

Chiral Symmetry and Hadron Physics - selected topics -

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- Low-energy QCD:
symmetries and **symmetry breaking** patterns
- **Strangeness** and **chiral SU(3) dynamics**
- The **sigma term** of the nucleon and its implications
- New constraints from **neutron stars**



Hierarchy of **QUARK MASSES** in **QCD**



$$\begin{aligned} m_d &\simeq 4 - 6 \text{ MeV} \\ m_u/m_d &\sim 0.3 - 0.6 \\ m_s &\simeq 80 - 130 \text{ MeV} \\ (\mu &\simeq 2 \text{ GeV}) \end{aligned}$$

- **LOW-ENERGY QCD: CHIRAL EFFECTIVE FIELD THEORY**
- **expansion in m_q and in powers of low momentum**

$$\begin{aligned} m_c &\simeq 1.25 \text{ GeV} \\ m_b &\simeq 4.2 \text{ GeV} \\ m_t &\simeq 174 \text{ GeV} \end{aligned}$$

- **Non-Relativistic QCD: HEAVY QUARK EFFECTIVE THEORY**
- **expansion in powers of $1/m_Q$**



Spontaneously Broken **CHIRAL** $SU(3)_L \times SU(3)_R$ **SYMMETRY**

- NAMBU - GOLDSTONE BOSONS:**

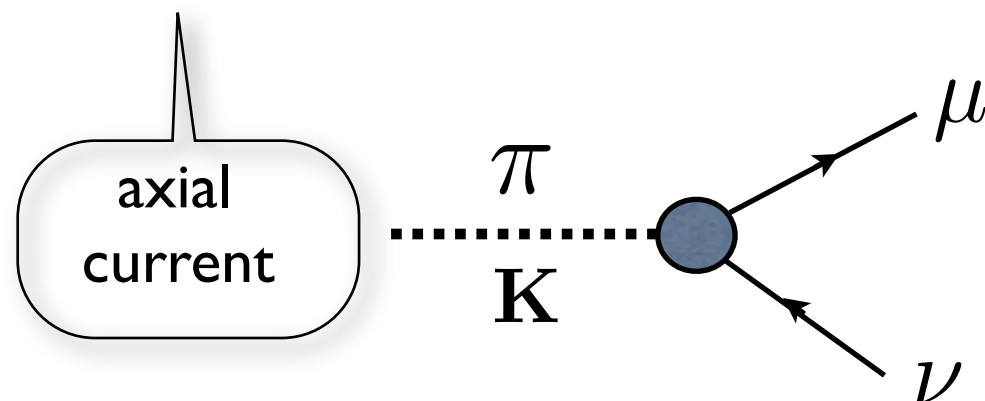
Pseudoscalar $SU(3)$ meson octet $\{\phi_a\} = \{\pi, \mathbf{K}, \bar{\mathbf{K}}, \eta_8\}$

- ORDER PARAMETERS:**

$$\langle 0 | \mathbf{A}_a^\mu(0) | \phi_b(p) \rangle = i \delta_{ab} p^\mu f_b$$

DECAY CONSTANTS

(chiral limit: $f = 86.2 \text{ MeV}$)



$$f_\pi = 92.4 \pm 0.3 \text{ MeV}$$

$$f_{\mathbf{K}} = 110.0 \pm 0.9 \text{ MeV}$$

$$f_\eta = 120.1 \pm 4.6 \text{ MeV}$$

spontaneous
symmetry breaking

$$m_\pi^2 f_\pi^2 = -m_q \langle \bar{\psi} \psi \rangle + \mathcal{O}(m_q^2)$$

explicit
symmetry breaking



PART 1.

LOW-ENERGY QCD with STRANGE QUARKS

... realized as an **EFFECTIVE FIELD THEORY** with SU(3) octet of pseudoscalar Nambu-Goldstone bosons coupled to the baryon octet.

