Structure of p-sd shell Λ hypernuclei modified and probed by Λ hyperon

Masahiro ISAKA

Institute of Physical and Chemical Research (RIKEN)

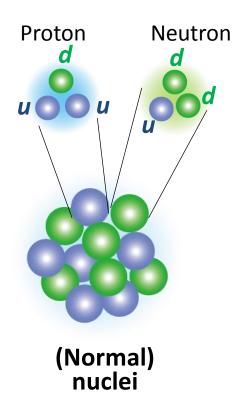
Collaborators: H. Homma, M. Kimura (Hokkaido Univ.)

A. Dote (KEK)

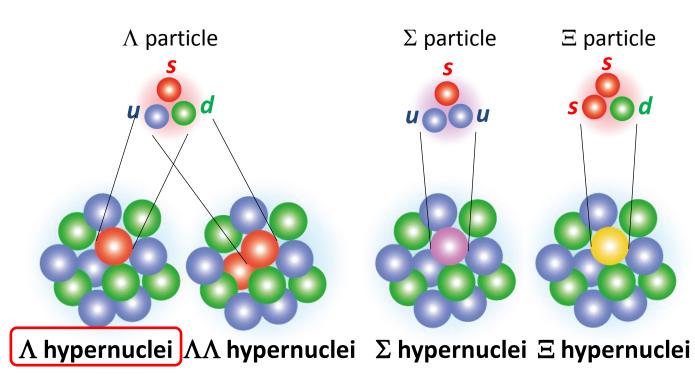
A. Ohnishi (YITP, Kyoto Univ.)

Hypernucleus

- Normal nuclei
 - Nucleons
 - proton
 - neutron



- Hypernuclei
 - Nucleons and hyperon(s) (Λ, Σ, Ξ)
 - Hyperons have strange quark(s)
 - → Hypernuclei are nuclei with s quark(s)



Extended to baryon (p, n and hyperons) many-body system

Grand challenge of hypernuclear physics

Interaction: To understand baryon-baryon interaction

- 2 body interaction between baryons (nucleon, hyperon)
 - hyperon-nucleon (YN)

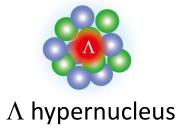
hyperon-hyperon (YY)

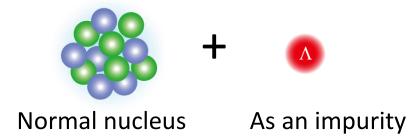
A major issue in hypernuclear physics

Structure: To understand properties of baryon many-body system

- Structure change caused by hyperon(s)
 - No Pauli exclusion between N and Y
 - YN interaction is different from NN

"Hyperon as an impurity in nuclei"





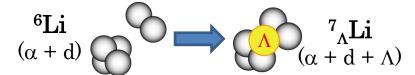
Unique aspects of Λ hypernuclei

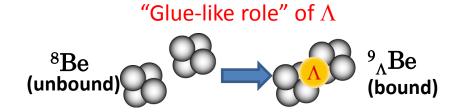
- ullet Λ has no Pauli blocking to nucleons
- ◆ AN attraction (different from NN)

Unique phenomena

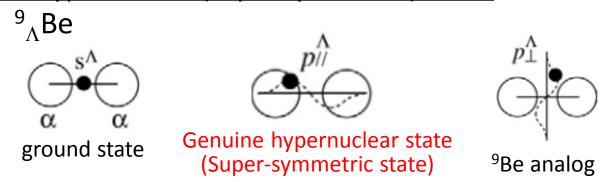
Structure change:

Shrinkage of the inter-cluster distance





Genuine hypernuclear (super symmetric) states:



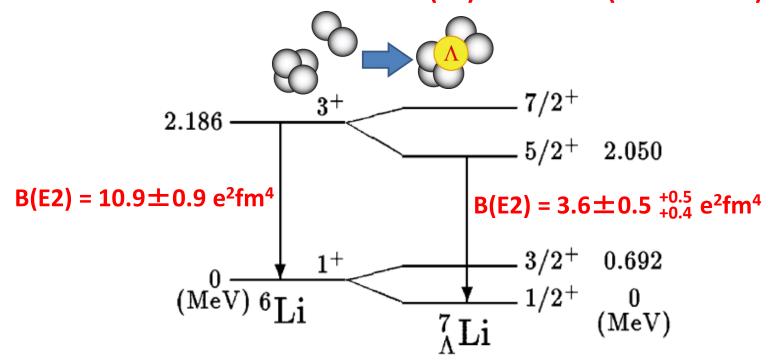
A unique probe: Λ can penetrate into nuclear interior

Structure change by Λ : "Shrinkage effect"

Shrinkage effect: Λ hyperon makes nucleus compact

Example: ${}^{7}_{\Lambda} \text{Li}^{\,[1,2]}$

- T. Motoba, et al., PTP **70**, 189 (1983); T. Motoba, et al., PTPS **81**, 42(1985).
- E. Hiyama, et al., Phys. Rev. C59 (1999), 2351.
- K. Tanida, et al., Phys. Rev. Lett. 86 (2001), 1982.
- $^6\mathrm{Li}$: α + d cluster structure
- ullet Λ hyperon penetrates into the nuclear interior
- Λ hyperon reduces $\alpha + d$ distance \longrightarrow B(E2) reduction (Observable)

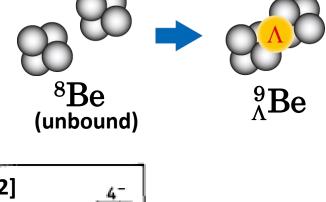


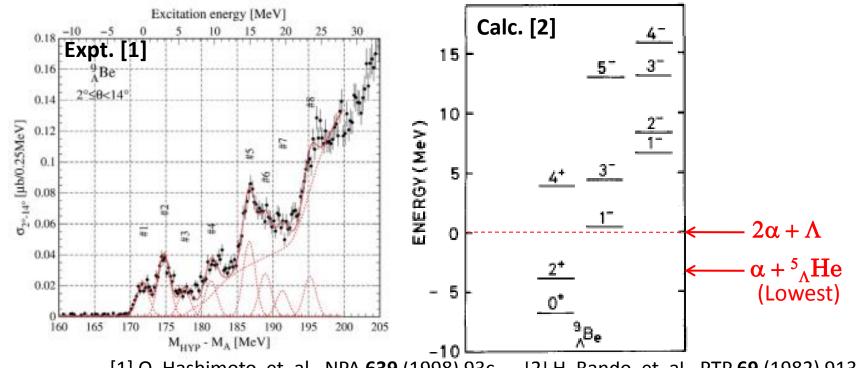
Structure change by Λ : "Glue-like role"

Glue-like role: Λ hyperon stabilizes unbound state

Example: $^9_\Lambda Be$

- 8Be is an unstable nucleus
- Its g.s. lies at about 100 keV above $\alpha + \alpha$ threshold
- ${}^{9}_{\Lambda}$ Be is bound with an $\alpha + \alpha + \Lambda$ structure





[1] O. Hashimoto, et. al., NPA **639** (1998) 93c. [2] H. Bando, et. al., PTP **69** (1982) 913.

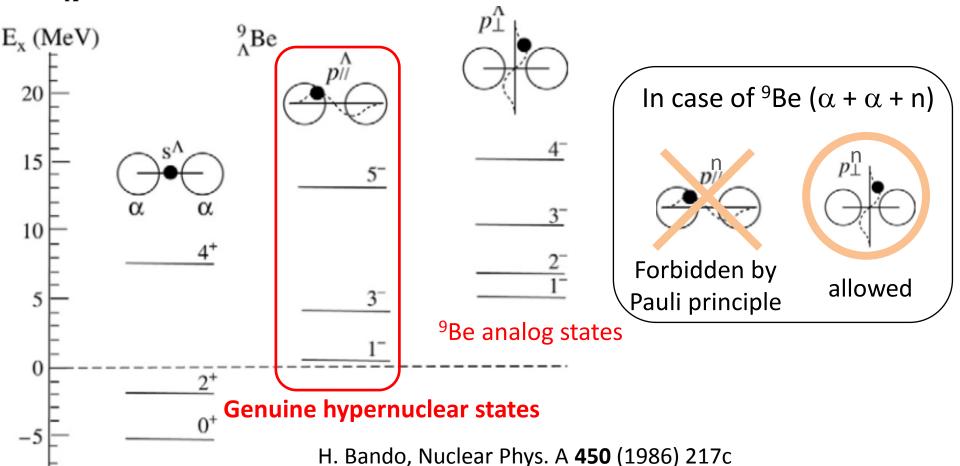
Genuine hypernuclear (super symmetric) state

