

# Quasi-bound states of a DNN system

## 1. Introduction

## 2. Setup for the variational calculation

- I. DN potential
- II. NN potential

## 3. Result of DNN states

- $J^\pi=0^- (S_{NN}=0)$  with  $T=1/2$
- $J^\pi=1^- (S_{NN}=1)$  with  $T=1/2$
- $J^\pi=0^- (S_{NN}=0)$  with  $T=3/2$

## 4. Comparison with strangeness sector

## 5. Summary

### Variational part:

A. Doté (KEK theory center)  
T. Hyodo, M. Oka (TITech)

### Faddeev-FCA part:

M. Bayar, C. W. Xiao,  
E. Oset (Valencia univ.)

Phys. Rev. C86,  
044004 (2012)

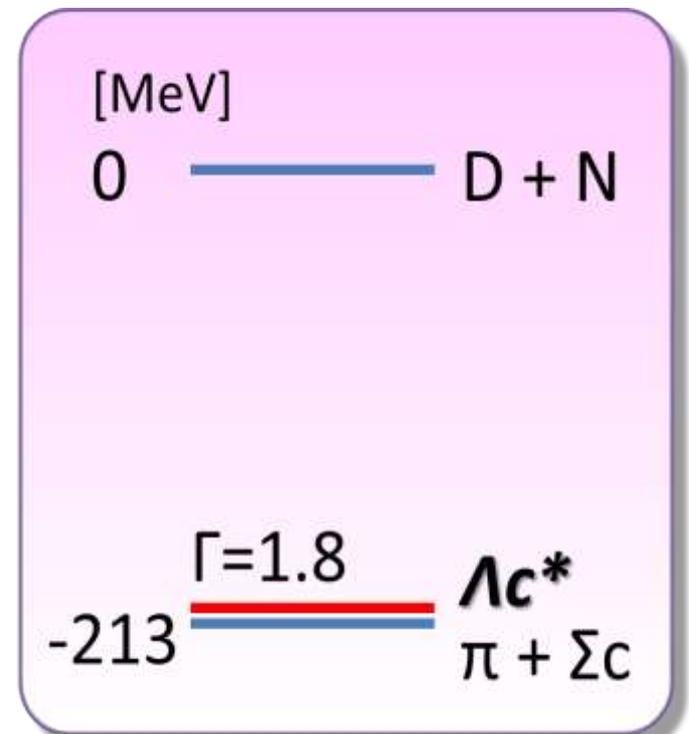
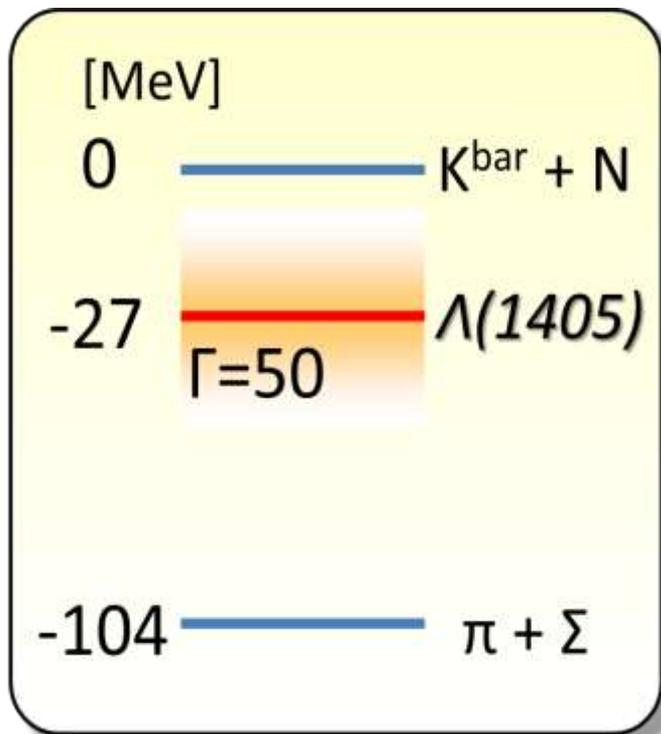
# 1. Introduction

# Analogy of strangeness and charm?

- P-wave baryon ( $J^P=1/2^-, I=0$ )

Strangeness:  $\Lambda(1405) \dots K^{\text{bar}}N$  quasi-bound state

Charm:  $\Lambda_c^+(2595) \dots DN$  quasi-bound state?



# Analogy of strangeness and charm?

- P-wave baryon ( $J^P=1/2^-, I=0$ )

Strangeness:  $\Lambda(1405) \dots K^{\text{bar}}N$  quasi-bound state

**Charm:  $\Lambda_c^+(2595) \dots DN$  quasi-bound state?**

- Nucleus with D meson (D nucleus)

... **Charm-analog state of kaonic nuclei ( $K^{\text{bar}}$  nuclei)**

Narrow resonance states?       $\Gamma(\Lambda_c^*) = 1.8 \text{ MeV} \ll \Gamma(\Lambda^*) = 50 \text{ MeV}$

Non-relativistic treatment!       $M_D = 1867 \text{ MeV} \gg M_K = 494 \text{ MeV}$

