

Mesons in nuclei and partial restoration of chiral symmetry

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mesons in nuclear matter in the context of chiral symmetry

- introduction
- K^{bar} meson in nuclear medium
- K^+ nucleus scattering revisited
- $\pi^0 \rightarrow \gamma\gamma$ in nuclear medium
- η mesonic nuclei
- η' in nuclear medium and η' -N interaction



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Motivation

Why do we study the properties of hadron in nucleus ?

- as nuclear physics

- interested in the nature of the strong interaction
- study many-body systems governed by the strong force
- discover new bound systems of the strong interaction
- exotic states are interesting

- as hadron physics

- in-medium change of hadron properties
- more fundamental interpretation in terms of QCD
- one of the key concept is partial restoration of **chiral symmetry**

- for other research areas

- provide basic informations of high density physics
- important constraints accessible in experiments on earth

In-medium change of hadron properties

medium effects on hadron

mass modification

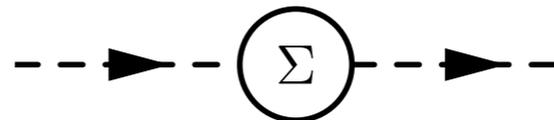
mass is given by pole of propagator at rest

vertex correction

wave function renormalization

$$Z = \left(1 - \frac{\partial \Sigma}{\partial p_0^2} \right)^{-1}$$

in-medium self-energy Σ

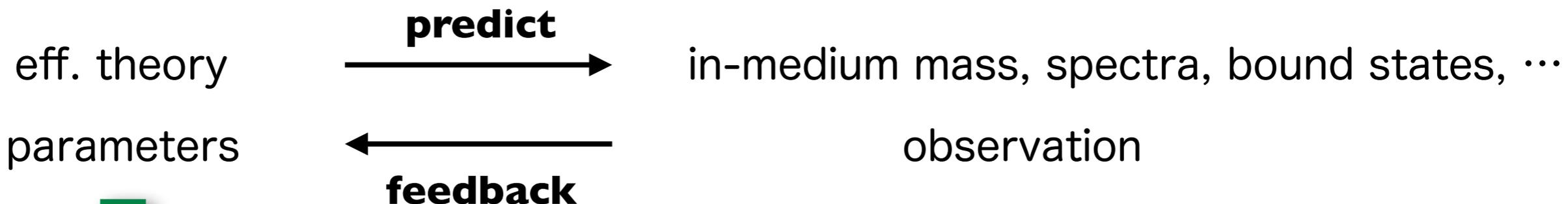


describes interaction between hadron and nuclear matter.

effective theory, effective model such as, in-medium ChPT

provides fundamental interactions between hadrons and nucleons

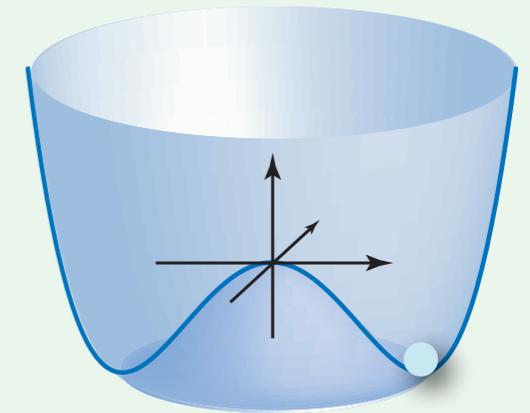
describes hopefully nuclear matter out of nucleon correlations (NN, NNN, ...)



more fundamental interpretation in terms of QCD

Chiral Symmetry

- a fundamental symmetry in QCD,
- dynamically broken by physical states
- dynamical ChS breaking determines **vacuum property** and describes **low energy hadron dynamics**
 - most of light hadron properties is affected by ChSB
 - hadrons are excitation modes upon vacuum
- DChSB is a **phase transition phenomenon**
 - broken symmetry can be restored at extreme conditions, such as high density, high temp.
 - partial (incomplete) restoration takes in nuclear medium
 - pionic atom experiments and pion nucleus scattering with theoretical consideration have suggested that chiral symmetry is partially restored in nuclear matter with 30% reduction of quark condensate



**light pion mass,
mass generation etc.**

K. Suzuki et al. PRL92, 072302 (04)

Friedman et al. PRL93, 122302 (04)

Kolomeitsev, Kaiser, Weise, PRL90, 092501 (03).

DJ, Hatsuda, Kunihiro, PLB 670, 109 (08).

Reduction of π decay constant

enhancement of s-wave repulsive interaction

Deeply bound pionic atom K. Suzuki et al. PRL92, 072302 (04)
systematic study of π^- bound states in Sn isotopes

$$b_1^{\text{free}}/b_1 = 0.78 \pm 0.05 \quad \rho \sim 0.6 \rho_0$$

Elastic scattering (Friedman et al.)

$$b_1^{\text{free}}/b_1 \sim 0.69$$

related to in-medium reduction of pion decay constant F_π

Weinberg-Tomozawa reation

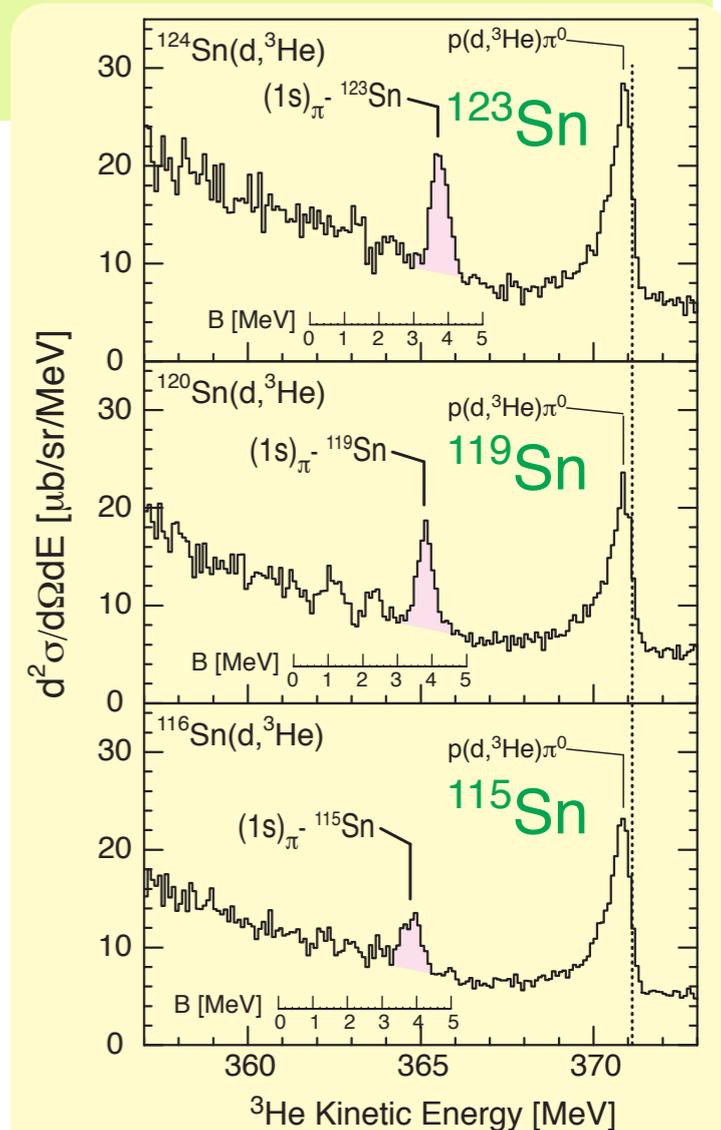
in vacuum
$$4\pi \left(1 + \frac{m_\pi}{m_N}\right) b_1^{\text{free}} = -\frac{m_\pi}{2F^2}$$

**in medium
at low-density**
$$4\pi \left(1 + \frac{m_\pi}{m_N}\right) b_1 = -\frac{m_\pi}{2(F_\pi^t)^2}$$

$$\frac{b_1^{\text{free}}}{b_1} = \left(\frac{F_\pi^t}{F_\pi}\right)^2$$

at low density

DJ, Hatsuda, Kunihiro, PLB 670 (2008), 109.



Chiral Symmetry

expectation in partial restoration of chiral symmetry in nuclear matter

- reduction of mass difference between parity partners

σ - π ρ - a_1 N - N^* etc.

η probes chiral symmetry for N and $N^*(1535)$

- wave function renormalization for Nambu-Goldstone bosons

amplitudes of NG bosons have energy dependence due to chiral symmetry

$$Z = \left(1 - \frac{\partial \Sigma}{\partial p_0^2} \right)^{-1}$$

DJ, Hatsuda, Kunihiro, PRD63, 011901(R);
PLB 670 (2008), 109.

K^+, π^0 K^+A scattering amplitude is enhanced due to Z

- mass reduction of hadrons whose mass is generated by spontaneous breaking of chiral symmetry

a part of nucleon mass is generated by spontaneous breaking of chiral symmetry

effective mass of nucleon in nuclear matter is $0.7 m_N$.

