



Lambda baryons from lattice QCD - from strange to charm -

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Our target is Λ

Negative parity Λ (1405)

- difficulty in mass reproduction in quark models
- possibility of meson-baryon (NK , $\pi\Sigma$) molecule
- NK strong attraction
- Has been problematic in Lattice QCD analyses
- Recently $\Lambda(1405)$ was identified in lattice QCD calculation
PRL 108, 112001 (2012)

Lattice
QCD

Spin-orbit partner of Λ

- Properties of spin 3/2 Λ , which is the $\Lambda(1405)$'s partner

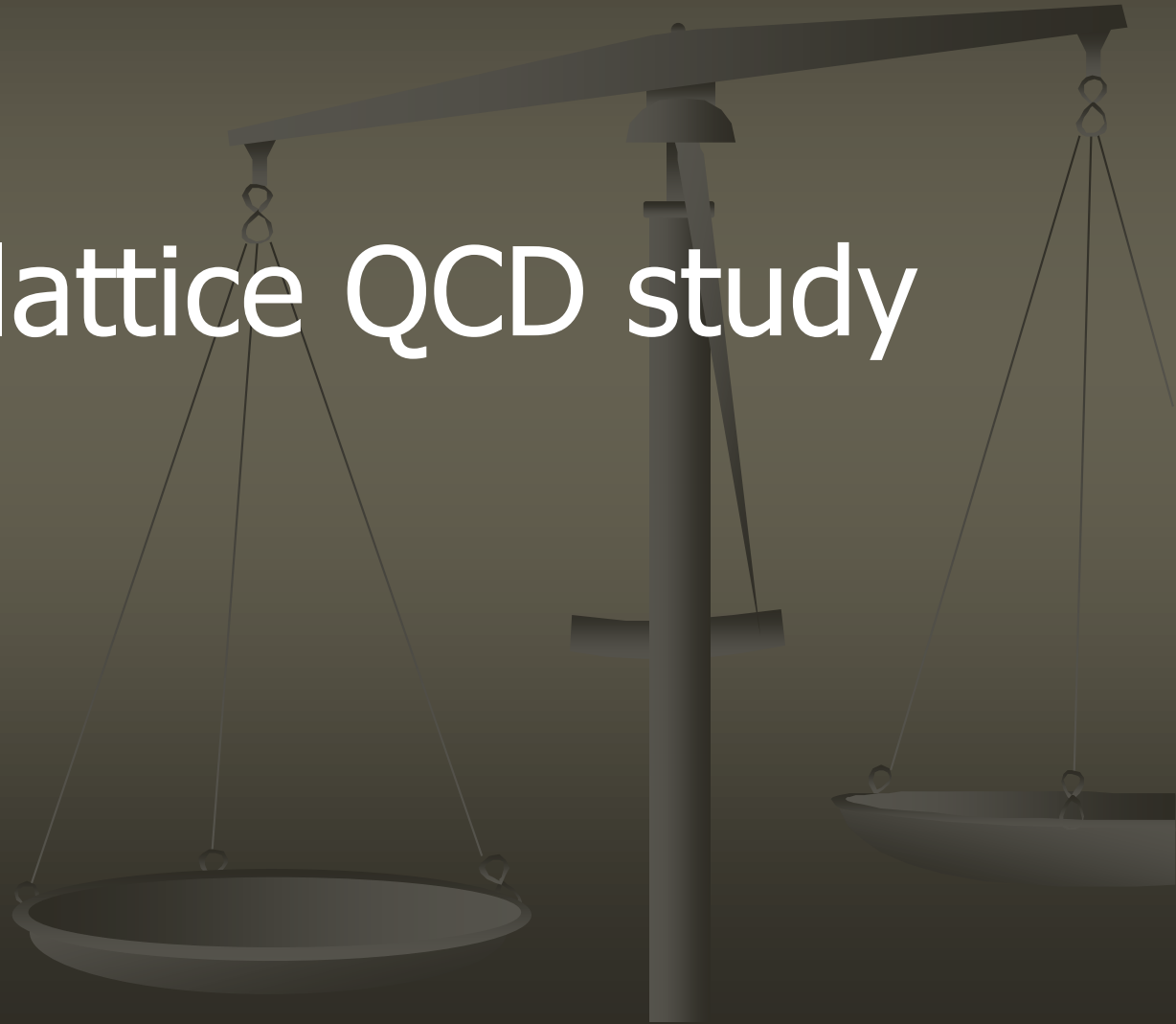
$\Lambda(1405)$'s structures

- Flavor structures
Internal wavefunctions

Λ_c 's properties

- properties of Λ_c , where the strange is replaced with the charm
- What does the HQ symmetry cause?

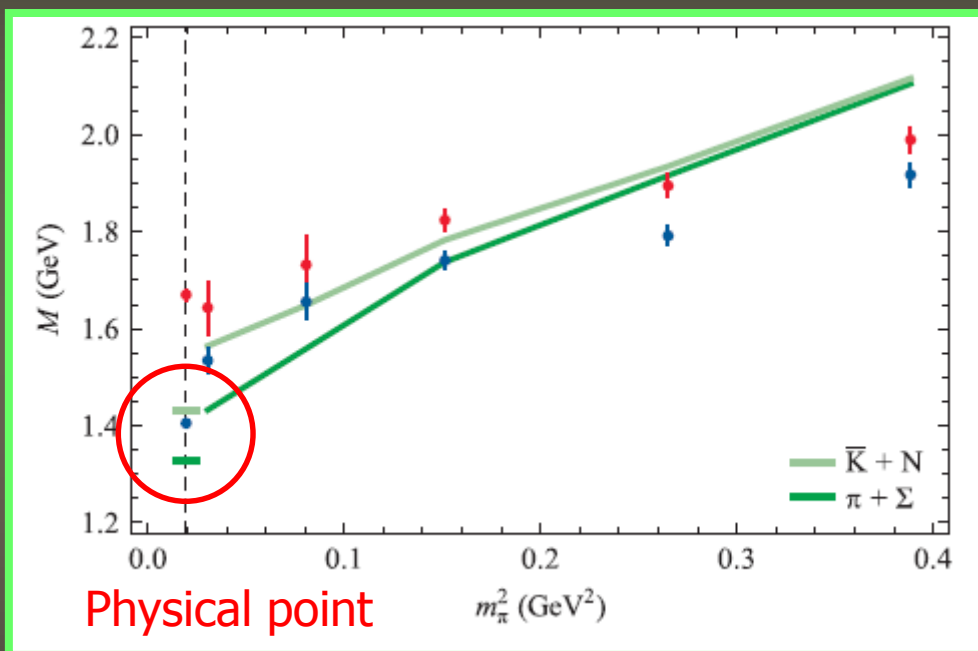
Recent lattice QCD study



Recent Lattice study of Λ

Isolating the $\Lambda(1405)$ in Lattice QCD,
Adelaide group ; PRL 108, 112001 (2012)

2+1 conf. by PACS-CS
Pion mass \rightarrow 156~702 MeV



Brief summary

- Correlation matrix analyses with many types of interpolating fields
- lowest state lies between $\bar{K}N$, $\pi\Sigma$ thresholds
 - \rightarrow Same order as the real world
 - \rightarrow Claim to have identified $\Lambda(1405)$ signal

Still too heavy

- Adjusted the valence s-quark mass so as to correctly reproduce the K-meson mass (partially quenching)

Gets experimental value

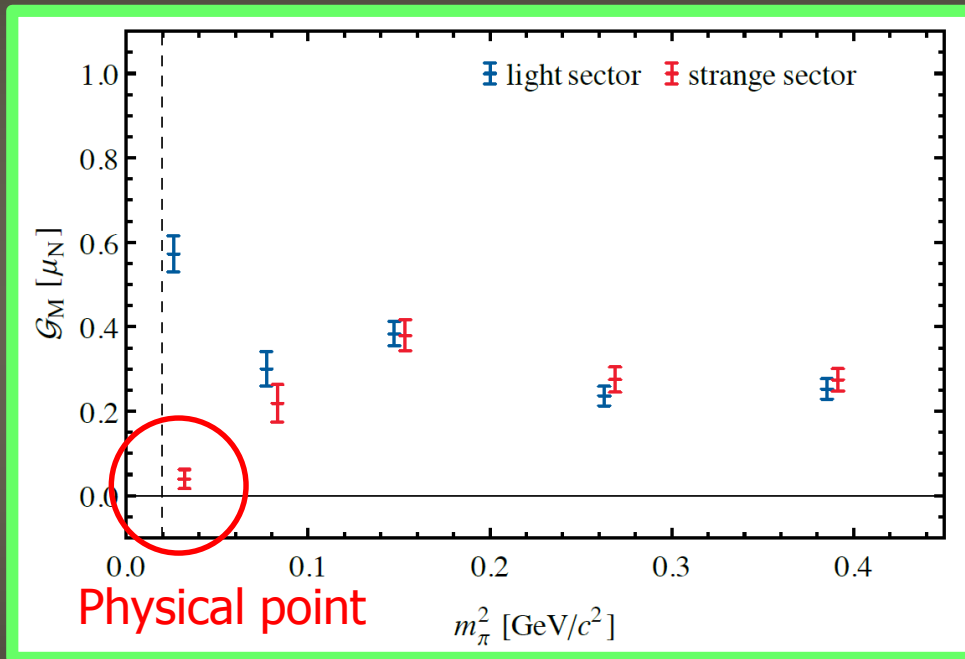
- lowest \rightarrow singlet dominant
- 2nd lowest \rightarrow octet dominant

Recent Lattice study of Λ

Lattice QCD Evidence that the $\Lambda(1405)$ Resonance is an Antikaon-Nucleon Molecule
Adelaide group ; Phys.Rev.Lett. 114 (2015) 13, 132002

2+1 conf. by PACS-CS

Pion mass \rightarrow 156~702 MeV



Electromagnetic properties

- Strange-quark magnetic moments in $\Lambda(1405)$ vanishes.

