

N* Properties and Coupled Channel Analysis of Meson Production Reactions

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- 1 Analysis of meson production reaction
- 2 Extraction of resonance parameters
- 3 Future plan

The Δ (1232) and others

Total Cross Sections of π^+ Positive Pions in Hydrogen*

H. L. ANDERSON, E. FERMI, E. A. LONG,† AND D. E. NAGLE
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Chicago, Illinois*
(Received January 21, 1952)

N* physics started 60 years ago

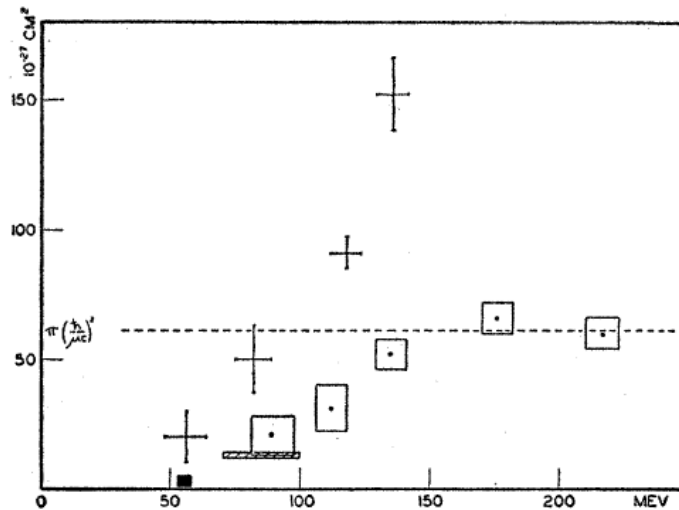
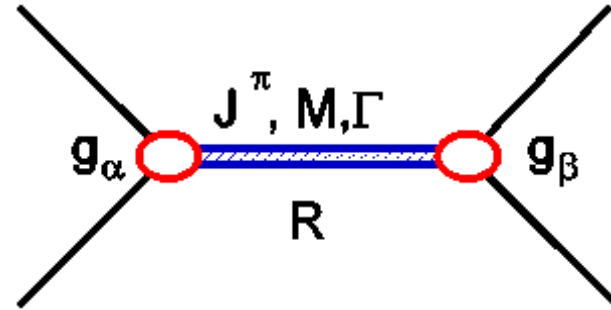


FIG. 1. Total cross sections of negative pions in hydrogen (sides of the rectangle represent the error) and positive pions in hydrogen (arms of the cross represent the error). The cross-hatched rectangle is the Columbia result. The black square is the Brookhaven result and does not include the charge exchange contribution.

Spectrum of hadron excited states and their decay scheme

mass, width,
form factor



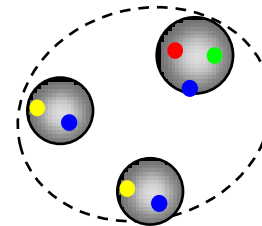
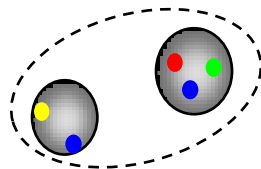
Recent 10 years

high precision data from electromagnetic probe
Jlab, Mainz, Bonn, GRAAL, Spring-8, MIT-bates

constituent quarks



hadron molecule



LQCD

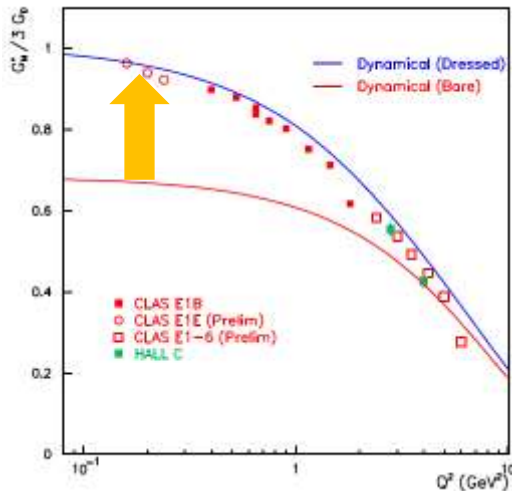
model of hadron

Note: excited baryons are not stable particles
 strong coupling with meson-baryon channels

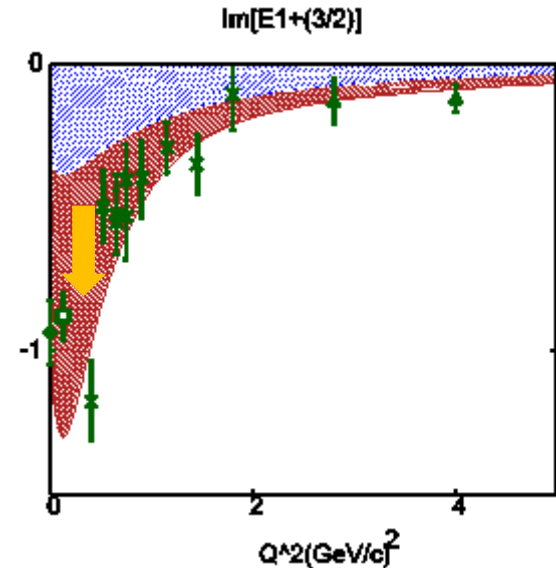
- affects spectrum, structure of resonances.
- analyze meson production reaction with dynamical coupled channel reaction model

Electromagnetic N(1/2+)-Delta_33(3/2+) transition form factor

pion cloud



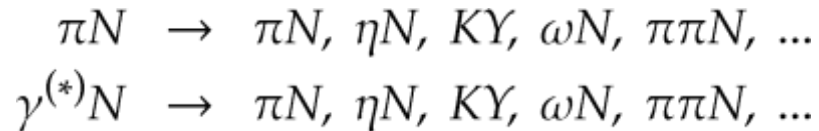
M1: Magnetic dipole
 [spin flip]



E2: Electric quadrupole
 [deformation]

Objective:

I. coupled channel analysis of meson production reaction



II Extract resonance information from partial wave amplitude

Establish spectrum of excited nucleons

Extract N^* coupling constants, form factors

interpret N^* parameters



Hadron Models

Lattice QCD

Dynamical Coupled Channel Approach

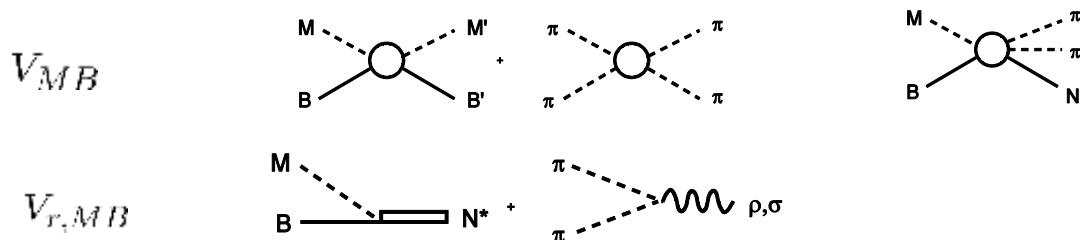
A. Matsuyama, T. Sato, T.-S.H. Lee Phys. Rep. 439 (2007) 193

Start from effective, Hermite Hamiltonian of meson-baryon

$$H = \begin{pmatrix} H_r & V_{r,MB} \\ V_{r,MB} & H_{MB} \end{pmatrix}$$

r : 'short range' $N^*, \Delta, \rho, \sigma$
 MB : 'long range'
 $\gamma N \oplus \pi N \oplus \eta N \oplus KY(\Lambda, \Sigma)$
 $\pi\pi N(\sigma N, \rho N, \pi\Delta)$

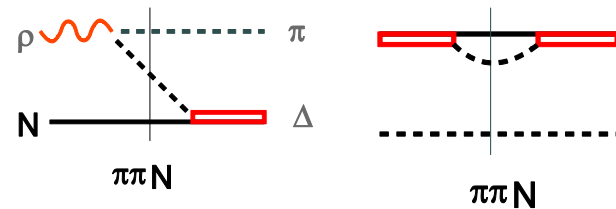
- meson/baryon exchange interactions using effective Lagrangian of meson and baryon



