

Narrow quasi-bound states *of DNN system*

1. Introduction

2. Setup for the variational calculation

I. DN potential

II. NN potential

3. Result

I. Variational calculation

- DNN bound state with $S_{NN}=0$*
- DNN state with $S_{NN}=1$*

II. Faddeev-FCA calculation

4. Comparison with strangeness sector

5. Summary

Variational part:

A. Doté (KEK theory center)
T. Hyodo, M. Oka (TITech)

Faddeev-FCA part:

M. Bayar, C. W. Xiao,
E. Oset (Valencia univ.)

*Phys. Rev. C86,
044004 (2012)*

1. Introduction

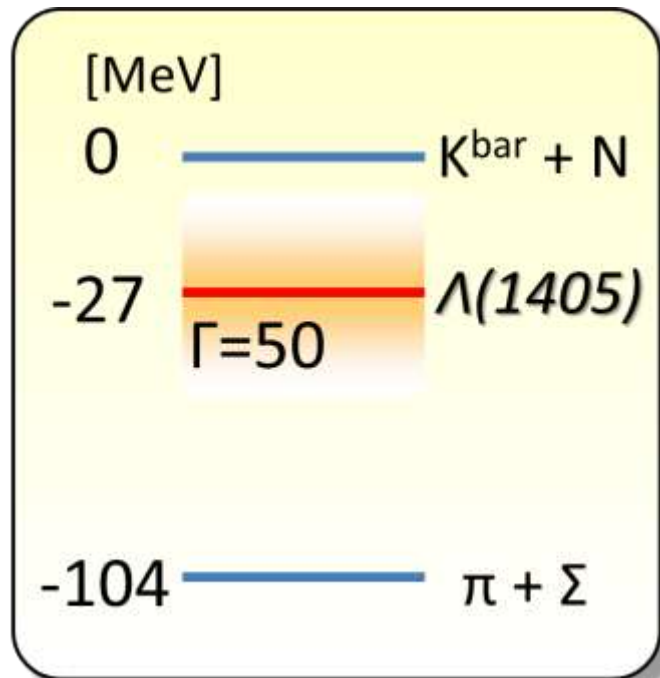
D mesic nuclei

= Charm analog system of K^{bar} nuclei?

Strangeness

$$K^{\text{bar}} = s q^{\text{bar}}$$

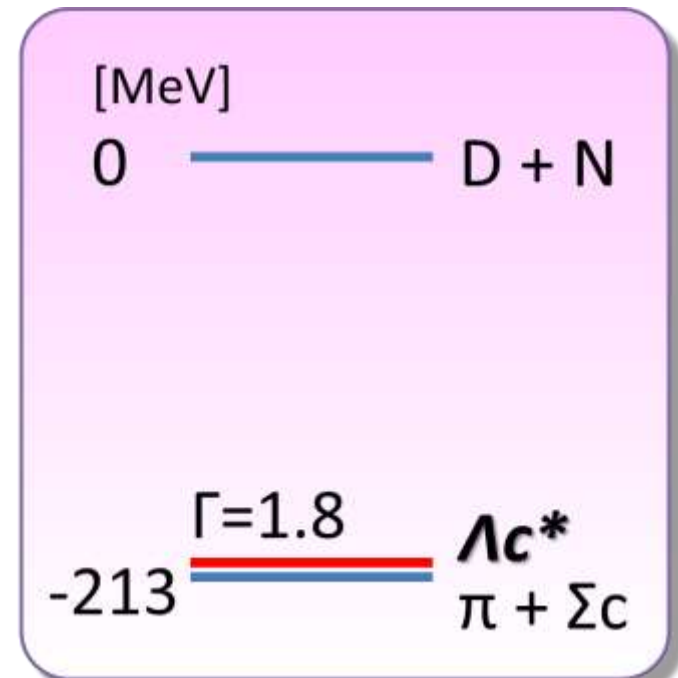
$$\Lambda(1405) = K^{\text{bar}} N \text{ Q.B.S.}$$



Charm

$$D = c q^{\text{bar}}$$

$$\Lambda_c(2595) = DN \text{ Q.B.S. ?}$$



D mesic nuclei

= Charm analog system of K^{bar} nuclei?

If $\Lambda_c(2595)$ is a quasi-bound state of $I=0$ DN system, ...

- *D nuclei may be a narrow state.*

$$\Gamma(\Lambda_c^*) = 1.8 \text{ MeV} \ll \Gamma(\Lambda^*) = 50 \text{ MeV}$$

- *Non-rela. treatment is justified.*

$$M_D = 1867 \text{ MeV} \gg M_K = 494 \text{ MeV}$$

*Physics of D mesic nuclei is more clear
than that of K^{bar} nuclei.
D nuclei may help the study of K^{bar} nuclei.*

Essential D mesic nucleus = DNN

$$\underline{K^-pp} \sim K^{\text{bar}}NN-\pi YN$$

Theoretical results:

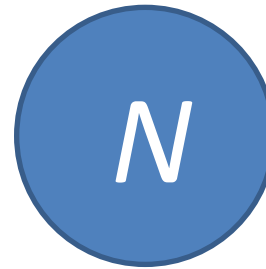
$$\text{B.E.} = 20 \sim 90 \text{ MeV}$$

$$\Gamma = 50 \sim 100 \text{ MeV}$$

K^{bar}

$$M_K = 494 \text{ MeV}$$

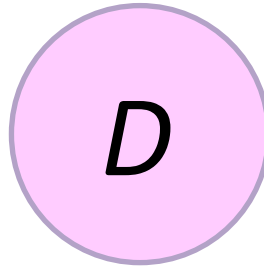
$$J^\pi = 0^-, T = 1/2$$



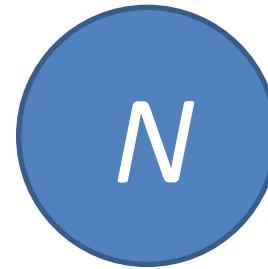
- $J^\pi = 0^-$ ($S_{NN} = 0, L = 0$), $T = 1/2$

Essential D mesic nucleus = DNN

$DNN-\pi Y_{\underline{C}}N$



$M_D = 1867 \text{ MeV}$
 $J^\pi = 0^-, T = 1/2$



- $J^\pi = 0^-$ ($S_{NN} = 0, L = 0$), $T = 1/2$

- $J^\pi = 1^-$ ($S_{NN} = 1, L = 0$), $T = 1/2$

2. Set up

2. Set up ... same as K^-pp study

A. D. , T. Hyodo and W. Weise, PRC79, 014003 (2009)

➤ Effective DN potential

Vector meson exchange picture potential

... Coupled-channel potential (DN , $\pi\Sigma_c$, $\pi\Lambda_c$...)