**➡ Theoretically and experimentally, clearer than kaonic nuclei**

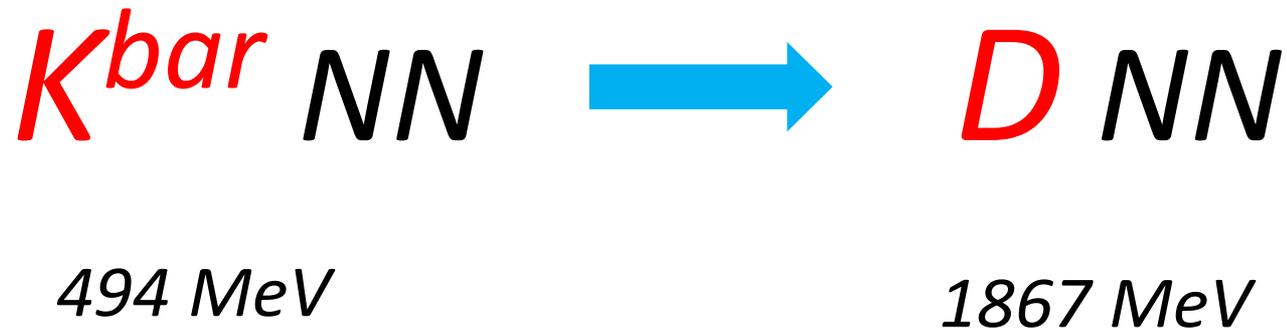
- Most essential three-body system

Strangeness: “ $K^-pp$ ” (a prototype of kaonic nuclei)

B. E. = 20 ~ 90 MeV,  $\Gamma = 50 \sim 100 \text{ MeV}$  (Theor.)

**➡ Consider DNN in charm sector.**

## 2. Set up



# 2. Set up ... same as $K^-pp$ study

*A. D. , T. Hyodo and W. Weise, PRC79, 014003 (2009)*

## ➤ Effective $DN$ potential

Vector meson exchange picture potential

... Coupled-channel potential ( $DN, \pi\Sigma_c, \pi\Lambda_c \dots$ )

*Generate dynamically the  $I=0$  resonance  $\Lambda_c(2595)$*

***$DN$  single-channel potential ... equivalent as for  $DN$  scattering amplitude***

# DN potential

Based on Mizutani-Ramos study<sup>†</sup>

Coupled-channel calculation in  $DN, \pi\Sigma_c, \pi\Lambda_c \dots$  etc  
with WT-type interaction

- $\kappa=1/4$  for charm exchange process  
...  $DN \longleftrightarrow \pi Y_c$
- $\kappa=1$  for other cases

$$v_{ij}^{(I)}(W) = -\frac{\kappa C_{ij}^{(I)}}{4f^2} (2W - M_i - M_j) \sqrt{\frac{M_i + E_i}{2M_i}} \sqrt{\frac{M_j + E_j}{2M_j}}$$

- WT interaction  $\approx$  Vector meson exchange potential  
Due to KSRF relation

## Effective DN potential

Similar way to the  $K^{bar}N$  study<sup>††</sup>

- ✓ Eliminate other channels than DN.
- ✓ Reproduce the original DN scattering amplitude.
- ✓ Single-range Gaussian form

<sup>†</sup> T. Mizutani and A. Ramos, PRC74, 065201 (2006)

<sup>††</sup> T. Hyodo and W. Weise, PRC77, 035204 (2007)

# DN potential

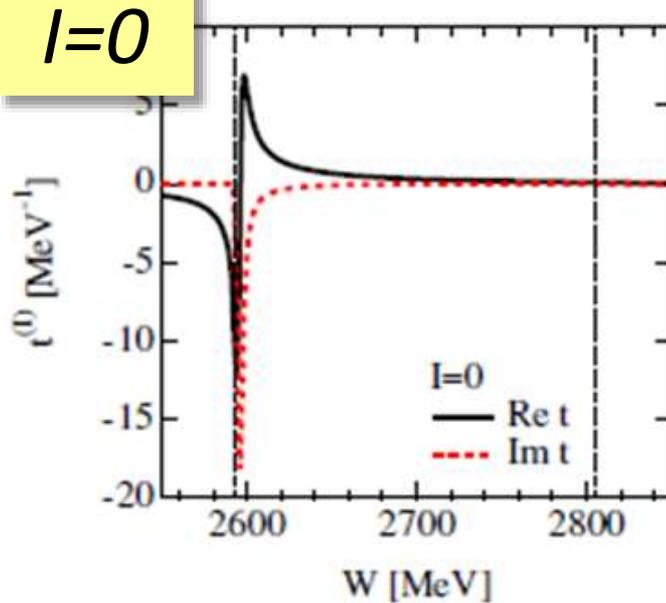
$$v_{DN}(r; W) = \frac{M_N}{2\pi^{3/2}a_s^3\tilde{\omega}(W)}$$

$$\times [v^{\text{eff}}(W) + \Delta v(W)] \exp[-(r/a_s)^2]$$

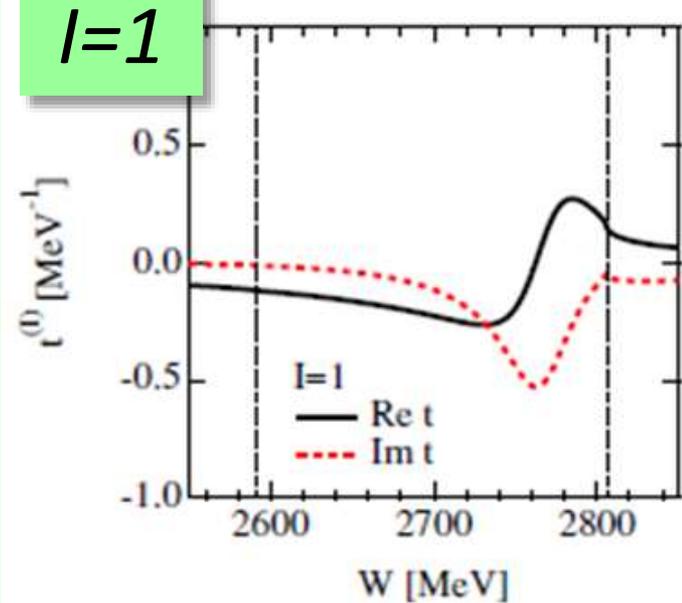
Energy-dependent pot.