Scattering amplitude of pion and photon induced meson production amplitudes:
solving coupled channel LS equation (3-dim reduction) in momentum space

$$T_{\beta,\alpha}(k', k, W) = V_{\beta,\alpha}(k', k) + \sum_{\gamma} \int_0^{\infty} dq q^2 V_{\beta,\gamma}(k', q) G_{\gamma}^0(q, W) T_{\gamma,\alpha}(q, k, W)$$

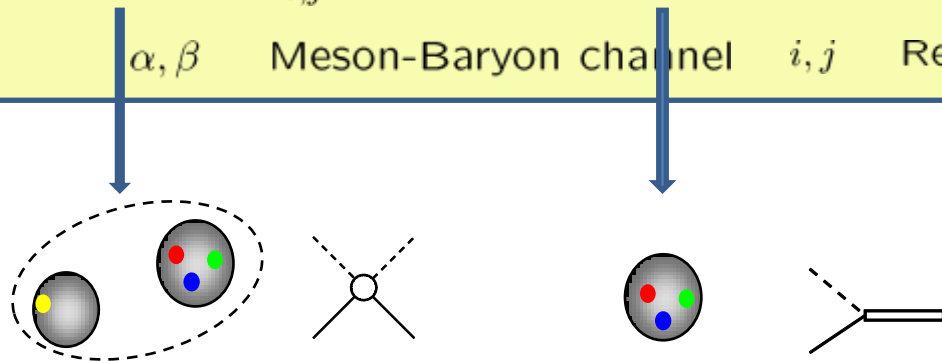
Scattering amplitudes satisfy **two-body and three-body unitarity**



2-2 amplitudes

$$T_{\alpha,\beta}(W) = t_{\alpha,\beta}^{nr}(W) + \sum_{i,j} \bar{\Gamma}_{\alpha,i}(W) \left[\frac{1}{W - m_0 - \Sigma(W)} \right]_{ij} \bar{\Gamma}_{\beta,j}(W)$$

α, β Meson-Baryon channel i, j Resonances



Analysis of meson production reaction:

(2006-2009)

$\pi N, \eta N, \pi\pi N$ ($\pi\Delta, \rho N, \sigma N$) coupled-channels calculations

Hadronic part

- ✓ $\pi N \rightarrow \pi N$: Used for constructing a hadronic model up to $W = 2 \text{ GeV}$. (JLMS)
Julia-Diaz, Lee, Matsuyama, Sato, PRC76 065201 (2007)
- ✓ $\pi N \rightarrow \eta N$: Used for constructing a hadronic model up to $W = 2 \text{ GeV}$
Durand, Julia-Diaz, Lee, Saghai, Sato, PRC78 025204 (2008)
- ✓ $\pi N \rightarrow \pi\pi N$: First full dynamical coupled-channels calculation up to $W = 2 \text{ GeV}$.
Kamano, Julia-Diaz, Lee, Matsuyama, Sato, PRC79 025206 (2009)

Electromagnetic part

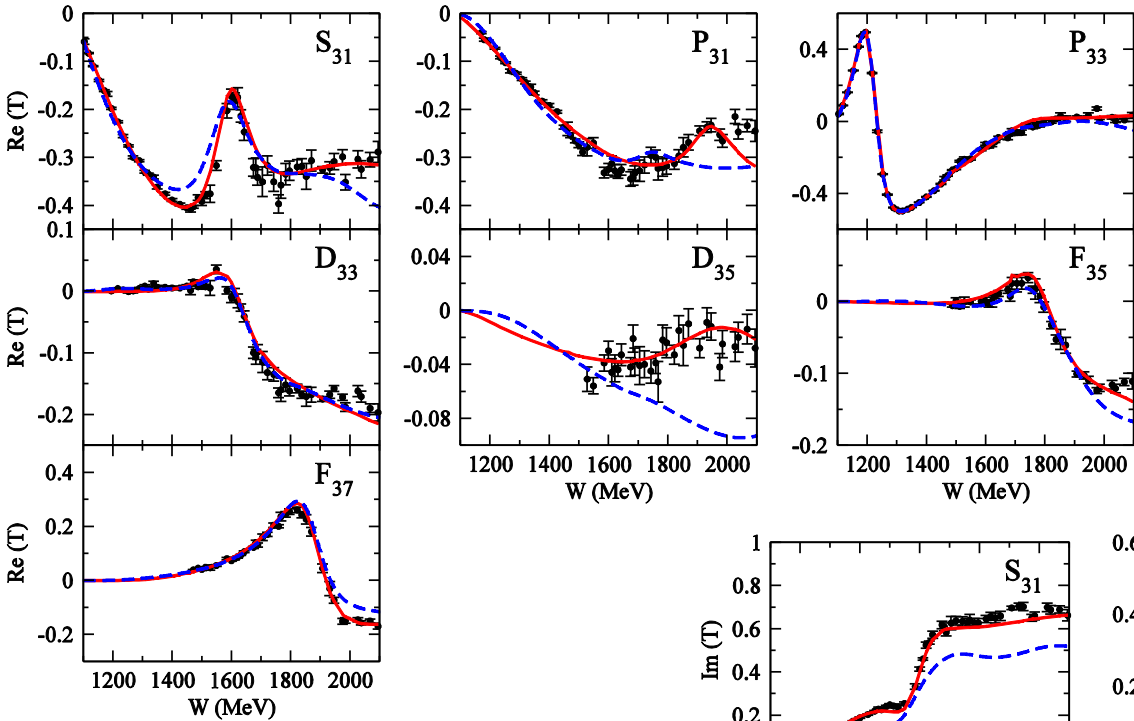
- ✓ $\gamma^{(*)} N \rightarrow \pi N$: Used for constructing a E.M. model up to $W = 1.6 \text{ GeV}$ and $Q^2 = 1.5 \text{ GeV}^2$
(photoproduction) Julia-Diaz, Lee, Matsuyama, Sato, Smith, PRC77 045205 (2008)
(electroproduction) Julia-Diaz, Kamano, Lee, Matsuyama, Sato, Suzuki, PRC80 025207 (2009)
- ✓ $\gamma N \rightarrow \pi\pi N$: First full dynamical coupled-channels calculation up to $W = 1.5 \text{ GeV}$.
Kamano, Julia-Diaz, Lee, Matsuyama, Sato, PRC80 065203 (2009)

Recently : $\pi N \rightarrow KY$, $\gamma N \rightarrow KY$ in preparation

of data points

pi N -> pi N ~ 23000
-> eta N ~ 300
-> KY ~ 2000
-> pipiN ~ 350

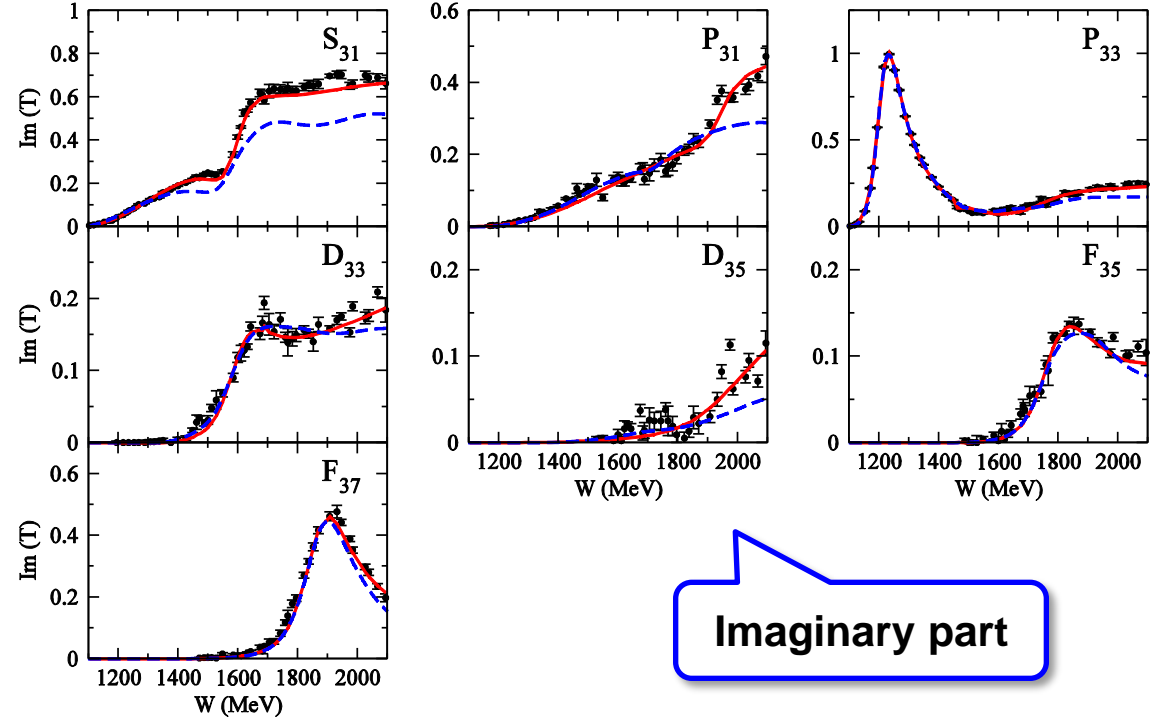
gamma N -> pi N ~ 18000
-> eta N ~ 1700
-> KY ~ 3300