Genuine hypernuclear states cannot be formed in ordinary ⁹Be

Example: ${}_{\Lambda}^{9}\mathrm{Be}$

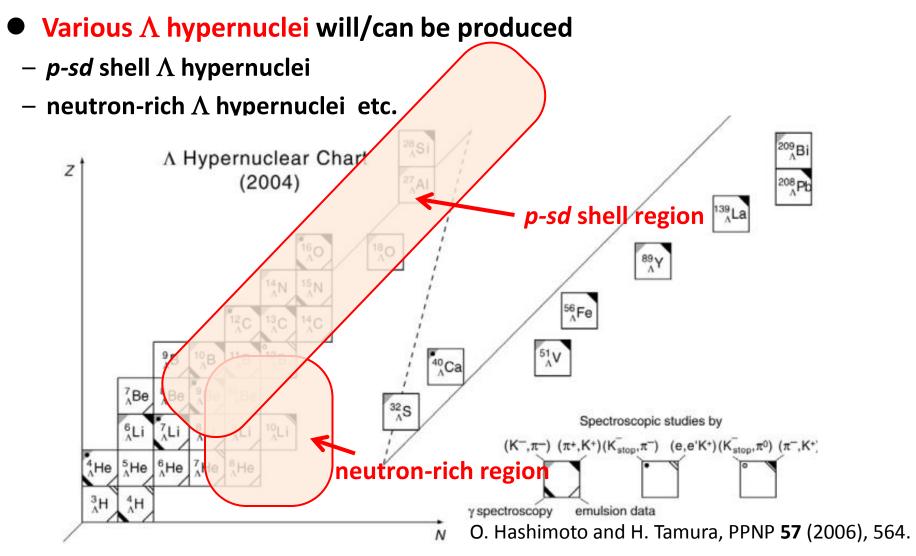
R.H. Dalitz, A. Gal, Phys. Rev. Lett. **36** (1976) 362 H. Bando, Nuclear Phys. A **450** (1986) 217c

• ${}^{9}_{\Lambda}$ Be: $\alpha + \alpha + \Lambda$ structure



Toward heavier and exotic Λ hypernuclei

Experiments at J-PARC, JLab and Mainz etc.



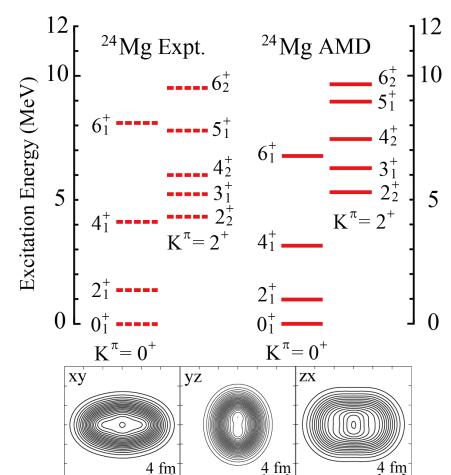
Structure study of such hypernuclei becomes one of interesting topics

Structure of sd shell and neutron-rich nuclei

Various structures

Ex) ²⁴Mg: typical *sd*-shell nucleus

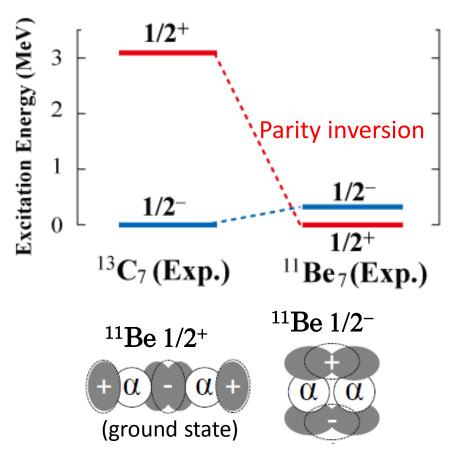
- Large deformation
- Candidate of triaxial deformed nucleus



Exotic (cluster) structure in n-rich nuclei

Ex) ¹¹Be: n-rich nucleus

- Parity inverted ground state
- Molecular orbit of extra neutrons



Y. Kanada-En'yo and H. Horiuchi, PRC 66 (2002), 024305.

Purpose of this study

- Purpose
 - ullet To reveal structure of Λ hypernuclei in (p-)sd shell and n-rich region
 - "Structure change"
 - " Λ as a probe to study nuclear structure"
- ◆ Individual problems (In this talk)
 - lacktriangle Possible structure changes caused by Λ

As general trends

– Deformation change by adding Λ

Λ 's effects to the observables (excitation spectra)

- Parity reversion of the ground state in n-rich $^{12}_{\Lambda}$ Be
- Changes of excitation spectrum in triaxially deformed $^{25}\Lambda$ Mg
- lacktriangle Probing nuclear deformation by using Λ
 - $^{25}{}_{\Lambda}Mg$: to reveal triaxial deformation of ^{24}Mg

Strategy: based on the developments

Developments of hypernuclear physics: interaction

■ Knowledge of AN effective interaction

E. Hiyama, NPA **805** (2008), 190c.

O. Hashimoto and H. Tamura, PPNP 57 (2006), 564.

Development of theoretical models

Through the study of unstable nuclei

Ex.: Antisymmetrized Molecular Dynamics (AMD)

Y. Kanada-En'yo et al., PTP **93** (1995), 115.

- AMD describes dynamical changes of various structure
- No assumption on clustering and deformation

 \longrightarrow Constructing a new model to describe hypernuclear structure "Systematic study of Λ hypernuclear structure"

Forthcoming experiments

- To compare our prediction with the forthcoming experiments
 - Variety of p-sd shell Λ hypernuclei

Theoretical framework: HyperAMD

We extended the AMD to hypernuclei

HyperAMD (Antisymmetrized Molecular Dynamics for hypernuclei)

♦ Hamiltonian

$$\hat{H}=\hat{T}_N+\hat{V}_{NN}+\hat{T}_\Lambda+\hat{V}_{\Lambda N}$$
 NN: Gogny D1S Λ N: YNG interaction (Central force) [1]

◆Wave function

Nucleon part: Slater determinant
 Spatial part of single particle w.f. is
 described as Gaussian packet

$$\varphi_{N}(\vec{r}) = \frac{1}{\sqrt{A!}} \det \left[\varphi_{i}(\vec{r}_{j}) \right]$$

$$\varphi_{i}(r) \propto \exp \left[-\sum_{\sigma=x,y,z} v_{\sigma}(r - Z_{i})_{\sigma}^{2} \right] \chi_{i} \eta_{i} \quad \chi_{i} = \alpha_{i} \chi_{\uparrow} + \beta_{i} \chi_{\downarrow}$$

• Single particle w.f. of Λ hyperon: Superposition of Gaussian packets

$$\varphi_{\Lambda}(r) = \sum_{m} c_{m} \varphi_{m}(r)$$

$$\varphi_{m}(r) \propto \exp \left[-\sum_{\sigma=x,y,z} \mu v_{\sigma}(r-z_{m})_{\sigma}^{2} \right] \chi_{m} \qquad \chi_{m} = a_{m} \chi_{\uparrow} + b_{m} \chi_{\downarrow}$$

• Total w.f.:

$$\psi(\vec{r}) = \sum_{m} c_{m} \varphi_{m}(r_{\Lambda}) \otimes \frac{1}{\sqrt{A!}} \det[\varphi_{i}(\vec{r}_{j})]$$

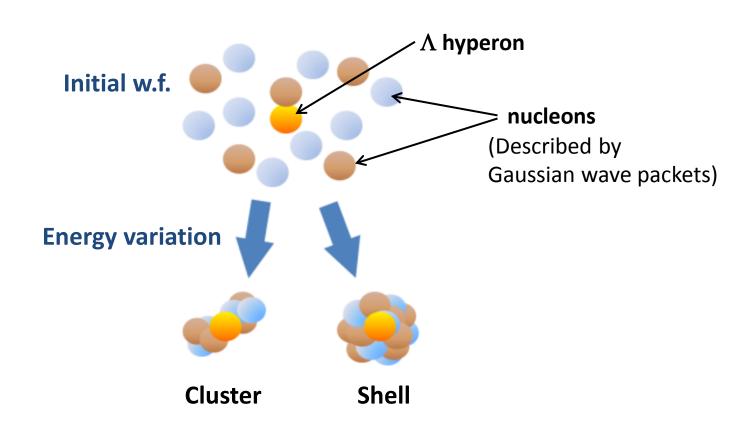
[1] Y. Yamamoto, T. Motoba, H. Himeno, K. Ikeda and S. Nagata, Prog. Theor. Phys. Suppl. 117 (1994), 361.