Generate dynamically the $I=0$ resonance $\Lambda_c(2595)$

DN single-channel potential ... equivalent as for DN scattering amplitude

DN potential

Based on Mizutani-Ramos study[†]

Coupled-channel calculation in $DN, \pi\Sigma_c, \pi\Lambda_c \dots$ etc
with WT-type interaction

- $\kappa=1/4$ for charm exchange process
... $DN \longleftrightarrow \pi Y_c$
- $\kappa=1$ for other cases

$$v_{ij}^{(I)}(W) = -\frac{\kappa C_{ij}^{(I)}}{4f^2} (2W - M_i - M_j) \sqrt{\frac{M_i + E_i}{2M_i}} \sqrt{\frac{M_j + E_j}{2M_j}}$$

- WT interaction $\approx$ Vector meson exchange potential
Due to KSRF relation

➡ Effective DN potential

Similar way to the $K^{bar}N$ study^{††}

- ✓ Eliminate other channels than DN.
- ✓ Reproduce the original DN scattering amplitude.
- ✓ Single-range Gaussian form

[†] T. Mizutani and A. Ramos, PRC74, 065201 (2006)

^{††} T. Hyodo and W. Weise, PRC77, 035204 (2007)

DN potential

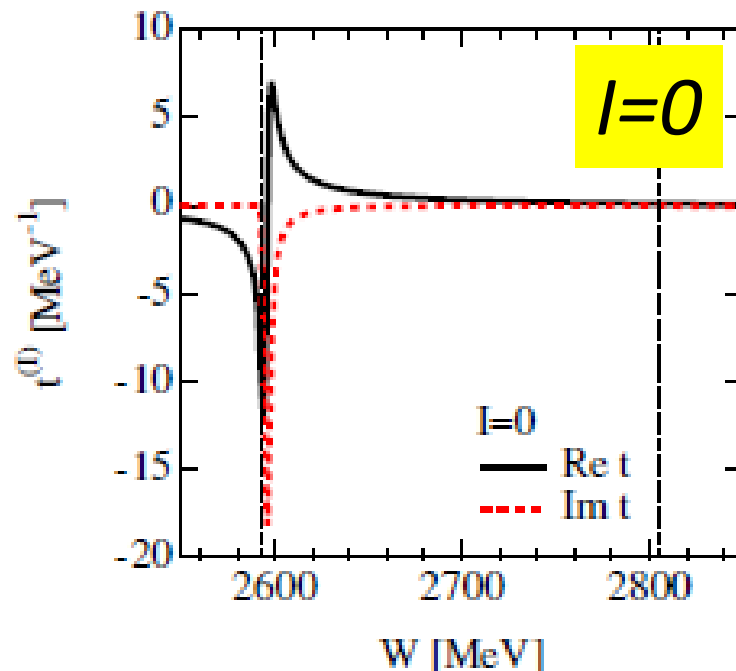
$$v_{DN}(r; W) = \frac{M_N}{2\pi^{3/2}a_s^3\tilde{\omega}(W)}$$

$$\times [v^{\text{eff}}(W) + \Delta v(W)] \exp[-(r/a_s)^2]$$

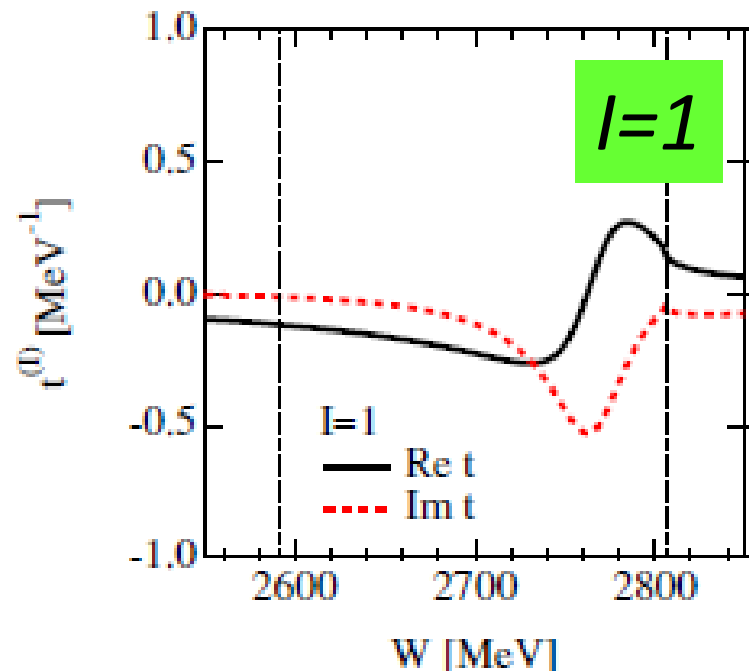
Energy-dependent pot.

$$a_s = 0.40\text{fm}$$

➤ DN scattering amplitude



$\Lambda_c(2595)$ dynamically generated



Resonance @ 2766 MeV

2. Set up ... same as K^-pp study

A. D. , T. Hyodo and W. Weise, PRC79, 014003 (2009)

➤ Effective DN potential

Vector meson exchange picture potential

... Coupled-channel potential (DN , $\pi\Sigma_c$, $\pi\Lambda_c$...)