η' part of eta' mass is generated by chiral symmetry breaking

K^{bar} meson

\bar{K} in nuclear medium

a lots of studies on in-medium kaon
one of the difficulties in observation

a recent review

Freedman, Gal, Phys.Rept. 425, 89 (2007)

large in-medium absorption

kaon is strongly absorbed in nuclear medium

mesonic $K^{\text{bar}}N$ to πY

nonmesonic $K^{\text{bar}}NN$ to YN 30% at ρ_0

Sekihara, Yamagata-Sekihara, DJ,
Kanada-En'yo, PRC86, 065205 (12)

hard to identify K^{bar} -nucleus bound states, even if they exist

$K^{\text{bar}}N$ interaction as a fundamental interaction of $K^{\text{bar}}A$

$\Lambda(1405)$ is sitting 30 MeV below the $K^{\text{bar}}N$ threshold

nature of $\Lambda(1405)$ is extremely important to be revealed



chiral symmetry determines low-energy $K^{\text{bar}}N$ interaction, but it may play a minor role on the in-medium K^{bar} properties, because dynamics of $K^{\text{bar}}N$, or $\Lambda(1405)$, is more significant

Nature of $\Lambda(1405)$

DJ, Oller, Oset, Ramos, Meissner, NPA725, 181 ('03)

a recent review, Hyodo, DJ, Prog. Part. Nucl. Phys. 67, 55 ('12)

- $\Lambda(1405)$ is most probably a quasi-bound state of $K^{\text{bar}}N$

low-energy theorem of chiral symmetry tells that $K^{\text{bar}}N$ interaction is attractive (model independent Weinberg-Tomozawa interaction)

how strong ??

the $l=0$ interaction is enough strong to form a bound state

dynamical calculations of the $K^{\text{bar}}N$ system with the chiral interaction and without sources of resonances conclude a $K^{\text{bar}}N$ bound state with 15 MeV binding energy

$\Lambda(1405)$ appears as a $K^{\text{bar}}N$ bound state with 15 MeV binding energy

theoretically, $K^{\text{bar}}N$ interaction is not so strong.

the binding energy is 15 MeV not 30 MeV

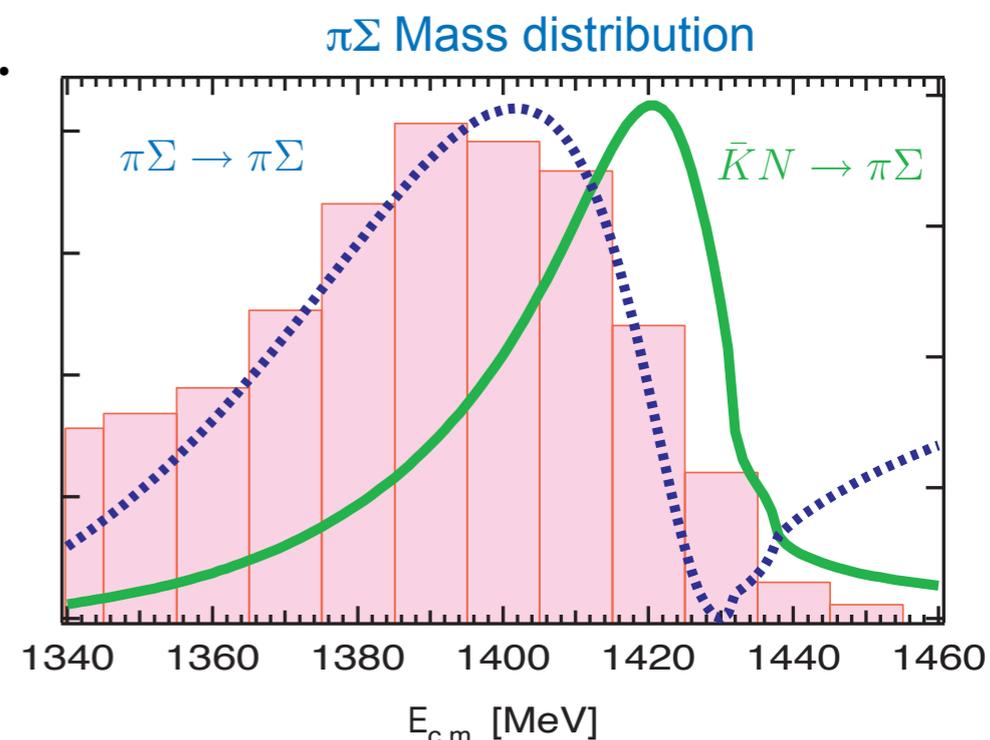
two-pole structure

the spectrum of $\Lambda(1405)$ is explained by interference between two components, $K^{\text{bar}}N$ bound state and $\pi\Sigma$ resonance.

Hyodo, Weise, PRC77, 035204 ('08)

to confirm this scenario,

we observe $\Lambda(1405)$ produced by $K^{\text{bar}}N$ channel



Subthreshold amplitude of $\bar{K}N$

$\Lambda(1405)$ is located below the $\bar{K}N$ threshold

cannot be produced by direct reaction $\bar{K}N \rightarrow \Lambda(1405)$

$\bar{K}N$	<u>1435 MeV</u>	$\Lambda(1405)$
$\pi\Sigma$	<u>1331 MeV</u>	

indirect reaction

use nuclear effect

to see subthreshold amplitude



nuclear effect

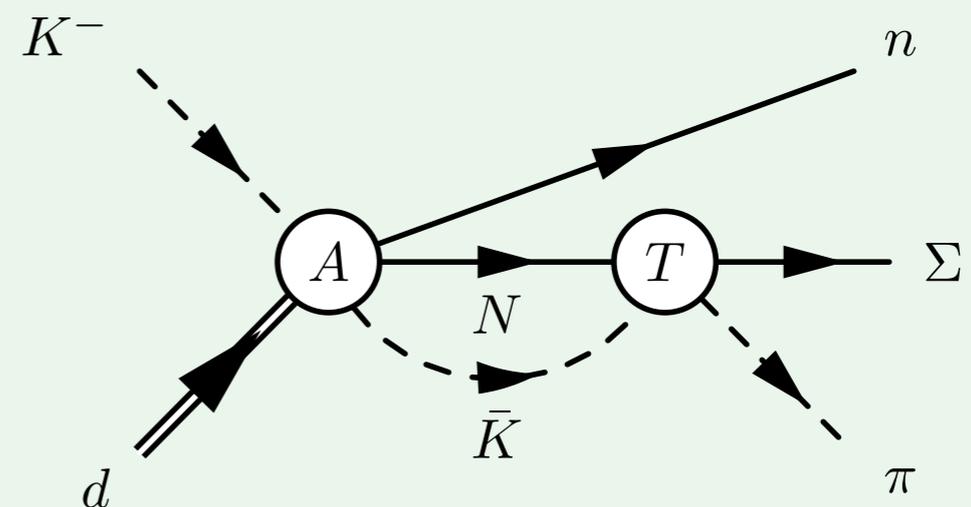
- fermi motion
- two-body effect

$\bar{K}N$ selective production

- strangeness carried by incident kaon

more sophisticated calculations given by Ohnishi and Miyagawa

production mechanism be under control



Want to extract T-amplitude from experiment. For this purpose, need to understand the production mechanism described by A-amplitude.

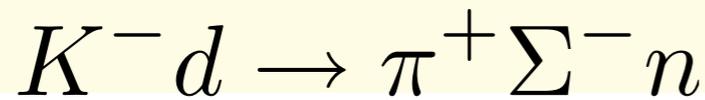
DJ, Oset, Sekihara, Eur.Phys.J.A. 42, 257 (2009).
Yamagata-Sekihara, Sekihara, DJ, PTEP 2013, 043D02