Real part

$$I = \frac{3}{2}$$

— Current model
 (fully combined analysis,
PRELIMINARY)
 - - - Previous model
 (fitted to $\pi N \rightarrow \pi N$ data only)
 [PRC76 065201 (2007)]



Imaginary part

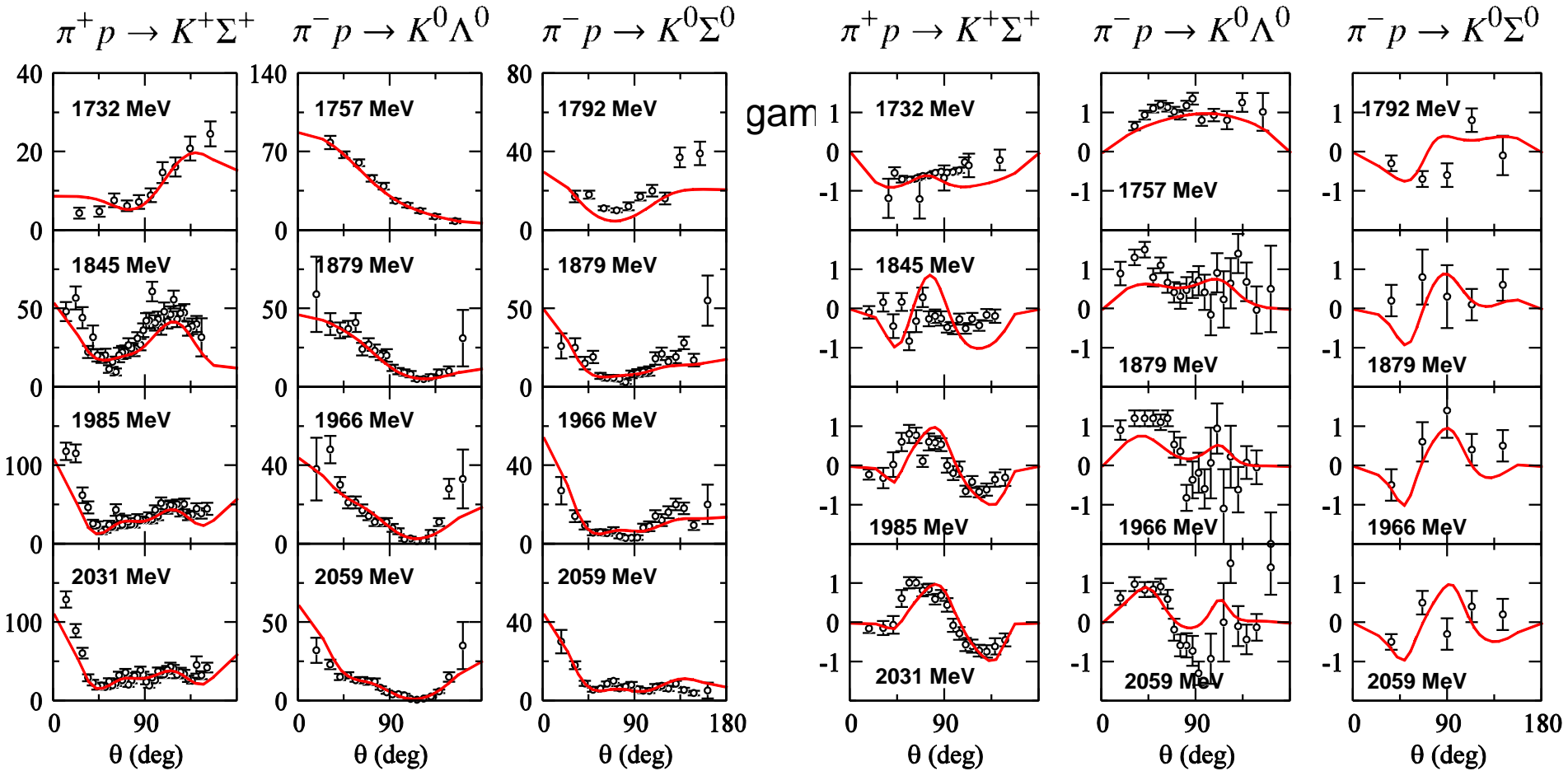
$\pi N \rightarrow KY$ reactions

Kamano, Nakamura, Lee, Sato in preparation

Preliminary!!

Angular distribution $d\sigma/d\Omega$ ($\mu\text{b}/\text{sr}$)

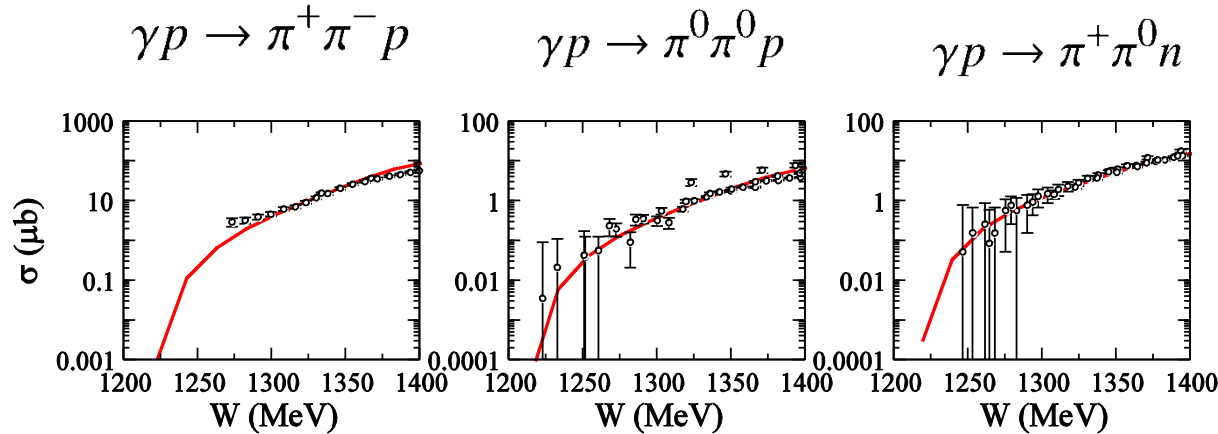
Recoil polarization



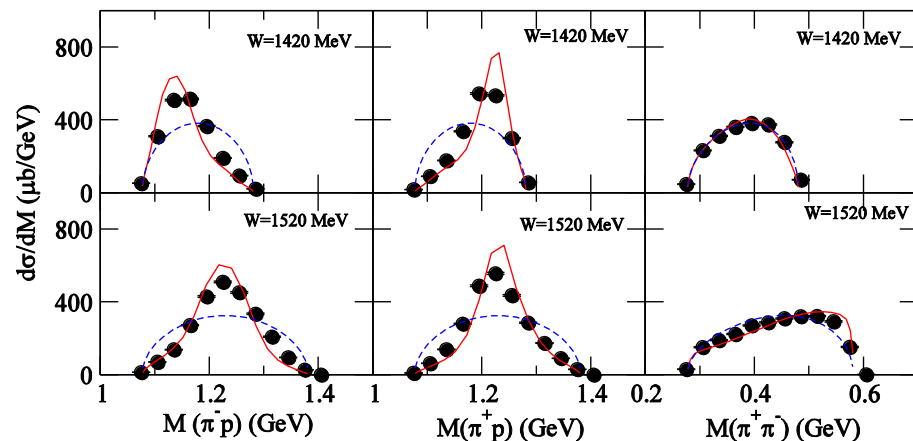
Double pion photoproduction

Kamano, Julia-Diaz, Lee, Matsuyama, Sato, PRC80 065203 (2009)

Parameters used in the calculation are from $\pi N \rightarrow \pi N$ & $\gamma N \rightarrow \pi N$ analyses.