$$a_s = 0.40\text{fm}$$

## ➤ DN scattering amplitude



**$\Lambda_c(2595)$  dynamically generated**



**Resonance @ 2766 MeV**

# 2. Set up ... same as $K^-pp$ study

*A. D. , T. Hyodo and W. Weise, PRC79, 014003 (2009)*

## ➤ Effective $DN$ potential

Vector meson exchange picture potential

... Coupled-channel potential ( $DN, \pi\Sigma_c, \pi\Lambda_c \dots$ )

*Generate dynamically the  $I=0$  resonance  $\Lambda_c(2595)$*

***DN single-channel potential ... equivalent as for DN scattering amplitude***

## ➤ NN potential ... NN phase shift respected

- |  |                |           |
|--|----------------|-----------|
| • Av18 <sup>1)</sup>                         | Repulsive core | ~ 3 GeV   |
| • Hasegawa-Nagata No.1 <sup>2)</sup> Revised |                | ~ 1 GeV   |
| • Minnesota <sup>3)</sup>                    |                | ~ 0.1 GeV |

1) R. B. Wiringa, V. G. J. Stoks and R. Schiavilla, PRC51, 38 (1995)

2) A. Hasegawa and S. Nagata, PTP45, 1786 (1971)

3) D. R. Thompson, M. Lemere and Y. C. Tang, NPA286, 53 (1977)

# 2. Set up ... same as $K^-pp$ study

A. D. , T. Hyodo and W. Weise, PRC79, 014003 (2009)

## ➤ Effective $DN$ potential = *Complex potential*

Vector meson exchange picture potential

... Coupled-channel potential ( $DN, \pi\Sigma_c, \pi\Lambda_c \dots$ )

*Generate dynamically the  $I=0$  resonance  $\Lambda_c(2595)$*

***DN single-channel potential ... equivalent as for DN scattering amplitude***

## ➤ NN potential ... NN phase shift respected

- |                                |                |                |
|--------------------------------|----------------|----------------|
| • Av18                         | Repulsive core | $\sim 3$ GeV   |
| • Hasegawa-Nagata No.1 Revised |                | $\sim 1$ GeV   |
| • Minnesota                    |                | $\sim 0.1$ GeV |

## ➤ Variational calculation

- Use the *real part* of the effective  $DN$  potential
- Expand the trial wave function with Gaussian base

# 3. Result

## Energy and width

$$J^\pi=0^-, T=1/2$$

$$J^\pi=1^-, T=1/2$$

$$J^\pi=0^-, T=3/2$$

# Binding energy and decay width

DN pot. :  $b=0.40\text{fm}$ ,  
 $B(D)=208.9\text{MeV}$  ( $T=1/2$ )  
 $B(D)=39.9\text{MeV}$  ( $T=3/2$ )

$J^p=0^-, T=1/2$

$J^p=1^-, T=1/2$

$J^p=0^-, T=3/2$

D-N-N  
 0 MeV

$\Lambda_c^* - N$   
 -209



B. E. ( $\Lambda_c^* - N$ ) = 42 ~ 0.5 MeV  
 $\Gamma(\pi Y_c) = 38 \sim 22 \text{ MeV}$

# Binding energy and decay width

DN pot. :  $b=0.40\text{fm}$ ,  
 $B(D)=208.9\text{MeV}$  ( $T=1/2$ )  
 $B(D)=39.9\text{MeV}$  ( $T=3/2$ )

$J^p=0^-, T=1/2$

$J^p=1^-, T=1/2$

$J^p=0^-, T=3/2$

D-N-N  
 0 MeV

$\Lambda_c^*-N$  scattering state

$\Lambda_c^*-N$   
 -209



*Av18*

*HN1R*

*Minnesota*

$B. E. (\Lambda_c^*-N) = 42 \sim 0.5 \text{ MeV}$   
 $\Gamma(\pi Y_c) = 38 \sim 22 \text{ MeV}$

# $DNN (J^\pi=0^-, T=3/2)$

According to the vector-meson exchange picture potential...

$I=0$  DN potential:

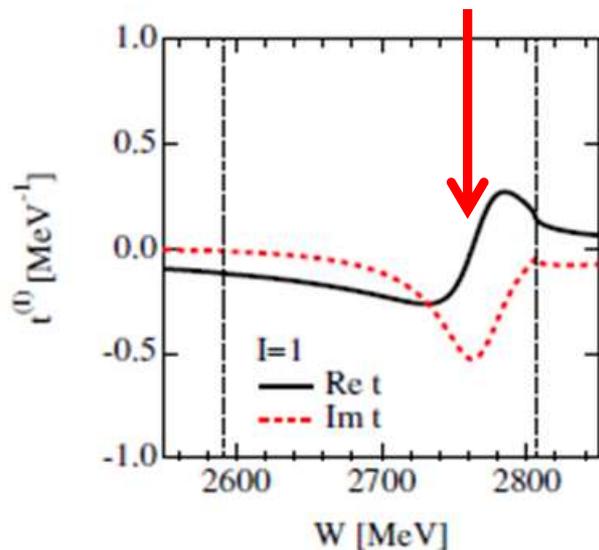
Strongly attractive to generate  $\Lambda_c(2595)$

$I=1$  DN potential:

Mildly attractive to generate a resonance at 2766 MeV

Assume Iso-symmetric cutoff

$\Sigma_c^*$  (?)



