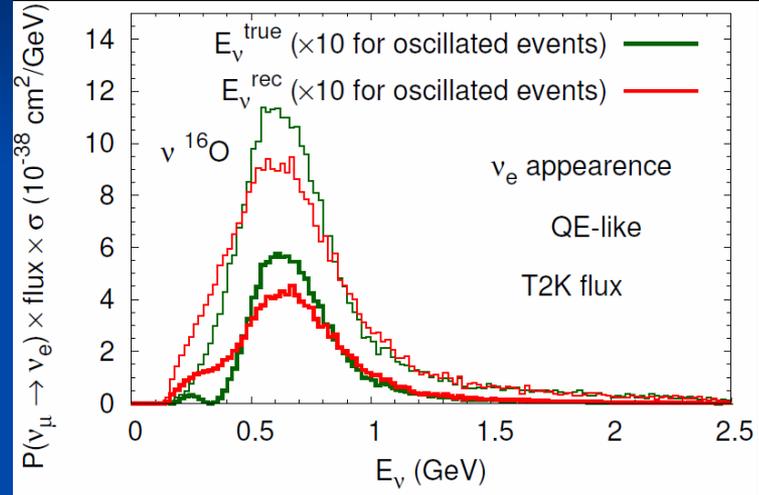


Fig. 2. $P_{\mu e}$ in matter versus neutrino energy for the T2K experiment. The blue curves depict the normal hierarchy, red the inverse hierarchy. Solid curves depict positive θ_{13} , dashed curves negative θ_{13}

D.J. Ernst et al., arXiv:1303.4790 [nucl-th]



Summary

- Energy and Q^2 reconstruction essential for precision determination of neutrino oscillation parameters (and neutrino-hadron cross sections)
- Energy and Q^2 reconstruction requires reliable event generators, of same quality as experimental equipment
- Precision era of neutrino physics requires much more sophisticated generators and a dedicated effort in theory



Generators

- Generator is an important part of any experiment:
Need generator for transformation
reconstructed energy \rightarrow true energy
- at the end of a very sophisticated experiment you do not want to have someone with a ‚crummy‘ code to mess up your data!
- **Generator-Development must be integral part of any experiment (and its funding)!**



Precision era requires better generators

- Present generators have evolved into a patchwork of theories, recipes and fit parameters without any theoretical justification and loose predictive power
- It is thus time to critically scrutinize existing generators, take the best parts from any of them, supplement them with consistent theory and build a

ν -GENIE (or NEUT)



Precision era requires better generators

What needs to be done? Theory

1. Develop consistent framework for many-body effects: spectral functions + couplings, consistent groundstates
2. Theory must comprise besides QE also pion and DIS region because all are entangled
3. Parametrize hadron tensors as function of relevant kinematical variables for use in generators
4. Consistency of inclusive and exclusive X-sections
5. Improve all important final state interactions



Guiding Principles for a new Generator

- **Consistency:**

e.g., same ground state for all subprocesses (negative example: combine free uniform Fermi gas with bound state local gas)

- **Detailed balance:**

e.g.: $\Delta + N \rightarrow NN$ (pionless Delta decay) must be related to $N + N \rightarrow \Delta + N$ (negative example: just take out 20% Δ s)

- **Relativity:**

e.g., generator collision criterion $\sigma = \pi d^2$ is incorrect

- **Correct:** in nuclear structure and reaction theory