- **Strange quarks** are intermediate between “**light**” and “**heavy**”:
 - ▶ interplay between **spontaneous** and **explicit chiral symmetry breaking**
- Testing ground: high-precision **antikaon-nucleon** threshold physics
- Nature and structure of $\Lambda(1405)$ ($B = 1$, $S = -1$, $J^P = 1/2^-$)
- Role of **strangeness** in dense baryonic matter ?
 - ▶ new constraints from **neutron stars**

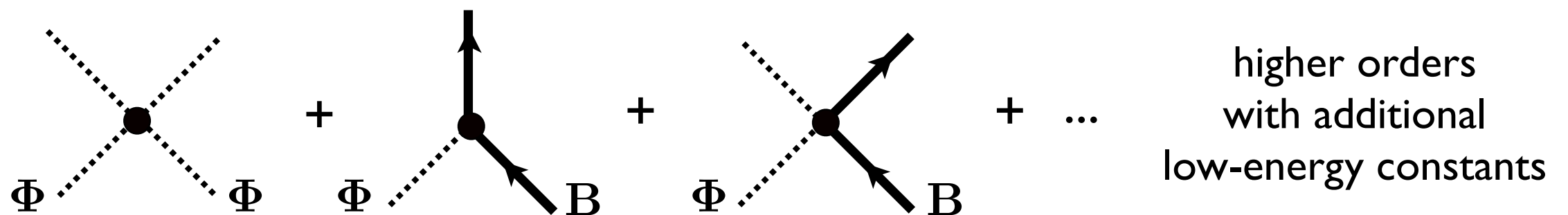


CHIRAL SU(3) EFFECTIVE FIELD THEORY

- Interacting systems of **NAMBU-GOLDSTONE BOSONS** (**pions, kaons**) coupled to **BARYONS**

$$\mathcal{L}_{eff} = \mathcal{L}_{mesons}(\Phi) + \mathcal{L}_B(\Phi, \Psi_B)$$

- Leading **DERIVATIVE** couplings (involving $\partial^\mu \Phi$) determined by spontaneously broken **CHIRAL SYMMETRY**



- Low-Energy Expansion: **CHIRAL PERTURBATION THEORY**

“small parameter”:

$$\frac{p}{4\pi f_\pi} \sim \frac{\text{energy / momentum}}{1 \text{ GeV}}$$

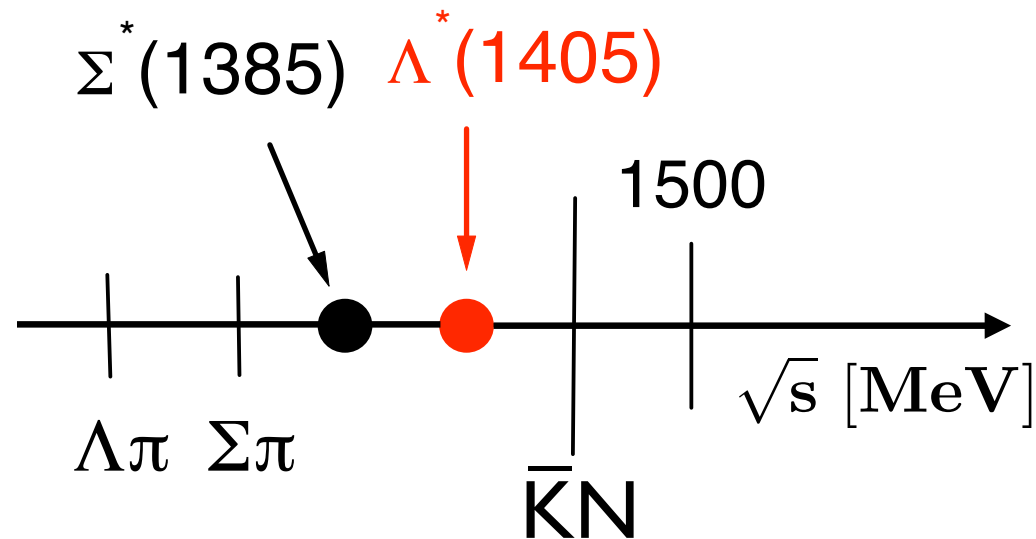
- works well for low-energy **pion-pion** and **pion-nucleon** interactions

► ... but **NOT** for systems with **strangeness** $S = -1$ ($\bar{K}N$, $\pi\Sigma$, ...)