$\Lambda(1405)$ in $K^{\text{bar}}N$ channel

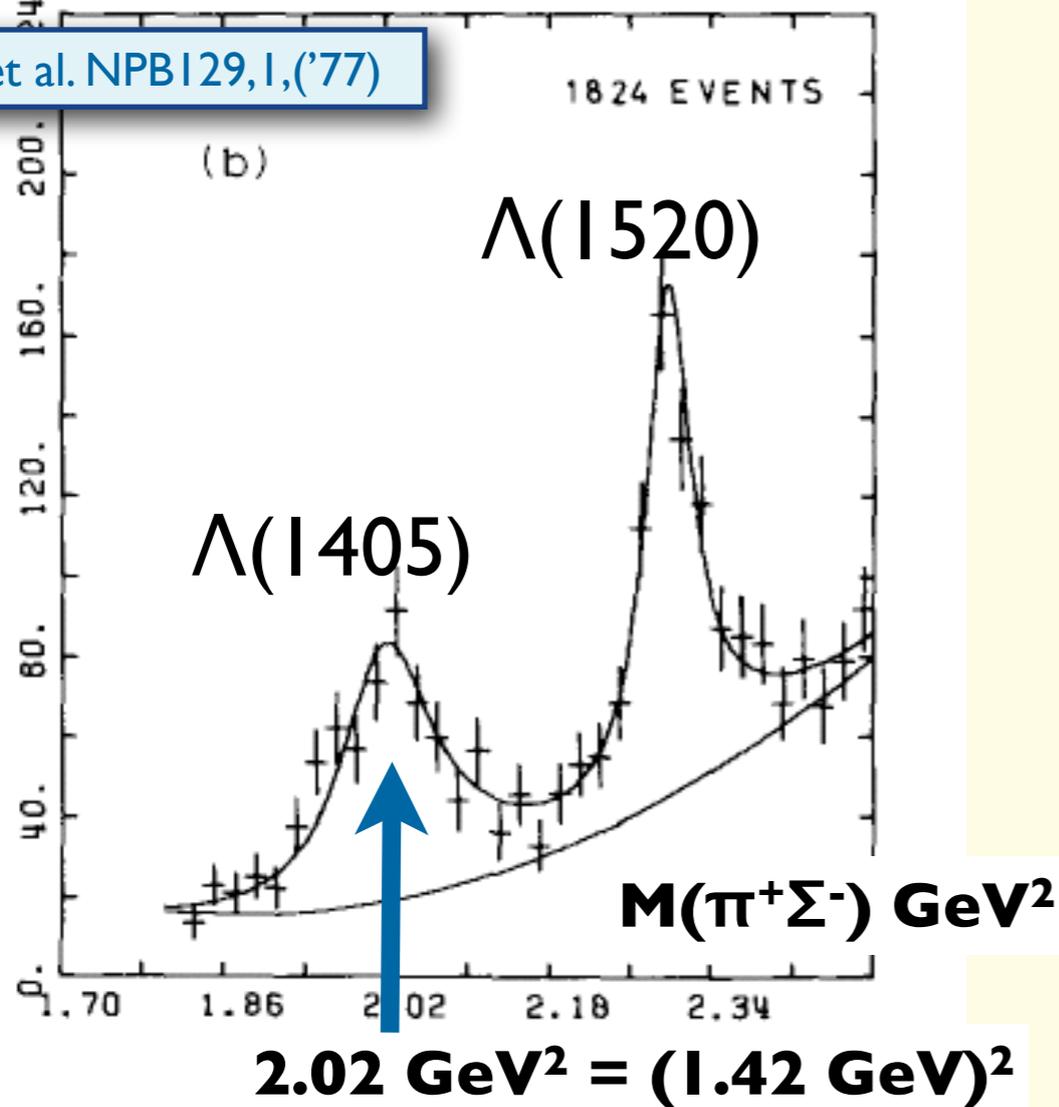
DJ, Oset, Sekihara, Eur.Phys.J.A. 42, 257 (09); ibid.A49, 95
Yamagata-Sekihara, Sekihara, DJ, PTEP 2013, 043D02

Experiment bubble chamber initial K momentum 686 ~ 844 MeV/c

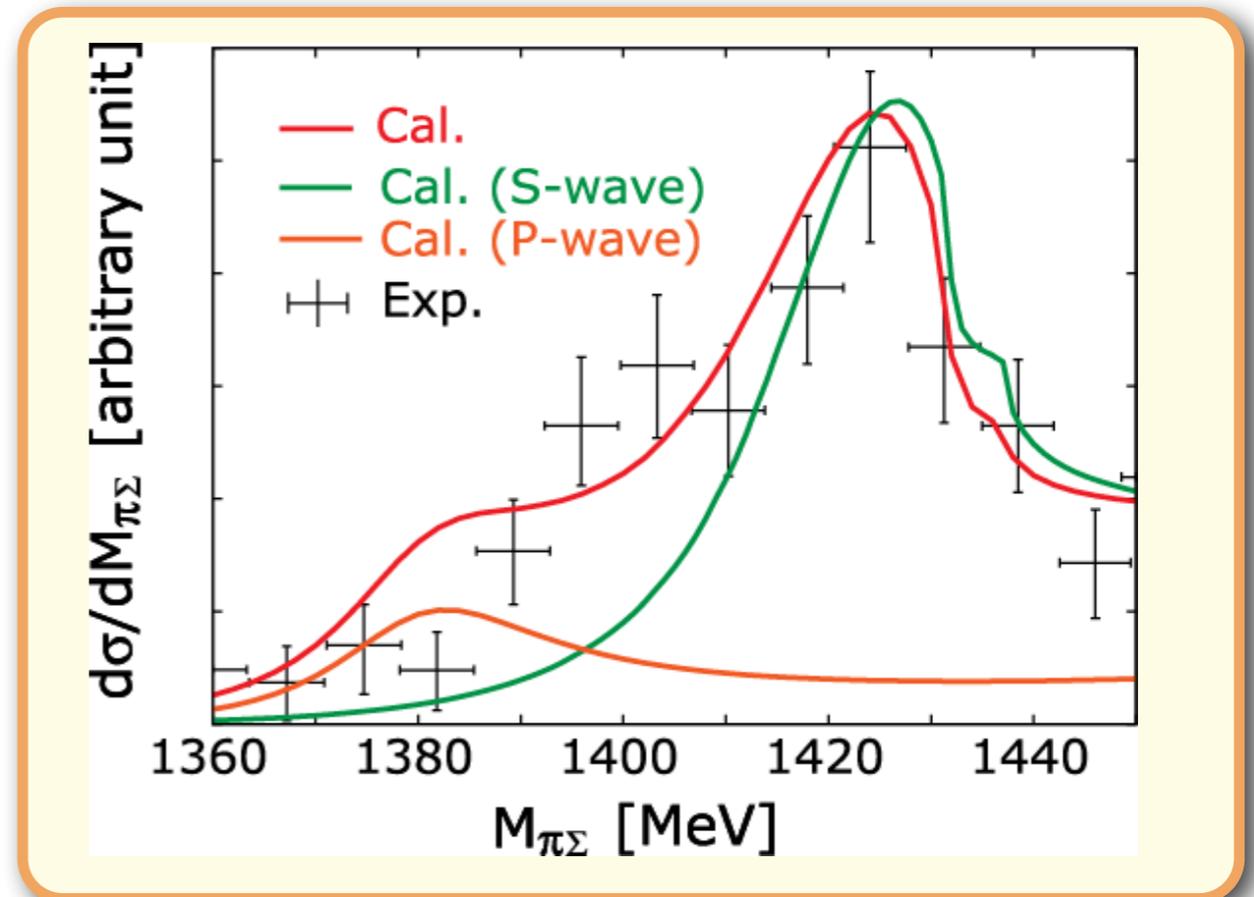
$\pi\Sigma$ invariant mass spectrum



Braun et al. NPB129,1,(77)



theoretical calculation in ChUM



production cross section of $\Lambda(1405)$

385 μb @ 800 MeV/c (exp. $410 \pm 100 \mu\text{b}$)
agrees with data in shape and size

inclusion of Σ^* does not distort the shape.

brand-new experiment at J-PARC (E31)

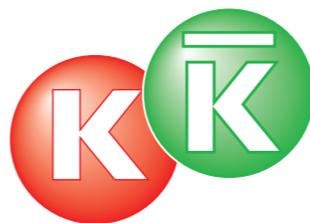
Family of kaonic few-body systems

$\Lambda(1405)$



BE ~10 MeV (30 MeV)

$f_0(980), a_0(980)$



BE ~10 MeV

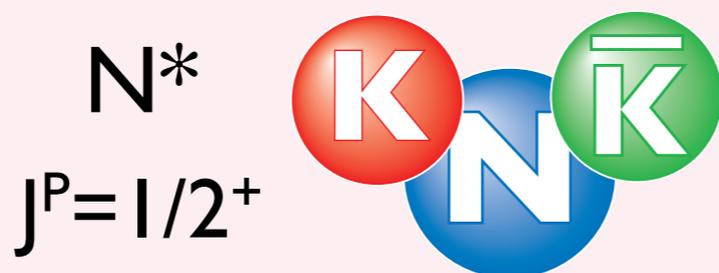
DJ, Kanada-En'yo, PRC78, 035203 (08).
 Martinez Torres, DJ, PRC82, 038202 (10).
 Martinez Torres, DJ, Kanada-En'yo, PRC83
 065205 (11).

$K^{\text{bar}}NN$



BE ~20 MeV
 or more

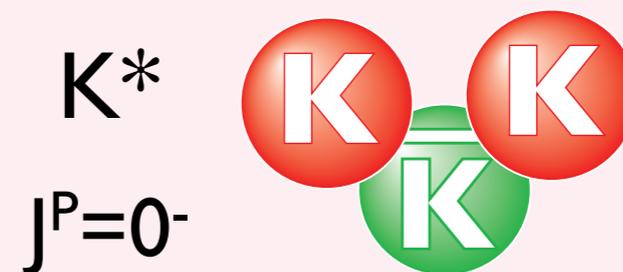
$K^{\text{bar}}KN$



a new N^* resonance N(1910)

BE ~20 MeV

$K^{\text{bar}}KK$



1420 ~ 1465 MeV

BE 20~60 MeV

and more

$K^{\text{bar}}K^{\text{bar}}N$

Kanada-En'yo, DJ

$K^{\text{bar}}NNN$

Akaishi, Yamazaki, Dote,..