- ✓ Good description near threshold
- ✓ Reasonable shape of invariant mass distributions
- ✓ Above 1.5 GeV, the total cross sections of $p\pi^0\pi^0$ and $p\pi^+\pi^-$ overestimate the data.

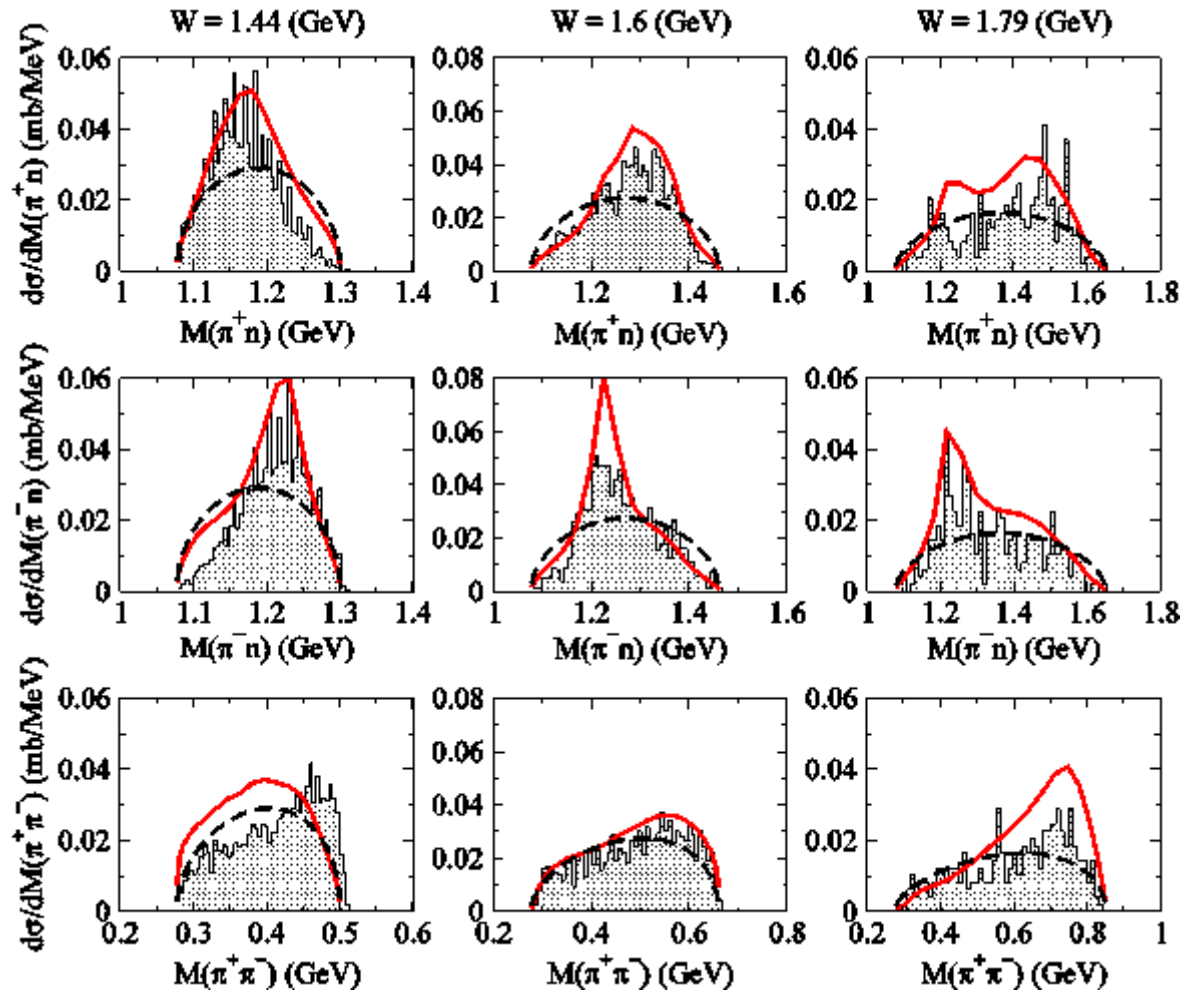


$$\pi^- p \rightarrow \pi^+ \pi^- n$$

Kamano, Julia-Diaz, Lee, Matsuyama, Sato, PRC79 025206 (2009)

Invariant mass distributions

- Full result
- - - Phase space

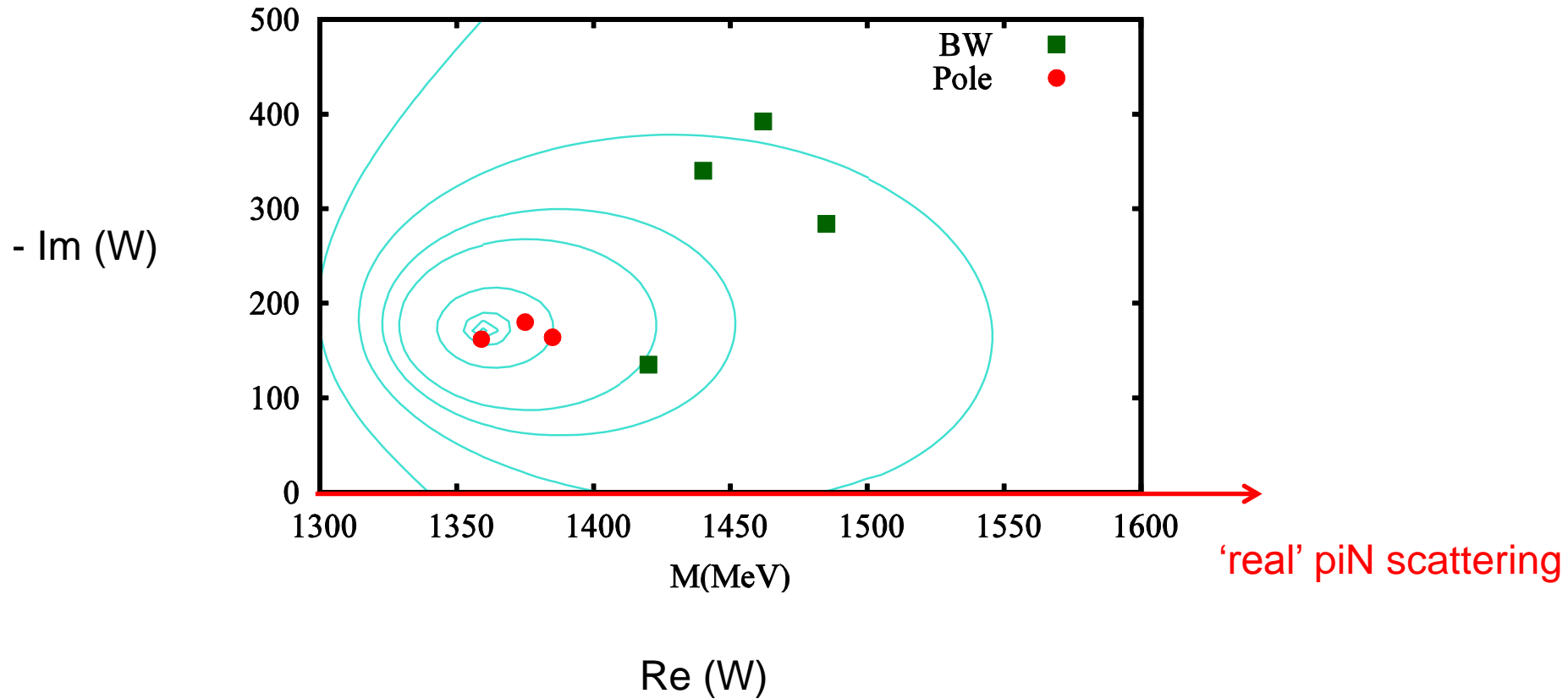


Data handled with the help of R. Arndt

Extraction of resonance parameters

N. Suzuki, Sato, Lee ,PRC82 (2010)045296
PRC79 (2009)025295

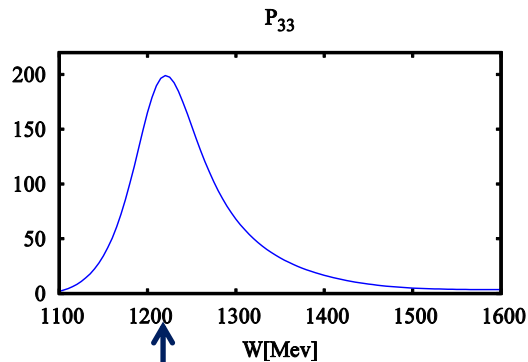
Resonance energy of P11 (BW, pole)
+ contour plot of piN scattering amplitude |F|