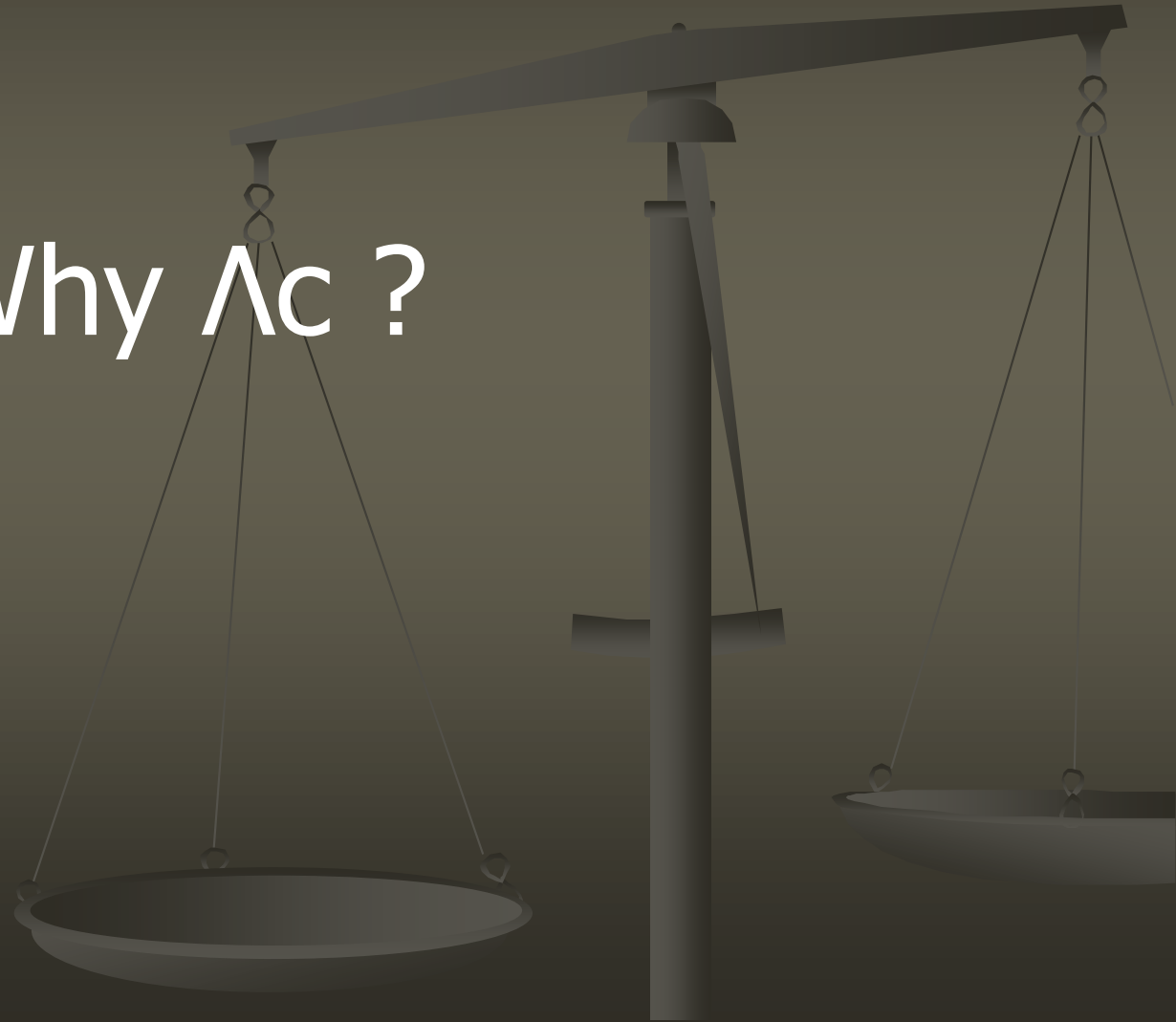
\rightarrow The strange quark is confined in the spin-0 Kaon in $\Lambda(1405)$

There are several issues to be clarified, but the signal can be the $\Lambda(1405)$.

K

N

Why Λ_c ?

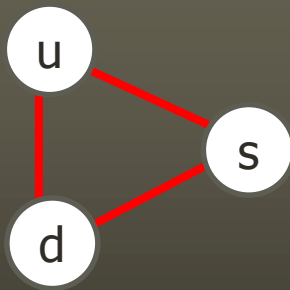


Our target is Λ

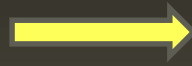
udS - Λ

$$m_u = m_d < m_s$$

SU(3)_F symmetry



Replace S with C



udC - Λ

$$m_u = m_d \ll m_c$$

Heavy quark spin symmetry appears

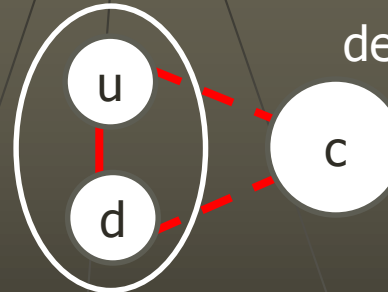
Spin-spin interactions become weak

Heavy quark spin decouples and is irrelevant

Largely broken SU(3)_F symmetry

Two excitation modes may decouple

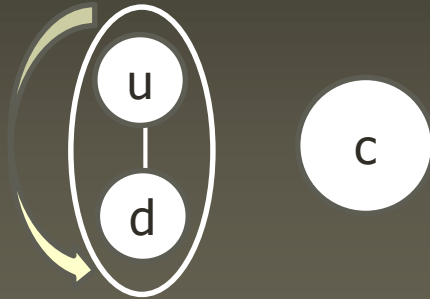
Hadron spectra would be much simpler



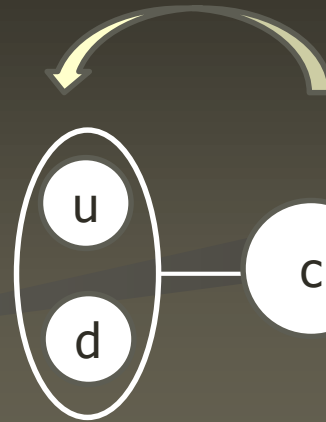
Manifestation of Diquark DOF ?