$K^{\text{bar}}K^{\text{bar}}NN$

Barnea, Gal, Liverts,

$K^{\text{bar}}N$ and $K^{\text{bar}}K$ Weinberg-Tomozawa interactions are “similar” in a sense of chiral dynamics
pion is too light to be bound in range of strong interaction

K^+ meson

K⁺ - nucleus scattering revisited

Aoki, DJ, on going

review articles

Dover, Walker, Phys. Rept. 89, 1 (1982)

Freedman, Gal, Phys.Rept. 425, 89 (2007)

Kaon in nucleus

- KN interaction is repulsive, and KN cross section is small
- mean free path of K in nuclear medium is around 5 fm
- Kaon has been consider to be a clean probe to investigate nuclear matter
- no strong resonances in KN channel
- relatively easy to investigate **in-medium effects on kaon**

breakdown of linear density approximation

thanks to large mean free path, K⁺A scattng could be written well by single step

$$\sigma_{K+A} \simeq A \sigma_{K+N} \quad p_{\text{lab.}} < 800 \text{ MeV}/c$$

the ratio of the cross sections is known to be larger than unity

$$\frac{\sigma_{K+^{12}\text{C}}}{6\sigma_{K+d}} > 1.0$$

K⁺ - nucleus scattering revisited

Aoki, DJ, on going

breakdown of $T\rho$ approximation

$$2m_K^+ V_{\text{opt}} \simeq -\rho T_{K+N} \quad \text{linear density approximation}$$

p_{lab}	V_{opt}	Re b_0 (fm)	Im b_0 (fm)	
488	$t\rho$	-0.203(26)	0.172(7)	obtained by χsq fitting free KN
	$t_{\text{free}}\rho$	-0.178	0.153	

$$T_{K+N} = -\frac{4\pi E_{\text{c.m.}}}{M_N} b_0$$

Friedman, Gal, Phys.Rept. 425, 89 (2007)

15% enhancement in in-medium KN scattering

possible explanation

- nucleon-nucleon correlation
- “swelling” of nucleon
- mass reduction of vector mesons

etc.

K^+ - nucleus scattering revisited

Aoki, DJ, on going

in the aspect of chiral symmetry

the 15% enhancement can be explained by wave function renormalization

argument by Kolomeitsev et al. for pion

Kolomeitsev, Kaiser, Weise, PRL90, 092501 (03)

when self-energy is energy-dependent,

See also, DJ, Hatsuda, Kunihiro, PRD63, 011901(R);
PLB 670 (2008), 109.

equivalent energy-independent optical potential can be obtain as follows

- consider in-medium dispersion relation $\omega^2 - m^2 - \Sigma(\omega) = 0$

- expanding self-energy around $\omega = m$

$$2mV_{\text{opt}}(m^*) = \Sigma(m) + (\omega^2 - m^2) \frac{\partial \Sigma}{\partial \omega^2} + \dots$$

$$\simeq \left(1 + \frac{\partial \Sigma}{\partial \omega^2} \right) \Sigma(m) \simeq Z \Sigma(m)$$

$$2mV_{\text{opt}} = -Z\rho T_{K+N}$$

one of the higher order corrections

$$Z = 1 + 0.1 \frac{\rho}{\rho_0}$$

leading order chiral perturbation theory calculation

$\pi^0 \rightarrow \gamma\gamma$ decay in nuclear medium

Goda, DJ, PTEP 2014, 033D03 (2014).
Nebreda, DJ, in preparation.

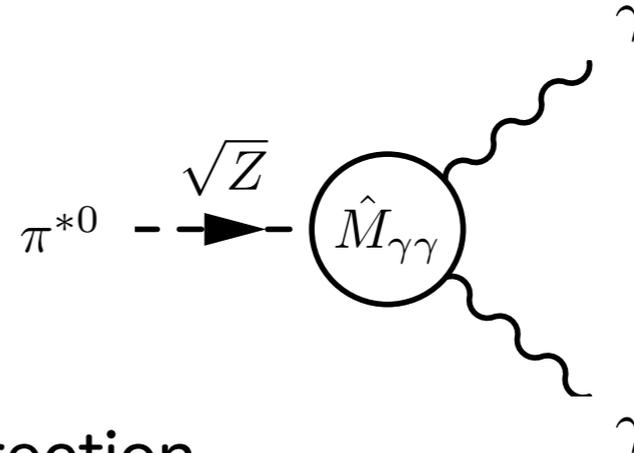
in-medium decay amplitude

$$M_{\gamma\gamma}^* = \sqrt{Z} \hat{M}_{\gamma\gamma}$$

Z wave function renormalization

$\hat{M}_{\gamma\gamma}$ 1-particle irreducible vertex correction

no correction in the linear density ←



Meissner, Oller, Wirzba, AnnPhys297, 27 (02)

in-medium change of the amplitude

$$\frac{M_{\gamma\gamma}^*}{M_{\gamma\gamma}} = \sqrt{Z}$$

$$\frac{\Gamma_{\gamma\gamma}^*}{\Gamma_{\gamma\gamma}} = Z \simeq 1 + 0.4 \frac{\rho}{\rho_0}$$

40% enhancement in nuclear density

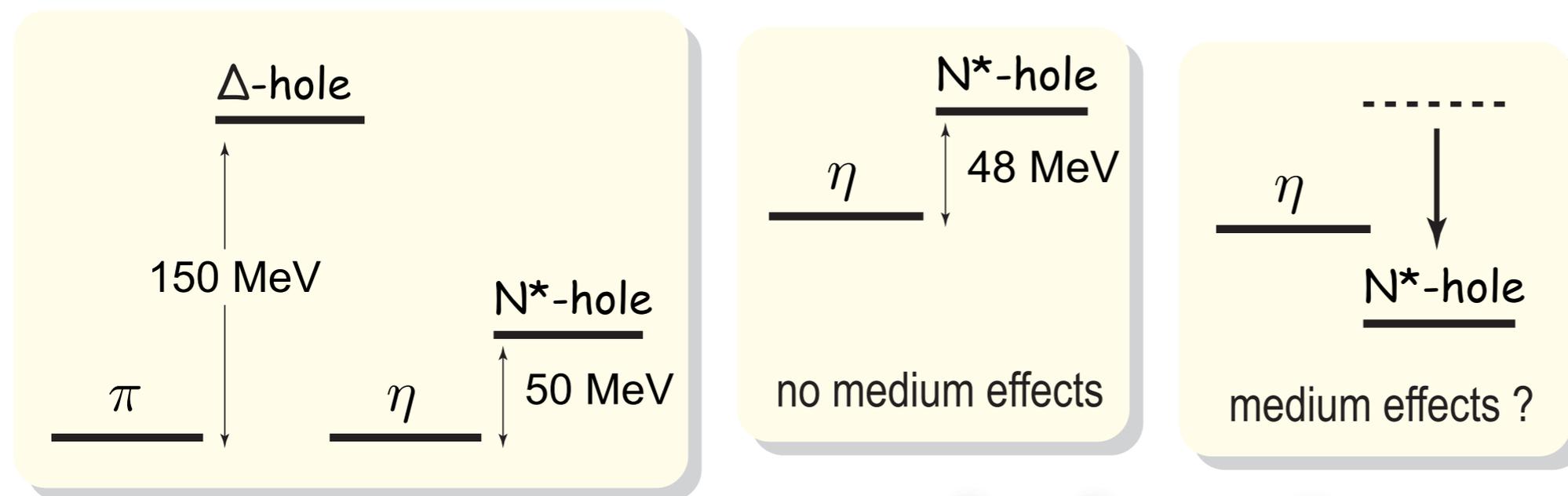
η meson

η mesonic nuclei

- eta N couples strongly to $N^*(1535)$
- $N^*(1535)$ is the first excited state with the opposite parity of nucleon
- can be a chiral partner of nucleon
- eta mesonic nuclei can prove chiral symmetry of N and N^*

chiral double picture for nucleons

- nucleon and $N^*(1535)$ are chiral partners (**chiral doublet**)
- masses of chiral doublets tend to degenerate when ChS is being restored
- mass difference of N and N^* decreases in nuclear medium