Extraction of resonance parameters

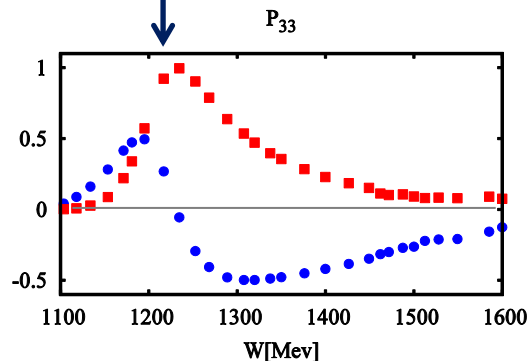
Breit-Wigner parametrization of partial wave amplitudes

$$T(E) = \frac{e^{2i\delta_b(E)} R_{BW}(E)}{M_{BW} - E - i\Gamma_{BW}(E)/2} + B(E)$$



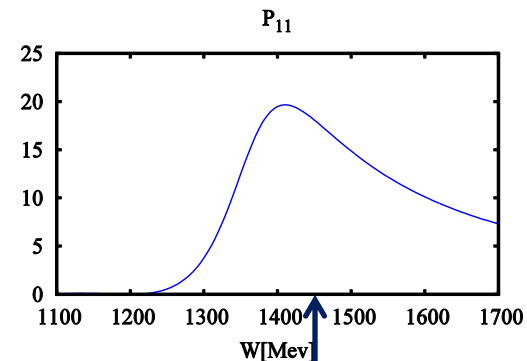
piN elastic scattering
partial wave cross
section

P33 1232

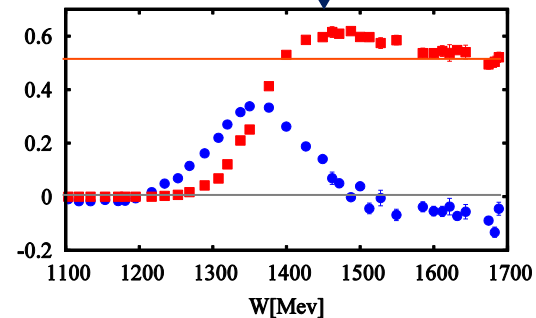


piN elastic scattering
amplitude

$$F = \frac{S - 1}{2i}$$



P11 1440



Im(F),

Re(F)

Resonance parameters from pole of amplitude on un-physical sheet

$$T(E) = \frac{R}{M - E - i\Gamma/2} + B(E)$$

✓ pole energy

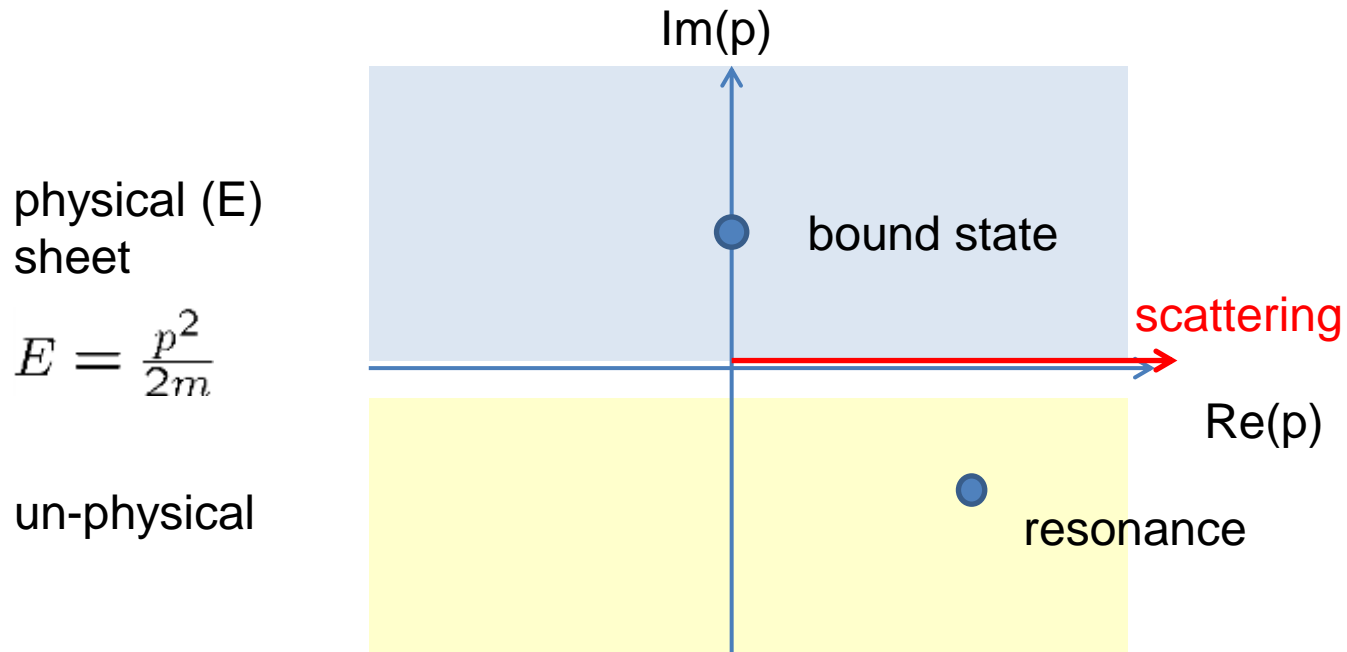


resonance mass and width $M \Gamma$

✓ residue of amplitude



coupling constant of resonance with meson-baryon



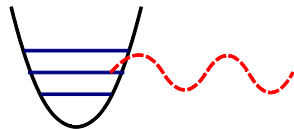
Resonance as eigen state of Hamiltonian with outgoing boundary condition(non-hermit) Siegert(39), R. H. Dalitz, R. G. Moorhouse(70)

$$H\psi_{res} = E_{res}\psi_{res} \quad \partial\psi_{res}/\partial r - iq_{res}\psi_{res} = 0$$

Coupling constant, form factor : residue of the amplitude at pole

$$\gamma_{em} = \langle \psi_{res} | j_{em} | \psi_N \rangle$$

Coupling constants need not be real



$$\psi_{res} = \psi('bound') + \psi('scattering')$$

Well defined resonance parameters can be a starting point to contact with hadron models

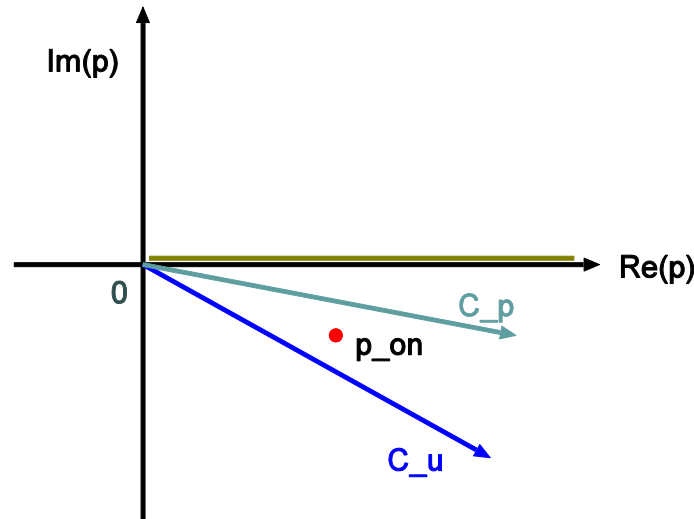
How to obtain T-matrix on un-physical/physical sheet for complex W

- Scattering amplitudes are obtained by solving LS equation in momentum space

$$T_{\beta,\alpha}(k', k, W) = V_{\beta,\alpha}(k', k) + \sum_{\gamma} \int_C dq q^2 V_{\beta,\gamma}(k', q) G_{\gamma}^0(q, W) T_{\gamma,\alpha}(q, k, W)$$

analytic continuation within the model by using contour deformation of momentum of momentum integral.

by choosing appropriate contour on each channel, we can obtain p- or u-sheet T-matrix.