Diquarks

Two diquark motion (ρ and λ modes) may decouple in heavy baryons

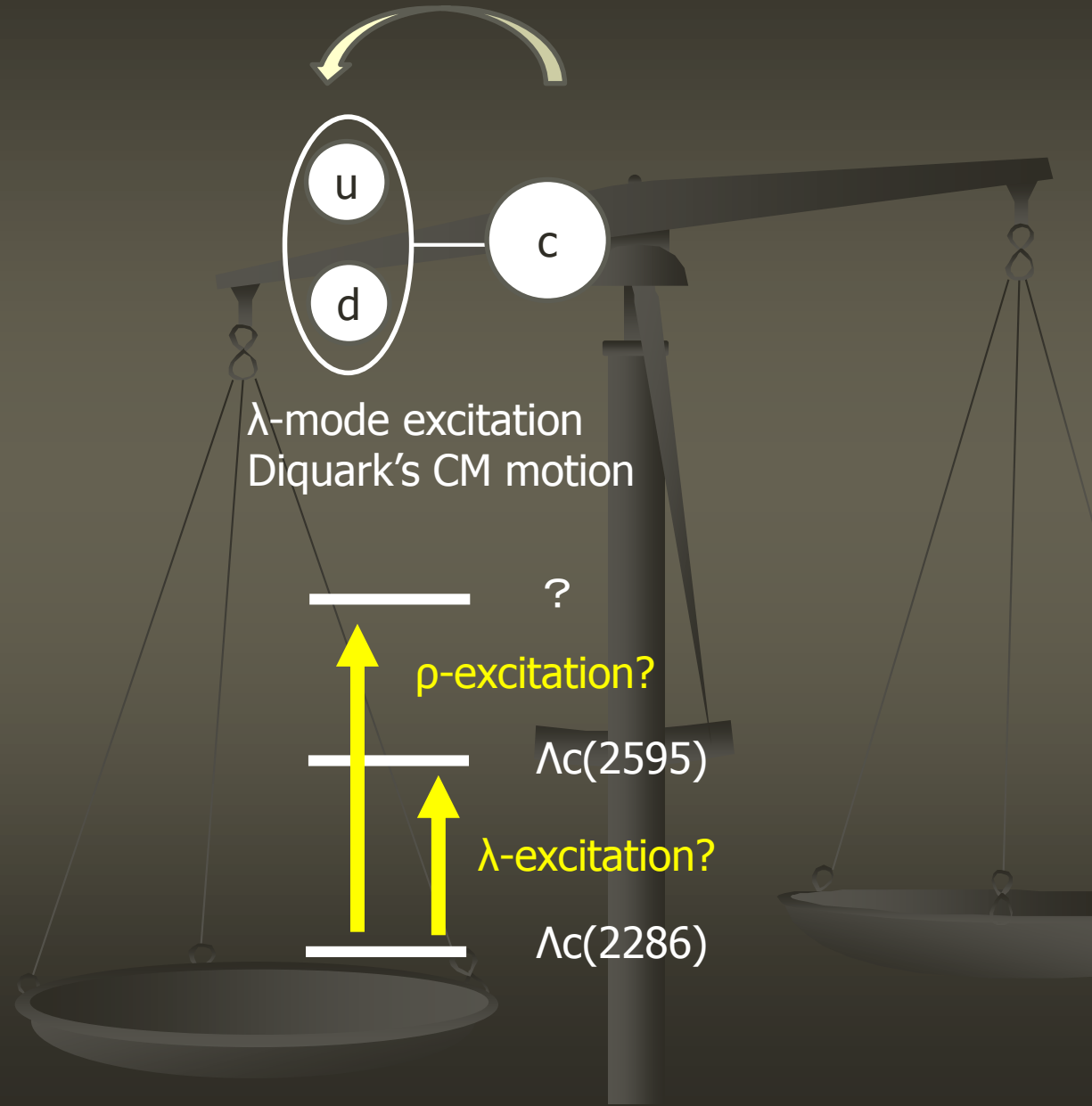


ρ -mode excitation
Diquark's relative motion



λ -mode excitation
Diquark's CM motion

Then, excited Λ_c spectra
can be simply explained
in terms of diquarks (?)



Diquarks

Replace S with C



udS - Λ

udC - Λ

$$m_u = m_d < m_s$$

$$m_u = m_d \ll m_c$$

SU(3)_F symmetry

HQ symmetry

— $\Lambda(1670)$

Octet?

— $\Lambda(1405)$

Singlet?

— $\Lambda(1116)$

Octet

?

— ?

ρ -excitation?

— $\Lambda_c(2595)$

λ -excitation?

— $\Lambda_c(2286)$

Then, what is the relationship between uds- Λ and udc- Λ ?

→ Internal structure change

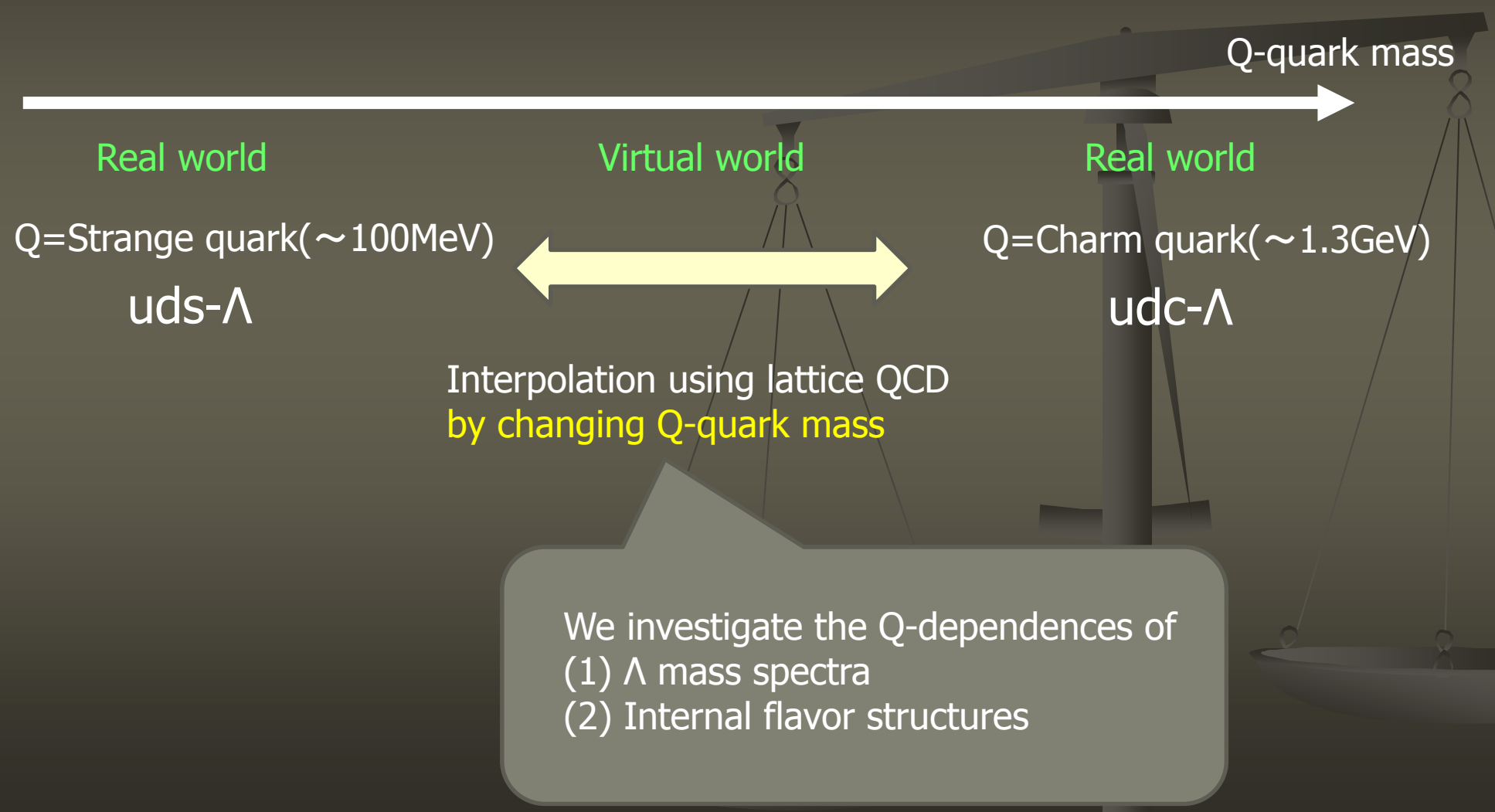
→ Manifestation of diquark's degrees of freedom

Strategies



Our strategy

We investigate **masses and flavor structures** of **udQ- Λ** baryons

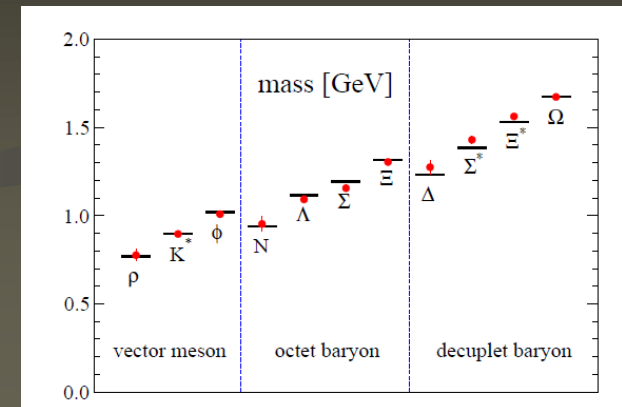


Our strategy

-- Lattice QCD setups --

2+1 gauge configuration by PACS-CS
Iwasaki gauge action, Wilson quark action
 $32^3 \times 64$, $a \sim 0.1$ fm, cut off ~ 2.2 GeV

→ Well reproduces light hadron mass spectra



We do not employ Relativistic Heavy Quark actions

- cut off of 2.2 GeV may be insufficient for $m_Q > 1$ GeV
- not good, but use a common quark action for u, d, Q quarks in order to see the internal structure changes

Our strategy

-- Hadronic operators --

We employ operators classified in terms of Cubic group irreducible rep.

→ 4x4 correlation matrix (We can extract **ground ~ 3rd excited states.**)

u, d, Q quark operator **sizes are the same.**

→ Operator mixing vanishes in the flavor-SU(3) limit ($m_u = m_d = m_Q$)

→ Easy to see the flavor structures of Λ particles

PRD72 (2005) 074501
LHPC group

Operator examples

TABLE VIII: Quasi-local Λ baryon operators.