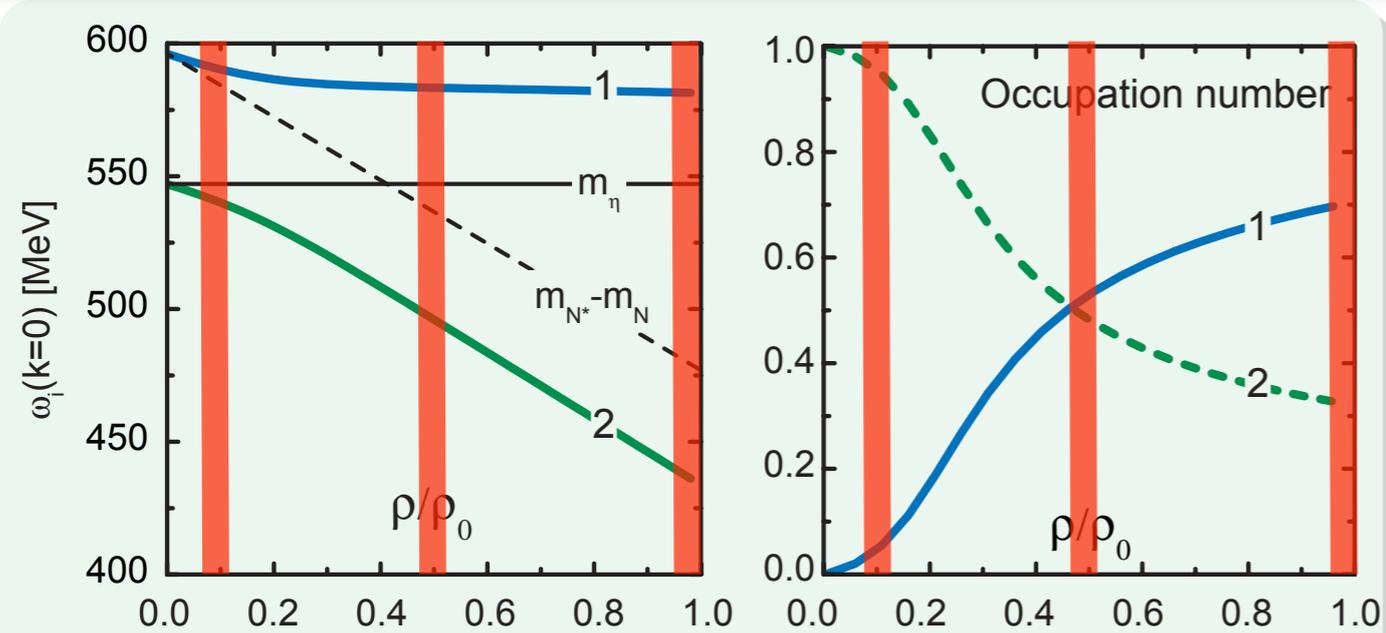
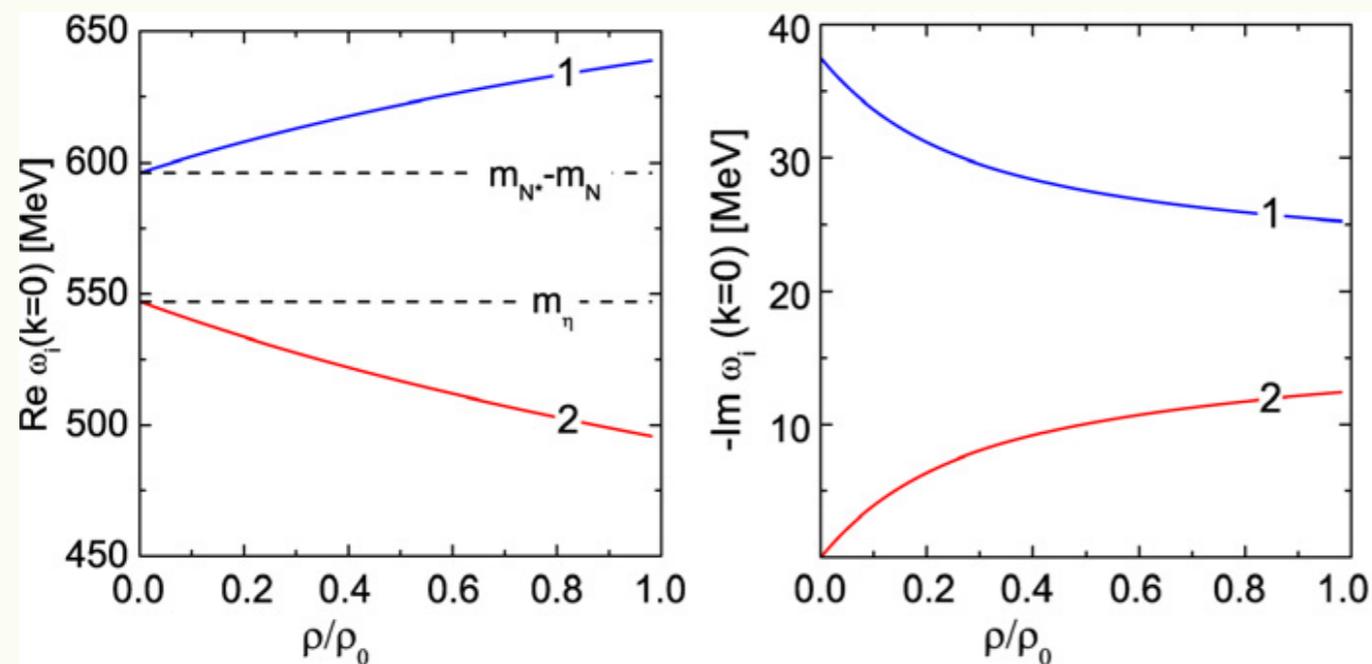


level crossing

Spectral function of in-medium eta meson

density dependence of two levels

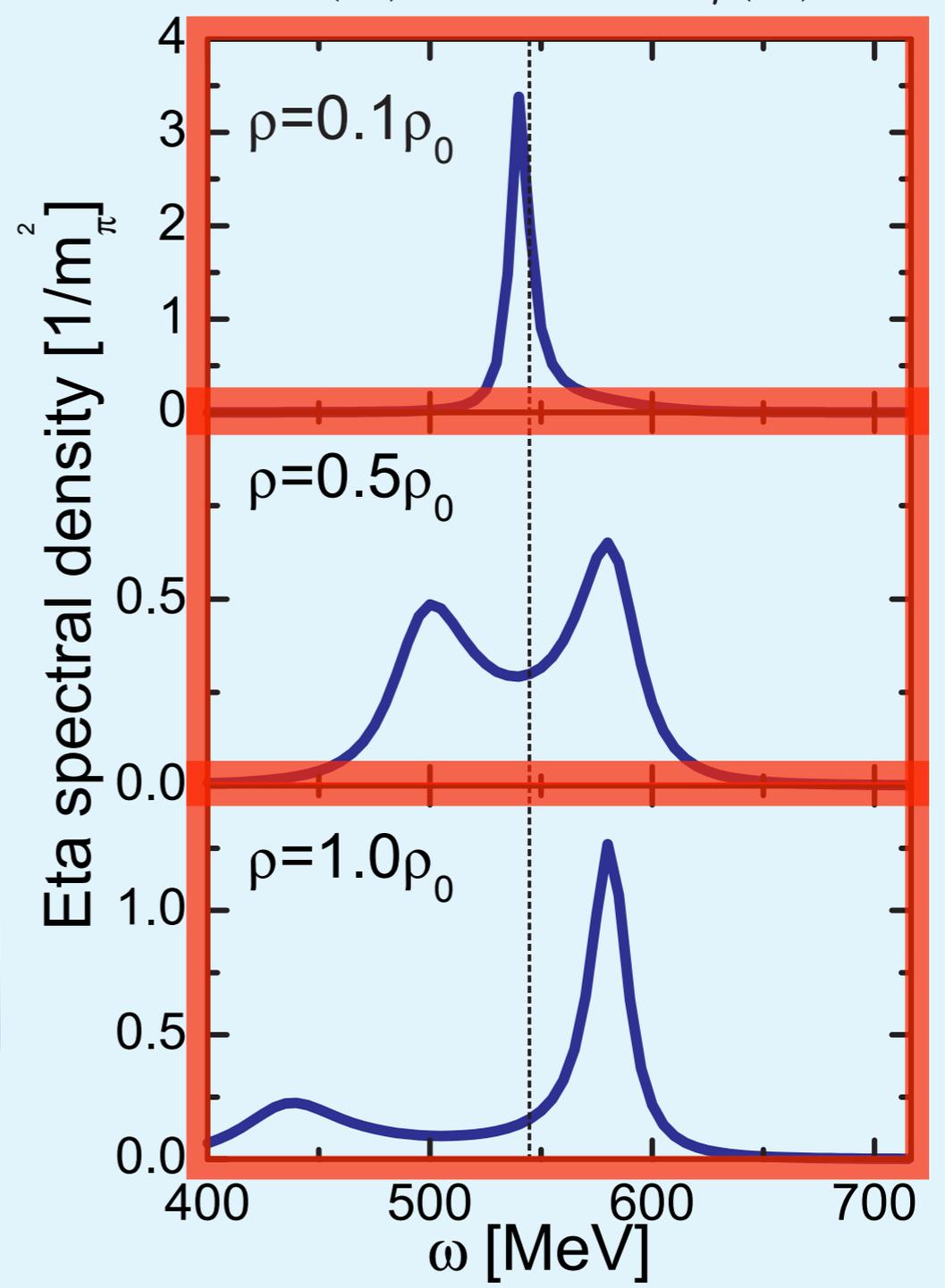
Jido, Kolomeitsev, Nagahiro, Hirenzaki, NPA811, 158 (2008)



$$G_\eta(\omega) = \sum_i \frac{Z_i}{\omega - \omega_i} \quad Z_i = \left(1 - \frac{\partial V_\eta(\omega)}{\partial \omega} \Big|_{\omega=\omega_i} \right)^{-1}$$