How to evaluate poles and residue

$$T_{\alpha,\beta}(W) = t_{\alpha,\beta}^{nr}(W) + \sum_{i,j} \bar{\Gamma}_{\alpha,i}(W) \left[\frac{1}{W - m_0 - \Sigma(W)} \right]_{ij} \bar{\Gamma}_{\beta,j}(W)$$

α, β Meson-Baryon channel i, j Resonances



- Determinant of N^* green function gives resonance position

$$Det[(W - m_0 - \Sigma(W))_{ij}]$$



- Resonance form factors from residue of amplitude MB

$$\bar{\Gamma} \sim \langle \tilde{N}^* | j | N \rangle = \langle N^* | j | N \rangle + \langle N^* | \Gamma G_0 t_j | N \rangle$$

poles on sheet near physical cut are searched.

(u-sheet for open channel, p-sheet for closed channel)

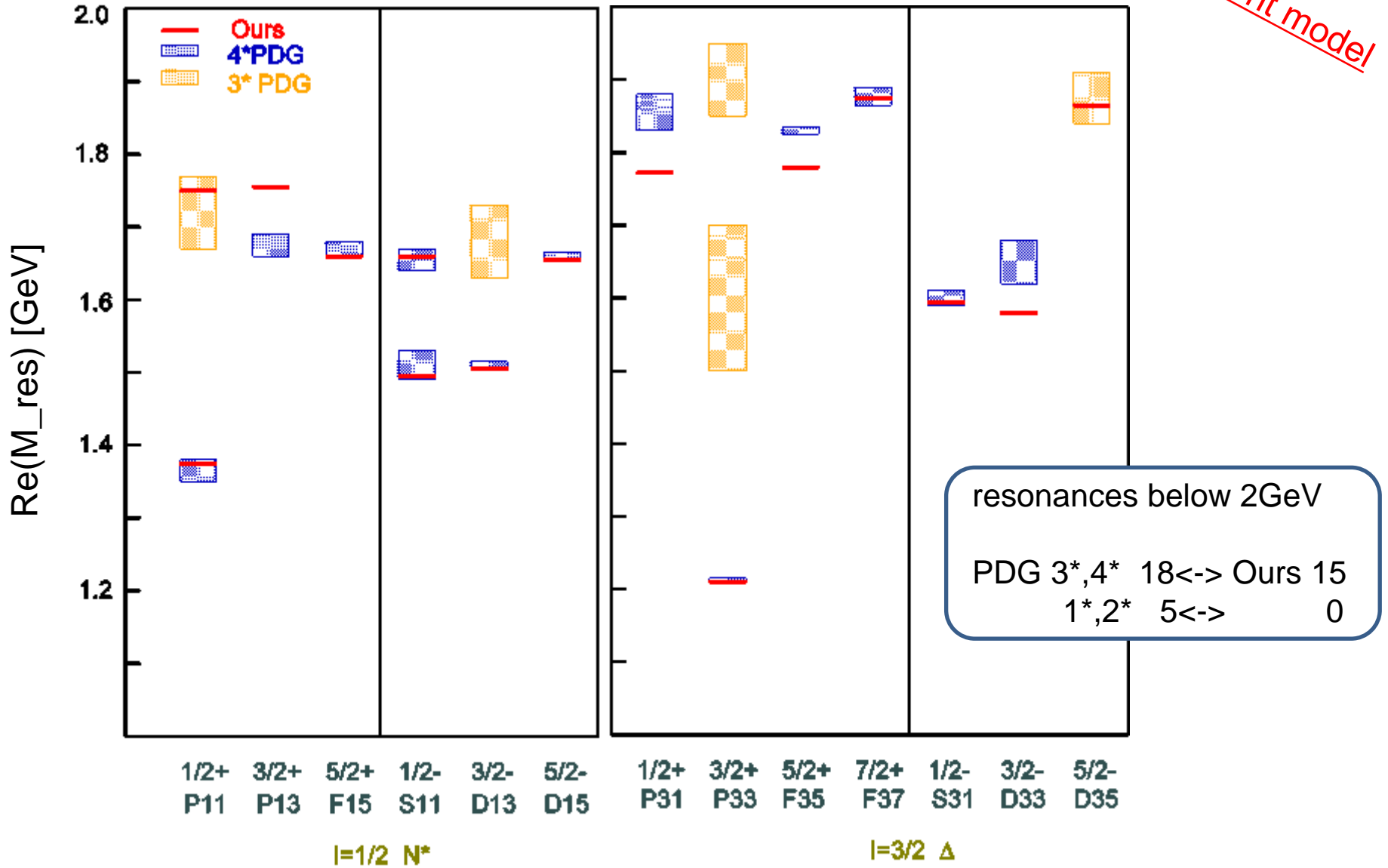
energy around threshold, both p- and u- sheets are searched.

Results using reaction model from global fit of meson production reaction

- Spectrum ($\text{Re}(M_{\text{res}})$)
- Width ($\text{Im}(M_{\text{res}})$)
- P11