$\bar{\Psi}_{S,S_z}^{\Lambda,k}$	$\bar{\Lambda}_{\mu_1\mu_2\mu_3}$	$\bar{\Psi}_{S,S_z}^{\Lambda,k}$	$\bar{\Lambda}_{\mu_1\mu_2\mu_3}$
$\bar{\Psi}_{\frac{1}{2},\frac{1}{2}}^{G_{1g},1}$	$\bar{\Lambda}_{121}$	$\bar{\Psi}_{\frac{1}{2},\frac{1}{2}}^{G_{1u},1}$	$\bar{\Lambda}_{123} + \bar{\Lambda}_{141} + \bar{\Lambda}_{321}$
$\bar{\Psi}_{\frac{1}{2},-\frac{1}{2}}^{G_{1g},1}$	$\bar{\Lambda}_{122}$	$\bar{\Psi}_{\frac{1}{2},-\frac{1}{2}}^{G_{1u},1}$	$\bar{\Lambda}_{124} + \bar{\Lambda}_{142} + \bar{\Lambda}_{322}$
$\bar{\Psi}_{\frac{1}{2},\frac{1}{2}}^{G_{1g},2}$	$\bar{\Lambda}_{143} + \bar{\Lambda}_{323} + \bar{\Lambda}_{341}$	$\bar{\Psi}_{\frac{1}{2},\frac{1}{2}}^{G_{1u},1}$	$\bar{\Lambda}_{343}$
$\bar{\Psi}_{\frac{1}{2},-\frac{1}{2}}^{G_{1g},2}$	$\bar{\Lambda}_{144} + \bar{\Lambda}_{324} + \bar{\Lambda}_{342}$	$\bar{\Psi}_{\frac{1}{2},-\frac{1}{2}}^{G_{1u},1}$	$\bar{\Lambda}_{344}$
$\bar{\Psi}_{\frac{1}{2},\frac{1}{2}}^{G_{1g},3}$	$\bar{\Lambda}_{134} + \bar{\Lambda}_{323} - \bar{\Lambda}_{341}$	$\bar{\Psi}_{\frac{1}{2},\frac{1}{2}}^{G_{1u},1}$	$-\bar{\Lambda}_{141} - \bar{\Lambda}_{312} + \bar{\Lambda}_{123}$
$\bar{\Psi}_{\frac{1}{2},-\frac{1}{2}}^{G_{1g},3}$	$\bar{\Lambda}_{144} + \bar{\Lambda}_{423} - \bar{\Lambda}_{342}$	$\bar{\Psi}_{\frac{1}{2},-\frac{1}{2}}^{G_{1u},1}$	$-\bar{\Lambda}_{322} - \bar{\Lambda}_{241} + \bar{\Lambda}_{124}$
$\bar{\Psi}_{\frac{1}{2},\frac{1}{2}}^{G_{1g},4}$	$\sqrt{\frac{2}{3}}(\bar{\Lambda}_{134} + \bar{\Lambda}_{341} + \bar{\Lambda}_{413})$	$\bar{\Psi}_{\frac{1}{2},\frac{1}{2}}^{G_{1u},4}$	$-\sqrt{\frac{2}{3}}(\bar{\Lambda}_{123} + \bar{\Lambda}_{231} + \bar{\Lambda}_{312})$
$\bar{\Psi}_{\frac{1}{2},-\frac{1}{2}}^{G_{1g},4}$	$\sqrt{\frac{2}{3}}(\bar{\Lambda}_{234} + \bar{\Lambda}_{342} + \bar{\Lambda}_{423})$	$\bar{\Psi}_{\frac{1}{2},-\frac{1}{2}}^{G_{1u},4}$	$-\sqrt{\frac{2}{3}}(\bar{\Lambda}_{124} + \bar{\Lambda}_{241} + \bar{\Lambda}_{412})$
$\bar{\Psi}_{\frac{3}{2},\frac{3}{2}}^{H_g}$	$\bar{\Lambda}_{133}$	$\bar{\Psi}_{\frac{3}{2},\frac{3}{2}}^{H_u}$	$\bar{\Lambda}_{131}$
$\bar{\Psi}_{\frac{3}{2},\frac{1}{2}}^{H_g}$	$\bar{\Lambda}_{134} + \bar{\Lambda}_{143} + \bar{\Lambda}_{233}$	$\bar{\Psi}_{\frac{3}{2},\frac{1}{2}}^{H_u}$	$\bar{\Lambda}_{132} + \bar{\Lambda}_{141} + \bar{\Lambda}_{231}$
$\bar{\Psi}_{\frac{3}{2},-\frac{1}{2}}^{H_g}$	$\bar{\Lambda}_{144} + \bar{\Lambda}_{234} + \bar{\Lambda}_{243}$	$\bar{\Psi}_{\frac{3}{2},-\frac{1}{2}}^{H_u}$	$\bar{\Lambda}_{142} + \bar{\Lambda}_{232} + \bar{\Lambda}_{241}$
$\bar{\Psi}_{\frac{3}{2},-\frac{3}{2}}^{H_g}$	$\bar{\Lambda}_{244}$	$\bar{\Psi}_{\frac{3}{2},-\frac{3}{2}}^{H_u}$	$\bar{\Lambda}_{242}$

1/2 octet (octet-1)

1/2 octet (octet-2)

1/2 octet (octet-3)

1/2 singlet

3/2 octet

Correlation matrix analyses

-- Mass and flavor structures --

2pt cross correlator QCD transfer matrix

$$\langle \Lambda^i(T) \Lambda^j(0) \rangle = \langle 0 | \Lambda^i e^{-HT} \Lambda^j | 0 \rangle = \langle 0 | \Lambda^i | k \rangle \exp(-E_k T) \langle k | \Lambda^j | 0 \rangle$$

i, j are operator indices

$$= c^T \Lambda(E_k) c$$

eigenvectors

eigenvalues

$$\Lambda(E_k) = \text{diag}(-E_1 T, -E_2 T, \dots)$$

Eigenvalue of correlation matrix \rightarrow mass of the state

Eigenvector of correlation matrix \rightarrow operator overlaps with the state

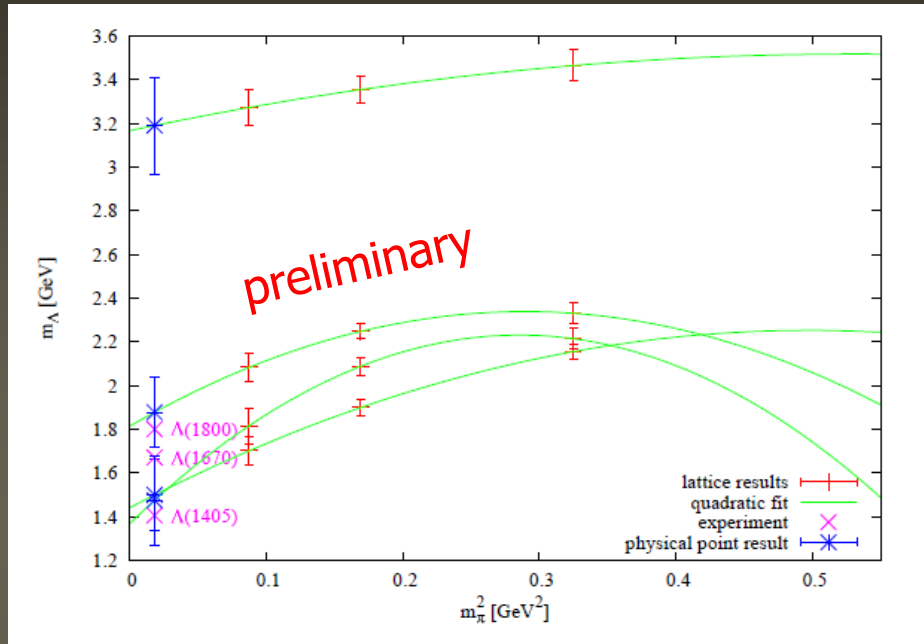
$$\langle 0 | \Lambda^i | \text{target state} \rangle$$

We can investigate internal structures.