Low-Energy $\bar{K} N$ Interactions

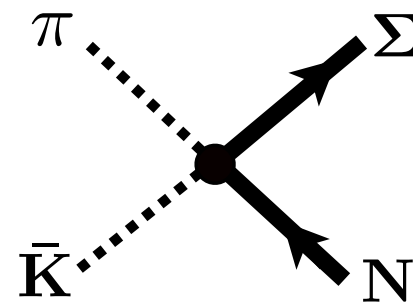
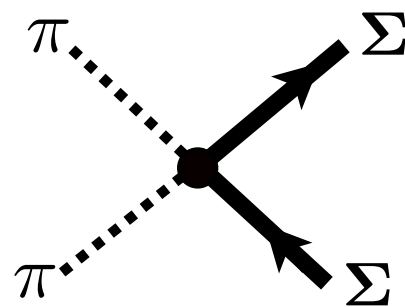
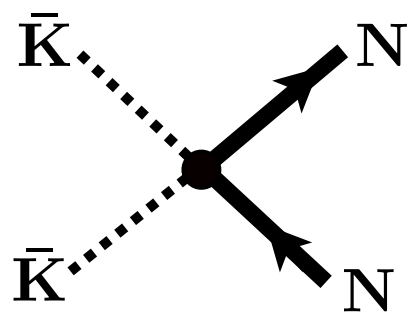
- Chiral Perturbation Theory **NOT** applicable:
 $\Lambda(1405)$ resonance 27 MeV below $K^+ p$ threshold



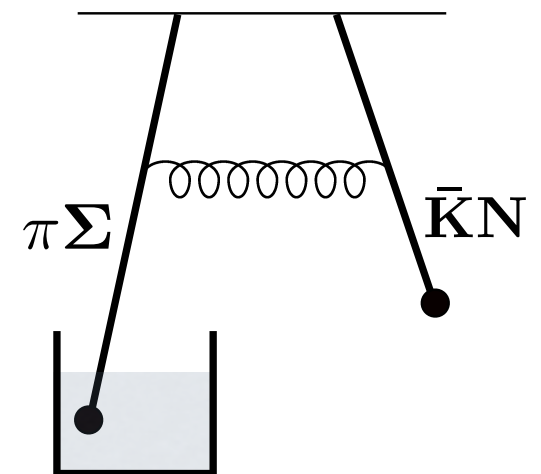
Non-perturbative
Coupled Channels
 approach based on
Chiral SU(3) Dynamics

N. Kaiser, P. Siegel, W.W. (1995)
 E. Oset, A. Ramos (1998)

- Leading s-wave $l = 0$ meson-baryon interactions (Tomozawa-Weinberg)



channel coupling

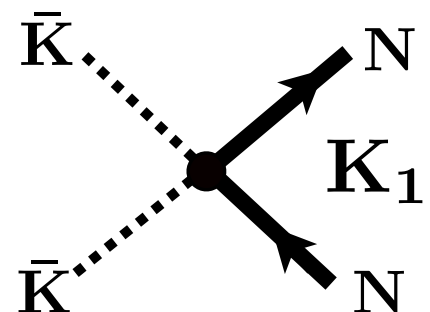


CHIRAL SU(3) COUPLED CHANNELS DYNAMICS

$$T_{ij} = K_{ij} + \sum_n K_{in} G_n T_{nj}$$

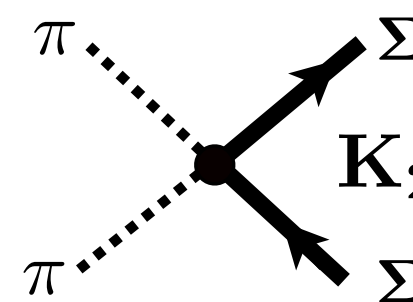
- Leading s-wave $I = 0$ meson-baryon interactions (Tomozawa-Weinberg)
Note: **ENERGY DEPENDENCE** characteristic of Nambu-Goldstone Bosons