Theoretical framework: HyperAMD

Procedure of the calculation

Variational Calculation

- $\frac{dX_i}{dt} = \frac{\kappa}{\hbar} \frac{\partial H^{\pm}}{\partial X_i^*} \qquad \kappa < 0$ • Imaginary time development method
- Variational parameters: $X_i = Z_i, z_i, \alpha_i, \beta_i, a_i, b_i, v_i, c_i$



Theoretical framework: HyperAMD

Procedure of the calculation

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Angular Momentum Projection

$$|\Phi_K^s; JM\rangle = \int d\Omega D_{MK}^{J^*}(\Omega) R(\Omega) |\Phi^{s+}\rangle$$

Generator Coordinate Method(GCM)

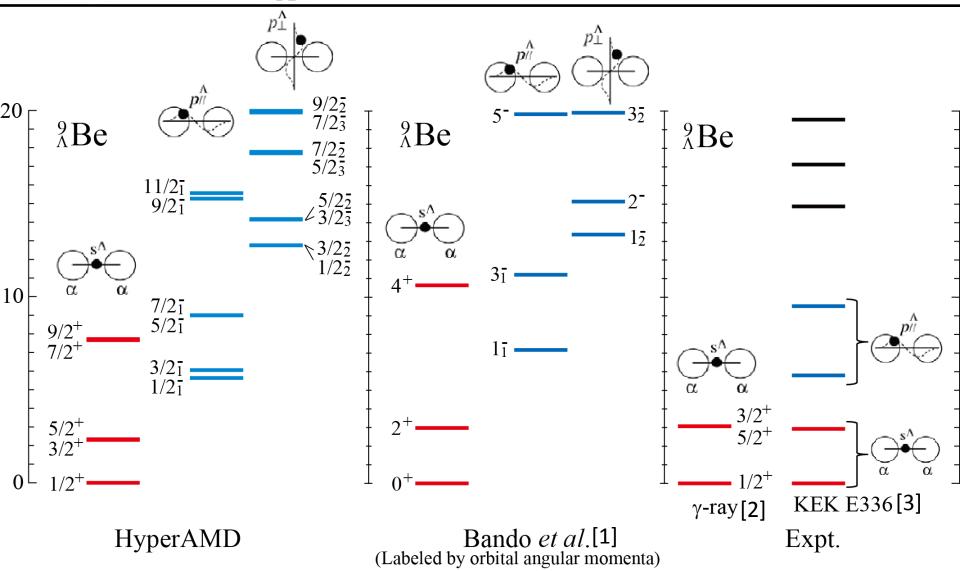
- •Superposition of the w.f. with different configuration
- •Diagonalization of $H^{J\pm}_{sK,s'K'}$ and $N^{J\pm}_{sK,s'K'}$

$$H_{sK,s'K'}^{J\pm} = \left\langle \Phi_K^s; J^{\pm}M \middle| \hat{H} \middle| \Phi_{K'}^{s'}; J^{\pm}M \right\rangle$$

$$N_{sK,s'K'}^{J\pm} = \left\langle \Phi_K^s; J^{\pm}M \middle| \Phi_{K'}^{s'}; J^{\pm}M \right\rangle$$

$$|\Psi^{J\pm M}\rangle = \sum_{sK} g_{sK} \middle| \Phi_K^s; J^{\pm}M \rangle$$

Application to ${}^{9}_{\Lambda}$ Be hypernucleus



[1] Bando *et al.*, PTP **66** (1981) 2118.

[2] M. May et al., PRL **51** (1983) 2085; H. Akikawa et al., PRL **88** (2002) 082501.

[3] O. Hashimoto et al., NPA **639** (1998) 93c

Structure change by Λ

• Nuclear deformation change by Λ (in s and p orbits)

Examples: ${}^{9}_{\Lambda}$ Be, ${}^{13}_{\Lambda}$ C, ${}^{20}_{\Lambda}$ Ne and ${}^{21}_{\Lambda}$ Ne

M. Isaka, M. Kimura, A. Dote and A. Ohnishi, PRC 83 (2011), 044323.

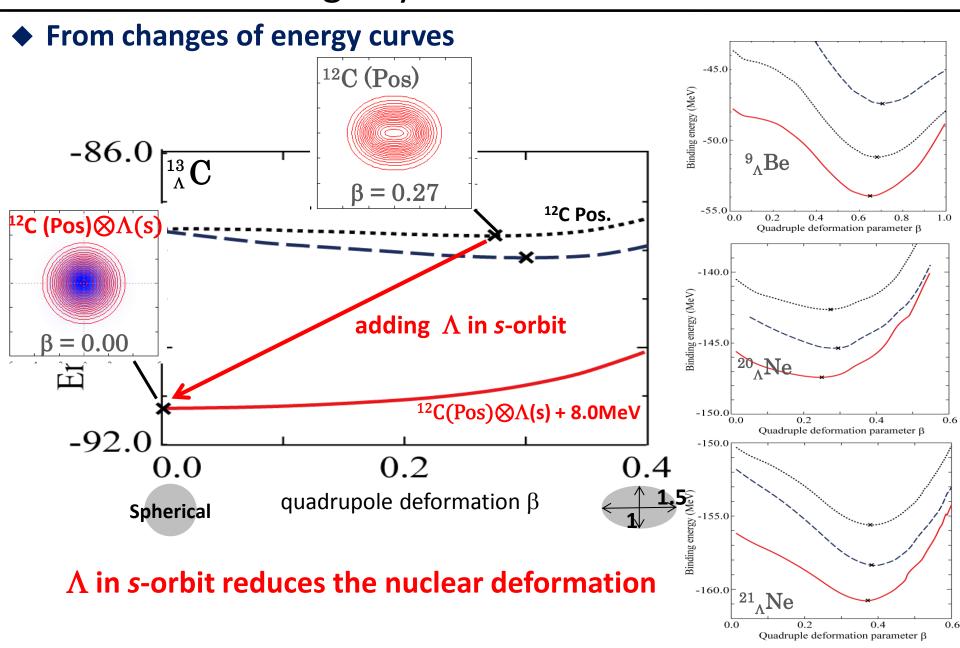
Parity reversion of the ground state in n-rich ¹² Be

H. Homma, M. Isaka and M. Kimura, to be submitted

Changes of excitation spectrum in triaxially deformed ²⁵ Mg

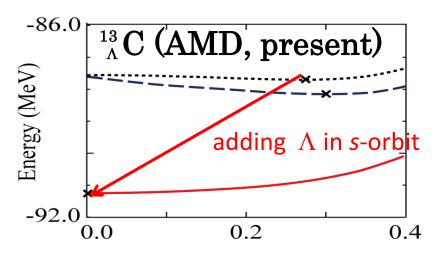
M. Isaka, M. Kimura, A. Dote and A. Ohnishi, PRC 85 (2012), 034303.

Deformation change by Λ in s-orbit

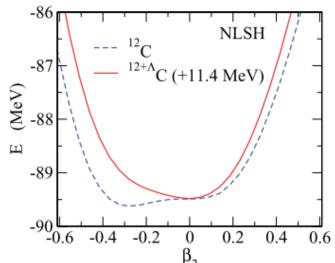


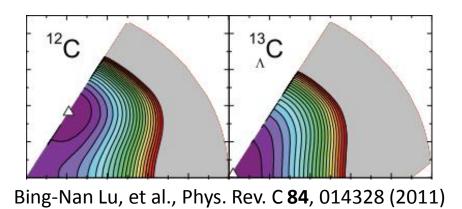
Deformation change by Λ in *s*-orbit

lacktriangle Many authors predict the deformation change by Λ in s-orbit



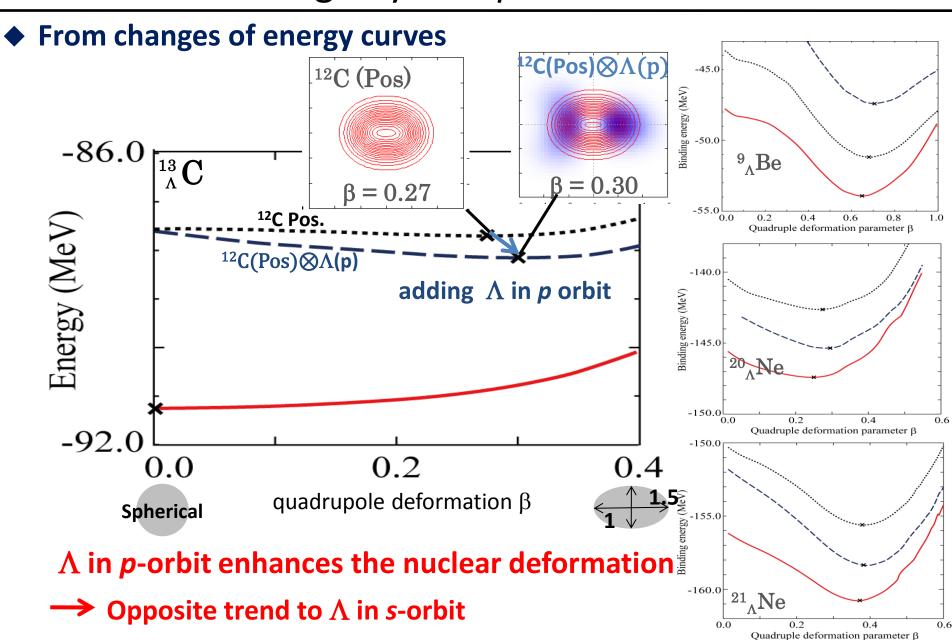
Ex.) Deformation change in ${}^{13}_{\Lambda}\mathrm{C}$ predicted by RMF calc.