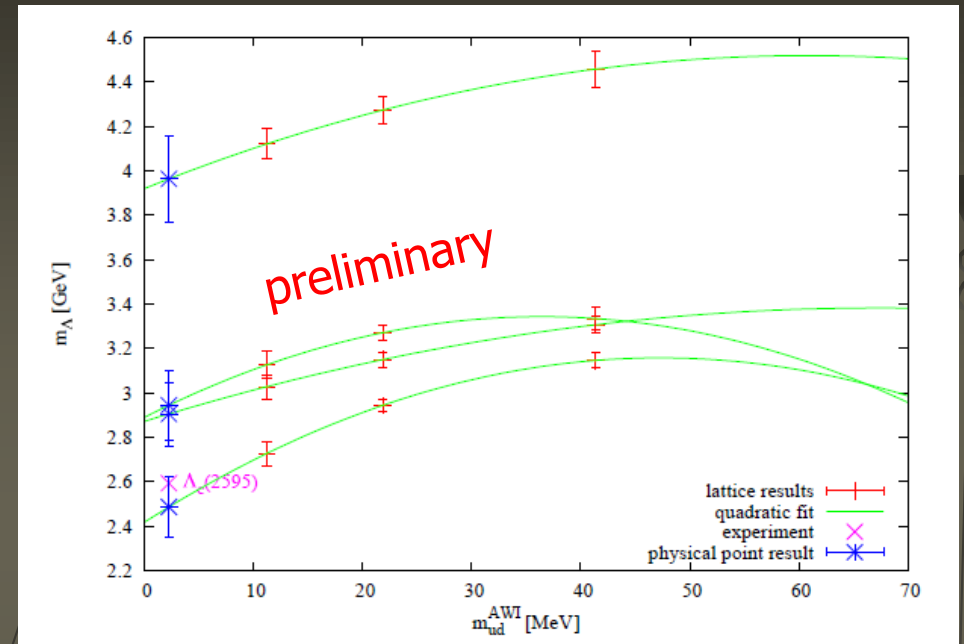
Mass spectra



1/2 negative Λ channel



1/2 negative Λ_c channel



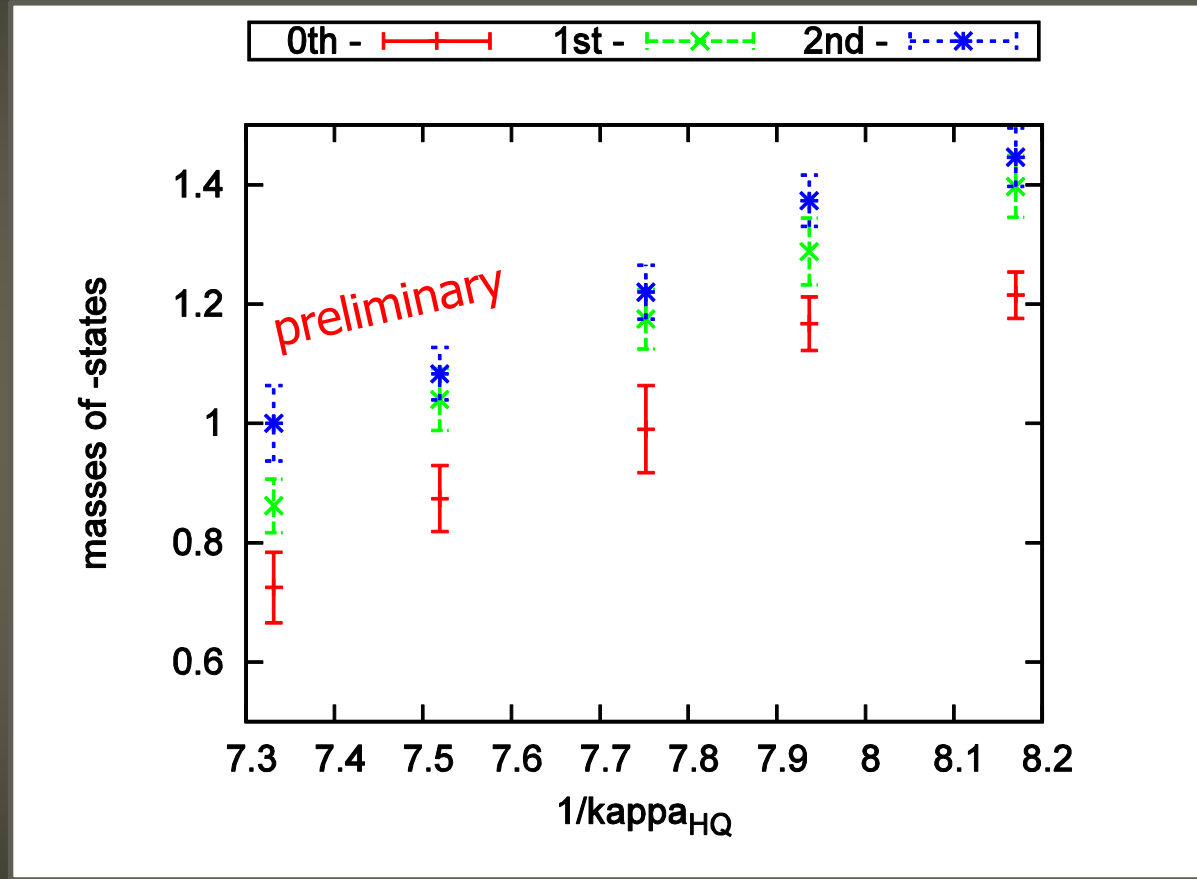
Spectra are similar in Λ and Λ_c channel

Still heavier than 1405 MeV
 → But very close

2nd state's behavior is a bit different
 from the Λ_s channel
 → Difference in internal structures

Mass spectra

Hadron mass dependences on Q-quark mass



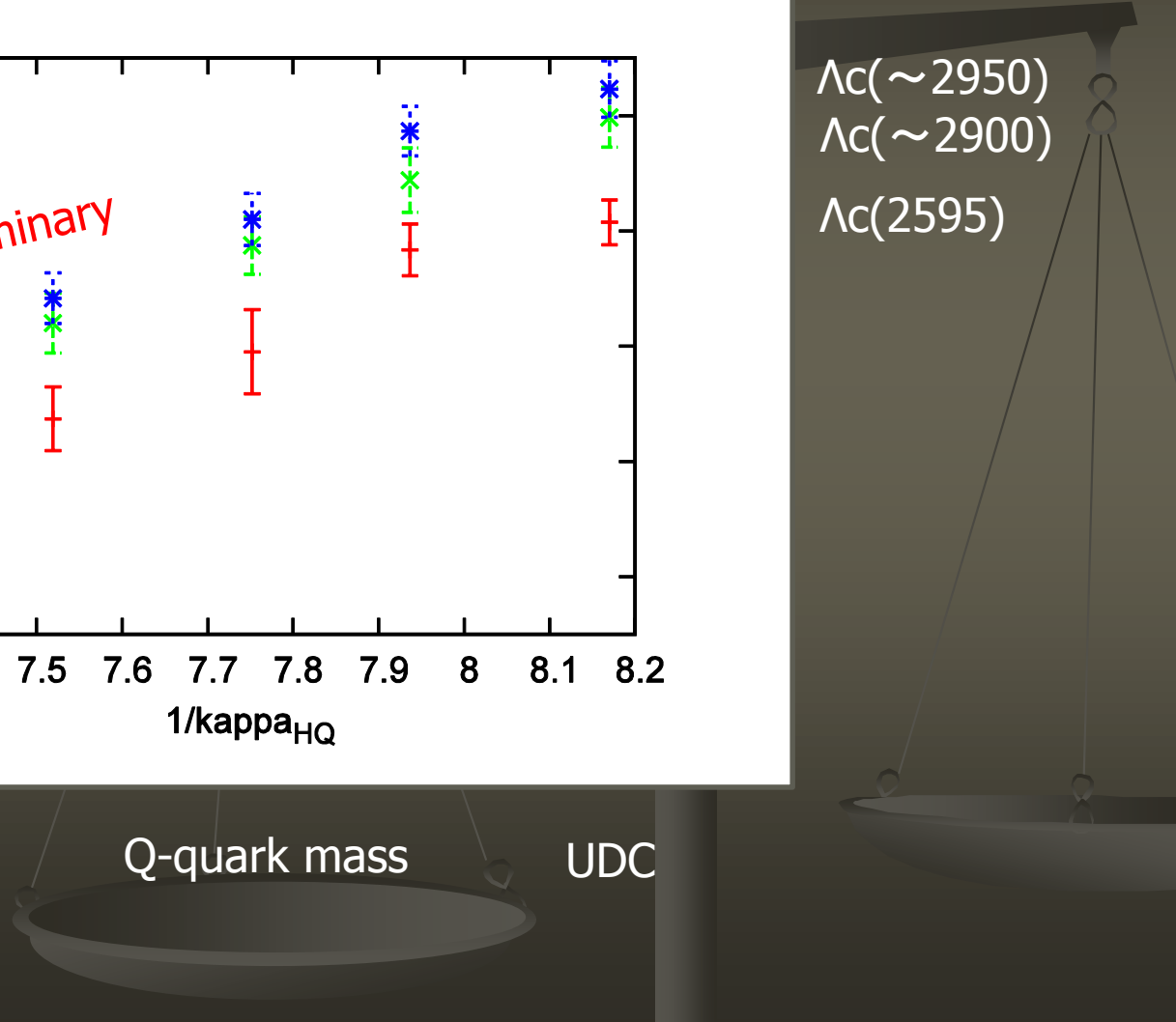
$\Lambda(1800)$
 $\Lambda(1670)$
 $\Lambda(1405)$