Spectral function

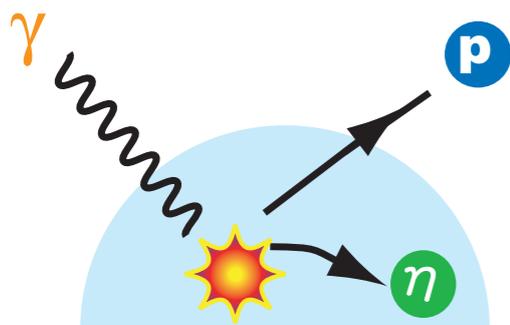
$$S(\omega) = -\text{Im} G_\eta(\omega)$$



Eta mesic nuclei

Nagahiro, Jido, Hirenzaki, PRC68, 035805 (03); NPA761, 92 (05)

Jido, Kolomeitsev, Nagahiro, Hirenzaki, NPA811, 158 (08)



(γ, p) reaction

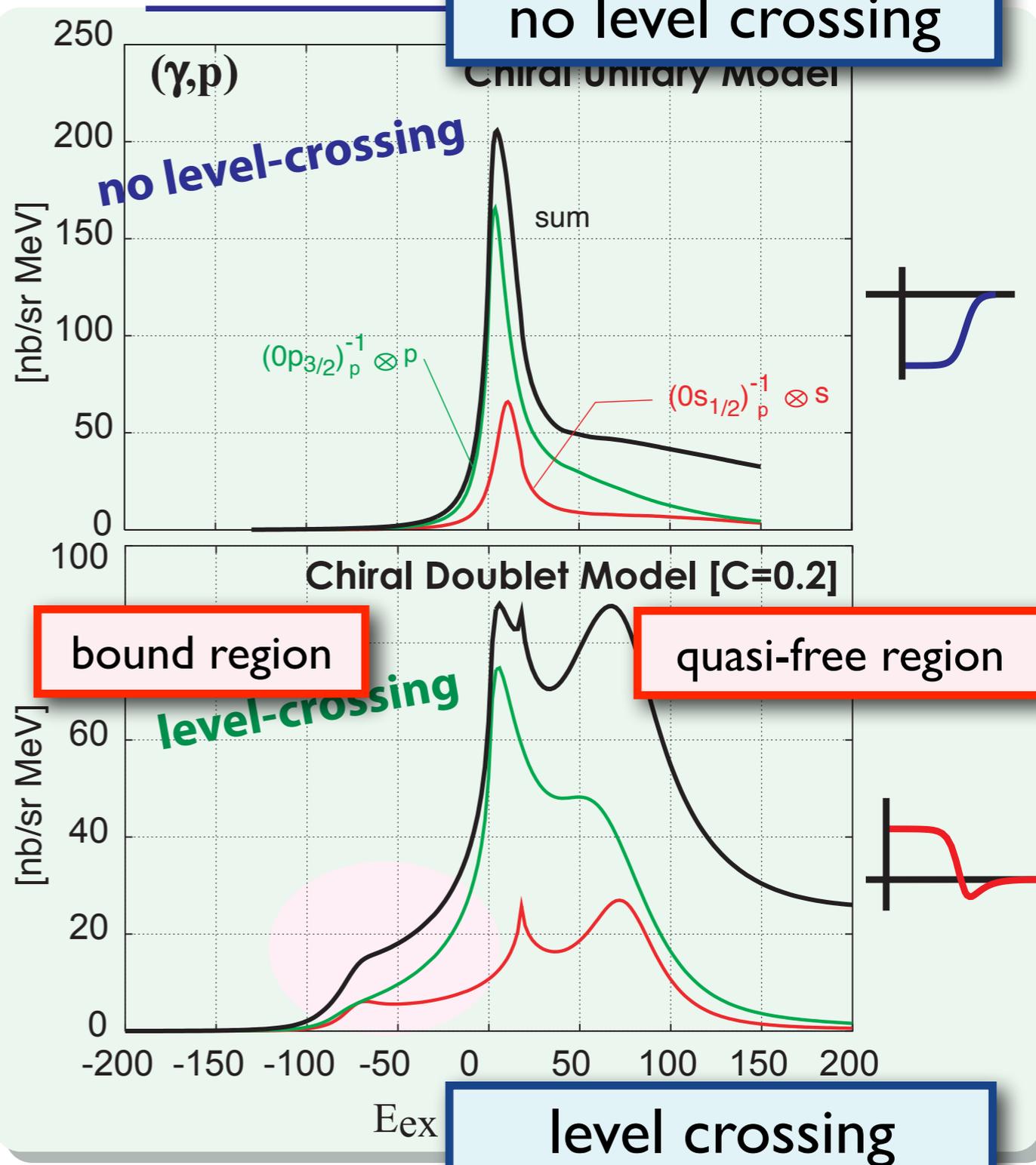
missing mass spectra of emitted proton

^{12}C target

in recoilless condition
(no momentum transfer)

level crossing effect can be seen in
quasi-free region as repulsive shift
of eta meson

Spectra of $^{12}\text{C}(\gamma, p)^{11}\text{B} \otimes \eta$



η' meson

η' meson and chiral symmetry

DJ, Nagahiro, Hirenzaki,
PRC85 (12) 032201(R)

Large eta' mass stems from quantum anomaly, which breaks axial U(1) symmetry. eta' failed to get a Nambu-Goldstone boson due to anomaly.

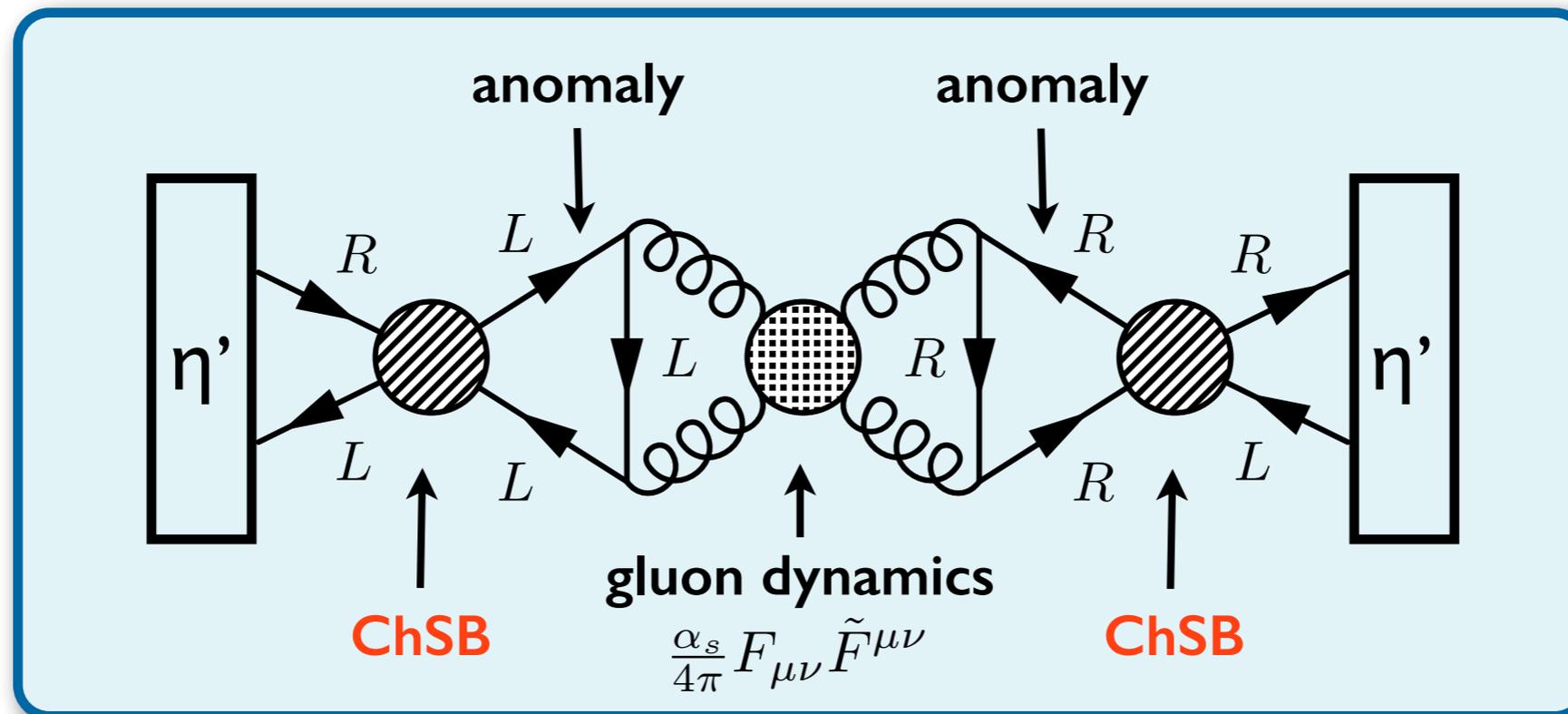
$\eta'(958)$

$$I^G(J^{PC}) = 0^+(0^-+)$$

Mass $m = 957.78 \pm 0.06$ MeV

Full width $\Gamma = 0.198 \pm 0.009$ MeV

eta' meson has a strong connection also to chiral symmetry breaking. in order that $U_A(1)$ anomaly affects the η' mass, chiral symmetry is necessarily broken spontaneously and/or explicitly.



nonchiral gluon field cannot couple to pseudoscalar states without chiral symmetry breaking.