$$|1\rangle = |\bar{K}N, I = 0\rangle$$



$$K_{11} = \frac{3}{2 f_K^2} (\sqrt{s} - M_N)$$

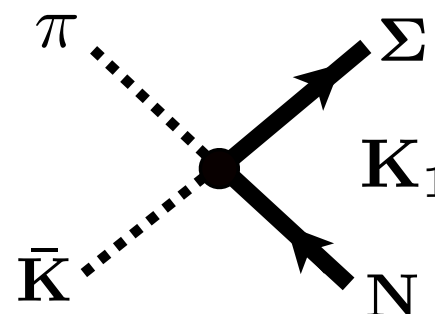
$$|2\rangle = |\pi\Sigma, I = 0\rangle$$



$$K_{22} = \frac{2}{f_\pi^2} (\sqrt{s} - M_\Sigma)$$

- driving interactions individually **strong** enough to produce
▶ $\bar{K}N$ **bound state**
▶ $\pi\Sigma$ **resonance**

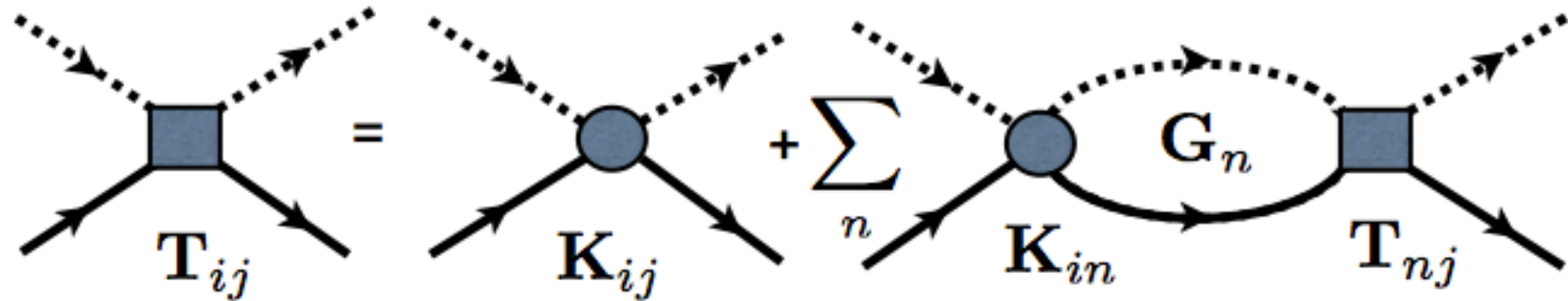
strong
channel coupling
 $12 \leftrightarrow 21$:



$$K_{12} = \frac{-1}{2 f_\pi f_K} \sqrt{\frac{3}{2}} \left(\sqrt{s} - \frac{M_\Sigma + M_N}{2} \right)$$



CHIRAL SU(3) COUPLED CHANNELS DYNAMICS



$$T_{ij} = K_{ij} + \sum_n K_{in} G_n T_{nj}$$

input from
chiral SU(3)
meson-baryon
effective Lagrangian

loop functions
(dim. regularization)
with subtraction constants
encoding short distance dynamics

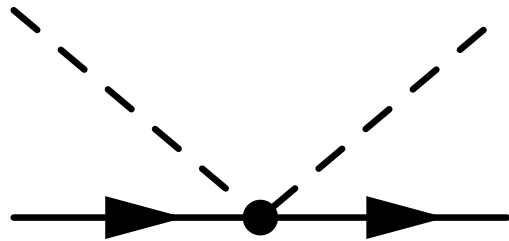
● coupled channels:

K^-p , \bar{K}^0n , $\pi^0\Sigma^0$, $\pi^+\Sigma^-$, $\pi^-\Sigma^+$, $\pi^0\Lambda$, $\eta\Lambda$, $\eta\Sigma^0$, $K^+\Xi^-$, $K^-\Xi^0$



CHIRAL SU(3) COUPLED CHANNELS DYNAMICS:

- NLO hierarchy of driving terms -

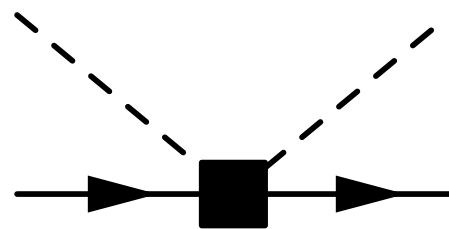
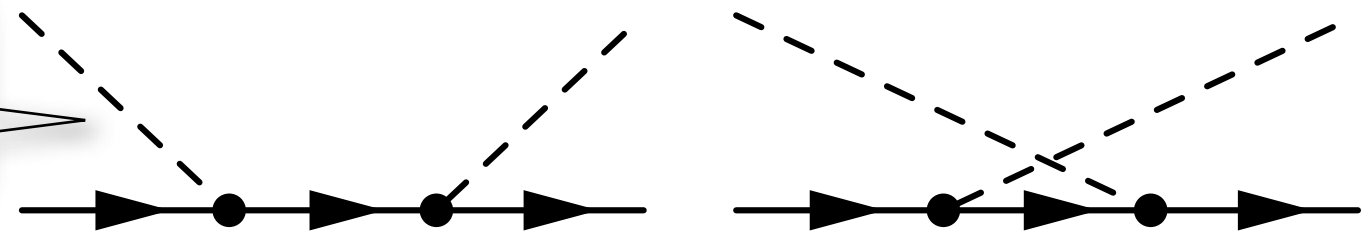


leading order (**W**einberg-**T**omozawa) terms
input: physical pion and kaon decay constants

direct and crossed **Born terms**
input: axial vector constants
 D and F from hyperon beta decays

$$g_A = D + F = 1.26$$

$$\mathcal{L}_1^{MB} = \text{Tr} \left(\frac{D}{2} (\bar{B} \gamma^\mu \gamma_5 \{u_\mu, B\}) + \frac{F}{2} (\bar{B} \gamma^\mu \gamma_5 [u_\mu, B]) \right)$$