$\Lambda_c(\sim 2950)$
 $\Lambda_c(\sim 2900)$
 $\Lambda_c(2595)$

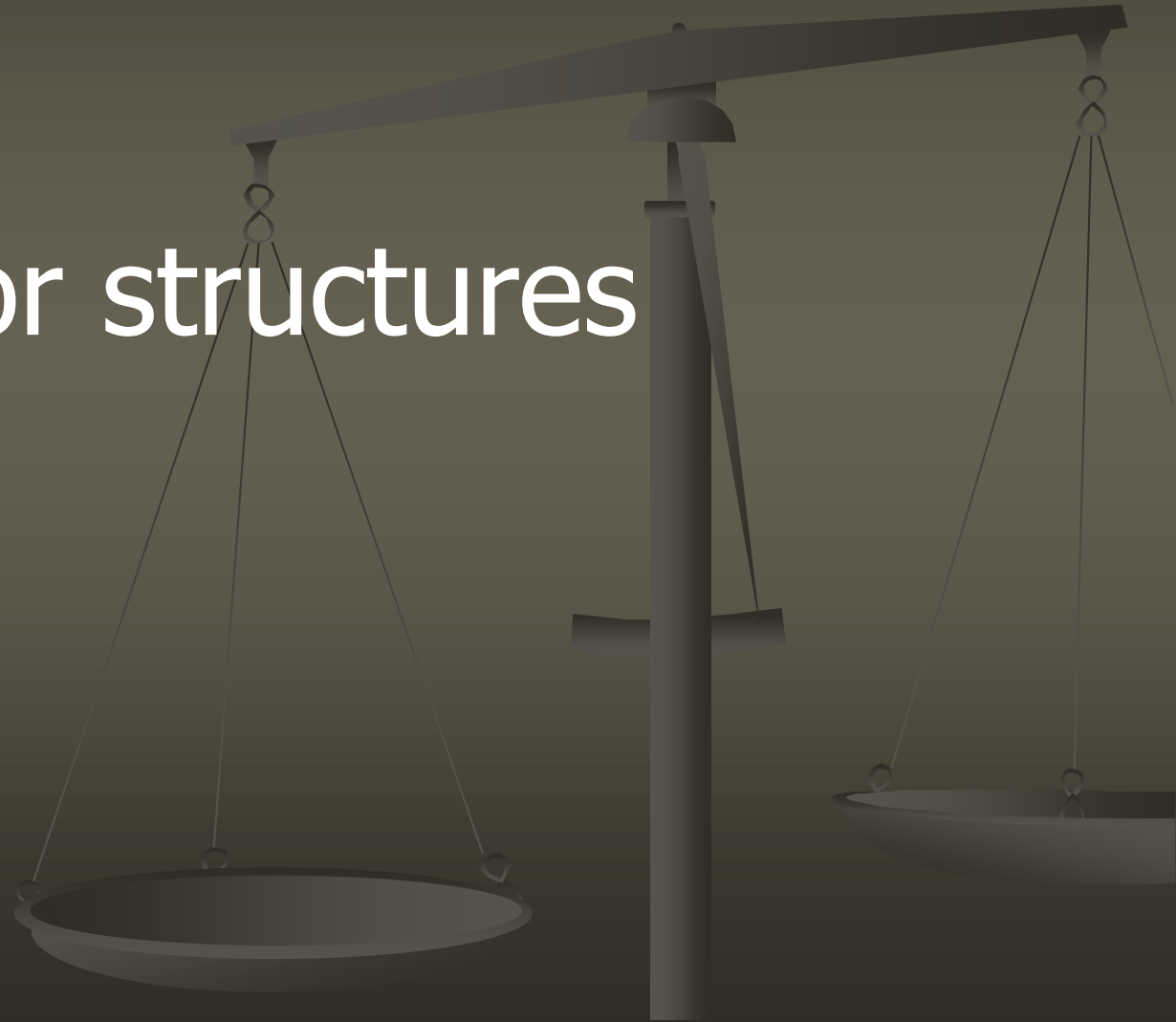
UDS

Q-quark mass

UDC



Flavor structures



Flavor structures

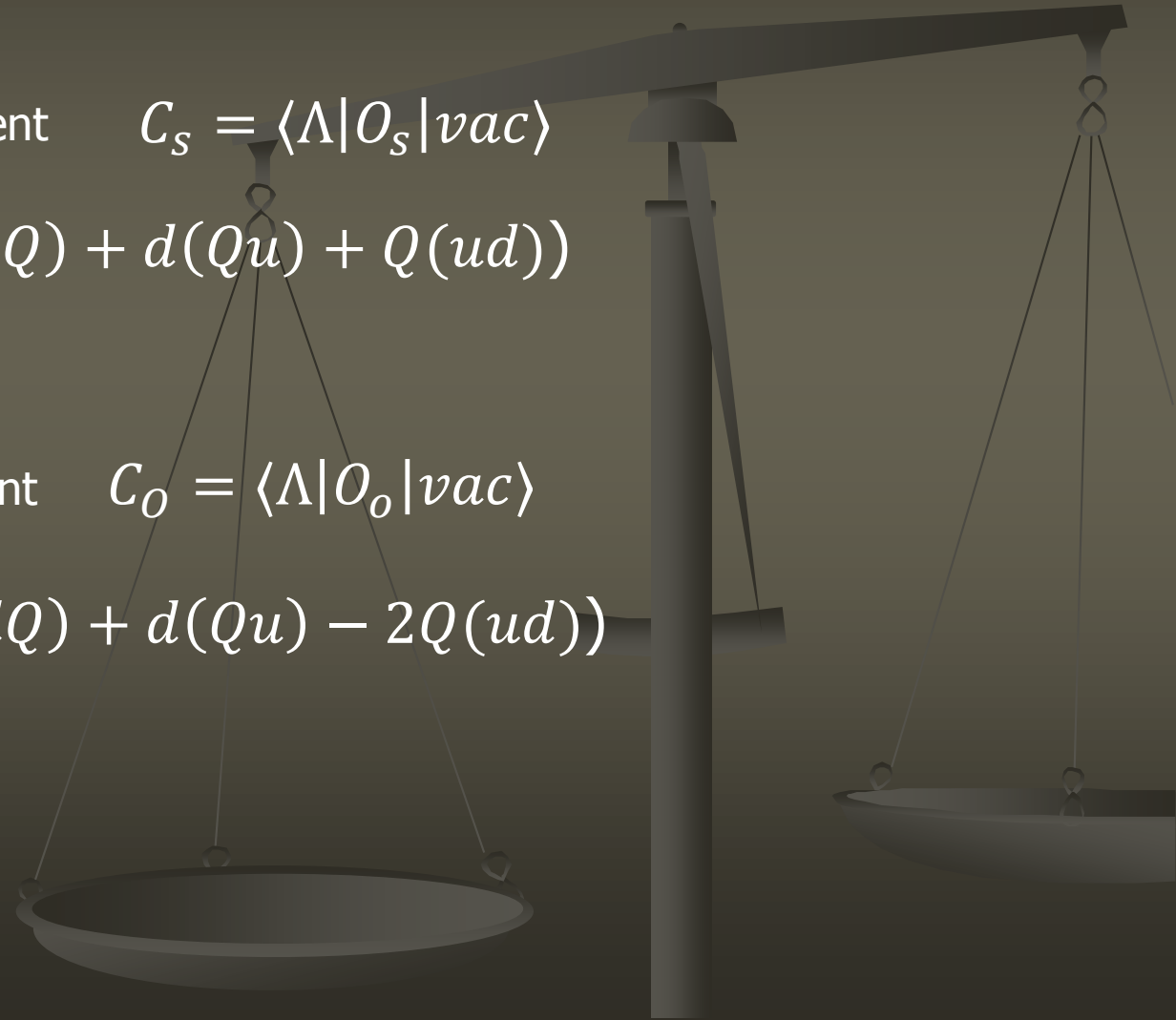
We consider "flavor symmetry" for u , d , Q quarks.
(even if Q =charm, we classify states still in terms of $SU(3)$)