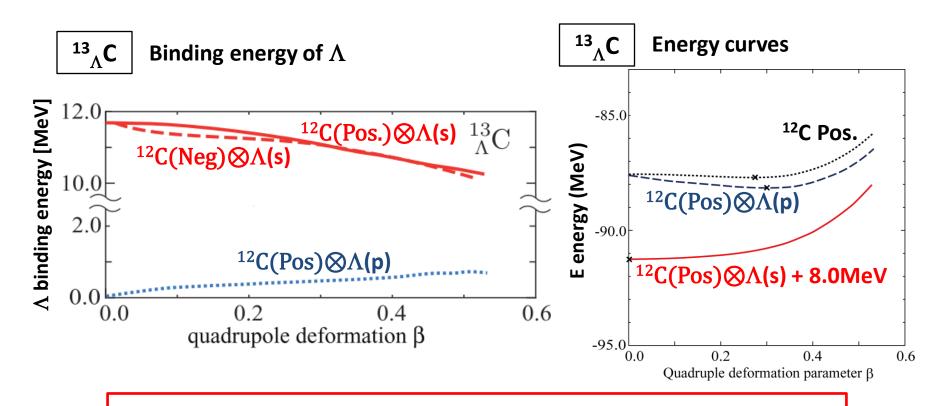
M. T. Win and K. Hagino, Phys. Rev. C **78**, 054311(2008)

Deformation change by Λ in p-orbit



Λ binding energy

- ◆ Variation of the Λ binding Energy
 - \bullet Λ in s-orbit is deeply bound at smaller deformation
 - Λ in p-orbit is deeply bound at larger deformation



Variation of the Λ binding energies causes the deformation change (reduction or enhancement)

Structure change by Λ

• Nuclear deformation change by Λ (in s and p orbits)

Examples: ${}^{9}_{\Lambda}$ Be, ${}^{13}_{\Lambda}$ C, ${}^{20}_{\Lambda}$ Ne and ${}^{21}_{\Lambda}$ Ne

M. Isaka, M. Kimura, A. Dote and A. Ohnishi, PRC 83 (2011), 044323.

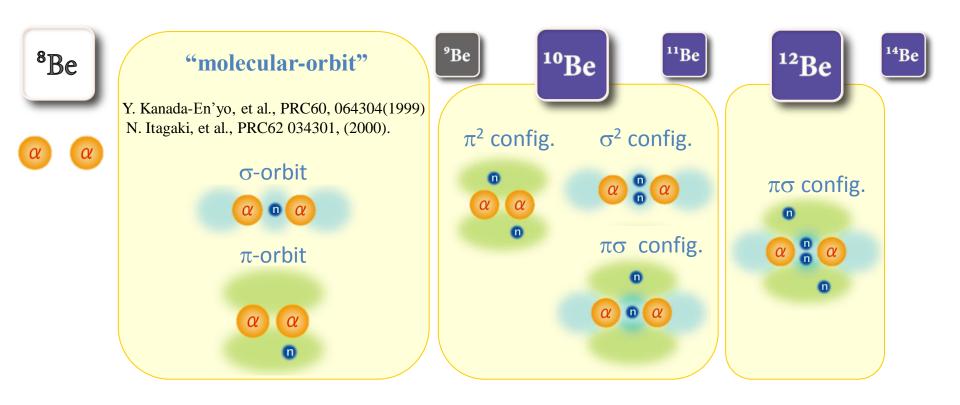
Parity reversion of the ground state in n-rich ¹² Be

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Changes of excitation spectrum in triaxially deformed ²⁵ Mg

M. Isaka, M. Kimura, A. Dote and A. Ohnishi, PRC 85 (2012), 034303.

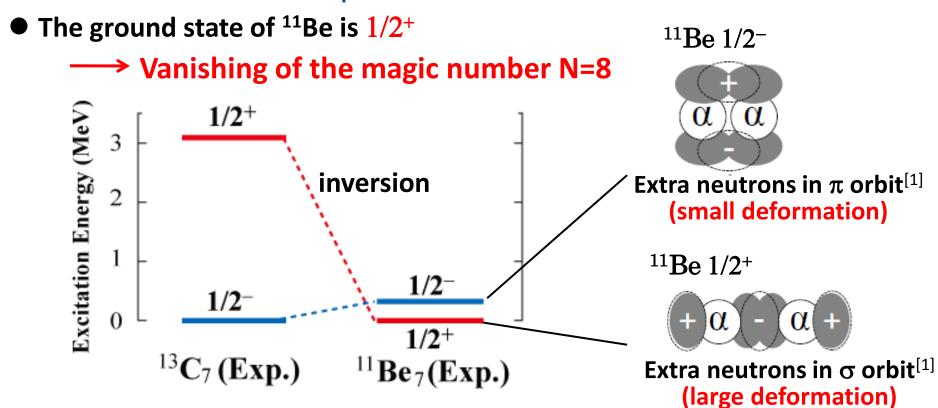
Structure of Be isotopes



- Be isotopes have 2α cluster structure
 - -2α cluster structure is changed depending on the neutron number

Exotic structure of ¹¹Be

◆ Parity inversion of the ¹¹/₄Be₇ ground state



One of the reasons of the parity inversion is the molecular orbit structure of the 1/2+ and 1/2- states.
 Difference of deformation

Purpose of this study

- Purpose of this study
 - ullet To reveal how Λ hyperon affects and modifies the low-lying states of Be isotopes with different deformation

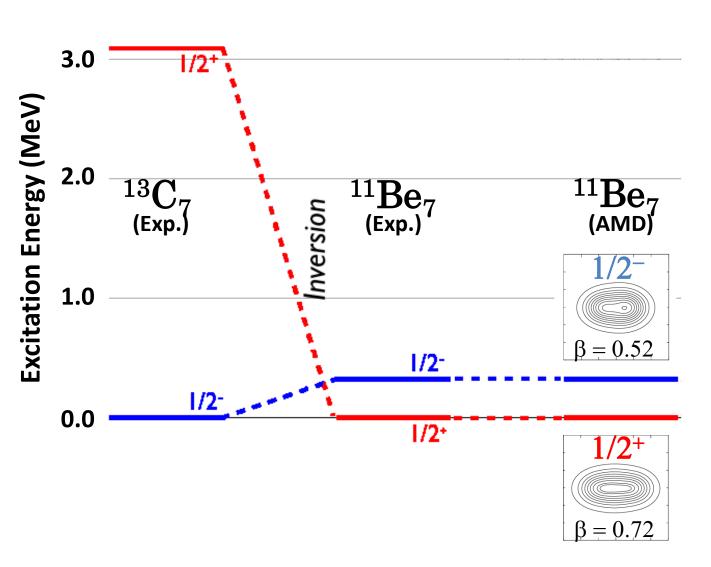
Examples:

¹²_∧Be: abnormal parity ground state of ¹¹Be

- ♦ Method: HyperAMD
 - Energy variation with β constraint
 - No assumption on 2α cluster structure
 - AMD has succeeded in the structure studies of Be isotopes
 - Angular momentum projection
 - GCM calculation
 - Prediction of the Excitation spectrum

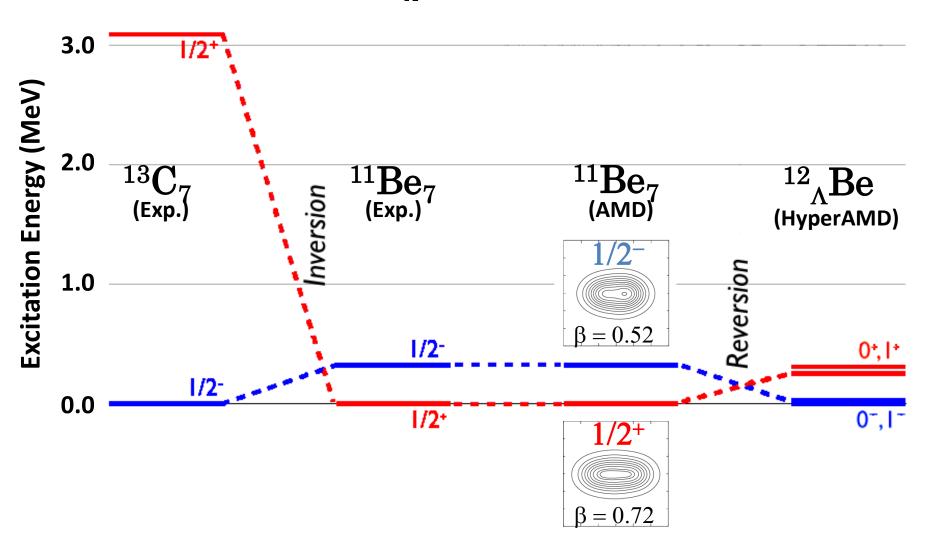
Structure change in n-rich ¹² _{\lambda}Be