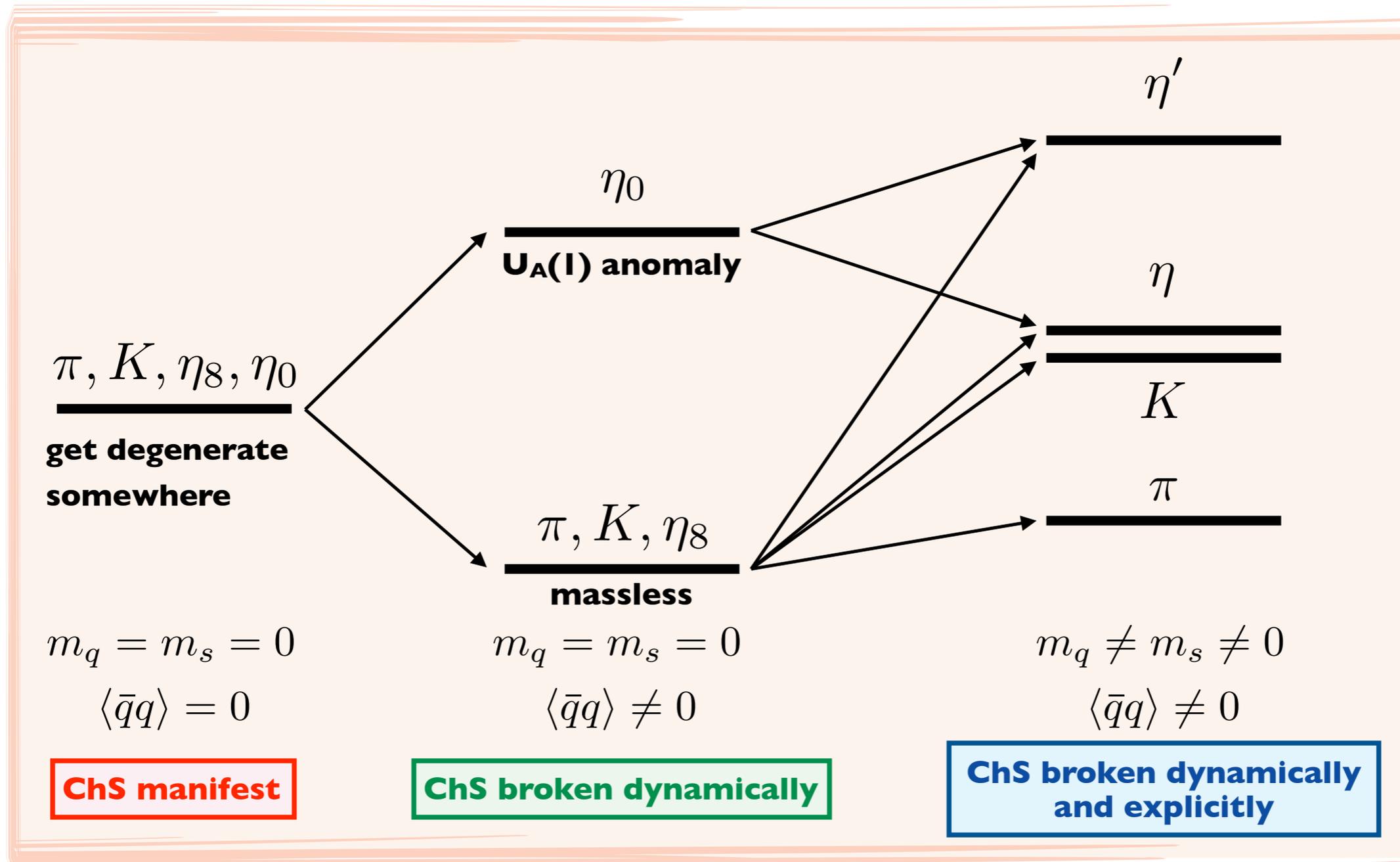
when chiral symmetry is restored, η and η' should degenerate due to SU(3) chiral symmetry. thus, $\eta - \eta'$ mass difference is generated by chiral symmetry breaking

η' meson in chiral restoration

DJ, Nagahiro, Hirenzaki, PRC85 (12) 032201(R);
Nagahiro, DJ, Fujioka, Itahashi, Hirenzaki,
PRC87 (12) 045201

When chiral symmetry is restored... as a consequence of $SU_L(3) \otimes SU_R(3)$

9 PS π, K, η_8, η_0 9 S σ, a_0, κ, f_0 get degenerate



in order that $U_A(1)$ anomaly affects the η' mass, chiral symmetry is necessarily broken spontaneously and/or explicitly.

η' meson in nuclear matter

DJ, Nagahiro, Hirenzaki,
PRC85 (12) 032201(R)

the mass gap of η' and η is generated by chiral symmetry breaking

the η' mass get reduced when chiral symmetry is being restored in nuclear medium

a simple order estimation

linear dependence of quark condensate on η' - η mass difference (400 MeV)

partial restoration of ChS takes place with 35% at ρ_0

we expect strong η' mass reduction $\Delta m_{\eta'} \sim 100 \text{ MeV} @ \rho = \rho_0$

chiral effective theories tell similar results.

linear sigma model

Sakai, DJ, PRC88 (13) 064906

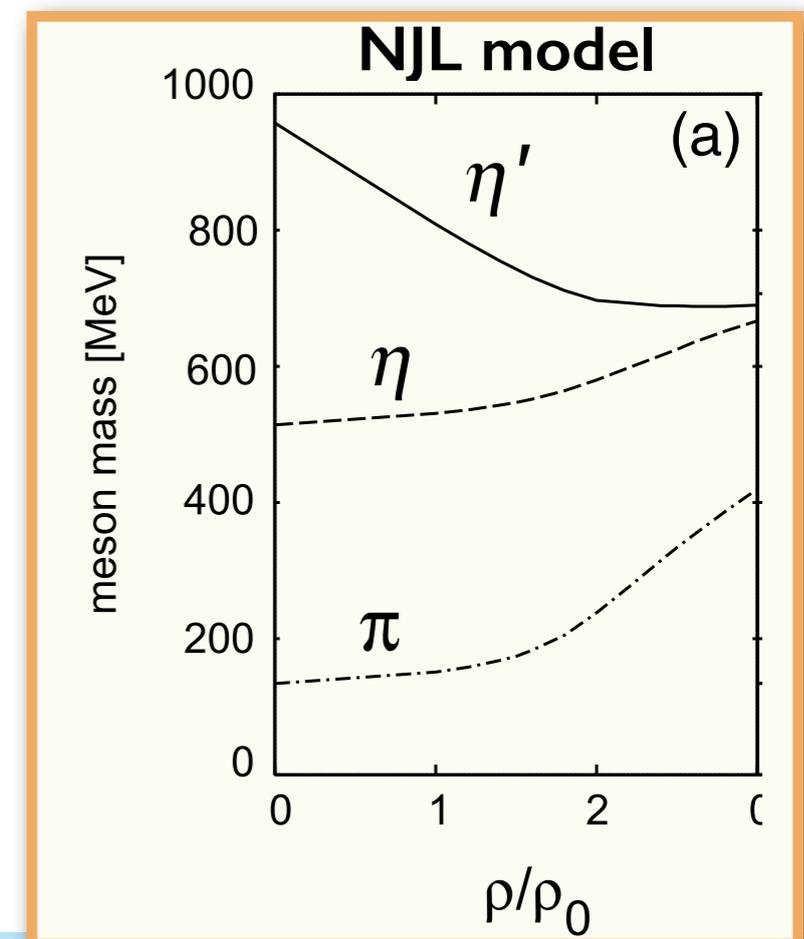
$$\Delta m_{\eta'} \sim 80 \text{ MeV} @ \rho = \rho_0$$

$$m_{\eta'} - m_{\eta} \sim 130 \text{ MeV} @ \rho = \rho_0$$

NJL model

P. Costa, M. C. Ruivo, and Y. L. Kalinovsky, PLB560, 171 (03).
Nagahiro, Takizawa, Hirenzaki, PRC74,045203 (2006)

$$\Delta m_{\eta'} \sim 150 \text{ MeV} @ \rho = \rho_0$$



Possible bound state spectra

DJ, Nagahiro, Hirenzaki,
PRC85 (12) 032201(R)

mass reduction in nuclear matter provides a scalar potential in finite nucleus

a simple η' optical potential

(Woods-Saxon type)