Generate dynamically the $I=0$ resonance $\Lambda_c(2595)$

DN single-channel potential ... equivalent as for DN scattering amplitude

➤ NN potential ... NN phase shift respected

- | | | |
|--|----------------|----------------|
| • Av18 ¹⁾ | Repulsive core | ~ 3 GeV |
| • Hasegawa-Nagata No.1 ²⁾ Revised | | ~ 1 GeV |
| • Minnesota ³⁾ | | ~ 0.1 GeV |

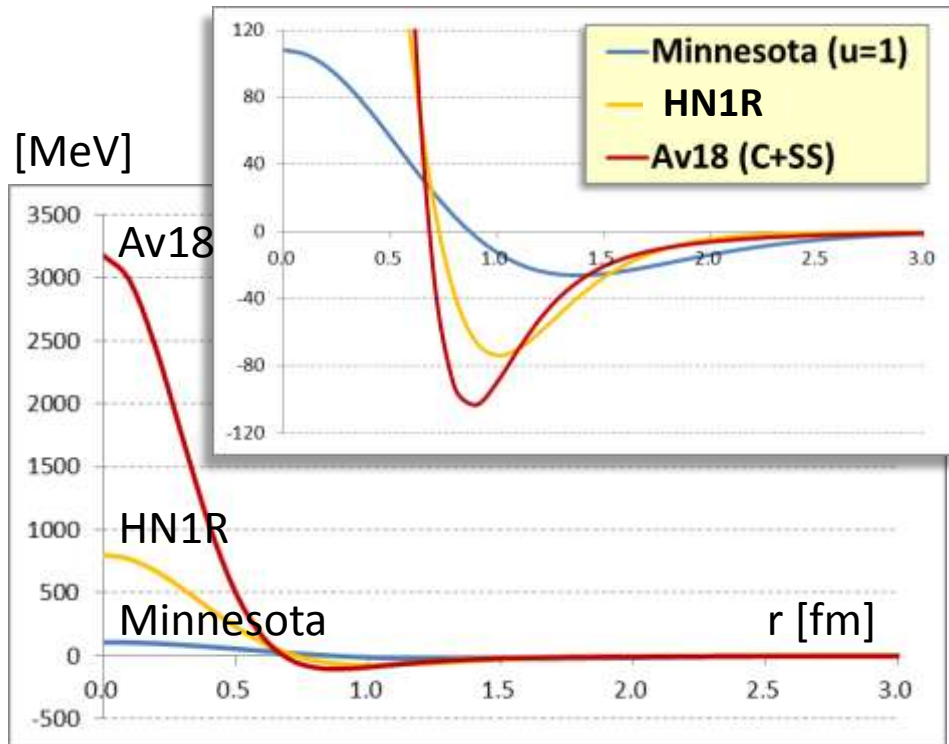
1) R. B. Wiringa, V. G. J. Stoks and R. Schiavilla, PRC51, 38 (1995)

2) A. Hasegawa and S. Nagata, PTP45, 1786 (1971)

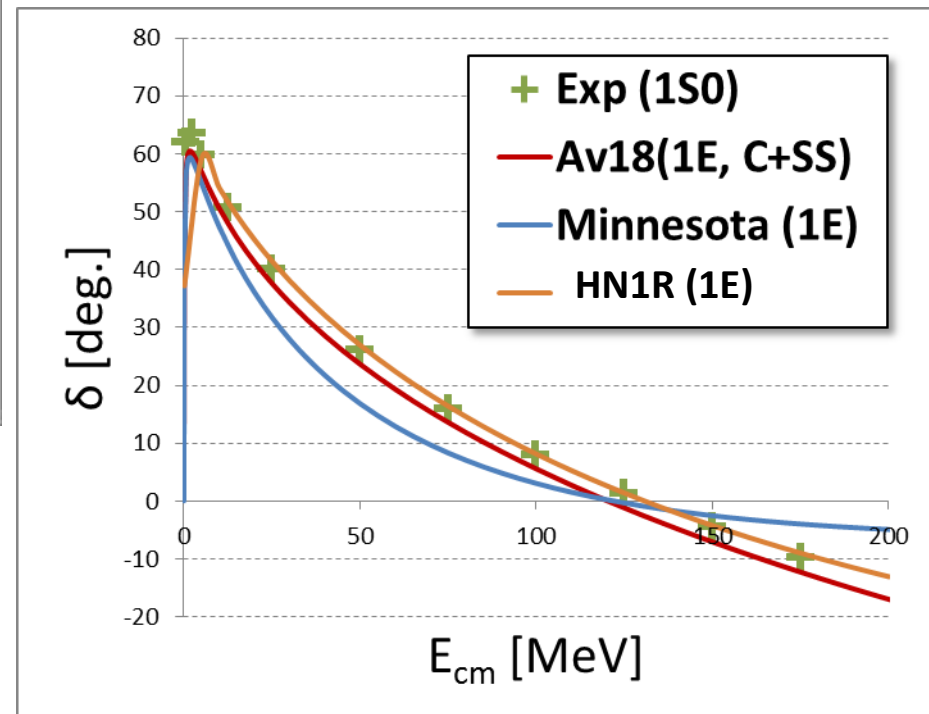
3) D. R. Thompson, M. Lemere and Y. C. Tang, NPA286, 53 (1977)

NN potentials = Minnesota, HN1R, Av18

Potential (1E channel)



Phase shift (1S_0)



* HN1R = slightly modified Hasegawa-Nagata No.1

- 3E channel: Reproduce B. E. of deuteron
- 1E channel: No bound state in 1S_0 channel

$$0.25 \times V_1 + 0.95 \times V_2 + 1.00 \times V_3$$

Long	Middle	Short
-range	-range	-range

2. Set up ... same as K^-pp study

A. D. , T. Hyodo and W. Weise, PRC79, 014003 (2009)

➤ Effective DN potential = Complex potential

Vector meson exchange picture potential

... Coupled-channel potential (DN , $\pi\Sigma_c$, $\pi\Lambda_c$...)