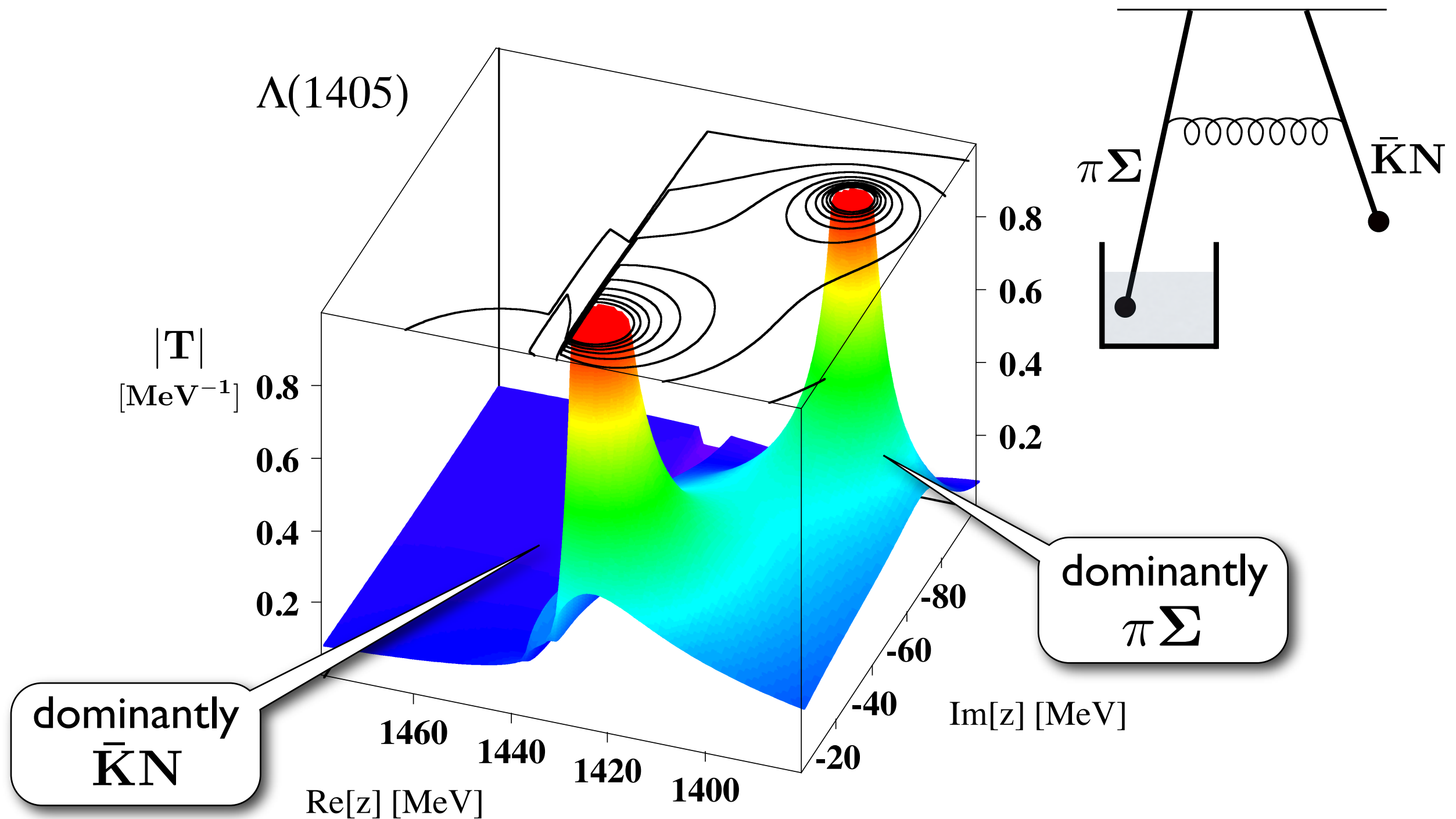


next-to-leading order (**NLO**)
input: 7 low-energy constants

$$\mathcal{O}(p^2)$$

$$\begin{aligned} \mathcal{L}_2^{MB} = & b_D \text{Tr}(\bar{B} \{\chi_+, B\}) + b_F \text{Tr}(\bar{B} [\chi_+, B]) + b_0 \text{Tr}(\bar{B} B) \text{Tr}(\chi_+) \\ & + d_1 \text{Tr}(\bar{B} \{u^\mu, [u_\mu, B]\}) + d_2 \text{Tr}(\bar{B} [u^\mu, [u_\mu, B]]) \\ & + d_3 \text{Tr}(\bar{B} u_\mu) \text{Tr}(u^\mu B) + d_4 \text{Tr}(\bar{B} B) \text{Tr}(u^\mu u_\mu), \end{aligned}$$