$DNN (S_{NN}=0, T=3/2)$

$$V_{DN} = v_{DN} (I=1)$$

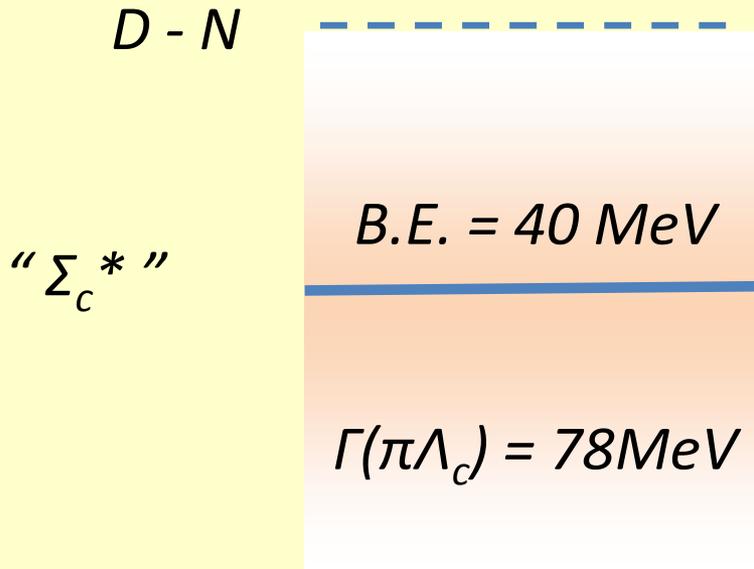
Interesting state?

$D^0 nn$  or  $D^+ pp$

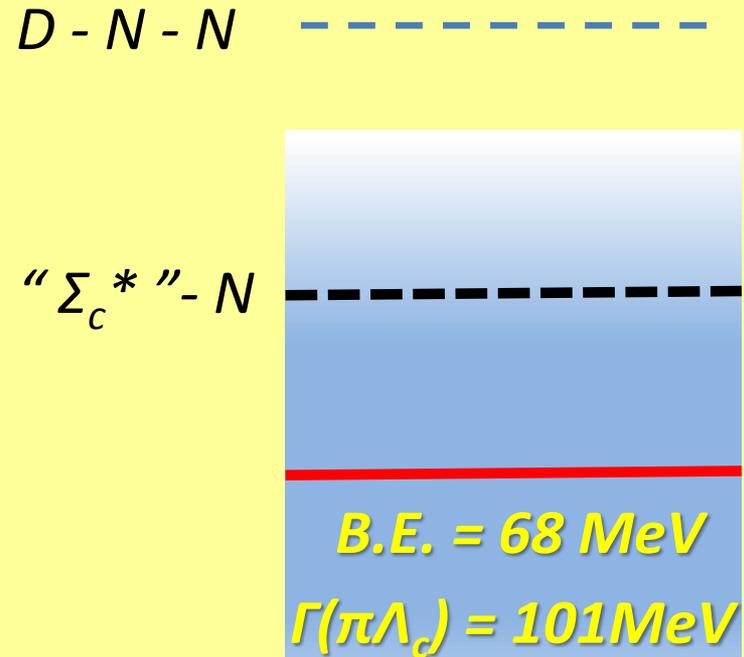
# $DNN (J^\pi=0^-, T=3/2)$

NN pot: HN1R  
DN pot. :  $b=0.40\text{fm}$ ,  
 $B(D)=39.9\text{MeV}$

" $\Sigma_c(2766)$ " ... DN ( $l=1$ )



$DNN (S_{NN}=0, T=3/2)$



- Bound below " $\Sigma_c^*$ " - N threshold by  $\sim 30\text{MeV}$
- Large decay width

DN pot. :  $b=0.40\text{fm}$ ,  
 $B(D)=208.9\text{MeV}$  ( $T=1/2$ )  
 $B(D)=39.9\text{MeV}$  ( $T=3/2$ )

# Binding energy and decay width

$J^p=0^-, T=1/2$

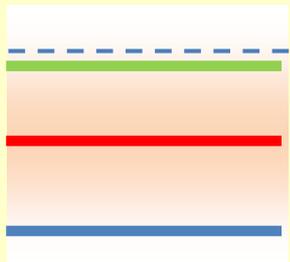
$J^p=1^-, T=1/2$

$J^p=0^-, T=3/2$

D-N-N  
 0 MeV

" $\Sigma_c^*$ " - N  
 -40

$\Lambda_c^*$  - N  
 -209



*Av18*

*HN1R*

*Minnesota*

$\Lambda_c^*$  - N scattering state

$B. E. (\Lambda_c^* - N) = 42 \sim 0.5 \text{ MeV}$   
 $\Gamma(\pi Y_c) = 38 \sim 22 \text{ MeV}$

$B. E. (\Sigma_c^* - N) = 28 \text{ MeV}$   
 $\Gamma(\pi \Lambda_c) = 101 \text{ MeV}$

# Binding energy and decay width

DN pot. :  $b=0.40\text{fm}$ ,  
 $B(D)=208.9\text{MeV}$  ( $T=1/2$ )  
 $B(D)=39.9\text{MeV}$  ( $T=3/2$ )

$J^p=0^-, T=1/2$

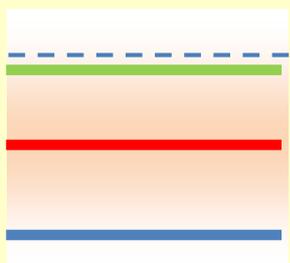
$J^p=1^-, T=1/2$

$J^p=0^-, T=3/2$

D-N-N  
 0 MeV

" $\Sigma_c^*$ " - N  
 -40

$\Lambda_c^*$  - N  
 -209



Av18

HN1R

Minnesota

$\Lambda_c^*$  - N scattering state

B. E. ( $\Lambda_c^*$  - N) =  $42 \sim 0.5 \text{ MeV}$   
 $\Gamma(\pi Y_c) = 38 \sim 22 \text{ MeV}$

$D^+pp$  (w/ Coulomb)  
 B. E. ( $\Sigma_c^*$  - N) =  $22 \text{ MeV}$   
 $\Gamma(\pi \Lambda_c) = 99 \text{ MeV}$