Spectrum of excited nucleons $\text{Re}(M_{\text{res}})$ below 2GeV

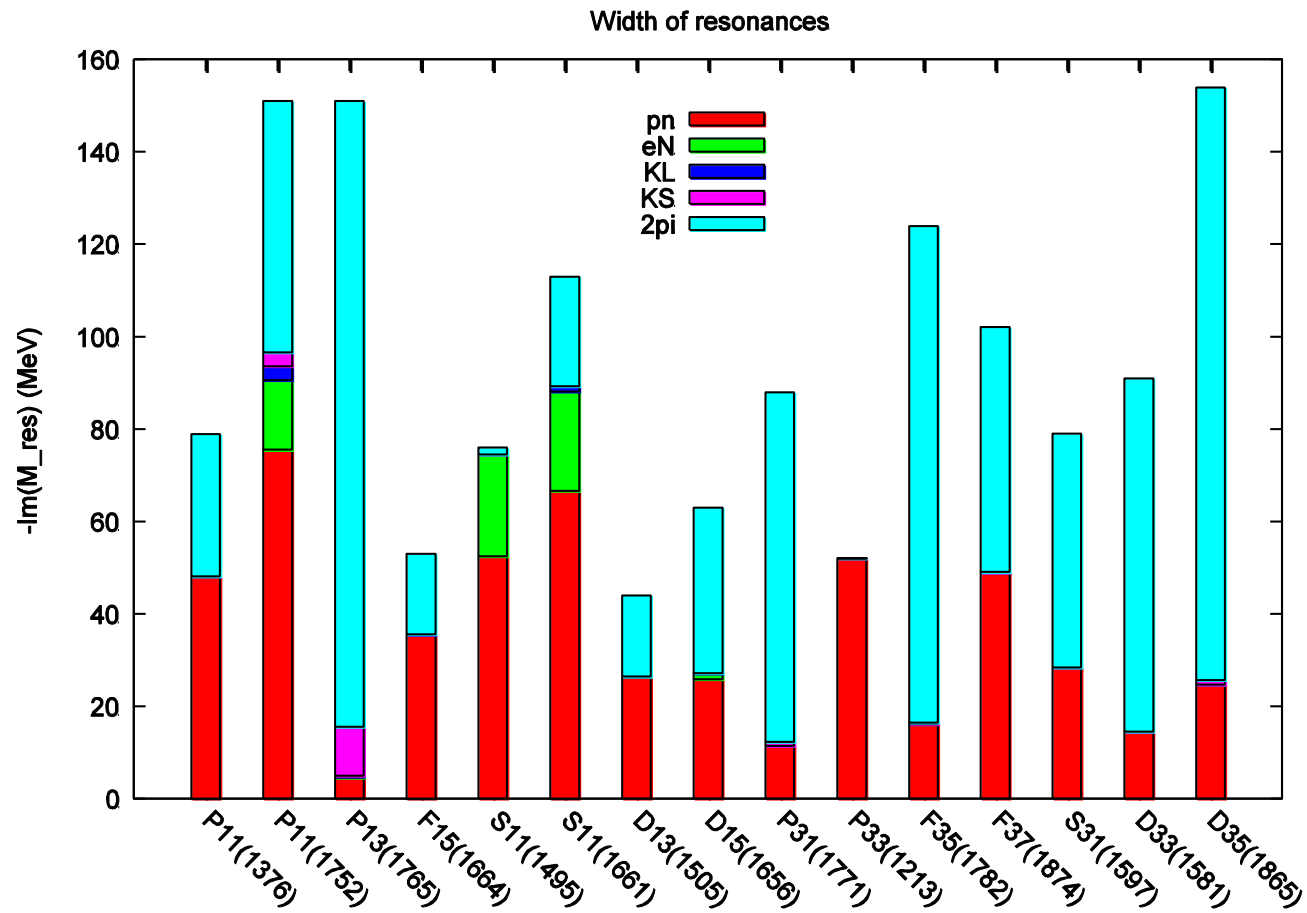
current model



Half width

$$\Gamma/2 = -\text{Im}(E_{res})$$

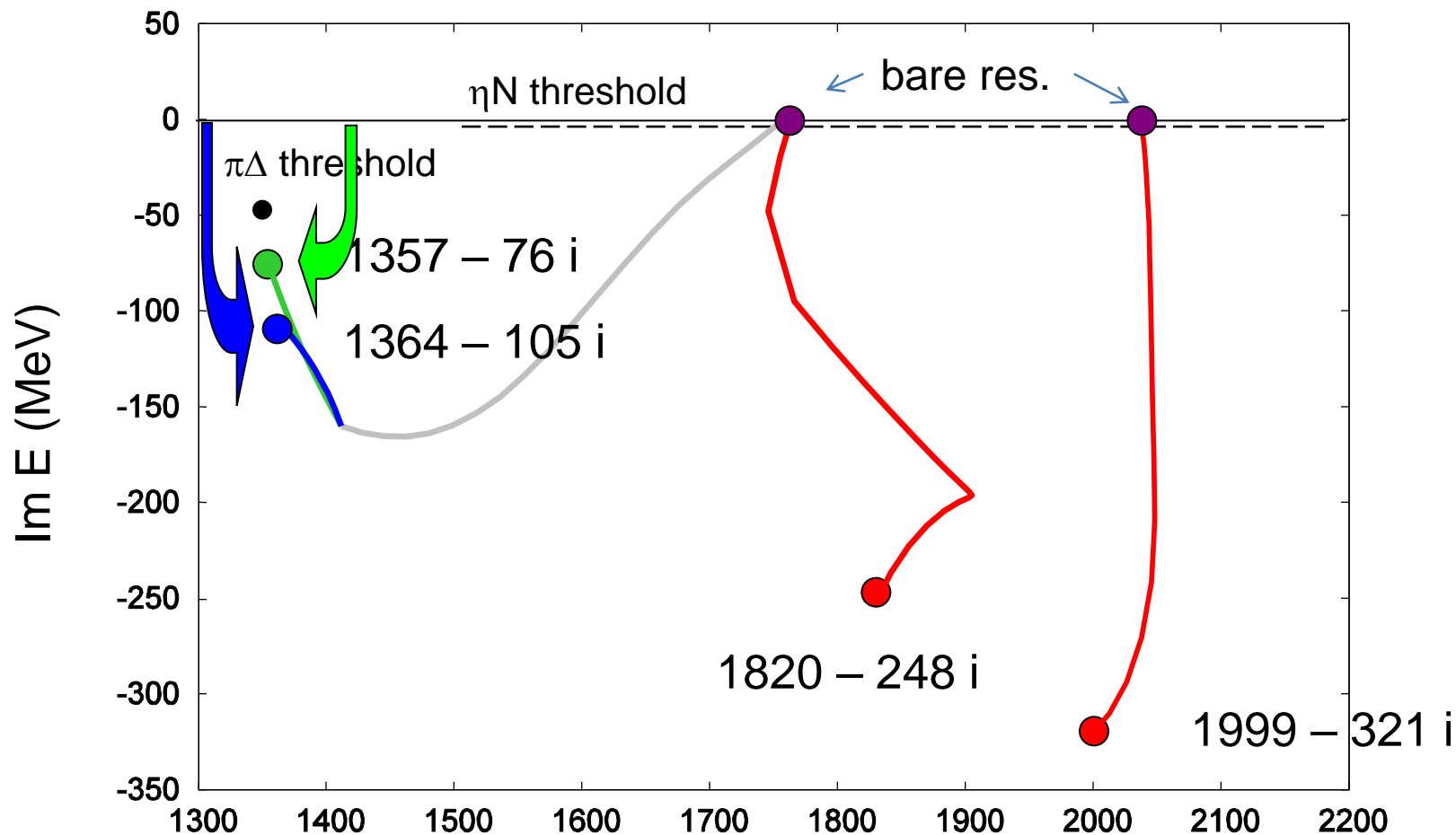
current model



Some freedom exists on the definition of partial width from the residue of the amplitude. The numbers should be taken as a one estimation of the MB-res coupling strength .

Trajectory of P11 poles from 'bare' to 'dressed'

$$\det[(W - M_i)\delta_{ij} - x\Sigma_{ij}(W)] = 0 \quad 0 \leq x \leq 1$$



* two poles near branching points

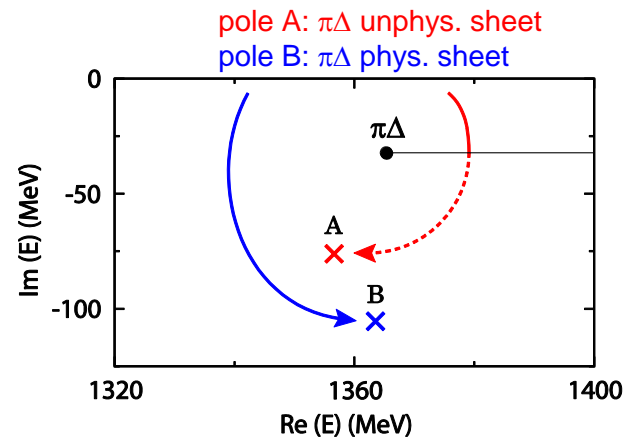
examples :

$$f_0(\pi\pi - K\bar{K})$$

$${}^5\text{He}(n - \alpha, d - t)$$

* input: 2 bare 'stable' resonances --> output: three resonance poles

P11 pole



Resonance in coupled channel problem

- * phys and un-phys sheets for each channel
- * poles of t-matrix on more than one sheet
(the above example, the resonance has two poles uu and up/pu)
- * usually one of the poles close to the real energy (scattering takes place) affects 'cross section', which is used to characterize resonance.
- * exceptional case: both poles can be near physical sheet.