♦ Ground state of ¹² ΛBe

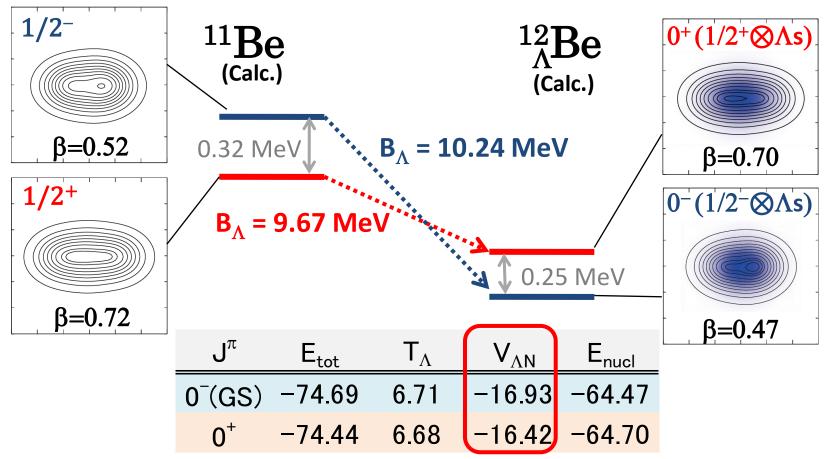


Structure change in n-rich ¹² _{\lambda} Be

- **♦** Ground state of ¹² _∧Be
 - ullet The parity reversion of the $^{12}{}_{\Lambda}$ Be g.s. occurs by the Λ hyperon



Deformation and Λ binding energy



- Λ hyperon coupled to the $1/2^-$ state is more deeply bound than that coupled to the $1/2^+$ state
 - This is because the deformation of the $1/2^-$ state is smaller than that of the $1/2^+$ state

Structure change by Λ

• Nuclear deformation change by Λ (in s and p orbits)

Examples: ${}^{9}_{\Lambda}$ Be, ${}^{13}_{\Lambda}$ C, ${}^{20}_{\Lambda}$ Ne and ${}^{21}_{\Lambda}$ Ne

M. Isaka, M. Kimura, A. Dote and A. Ohnishi, PRC 83 (2011), 044323.

Parity reversion of the ground state in n-rich ¹² Be

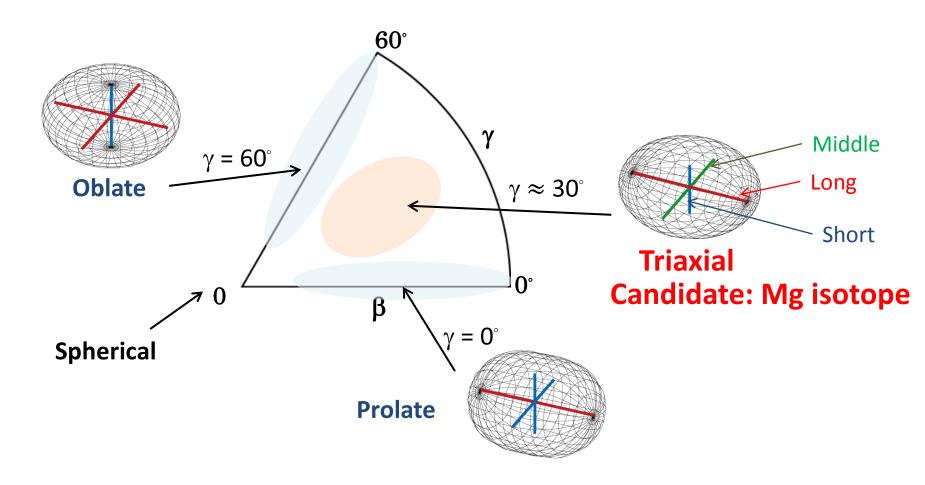
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Changes of excitation spectrum in triaxially deformed ²⁵ Mg

M. Isaka, M. Kimura, A. Dote and A. Ohnishi, PRC 85 (2012), 034303.

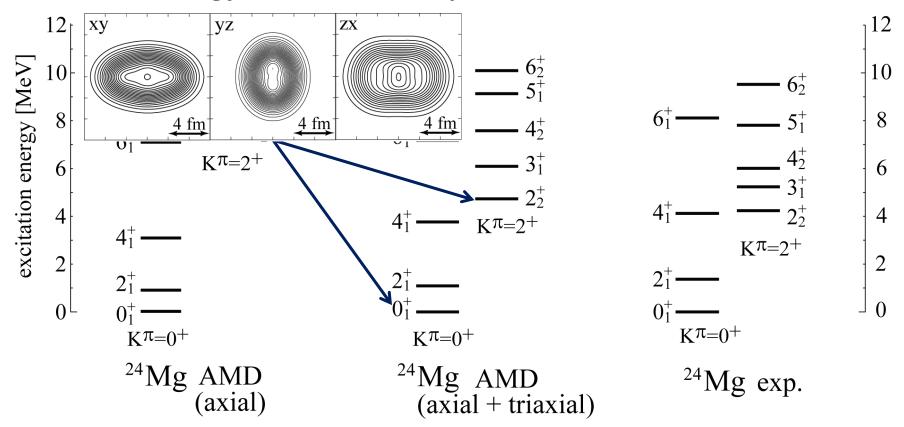
Deformation of nuclei

- Many nuclei manifests various quadrupole deformation (parameterized by quadrupole deformation parameters β and γ)
- Most of them are prolate or oblate deformed (axially symmetric)



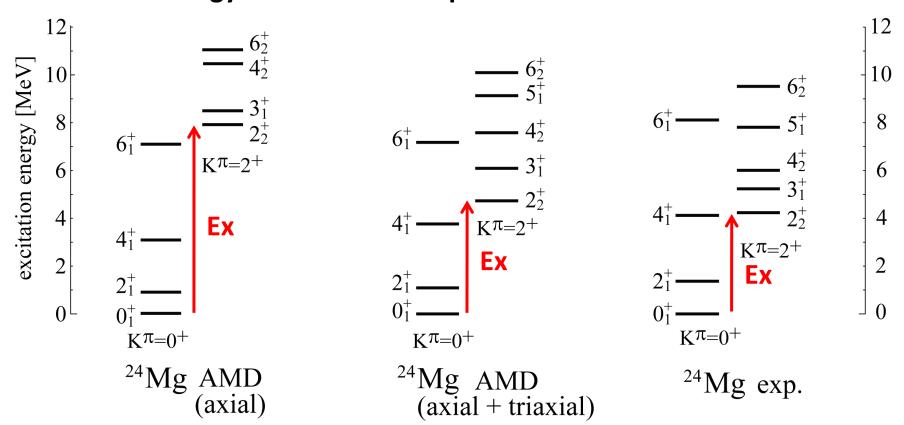
Structure of ²⁴Mg

- Large deformation • Candidate of triaxial deformed nuclei
- Excitation energy of $K^{\pi}=2^+$ band depends on the triaxial deformation [1,2]



Structure of ²⁴Mg

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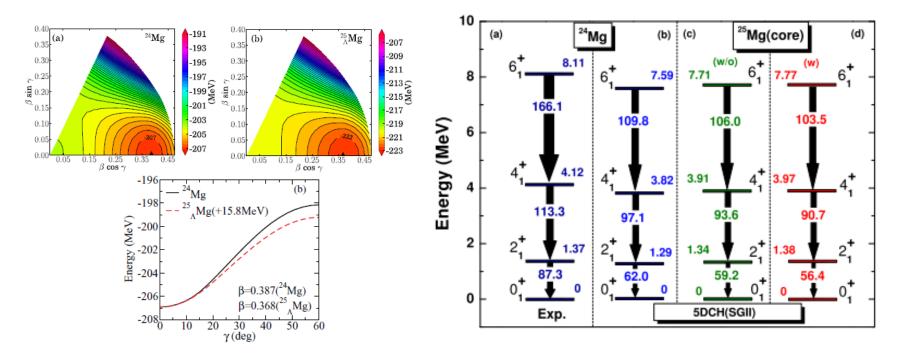
 K^{π} = 2⁺ band is rigid against the exclusion of the triaxial deformation How does Λ modify triaxial deformation of ²⁴Mg?

[1] M. Bender and P-H. Heenen, Phys. Rev. **C78**, 024309 (2008). [2] M. Kimura, R. Yoshida and M.Isaka, Prog. Theor. Phys. **127**, 287(2011).