# 3. Result

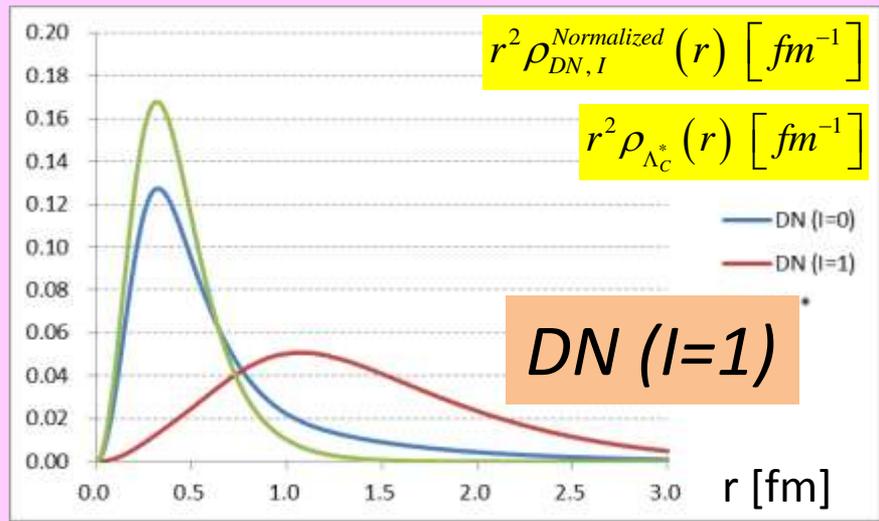
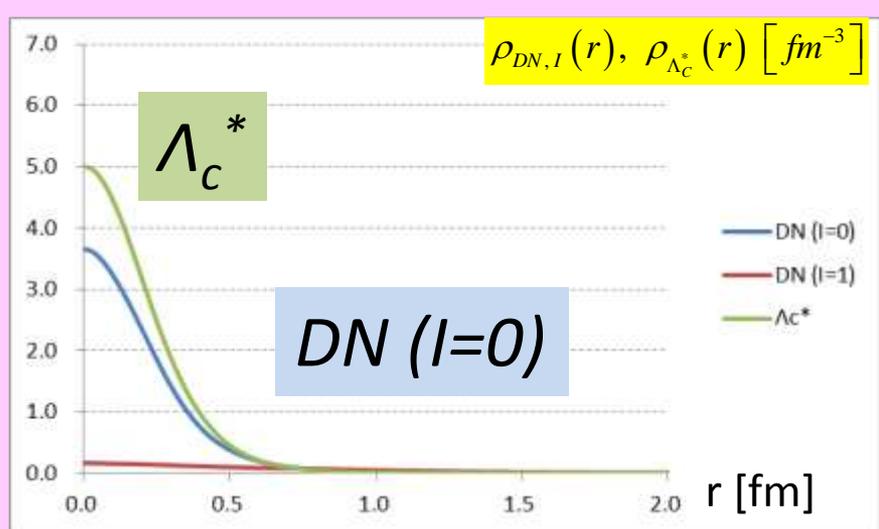
## *Structure of DNN*

$$J^\pi = 0^-, T = 1/2$$

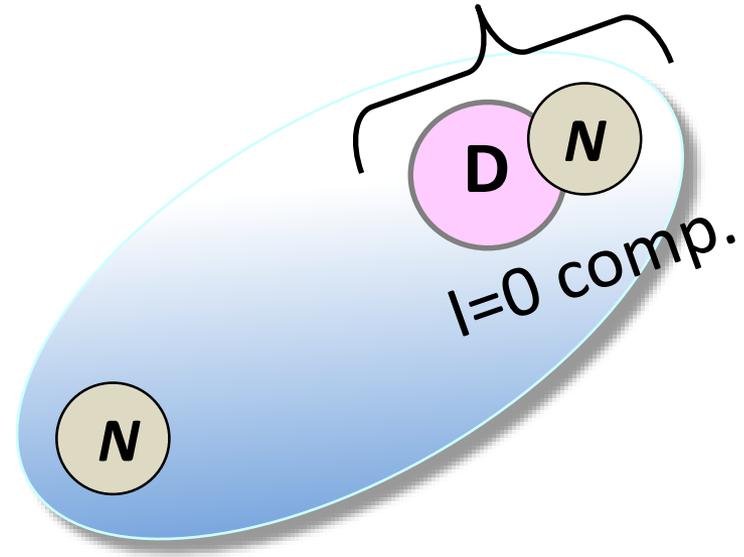
# Structure of DNN ( $S=0$ )