Singlet component $C_s = \langle \Lambda | O_s | vac \rangle$

$$O_s = \frac{1}{\sqrt{3}} (u(dQ) + d(Qu) + Q(ud))$$

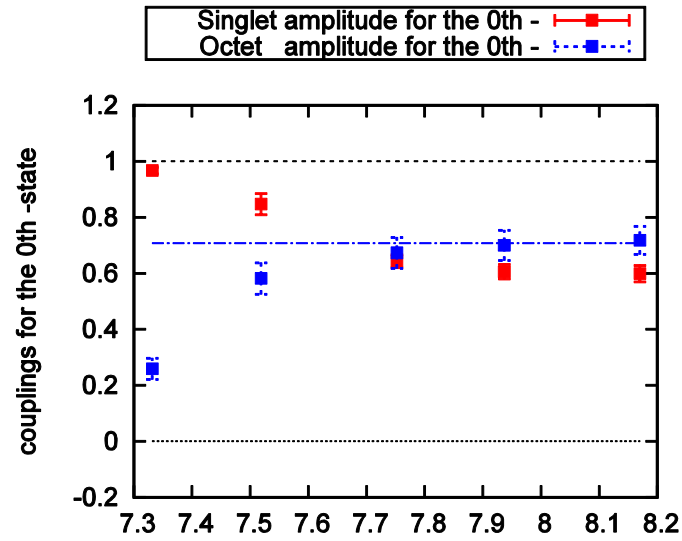
Octet component $C_o = \langle \Lambda | O_o | vac \rangle$

$$O_o = \frac{1}{\sqrt{6}} (u(dQ) + d(Qu) - 2Q(ud))$$

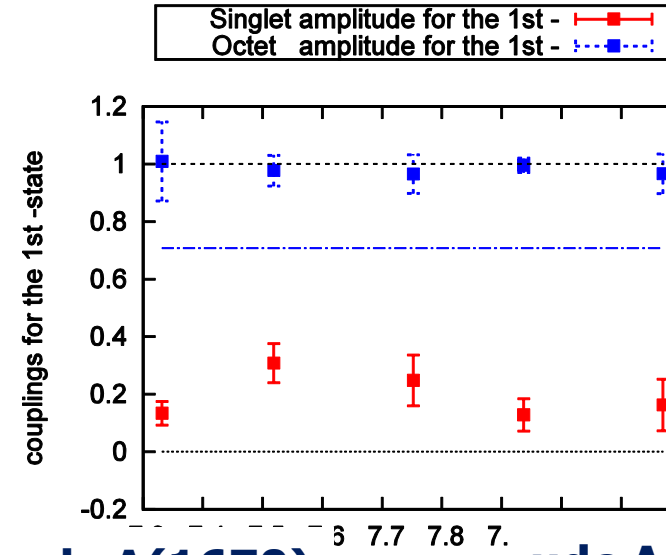


Flavor structures

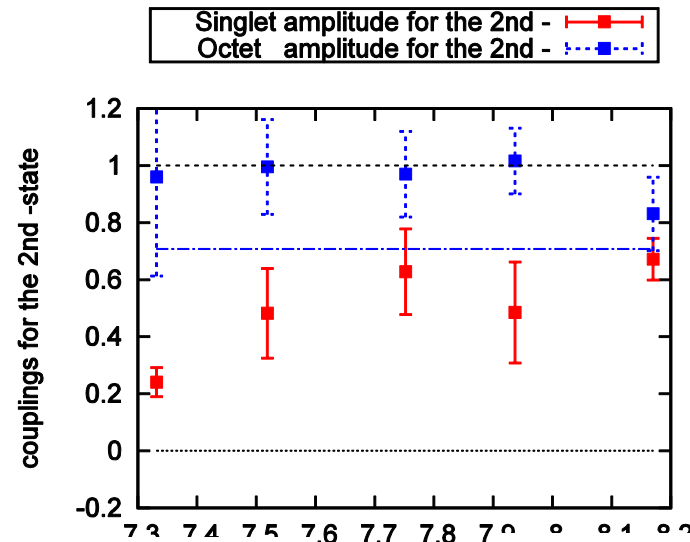
Lowest 3 states in $\frac{1}{2}$ - channel



uds $\Lambda(1405)$ $1/\kappa_{HQ}$ udc $\Lambda(2595)$



uds $\Lambda(1670)$ $1/\kappa_{HQ}$ udc $\Lambda(\sim 2900)$

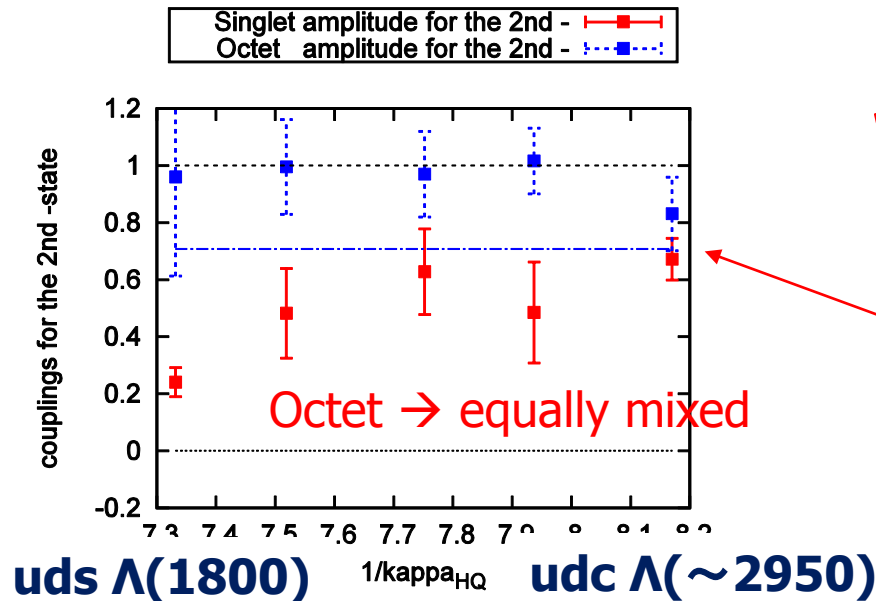
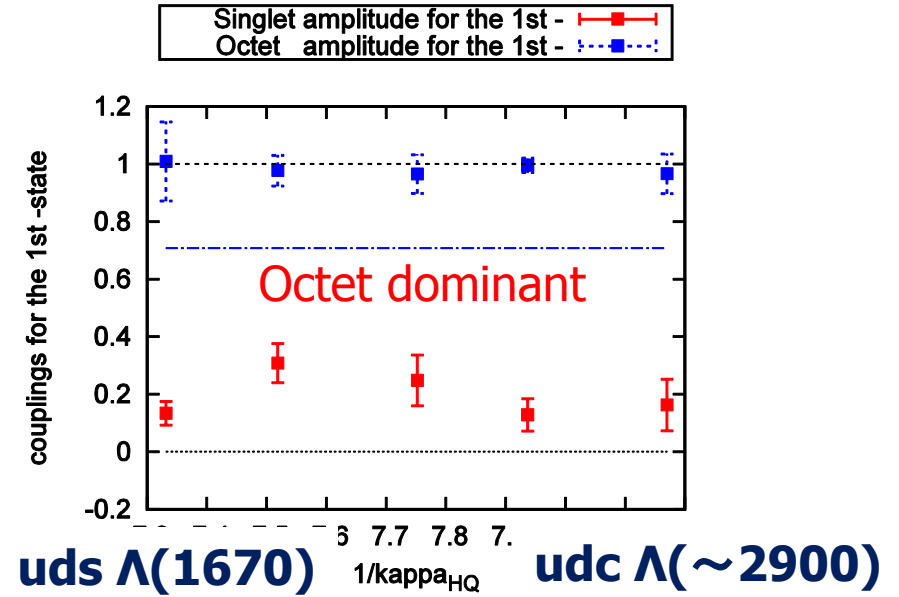
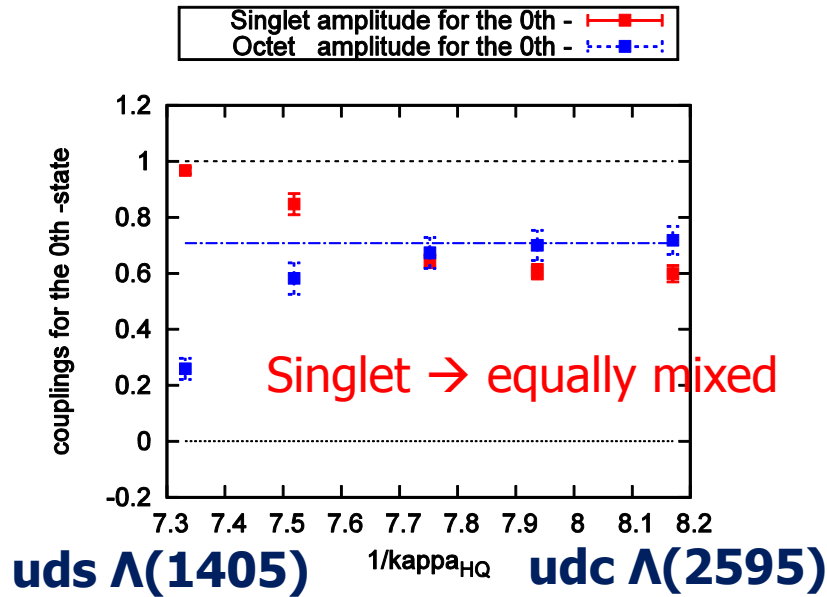


uds $\Lambda(1800)$ $1/\kappa_{HQ}$ udc $\Lambda(\sim 2950)$

preliminary

Flavor structures

Lowest 3 states in $\frac{1}{2}$ - channel



preliminary

Amplitudes here are normalized so that squared sum is 1.
 The ratio $1/\sqrt{2} : 1/\sqrt{2}$ implies 50:50 mixture