Generate dynamically the $I=0$ resonance $\Lambda_c(2595)$

DN single-channel potential ... equivalent as for DN scattering amplitude

➤ NN potential ... NN phase shift respected

- | | | |
|--------------------------------|----------------|----------------|
| • Av18 | Repulsive core | ~ 3 GeV |
| • Hasegawa-Nagata No.1 Revised | | ~ 1 GeV |
| • Minnesota | | ~ 0.1 GeV |

➤ Variational calculation

- Use the ***real part*** of the effective DN potential
- Expand the trial wave function with Gaussian base

3. Result

DNN bound state
with $S_{\underline{NN}}=0$

$L=0$

$$J^\pi=0^-, T=1/2$$

$DNN(S=0)$: Minnesota, HN1R, Av18

DN pot. :
 $b=0.40\text{fm}$,
 $B(D)=208.9\text{MeV}$

B. E. and size of $DNN(S=0)$

NN

Minnesota

HN1R

Av18 (C+SS)

B. E.

250.9 MeV

225.4 MeV

209.4 MeV

R_{rms}

0.5 fm

0.75 fm

1.26 fm

$\Lambda_c^* - N$

42 MeV

16.5 MeV

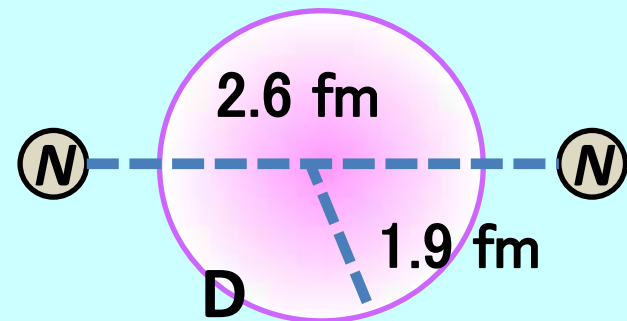
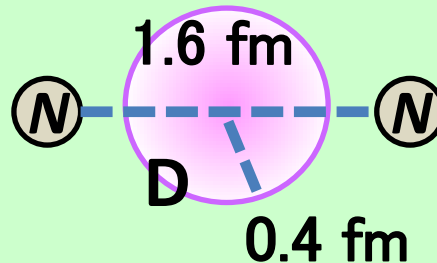
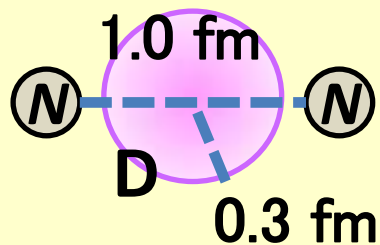
0.5 MeV

DNN
($S=0$)

$\Gamma(\pi Y_c)=38\text{MeV}$

$\Gamma(\pi Y_c)=26\text{MeV}$

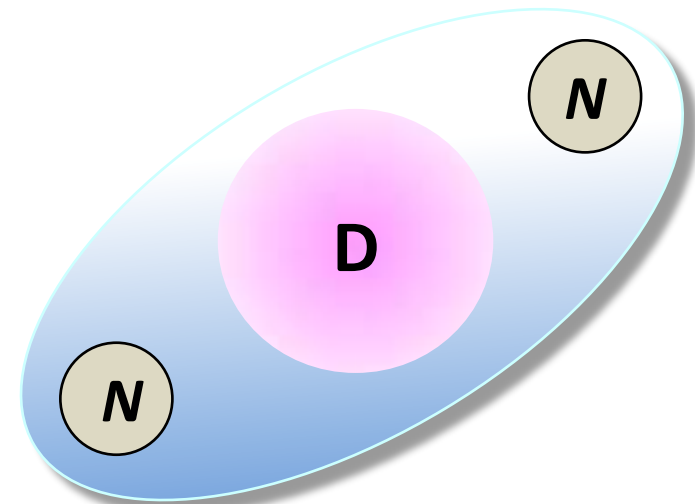
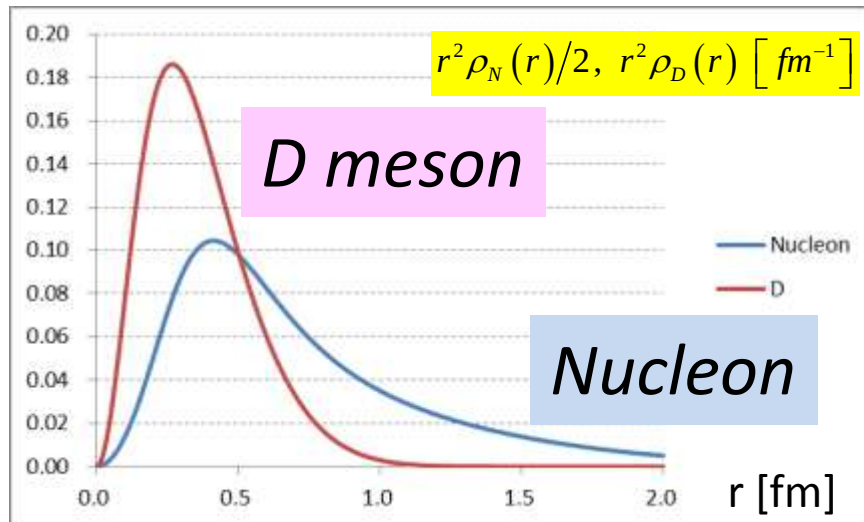
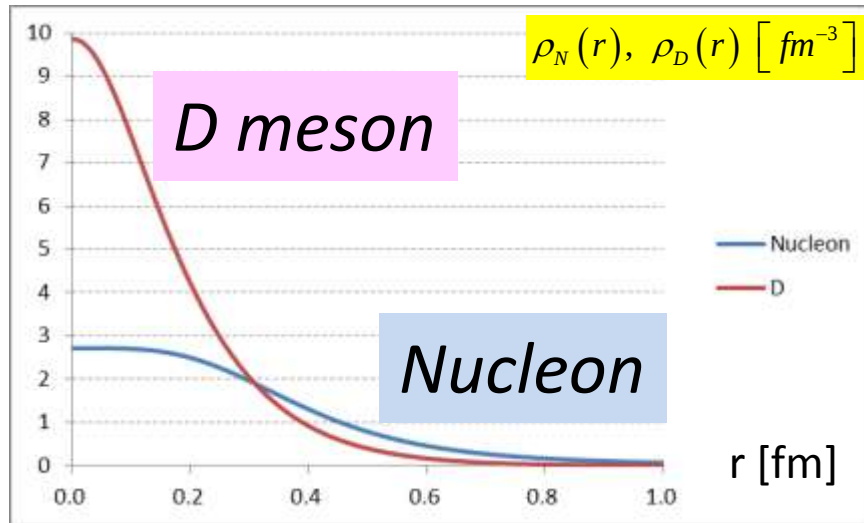
$\Gamma(\pi Y_c)=22\text{MeV}$



Structure of DNN ($S=0$)