Predictions for ²⁵ Mg

Predicted Structure changes by Λ (in s-orbit)

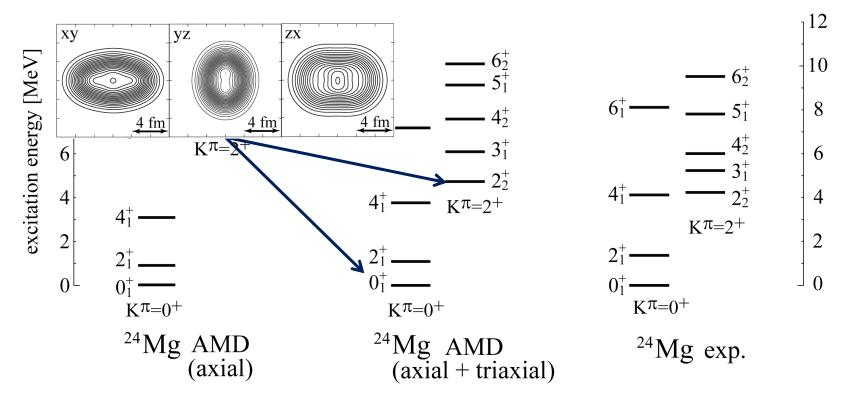
- Energy surface becomes slightly soft against γ deformation
 Myaing Thi Win, et al., Phys. Rev. C83, 014301 (2011).
- A reduces the deformation and stretches the level spacing of the ground band
 J. M. Yao, et al., Nucl. Phys. A868 (2011), 12.



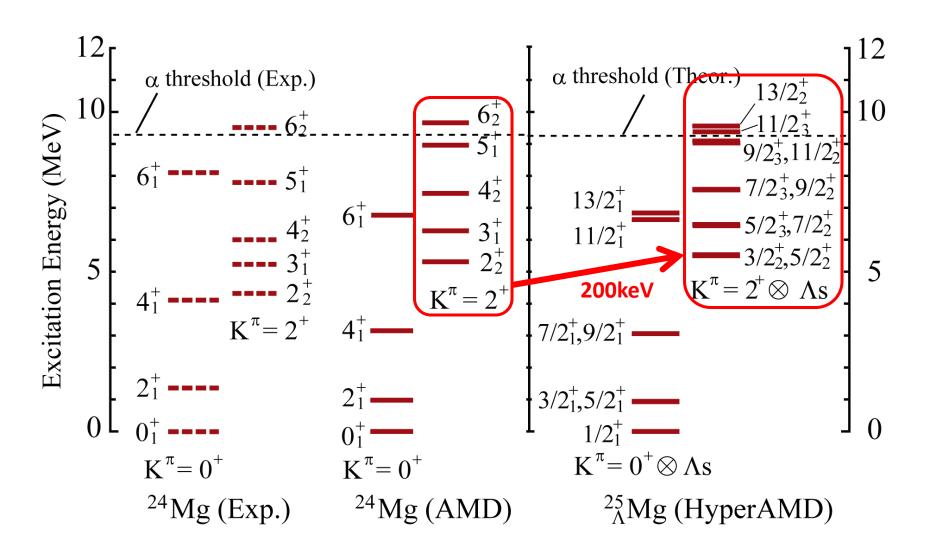
In triaxial deformed nuclei, the response to the addition of Λ hyperon will be different from axial symmetric nuclei

Individual Problem ($^{25}_{\Lambda}$ Mg)

- Purpose of this study
 - To reveal how Λ hyperon affects the triaxial deformation and observables such as excitation energies
 - Example: $^{25}\Lambda Mg$
 - K^{π} = 0⁺⊗Λ(s) band ••• (ground band of ²⁴Mg) ⊗Λ(s orbit)
 - $K^{\pi} = 2^{+} \bigotimes \Lambda(s)$ band ••• ($K^{\pi} = 2^{+}$ band of ${}^{24}Mg$) $\bigotimes \Lambda(s)$ orbit)



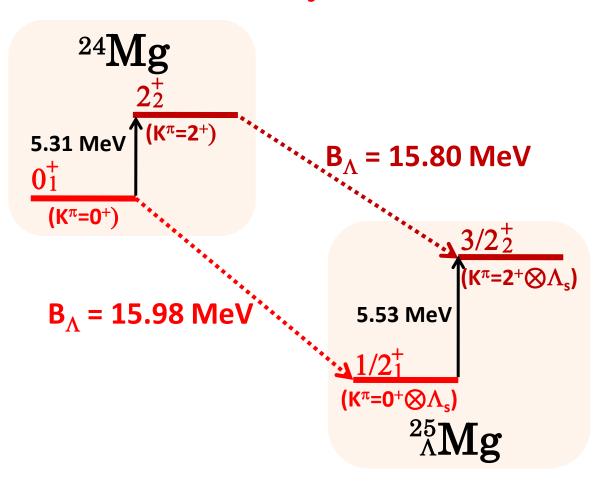
Results: Excitation spectra of $^{25}\Lambda Mg$



Excitation energy of $K^{\pi}=2^{+}\otimes\Lambda_{s}$ band is shifted up by about 200 keV

Results: Reasons for the shift up

- lacktriangle Difference of the Λ binding energy B_{Λ}
 - ullet B $_{\Lambda}$ for the K $^{\pi}$ =0 $^{+}\otimes\Lambda_{s}$ band is larger than that for the K $^{\pi}$ =2 $^{+}\otimes\Lambda_{s}$ band
 - \longrightarrow Energy shift of the $K^{\pi}=2^{+}\otimes\Lambda_{s}$ band

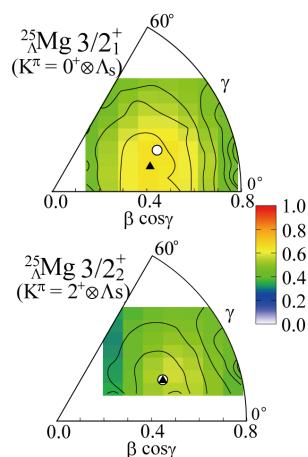


Results: Deformation change by Λ hyperon

- Large B_{Λ} of the $K^{\pi}=0^+ \bigotimes \Lambda_s$ band is due to the smaller deformation
- Λ reduces the (β, γ) deformation in the $K^{\pi}=0^{+} \otimes \Lambda_{s}$ band, while the deformation of the $K^{\pi}=2^{+} \otimes \Lambda_{s}$ band is almost unchanged

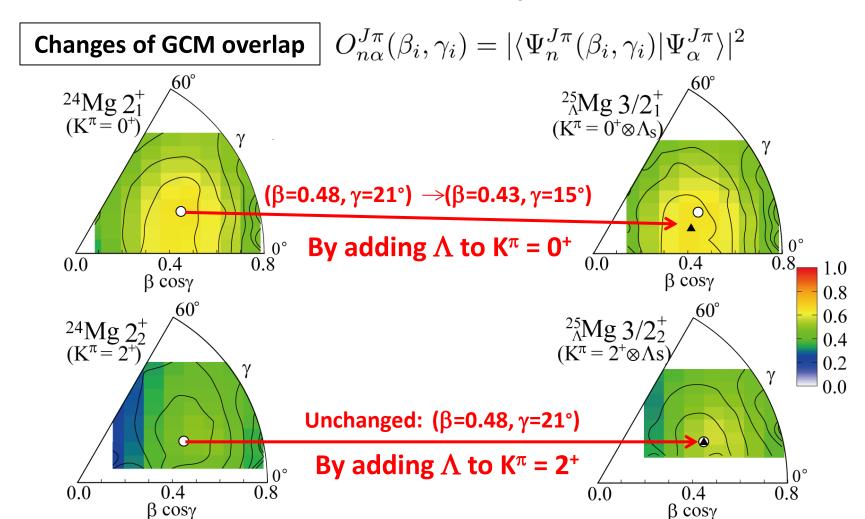
Changes of GCM overlap

$$O_{n\alpha}^{J\pi}(\beta_i, \gamma_i) = |\langle \Psi_n^{J\pi}(\beta_i, \gamma_i) | \Psi_{\alpha}^{J\pi} \rangle|^2$$

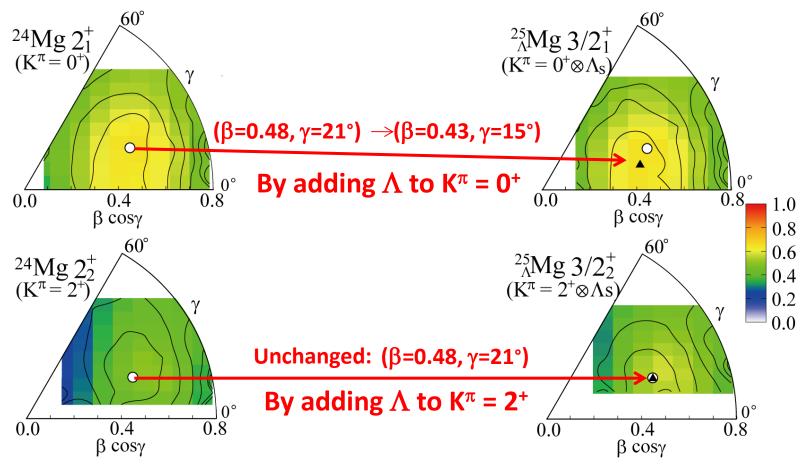


Results: Deformation change by Λ hyperon

- lacktriangle Large B_{Λ} of the $K^{\pi}=0^+ igotimes \Lambda_s$ band is due to the smaller deformation
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Results: Deformation change by Λ hyperon