NN pot: HN1R  
 DN pot. :  $b=0.40\text{fm}$ ,  
 $B(D)=208.9\text{MeV}$

## DN correlation density    Isospin-decomposed



$\Lambda_c^*$

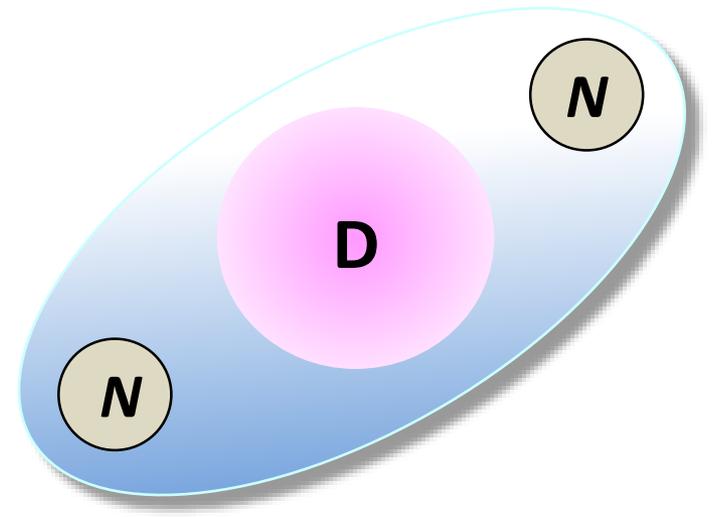
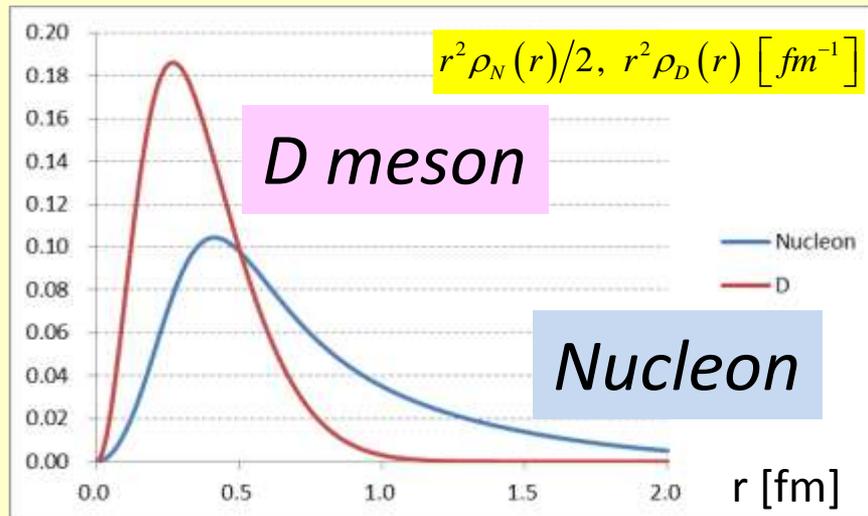
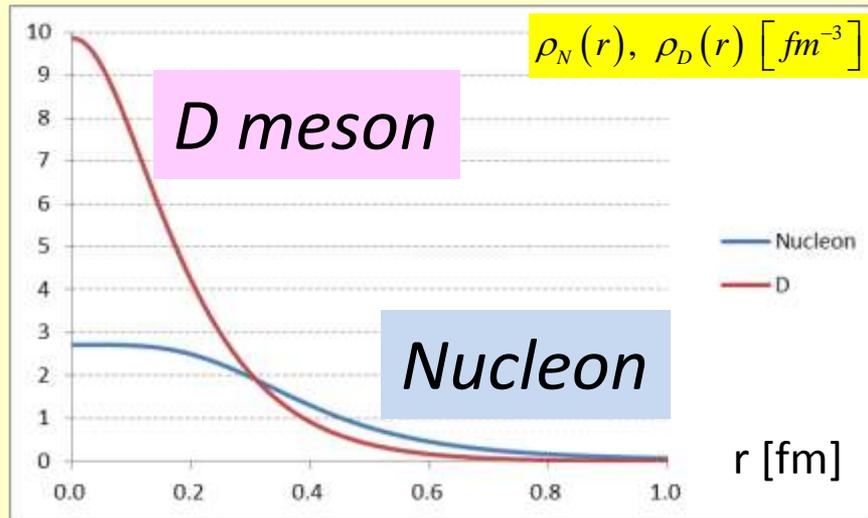


• The distribution of the  $I=0$  DN component in DNN ( $S=0$ ) system is similar to that of **the DN forms  $\Lambda_c^*$** . (Similar to  $K^{bar}NN$  case)

# Structure of DNN ( $S=0$ )

NN pot: HN1R  
DN pot. :  $b=0.40\text{fm}$ ,  
 $B(D)=208.9\text{MeV}$

## One-body density



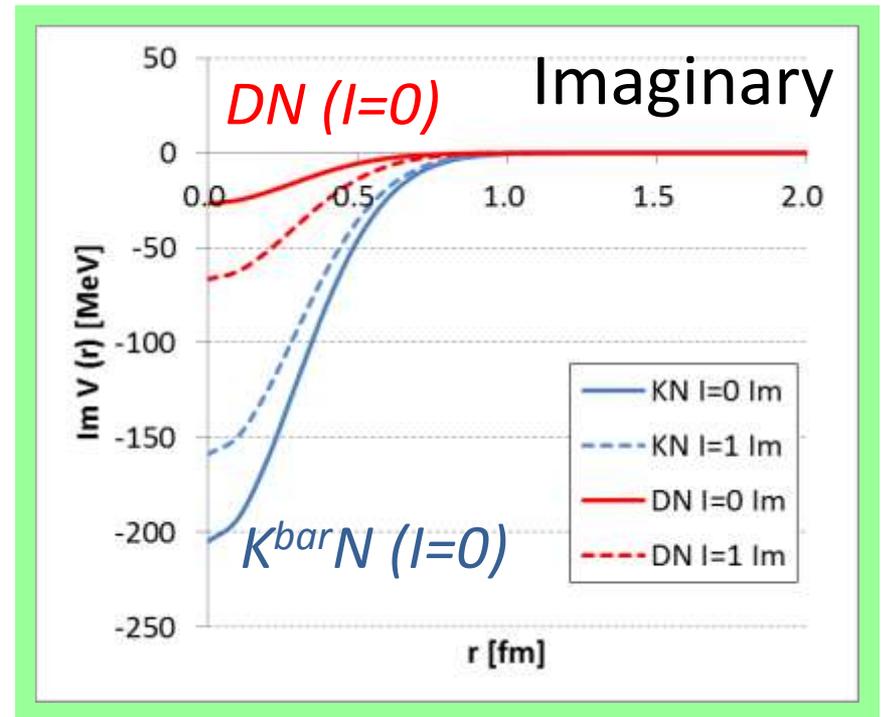
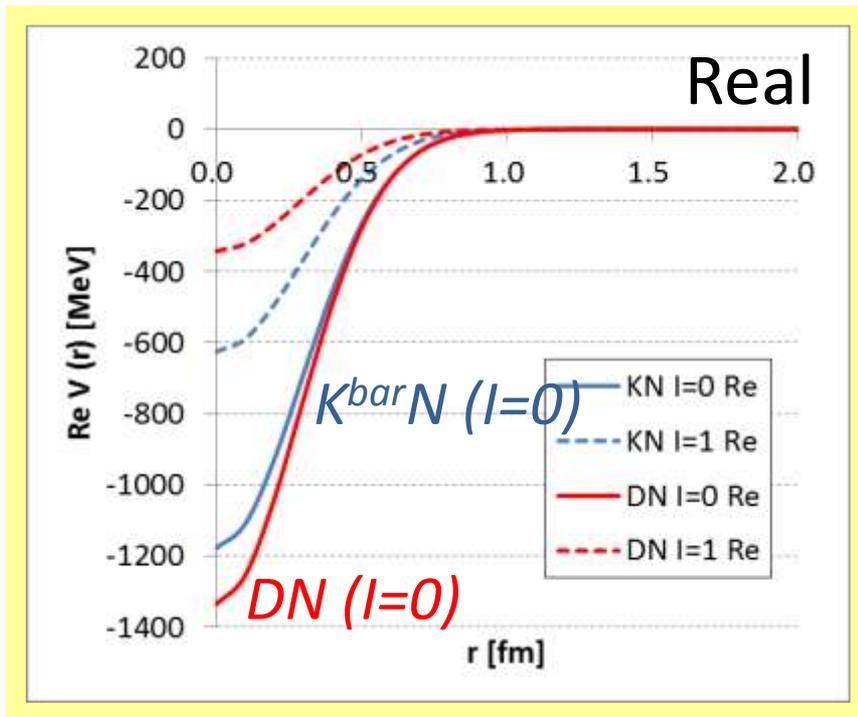
*D meson distributes compactly inside of the system.*