NN pot: HN1R
DN pot. : $b=0.40\text{fm}$,
 $B(D)=208.9\text{MeV}$

One-body density

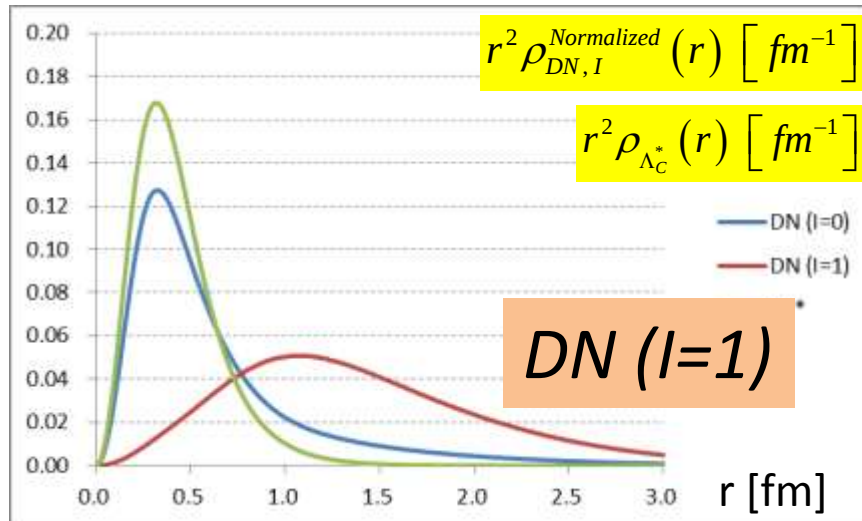
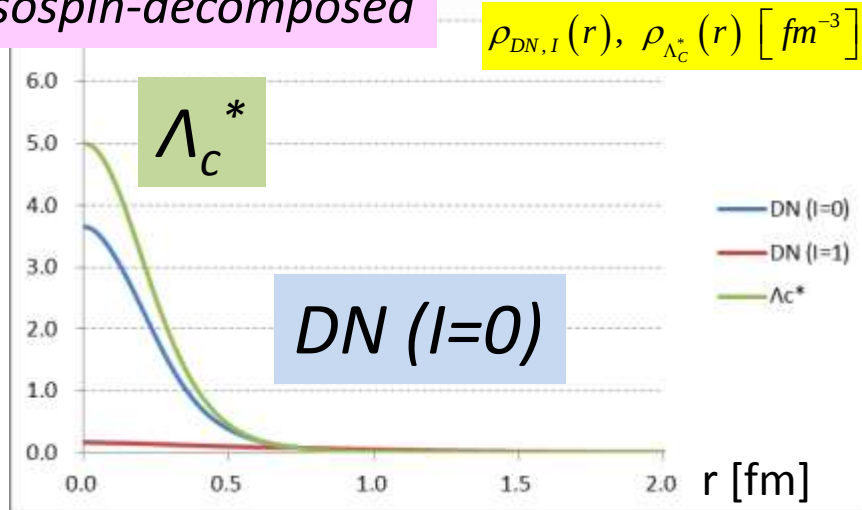


D meson distributes compactly inside of the system.

Structure of DNN ($S=0$)

DN correlation density

Isospin-decomposed

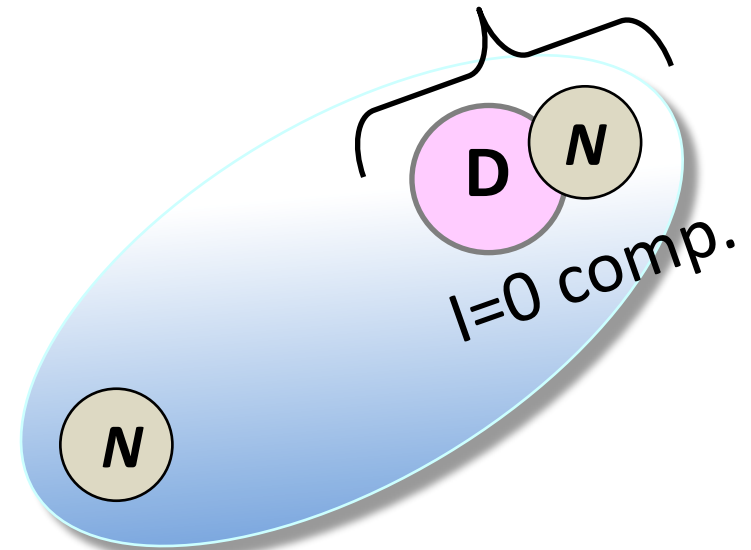


NN pot: HN1R

DN pot. : $b=0.40\text{fm}$,

$B(D)=208.9\text{MeV}$

Λ_c^*



- The distribution of the $l=0$ DN component in DNN ($S=0$) system is similar to that of **the DN forms Λ_c^*** . (Similar to $K^{\text{bar}}\text{NN}$ case)