Flavor structures to Diquark picture

SU(3) wave functions can be expressed in terms of diquark wave functions

ORBITAL	R_ρ	\rightarrow ρ mode (diquark p-wave excitation)	λ -mode
	R_λ	\rightarrow λ mode (diquark's CM p-wave excitation)	
SPIN	χ_ρ	\rightarrow Diquark has spin 1 (total 1/2)	ρ -mode
	χ_λ	\rightarrow Diquark has spin 0 (total 1/2)	
	χ_s	\rightarrow Diquark has spin 1 (total 3/2)	

singlet	$ \Lambda ; 1 \rangle = \frac{1}{\sqrt{2}} (R_\lambda \chi_\rho - R_\rho \chi_\lambda)$	λ -mode - ρ -mode
octet	$ \Lambda ; 8 \rangle = \frac{1}{\sqrt{2}} (R_\lambda \chi_\rho + R_\rho \chi_\lambda)$	λ -mode + ρ -mode
octet	$ \Lambda ; 8 \rangle = \frac{1}{\sqrt{2}} (R_\rho \chi_s)$	ρ -mode

Flavor structures to Diquark picture

Spin $\frac{1}{2}$ negative parity channel

$udS - \Lambda$

$$m_u = m_d < m_s$$

SU(3)_F symmetry

$\Lambda(1800)$

Octet dominant

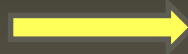
$\Lambda(1670)$

Octet dominant

$\Lambda(1405)$

Singlet dominant

Replace S with C



$udC - \Lambda$

$$m_u = m_d \ll m_c$$

Broken SU(3)_F

$\Lambda_c(\sim 2950)$

ρ -mode dominant

$\Lambda_c(\sim 2900)$

ρ -mode dominant (spin total 3/2)

$\Lambda_c(2595)$

λ -mode dominant

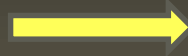
Diquark DOF seem to appear around $m_Q \sim 700\text{MeV}$

Flavor structures to Diquark picture

Spin $\frac{1}{2}$ negative parity channel

$udS - \Lambda$

Replace S with C



$udC - \Lambda$

$$m_u = m_d < m_s$$

SU(3)_F symmetry

$$m_u = m_d \ll m_c$$

Broken SU(3)_F

Possibility of level crossing (or misidentification?)

$\Lambda(1800)$

Octet dominant

O:S=1:-1

$\Lambda_c(\sim 2950)$

ρ -mode dominant

$\Lambda(1670)$

Octet dominant

O:S=1:0

$\Lambda_c(\sim 2900)$

ρ -mode dominant (spin total 3/2)

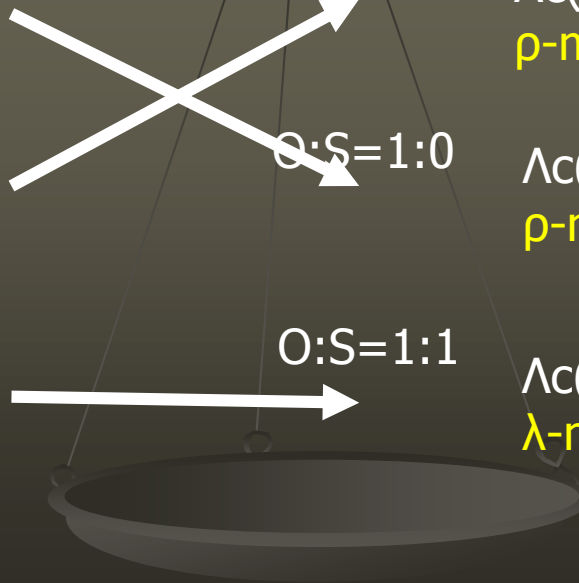
$\Lambda(1405)$

Singlet dominant

O:S=1:1

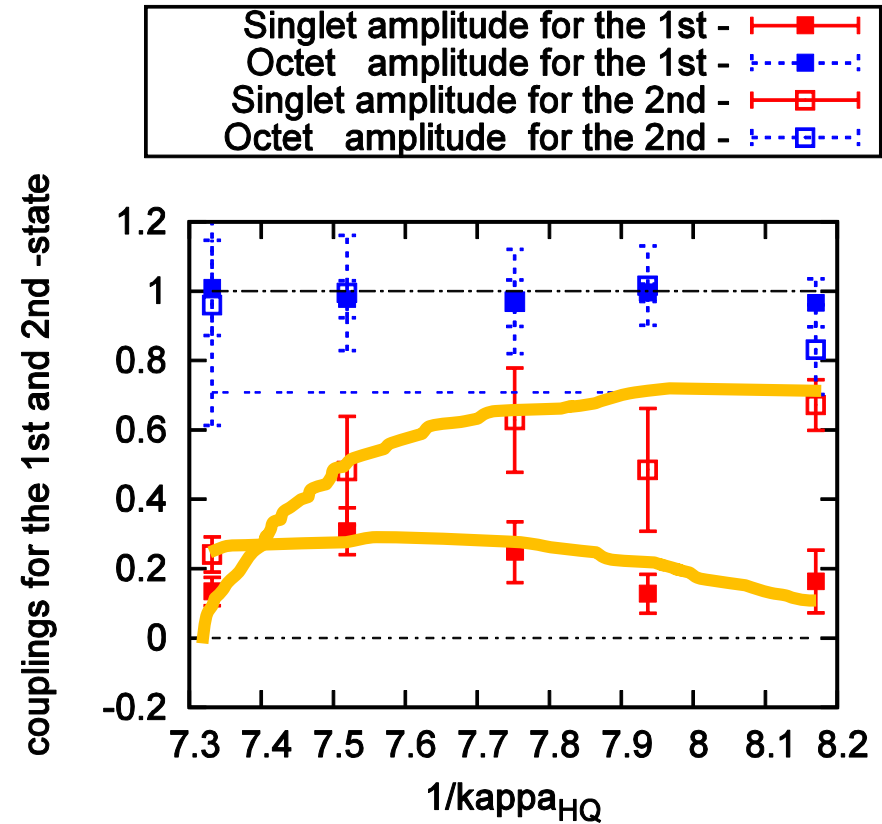
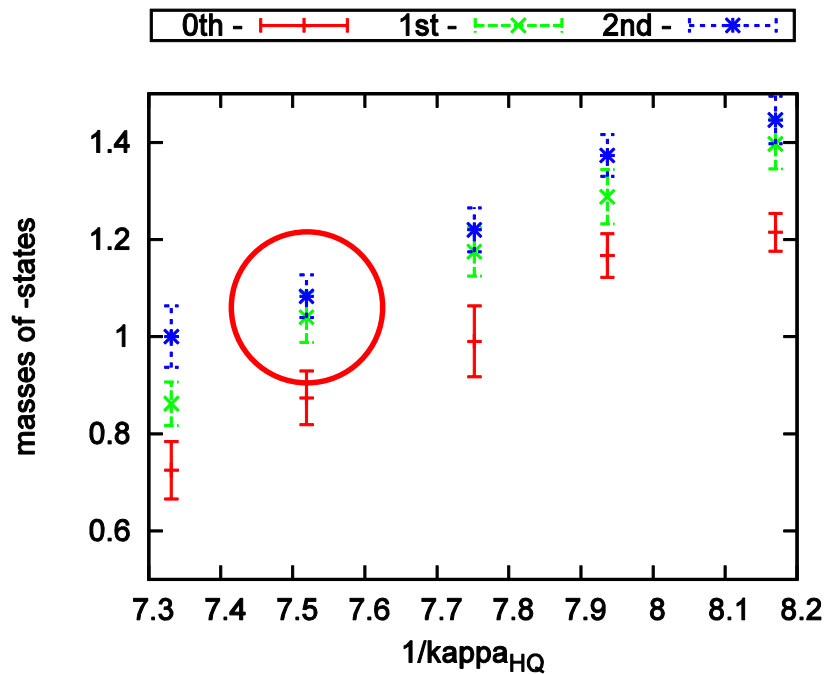
$\Lambda_c(2595)$

λ -mode dominant



Flavor structures to Diquark picture

Level crossing occurs ?



Summary

Summary

We investigated the flavor structure of the low-lying Λ 's in lattice QCD.

Mass

The mass spectra of Λ_c and Λ_s are similar though their flavor structures are completely different

Flavor structure

Ground state : (UDS) singlet dominant state \rightarrow (UDC) λ -mode excitation

Excited state : (UDS) octet dominant state \rightarrow (UDC) ρ - and λ -mode excitations

Well classified in terms of diquark excitations
above (current) $m_Q > 700$ MeV

Future work?

Other channels?

More sophisticated analysis on the internal structures of Λ baryons