Color plots: GCM overlap

Contour lines: energy surface

- $K^{\pi}=0^+$ band: Energy surface is soft (flat) against the (β, γ) reduction
- $K^{\pi}=2^+$ band: rigid against the deformation change

Probing nuclear deformation by using Λ

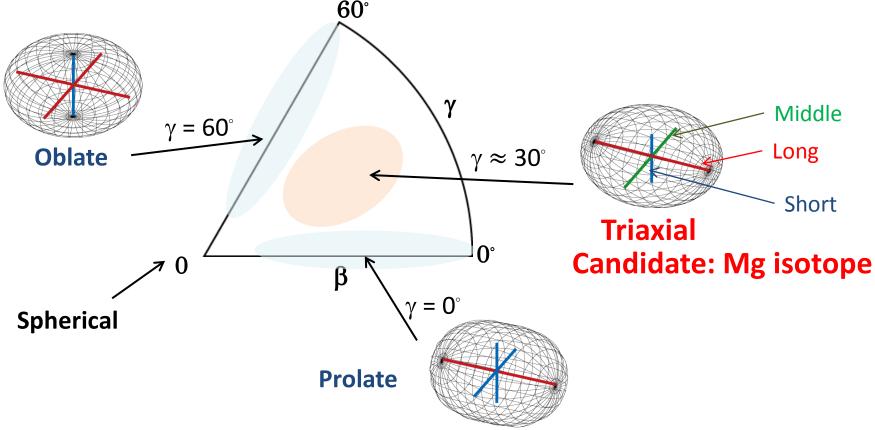
Example: Triaxial deformation of Mg

M. Isaka, et al., PRC 87, 021304(R) (2013)

Deformation of nuclei

• Many nuclei manifests various quadrupole deformation (parameterized by quadrupole deformation parameters β and γ)

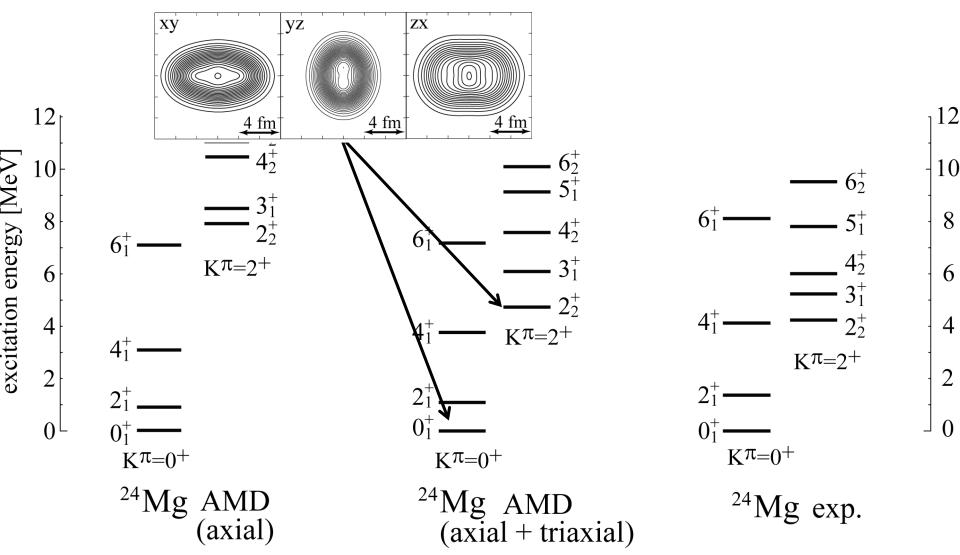
Most of them are prolate or oblate deformed (axially symmetric)



Triaxial deformed nuclei are not many and its identification is not easy.

Deformation of ²⁴Mg

• ²⁴Mg: candidate of triaxially deformed nuclei [1,2]



[1,2] R. Batchelor, et al., Nucl. Phys. 16, 38 (1969)., A. Cohen and J. Cookson, Nucl. Phys. 29, 604 (1962).

Example: p-states of ${}^{9}_{\Lambda}$ Be

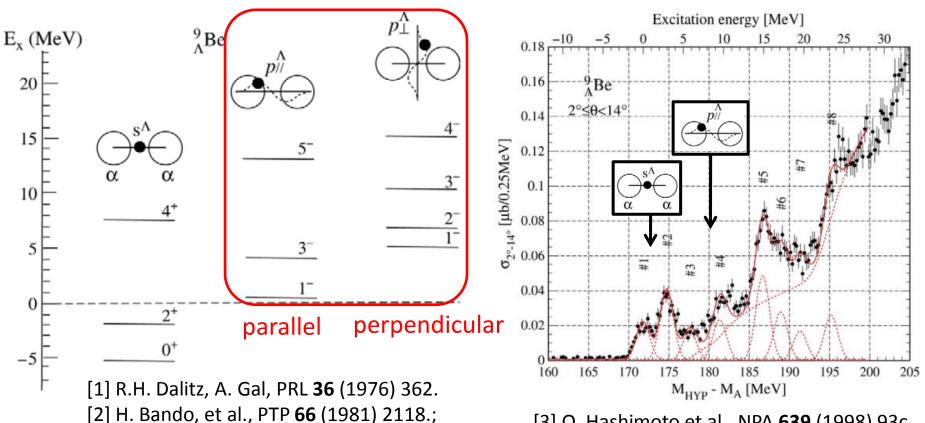
$^{9}_{\Lambda}$ Be: axially symmetric 2α clustering

Two bands will be generated as p-states [1,2]

- $\int \bullet$ Anisotropic p orbit of Λ hyperon
 - Axial symmetry of 2α clustering

H. Bando, et al., IJMP **21** (1990) 4021.

\rightarrow p-orbit parallel to/perpendicular to the 2α clustering

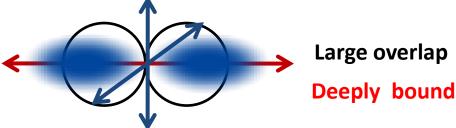


[3] O. Hashimoto et al., NPA **639** (1998) 93c.

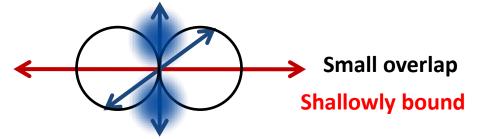
Split of *p*-state in ${}^9_{\Lambda}$ Be

• $^{9}_{\Lambda}$ Be with 2α cluster structure

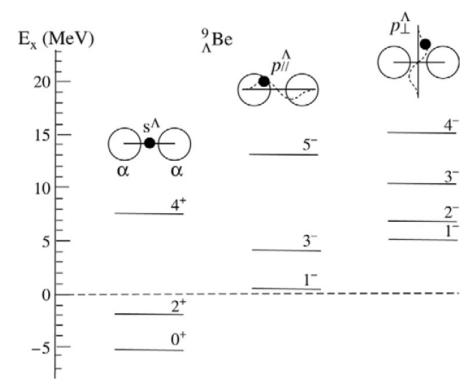
p orbit parallel to 2α (long axis)



p orbit perpendicular to 2α (short axes)



Split corresponding to long/short axes



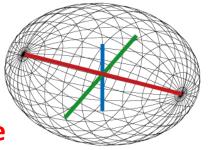
R.H. Dalitz, A. Gal, PRL 36 (1976) 362.H. Bando, et al., PTP 66 (1981) 2118.;H. Bando, et al., IJMP 21 (1990) 4021.

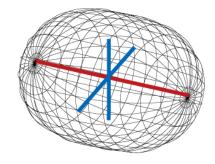
p-states splits into 2 bands depending on the direction of p-orbits

Triaxial deformation

If ²⁴Mg is triaxially deformed nuclei

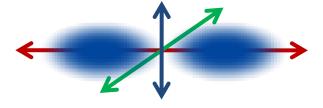
---> p-states split into 3 different state



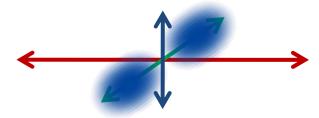


Triaxial deformation

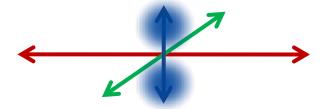
Prolate deformation



Large overlap leads deep binding



Middle



Small overlap leads shallow binding

cf. prolate deformation

Ex.) ${}^9_{\Lambda}$ Be

p orbit parallel to 2α (long axis)



Large overlap

Deeply bound

p orbit perpendicular to 2α (short axes)



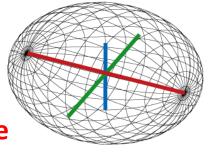
Small overlap Shallowly bound

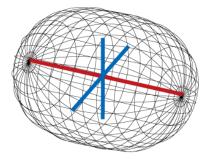
Split corresponding to long/short axes

Triaxial deformation

If ²⁴Mg is triaxially deformed nuclei

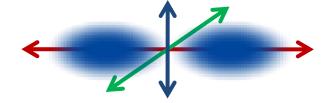
--> p-states split into 3 different state