3. Result

DNN bound state

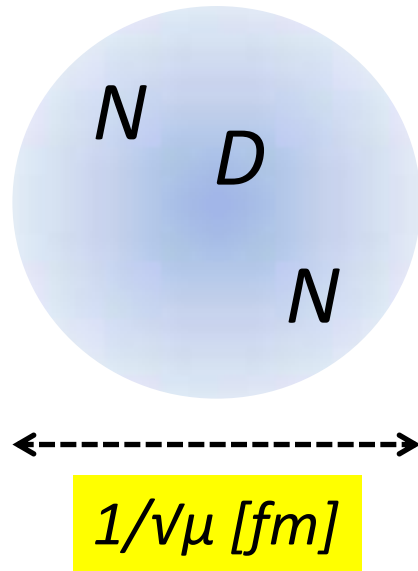
with $S_{\underline{NN}}=1$

$L=0$

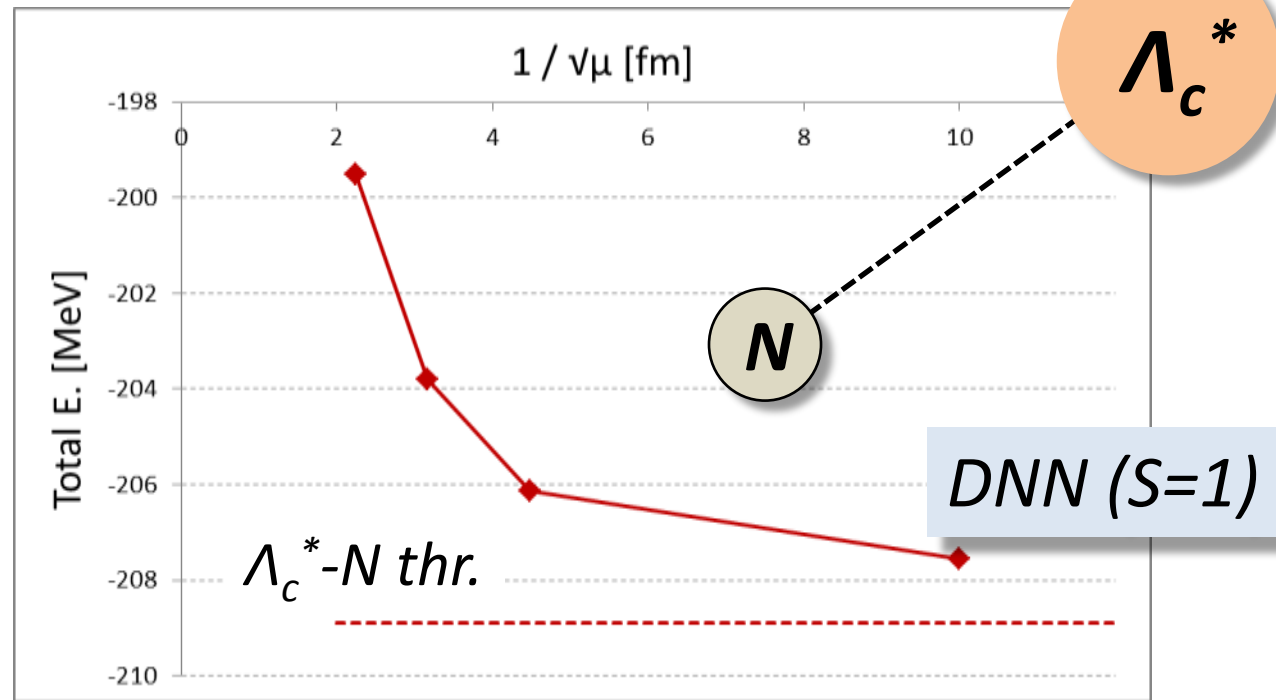
$$J^\pi=1^-, T=1/2$$

$S=1$ state of DNN

NN pot: HN1R
DN pot. : $b=0.40\text{fm}$,
 $B(D)=208.9\text{MeV}$



Total energy vs $1/v\mu$



- Increase $1/v\mu$
 $\Rightarrow$ DNN ($S=1$) energy $\rightarrow \Lambda_c^*-N$ threshold energy

$\rightarrow \Lambda_c^*-N$ scattering state !

3. Result

*Faddeev calculation
with **Fixed Center Approximation***

$$J^\pi=0^-, T=1/2$$

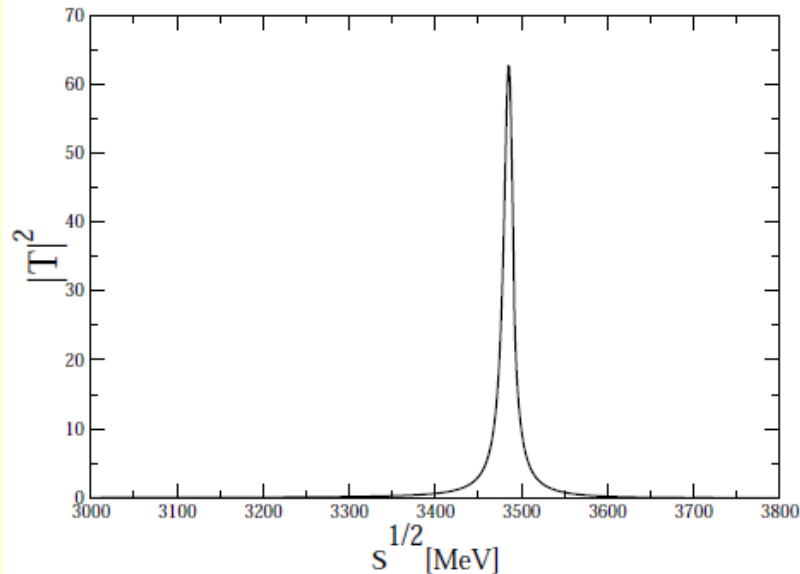
$$J^\pi=1^-, T=1/2$$

DNN with Faddeev-FCA calculation

Result (with 2N absorption)

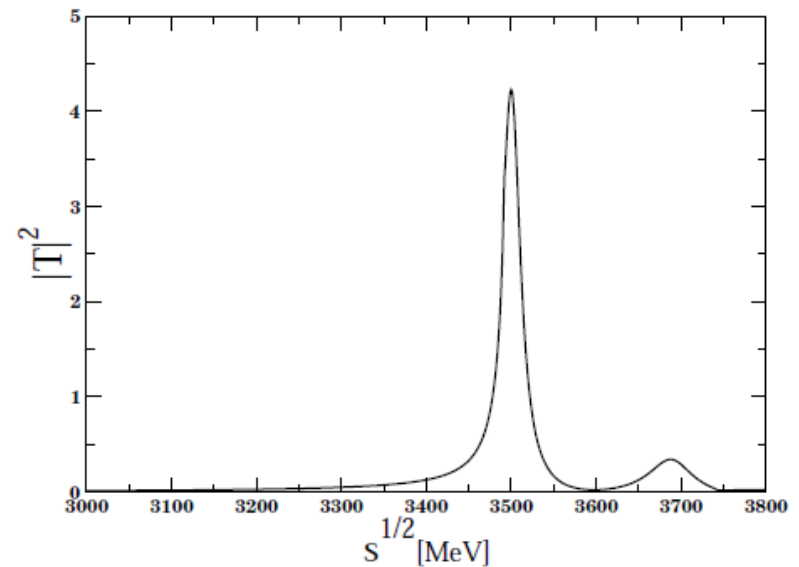
$$J^\pi=0^-, T=1/2$$

Total mass ~ 3490 MeV



$$J^\pi=1^-, T=1/2$$

Total mass ~ 3500 MeV



- ~ 250 MeV below DNN threshold
- ... both states are below $\Lambda_c^* N$ threshold
- Full decay width ~ 20 -25 MeV