# 4. Comparison with strangeness sector

*D*NN vs *K<sup>bar</sup>*NN

# Potential at $I=0$ resonance

$K^{\text{bar}}N$  pot. : BMN ( $b=0.41\text{fm}$ ) @  $B_K=13.3\text{MeV}$  ...  $\Lambda^*$   
DN pot. : Hyodo ( $b=0.40\text{fm}$ ) @  $B_D=208.9\text{MeV}$  ...  $\Lambda_c^*$



$I=0$  channel,  
 $K^{\text{bar}}N$  pot.  $\sim$  DN pot.

Imaginary potential,  
 $K^{\text{bar}}N$  pot.  $\gg$  DN pot.

*DNN vs  $K^{\text{bar}}NN$*  $K^{\text{bar}}N$  potential $DN$  potential $M_K$  $K^{\text{bar}}NN$ 

Total B.E. = 28 MeV  
 $\Gamma$  = 67 MeV

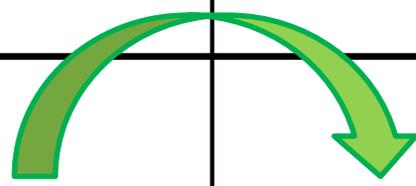
 $M_D$  $DNN$ 

Total B.E. = 225 MeV  
 $\Gamma$  = 26 MeV

# DNN vs $K^{\text{bar}}\text{NN}$

NN pot.: HN1R

	$K^{\text{bar}}N$ potential	DN potential
$M_K$	<p><u><math>K^{\text{bar}}\text{NN}</math></u></p> <p>Total B.E. = 28 MeV <math>\Gamma</math> = 67 MeV</p>	<p>B.E. not so increase.</p> <p>Total B.E. = 40 MeV <math>\Gamma</math> = 11 MeV</p> <p><math>\Gamma</math> decreases.</p>
$M_D$		<p><u>DNN</u></p> <p>Total B.E. = 225 MeV <math>\Gamma</math> = 26 MeV</p>



# DNN vs $K^{\text{bar}}\text{NN}$

NN pot.: HN1R

$K^{\text{bar}}N$  potential

$DN$  potential

$K^{\text{bar}}\text{NN}$

Total B.E. = 28 MeV  
 $\Gamma$  = 67 MeV

Total B.E. = 40 MeV  
 $\Gamma$  = 11 MeV

$M_K$

***B.E. drastically increases.***

$D\text{NN}$

Total B.E. = 187 MeV  
 $\Gamma$  = 180

Total B.E. = 225 MeV

$M_D$

***Suppression of kinetic energy due to large mass of  $D$  meson***

# 5. Summary and Future plan

# 5. Summary

*DNN system studied with a variational approach*

*DN pot.: Vector-meson exchange picture potential,  $\Lambda_c(2595) = DN \text{ q.b.s}$*

*NN pot.: Av18, Hasegawa-Nagata No.1 (R), Minnesota*

*DNN ( $J^\pi=0^-, T=1/2$ ) ... bound below  $\Lambda_c(2595)$ -N threshold*

- *Total B. E.  $\sim 225 \text{ MeV}$  ( $\sim 15 \text{ MeV}$  below  $\Lambda_c(2595)$ -N threshold)*
- *Decay width ( $\pi Y_c$ )  $\sim 25 \text{ MeV}$  ... Narrow compared with total B.E.*

*D meson stays at center of the system,  $l=0$  DN component  $\sim \Lambda_c(2595)$*

*DNN ( $J^\pi=1^-, T=1/2$ ) ... scattering state of  $\Lambda_c(2595)$ -N*

*DNN ( $J^\pi=0^-, T=3/2$ ) ... bound below " $\Sigma_c^*$ "-N threshold*

- *Total B. E.  $\sim 70 \text{ MeV}$  ( $60 \text{ MeV}$  w/ Coulomb)*
- *Decay width ( $\pi \Lambda_c$ )  $\sim 100 \text{ MeV}$*