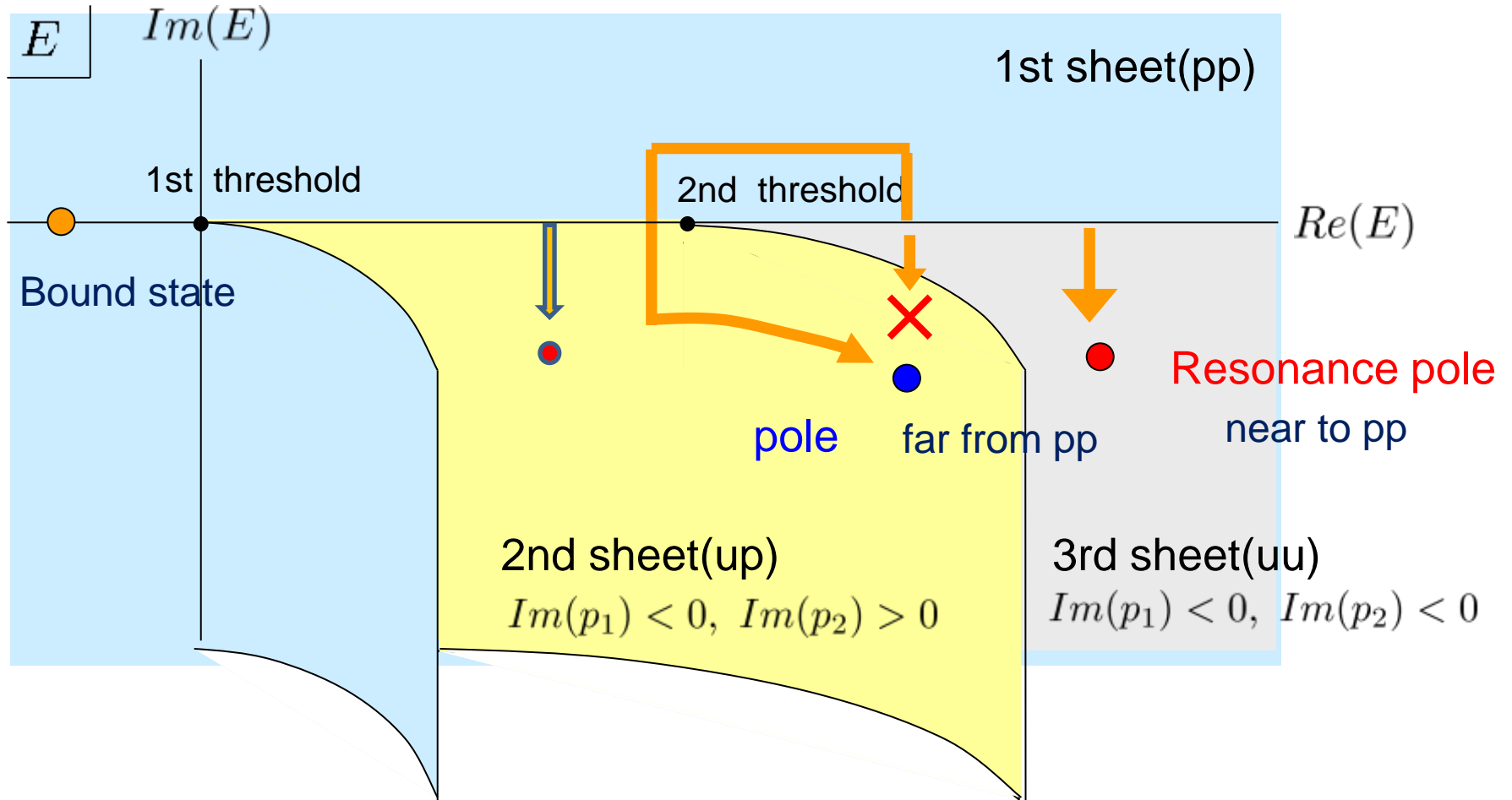
Simple example of two-channel Breit-Wigner formula

$$T_{11}(E) = \frac{-\gamma_1 p_1}{E - M + i\gamma_1 p_1 + i\gamma_2 p_2}$$

$$p_i = \sqrt{2\mu_i(E - m_{ia} - m_{ib})}$$

pole position : $E - M + i\gamma_1 p_1 + i\gamma_2 p_2 = 0$

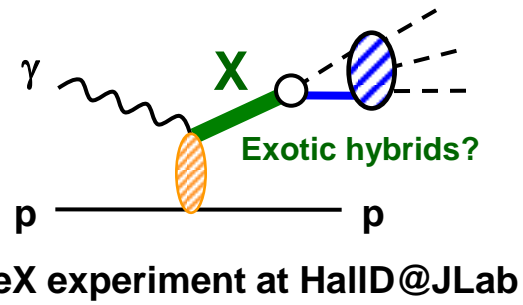
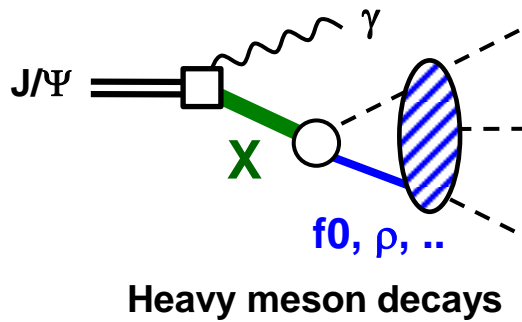
Pole of scattering amplitude on complex energy plane



- reaction dynamics strongly affects resonance properties !
- more analysis necessary to understand the mechanism why those phenomena happened.
- understanding of hadron's reaction dynamics is important before we are able to compare extracted resonance parameters with model of hadron.

Future plan

Study of meson spectroscopy , Exotic meson, CP phase

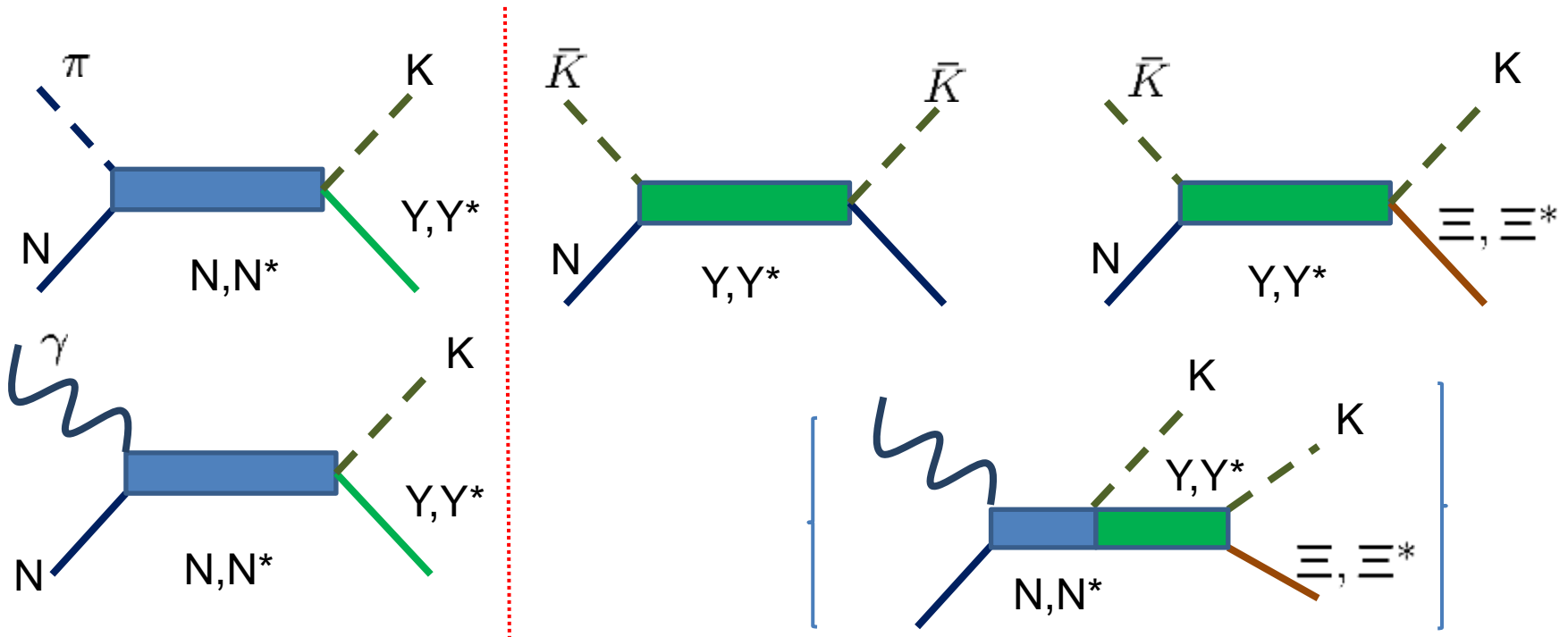


Kamano, Nakamura, Lee, Sato, arXiv:1106.4523 to appear in PRD

Theory Projects for Strangeness production Reactions on the Nucleon and Nuclei

H. Kamano (RCNP, Osaka U.) T.-S. H. Lee (ANL) Y. Oh (Kyungpook U.)
 T. Sato (Osaka U.) Dec. 4-10 2011 @ Kyungpook Univ.

use developed tools, code of coupled channel reaction for N^* to investigate strange baryon $Y^* \rightarrow \text{cascade}^*$
 \rightarrow [reaction on a few nucleon system (BB interaction)]



Summary

Meson production reactions for $W < 2\text{GeV}$ are analyzed with dynamical coupled channel reaction theory and partial wave amplitudes are extracted with improved description of meson production reaction.

Resonance parameters defined as the pole of the scattering amplitude are extracted from analytic continuation of PWA.

Reaction dynamics of meson and baryon plays significant role on resonance properties.

Combined analysis of the 'reaction theory' + 'structure of hadron' is necessary ways to understand excited states of nucleon.

- > extended works using developed tools
 - * strange (hyperon, cascade) baryons
 - * meson resonances in heavy meson decay and pion and photon induced meson resonance production
 - * reactions on electroweak probe
 - * contact with LQCD, scattering in finite box