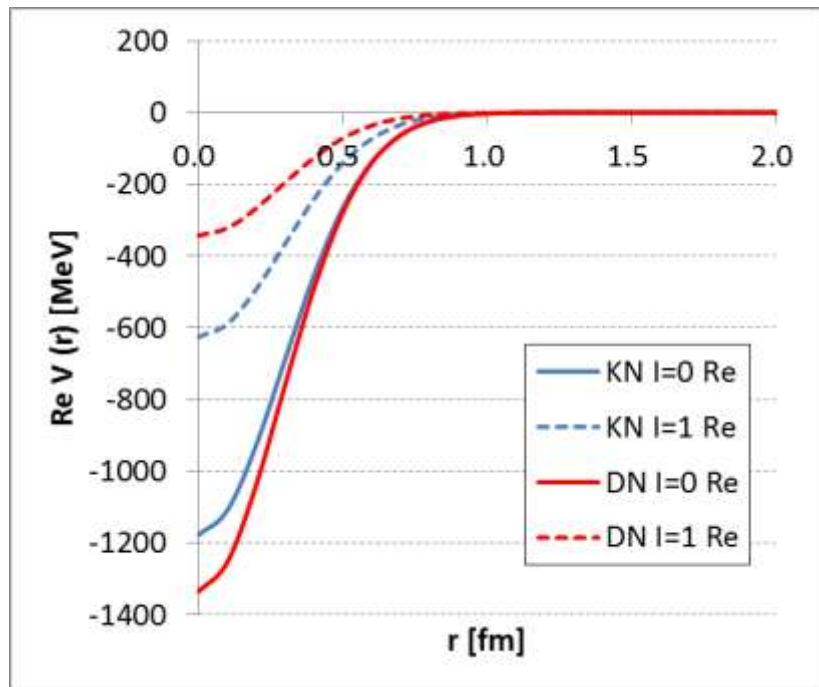
4. Comparison with strangeness sector

DNN vs K^{bar} NN

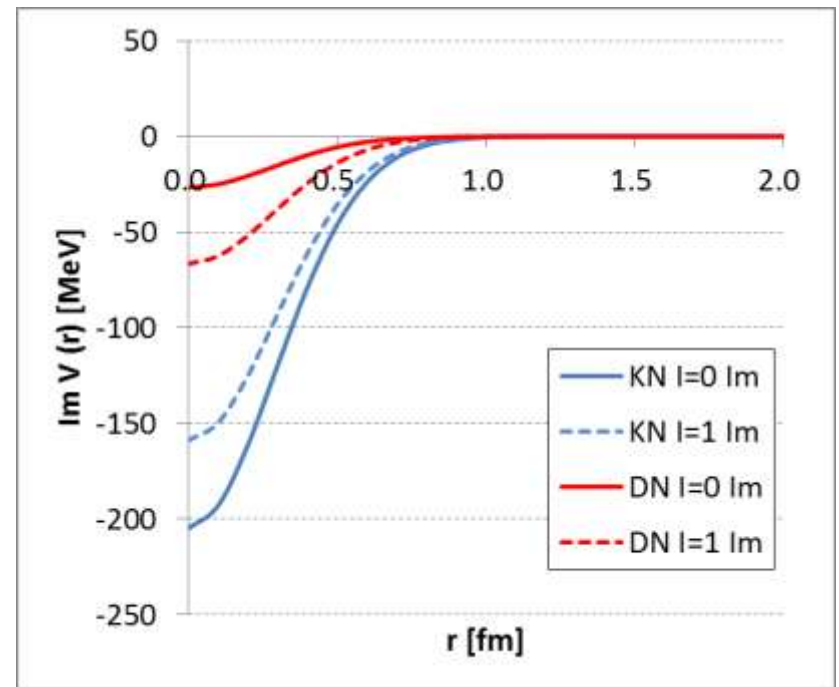
Potential at $I=0$ resonance

$K^{\text{bar}}N$ pot. ($b=0.41\text{fm}$) @ $B_K=13.3\text{MeV}$... Λ^* $R(K^{\text{bar}}N) = 1.72\text{ fm}$
DN pot. ($b=0.40\text{fm}$) @ $B_D=208.9\text{MeV}$... Λ_c^* $R(DN) = 0.49\text{ fm}$

Real



Imaginary



*In $I=0$ channel,
 $K^{\text{bar}}N$ pot. $\doteq$ DN pot.*

*Imaginary potential,
 $K^{\text{bar}}N$ pot. $\gg$ DN pot.*

DNN vs K^{bar} NN

NN pot.: HN1R

$K^{\text{bar}}N$ potential

DN potential

M_K

$K^{\text{bar}}NN$

Total B.E. = 28 MeV
 Γ = 67 MeV

M_D

DNN

Total B.E. = 225 MeV
 Γ = 26 MeV

DNN vs K^{bar} NN

NN pot.: HN1R

$K^{\text{bar}}N$ potential

DN potential

$K^{\text{bar}}NN$

B.E. not so increase.

M_K

Total B.E. = 28 MeV
 Γ = 67 MeV

Total B.E. = 40 MeV
 Γ = 11 MeV

*Γ decreases,
due to small $\text{Im } V_{DN}$*

M_D

DNN

Total B.E. = 225 MeV
 Γ = 26 MeV

DNN vs $K^{\text{bar}}NN$

$K^{\text{bar}}N$ potential

DN potential

$K^{\text{bar}}NN$

Total B.E. = 28 MeV
 Γ = 67 MeV

Total B.E. = 40 MeV
 Γ = 11 MeV

B.E. drastically increases.