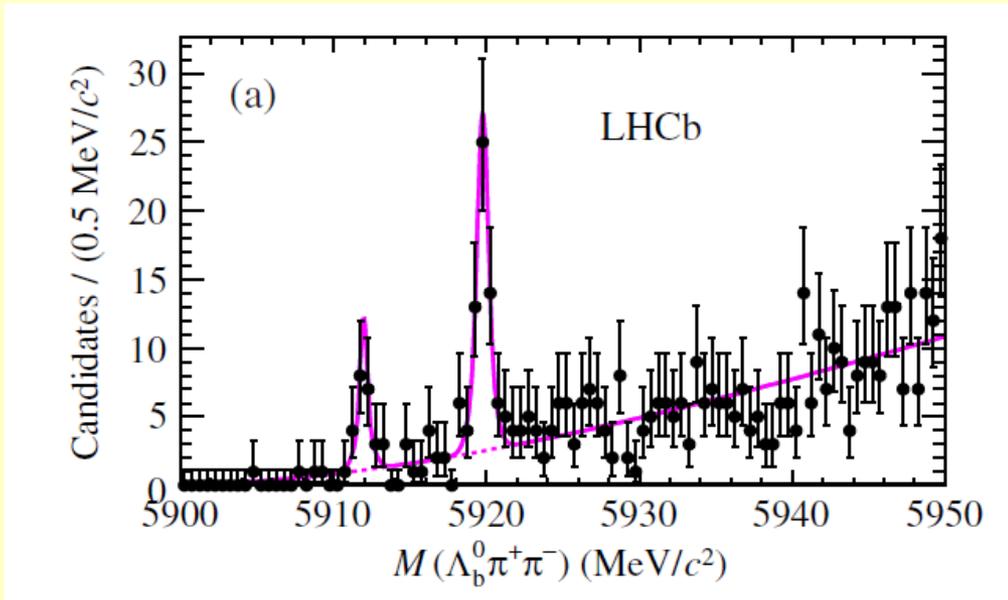
*but large width*

*"Mass effect" = Suppression of kinetic energy of D meson due to its heavy mass*

# 5. Future plan

## How is the bottom sector?

LHCb reported excited  $\Lambda_b$ 's.



$\Lambda_b^0(5912) \sim B^{\text{bar}} N q.b.s?$

➔  $\text{How is } B^{\text{bar}} NN??$

$$M_{\Lambda_b^{*0}(5912)} = 5911.97 \pm 0.12 \pm 0.02 \pm 0.66 \text{ MeV}/c^2,$$

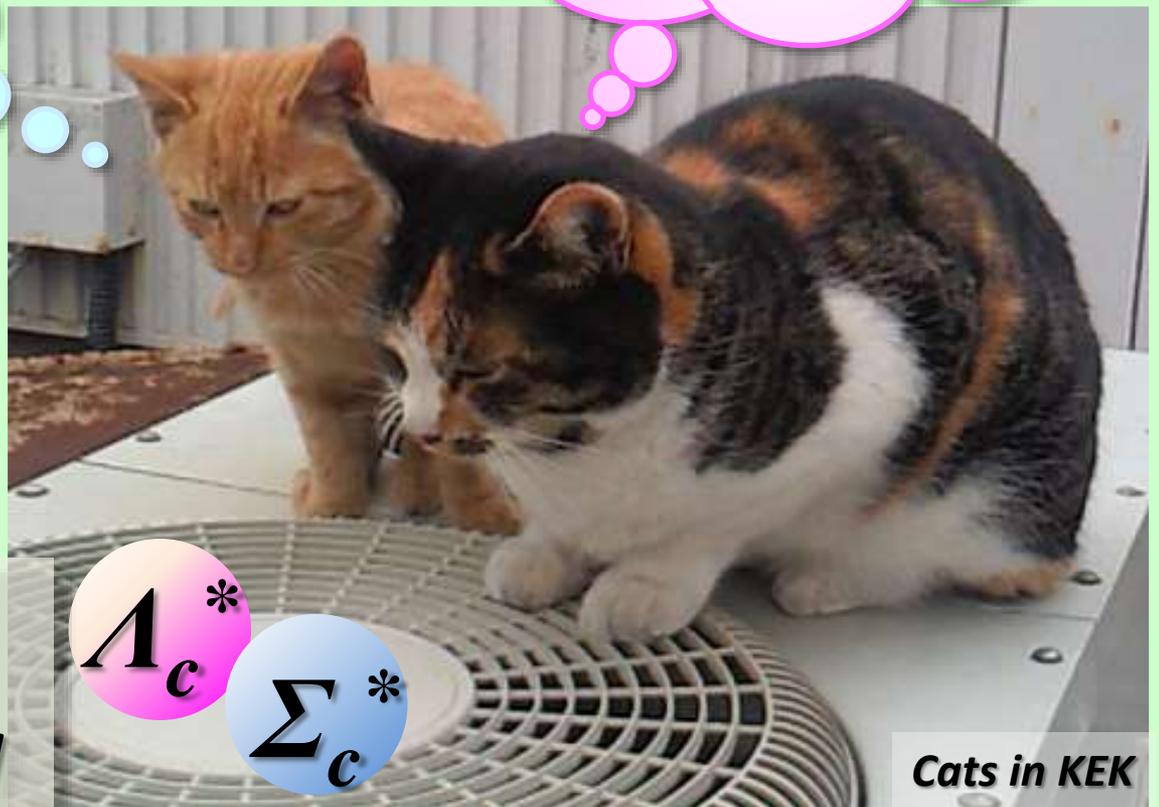
$$M_{\Lambda_b^{*0}(5920)} = 5919.77 \pm 0.08 \pm 0.02 \pm 0.66 \text{ MeV}/c^2,$$

R. Aaij, et al. PRL109, 172003(2012)

***Need more information of  
excited charmed baryons!***

***Isospin?  
Spin??  
Parity???***

***Belle! J-PARC !?  
Lattice QCD ??***



***Thank you for  
your attention!***



***Cats in KEK***