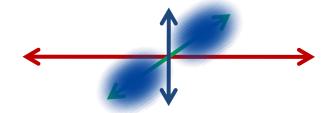


Triaxial deformation

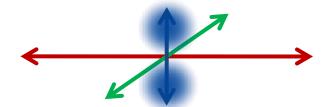
Prolate deformation



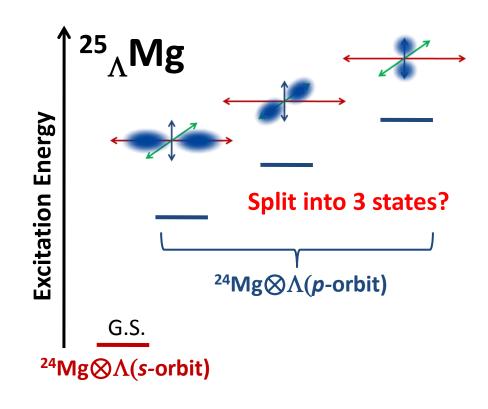
Large overlap leads deep binding



Middle



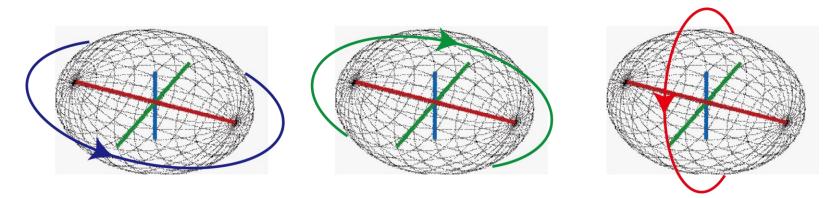
Small overlap leads shallow binding



Observing such 3 different states is strong evidence for triaxial deformation of ²⁴Mg

Purpose

- Purpose and problem
 - To reveal triaxial deformation of ²⁴Mg, we will predict the level structure of the p states in ²⁵ Mg
 - ²⁵ Mg
 - p-states will split into 3 different states, if ²⁴Mg is triaxially deformed



- Method
 - HyperAMD + GCM calculation

(Antisymmetrized Molecular Dynamics for hypernuclei)

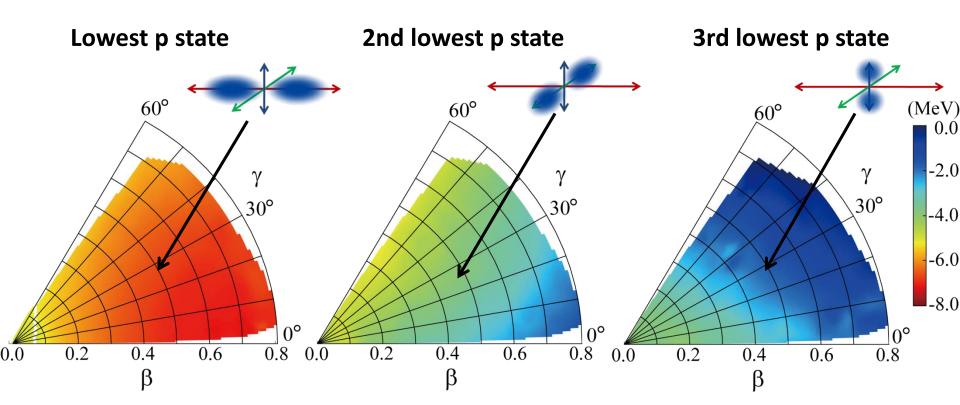
- Constraints on (β, γ) , and single particle w.f. of Λ
- YNG-NSC97f interaction

Results: Single particle energy of Λ hyperon

lacktriangle Λ single particle energy on (β, γ) plane

$$\varepsilon_{\Lambda}(\beta_{i},\gamma_{i}) = \langle \Psi^{\pi}(\beta_{i},\gamma_{i}) | (\hat{T}_{\Lambda} + \hat{V}_{\Lambda N}) \Psi^{\pi}(\beta_{i},\gamma_{i}) \rangle$$

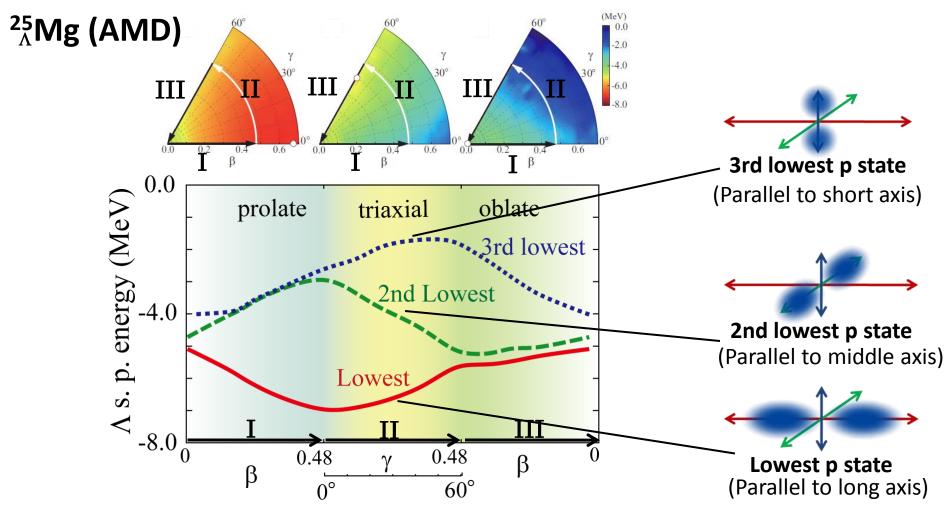
25 Mg (AMD, Λ in p orbit)



- ullet Single particle energy of Λ hyperon is different from each p state
 - This is due to the difference of overlap between Λ and nucleons

Results: Single particle energy of Λ hyperon

 $lacklosh \Lambda$ single particle energy in axial/triaxial deformed nucleus

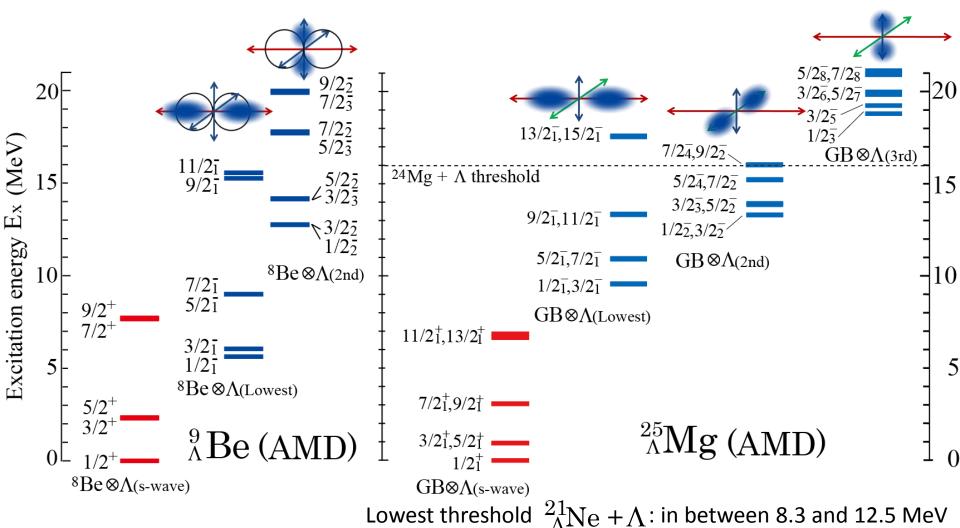


 $\boldsymbol{\Lambda}$ s. p. energy is different from each other with triaxial deformation

→ split into 3 p-orbit states

Results: Excitation spectra

- 3 bands are obtained by Λ hyperon in p-orbit \rightarrow Splitting of the p states
 - ${}^{24}\text{Mg} \otimes \Lambda p(lowest), {}^{24}\text{Mg} \otimes \Lambda p(2nd lowest), {}^{24}\text{Mg} \otimes \Lambda p(3rd lowest)$



Summary

Knowledge of YN interaction will allow us to reveal structure of hypernuclei

- Structure change and modification of nuclear properties by adding a hyperon
- Bounding unbound systems by using hyperons as a glue
- Probing nuclear structure (deformation) by using hyperon

Combination of the modern YN interaction with nuclear models

Antisymmetrized molecular dynamics + effective YN interaction

Structure changes caused by Λ

- Λ in p-orbit enhances the nuclear deformation, while Λ in s-orbit reduces it.
- Difference of the Λ binding energy causes the changes of the excitation spectra in n-rich $^{12}{}_{\Lambda}$ Be, and triaxially deformed $^{25}{}_{\Lambda}$ Mg hypernuclei

Probing nuclear deformation by using Λ

– Splitting of the p orbits in $^{25}_{\Lambda}$ Mg due to triaxial deformation