proportional to nuclear density

$$V_{\eta'}(r) = V_0 \frac{\rho(r)}{\rho_0}$$

$$\Delta m = 150 \text{ MeV}$$

$$\Gamma/2 = 20 \text{ MeV}$$

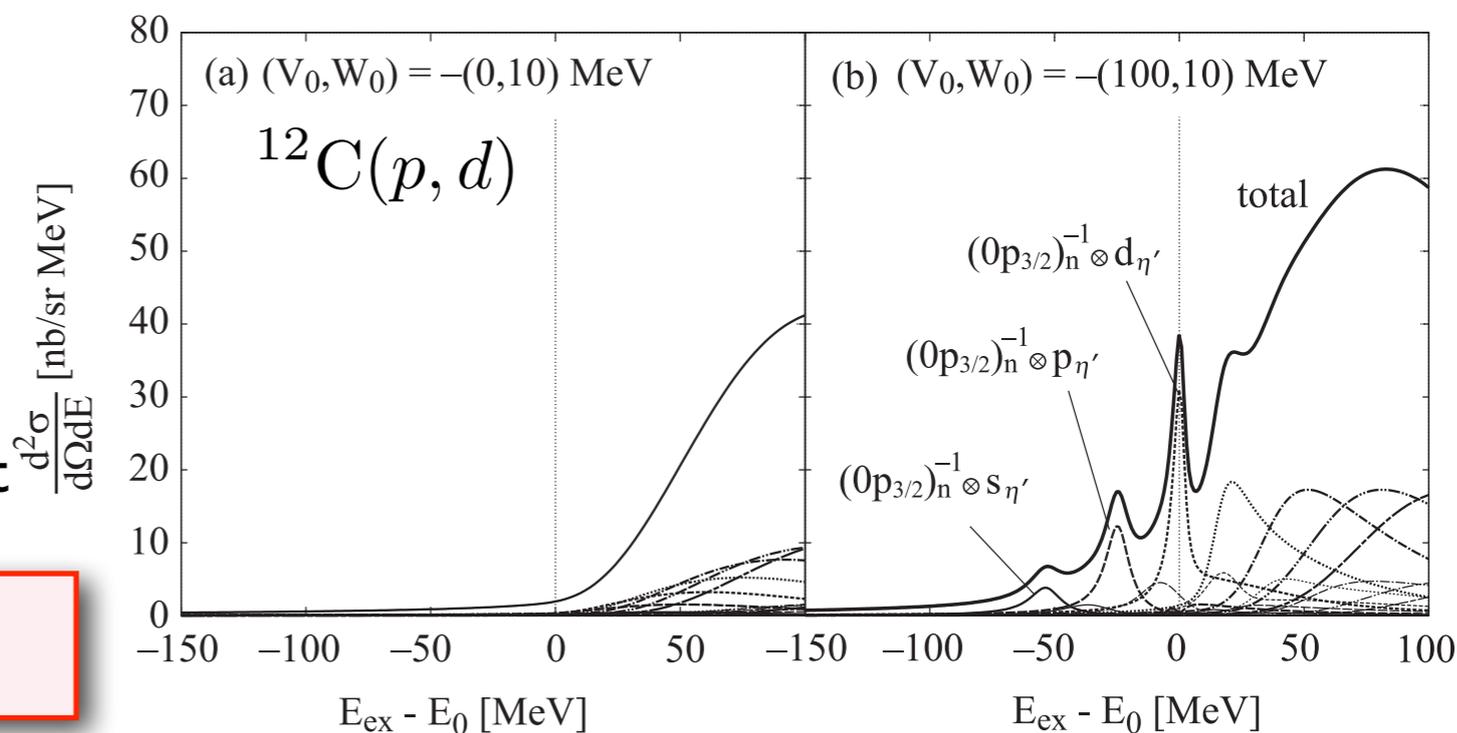
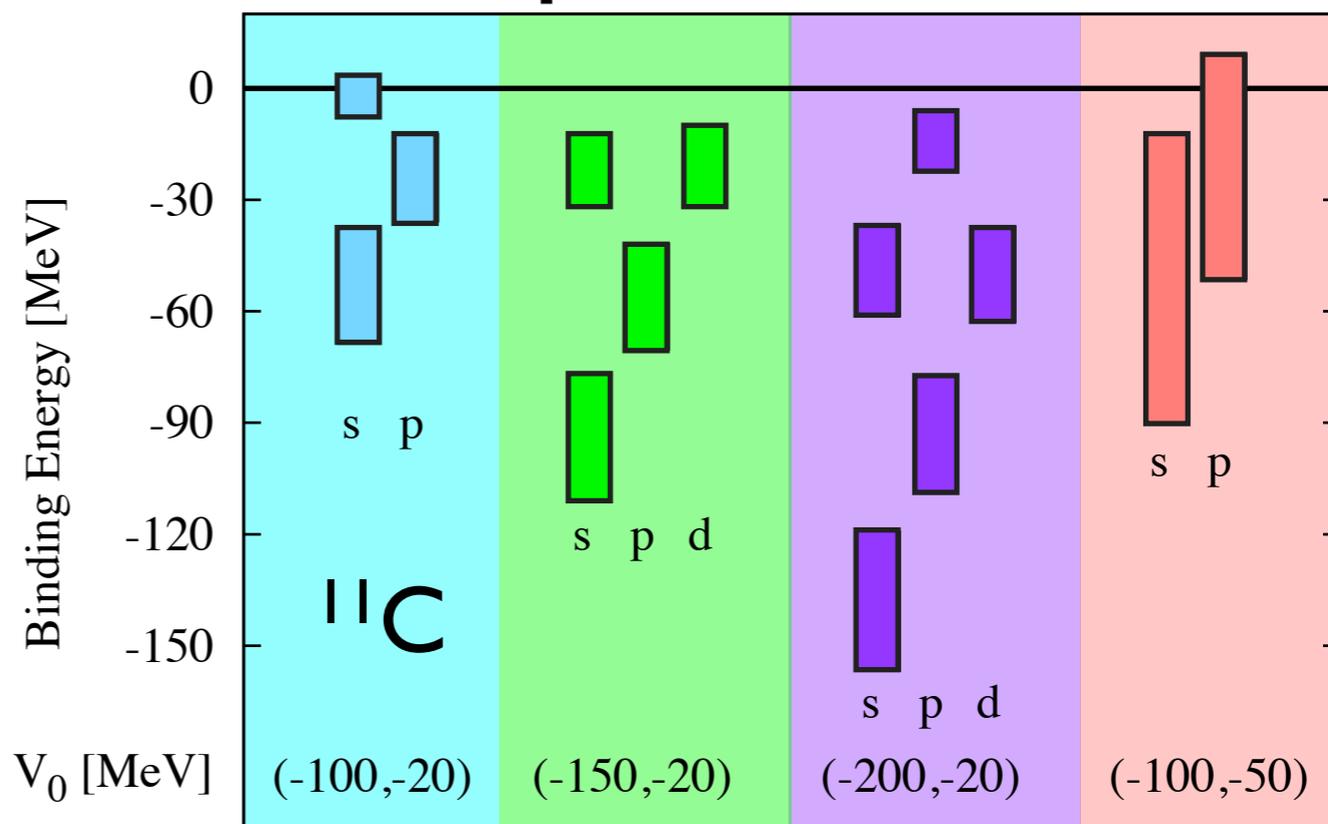
Re: theoretical expectation

Im: phenomenological observation

well-separated bound states

for realistic calculation

core polarization effect could be important



Nagahiro, DJ, Fujioka, Itahashi,
Hirenzaki, PRC87 (12) 045201

η' -N interaction

Sakai, DJ, PRC88 (13) 064906;
in preparation

in linear sigma model

nucleon mass is generated also by spontaneous breaking of ChS

$$m_N = g\langle\sigma_0\rangle$$

→ presence of strong coupling σNN

this is the origin of the scalar attraction in NN interaction

in the same way

chiral symmetry breaking generates a part of eta' meson with help of anomaly

$$m_{\eta_0}^2 - m_{\eta_8}^2 = 6B\langle\sigma_0\rangle$$

→ presence of strong coupling $\sigma\eta'\eta'$

B term : anomaly effect

we expect strong attraction in η' -N in scalar-isoscalar exchange

with this attraction

two body η' N bound state is expected with several MeV binding energy

two-body bound state ~ 6 MeV

coupled channel effect (η' N, η N) BE = 12 - 3i [MeV]

calculated in the same way as $\Lambda(1405)$ of $K^{\text{bar}}N$ bound state

Summary

we have discussed mesons in nuclear medium under the situation that chiral symmetry is partially (30%) restored in nuclear medium

expectations in partial restoration of chiral symmetry

- **reduction of mass difference of chiral partners**

the reduction of N-N* mass difference could be seen in eta mesonic nuclei

- **substantial effect from wave function renormalization of NG bosons**

self-energy of NG boson has energy dependence (low energy theorem)

$$Z = \left(1 - \frac{\partial \Sigma}{\partial p_0^2} \right)^{-1}$$

enhancement of K+A scattering is explained by K+ wave function renorm.

large enhancement of $\pi^0 \rightarrow \gamma \gamma$ in medium is expected

- **reduction of hadron mass**

a part of eta' meson mass is generated by chiral symmetry breaking

100 MeV reduction of eta' mass is expected in nuclear density

strong attraction of eta'-N int. from isoscalar-scalar σ exchange