DNN

Total B.E. = 187 MeV
 Γ = 180 MeV

Total B.E. = 225 MeV
 Γ = 26 MeV

Suppression of kinetic energy of D meson

M_K

M_D

DNN vs $K^{\text{bar}}NN$

NN pot.: HN1R

	$K^{\text{bar}}N$ potential	DN potential
M_K	<u>$K^{\text{bar}}NN$</u> Total B.E. = 28 MeV Γ = 67 MeV	Total B.E. = 40 MeV Γ = 11 MeV Kin. E. 352 $\rightarrow$ 681 MeV if $m_D \rightarrow m_K$.
M_D	Total B.E. = 187 MeV Γ = 180 MeV	<u>DNN</u> Total B.E. = 225 MeV Γ = 26 MeV

Suppression of kinetic energy of D meson

5. Summary

5. Summary

The DNN system studied with two approaches:

Variational and Faddeec-FCA approaches

- Charm analog state of $K^{bar}NN$
- $J^\pi=0^-$ ($S_{NN}=0$) and 1^- ($S_{NN}=1$), $T=1/2$

DN potential

- Based on *vector-meson exchange picture*
- $\Lambda_c(2595)$... described as a *DN resonance of $l=0$*
- [Variational] Effective DN potential reproducing
 $l=0$ scattering amplitude with single Gaussian form

NN potentials [Variational]

- | | | |
|----------------------------|-----|--------------------|
| • Minnesota | ... | Soft core (0.1GeV) |
| • Hasegawa Nagata No.1 (R) | ... | Mild core (1GeV) |
| • Av18 (Gaussian fitted) | ... | Hard core (3GeV) |

5. Summary

As a result of variational calculation, ...

DNN ($J^\pi=0^-$) ... bound below $\Lambda_c(2595)$ -N threshold

- Total B. E. ~ 225 MeV
(~ 15 MeV below $\Lambda_c(2595)$ -N threshold
Total mass ~ 3520 MeV)
- Decay width (πY_c) ~ 25 MeV
... narrow compared with total B.E.

D meson stays at center of the system, $l=0$ DN component $\doteq \Lambda_c(2595)$

DNN ($J^\pi=1^-$) ... scattering state of $\Lambda_c(2595)$ -N

Faddeev-FCA calculation supports the result of variational calculation.

“Mass effect” = Suppression of kinetic energy of D meson
due to its heavy mass

Dora-cat in KEK

***Thank you
for
your attention!***

D

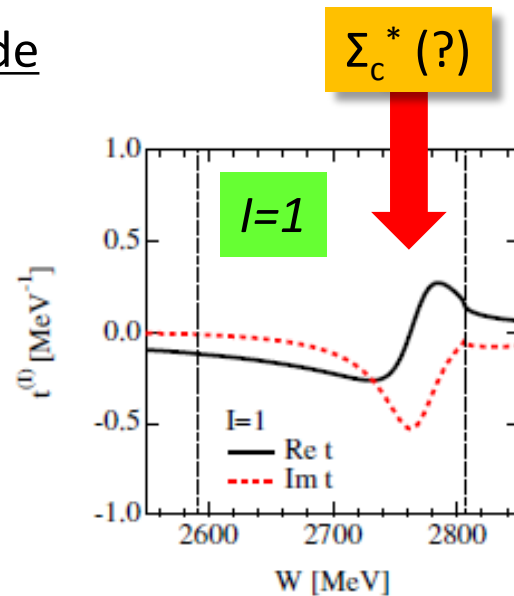
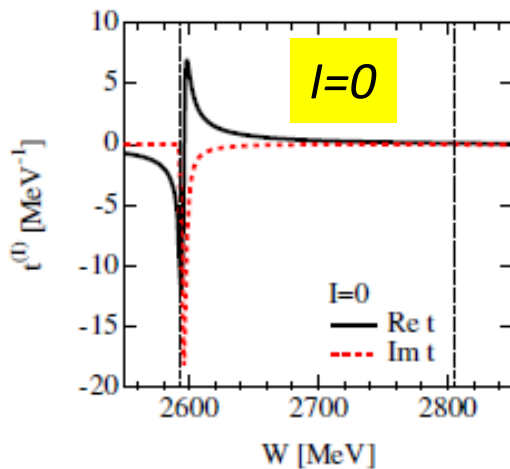
N

N

与太話

- DNN (T=3/2)は？ ... DN(I=1)がdominate

DN scattering amplitude



共鳴状態が出来るほど、
DN $I=1$ チャンネルも引力が強い。

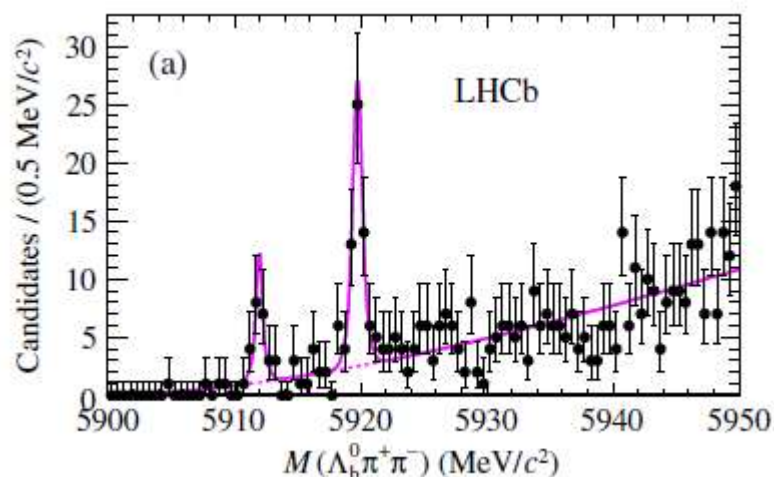
$W \sim 2766$ MeV
($B(\text{DN}) \sim 40$ MeV)

Σ_c^* N より束縛するか？

与太話

• Bottom sectorは？

LHCbで見つかった二つの Λ_b^*



$\Lambda_b^*(5912), \Lambda_b^*(5920)$

$\Gamma < 0.66, 0.63$ MeV

R. Aaij, et al., PRL109, 172003 (2012)

BN ————— 6218 (0)

$\pi \Sigma_b$ ————— 5949 (-269)

$\Lambda_b^*(5920)$ ————— 5920 (-298)
 $\Lambda_b^*(5912)$ =————= 5912 (-306)

$\pi \pi \Lambda_b$ ————— 5895 (-323)

Σ_b ————— 5811 (-407)

$\pi \Lambda_b$ ————— 5757 (-461)

Λ_b ————— 5619 (-599)

$B^\pm$ (5279), B^0 (5280)