The TWO POLES scenario



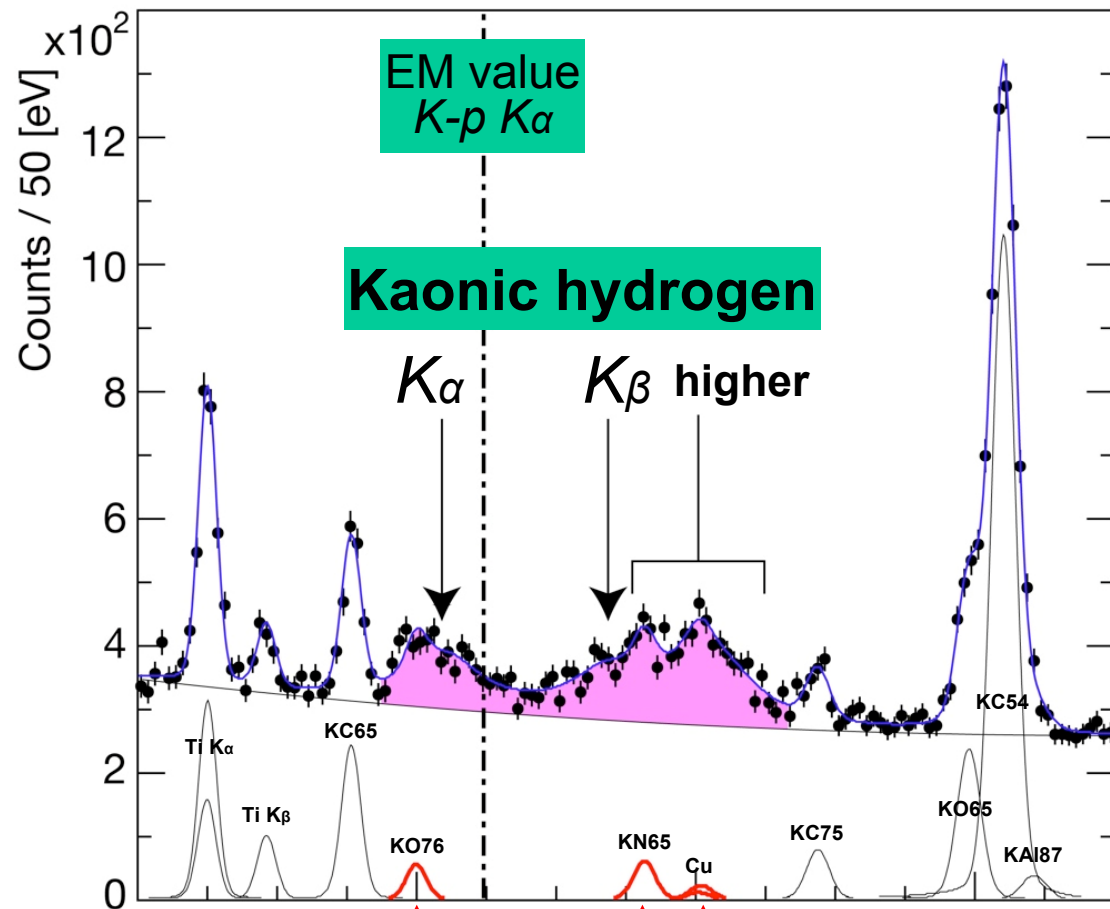
D.Jido et al., Nucl. Phys. A723 (2003) 205

T.Hyodo, W.W.: Phys. Rev. C 77 (2008) 03524

T.Hyodo, D.Jido : Prog. Part. Nucl. Phys. 67 (2012) 55

ANTIKAON - NUCLEON THRESHOLD PHYSICS and LOW-ENERGY OBSERVABLES

New kaonic hydrogen data



SIDDHARTA

M. Bazzi et al.: Phys. Lett. B 704 (2011) 113

strong interaction shift and width:

$$\Delta E = 283 \pm 36 (stat) \pm 6 (syst) \text{ eV}$$

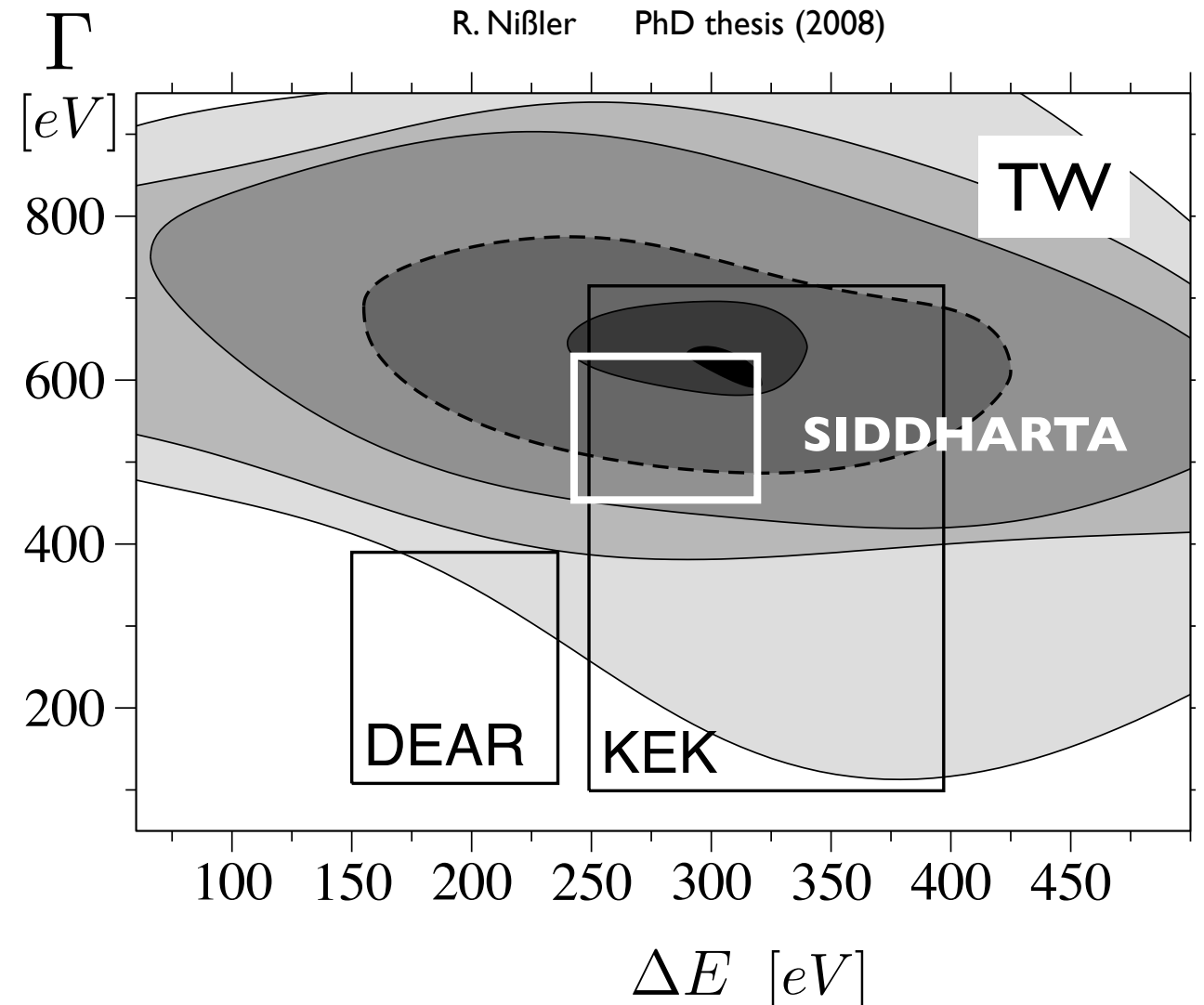
$$\Gamma = 541 \pm 89 (stat) \pm 22 (syst) \text{ eV}$$

Theory:
leading order
(Tomozawa - Weinberg)

B. Borasoy, R. Nißler, W.W. Eur. Phys. J. A25 (2005) 79

B. Borasoy, U.-G. Meißner, R. Nißler PRC74 (2006) 055201

R. Nißler PhD thesis (2008)



Improved constraints on chiral SU(3) dynamics from kaonic hydrogen

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^b*RIKEN Nishina Center, 2-1, Hirosawa, Wako, Saitama 351-0198, Japan*

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Abstract

A new improved study of K^- -proton interactions near threshold is performed using coupled-channels dynamics based on the next-to-leading order chiral SU(3) meson-baryon effective Lagrangian. Accurate constraints are now provided by new high-precision kaonic hydrogen measurements. Together with threshold branching ratios and scattering data, these constraints permit an updated analysis of the complex $\bar{K}N$ and $\pi\Sigma$ coupled-channels amplitudes and an improved determination of the K^-p scattering length, including uncertainty estimates.

arXiv:1109.3005

Physics Letters B 706 (2011) 63



UPDATED ANALYSIS of K^-p THRESHOLD PHYSICS

Y. Ikeda, T. Hyodo, W.W. Phys. Lett. B 706 (2011) 63 Nucl. Phys. A (2012), in print

- Chiral SU(3) coupled-channels dynamics
Tomozawa-Weinberg + **Born** terms + NLO

kaonic hydrogen shift & width	theory (NLO)	exp.
ΔE (eV)	306	$283 \pm 36 \pm 6$
Γ (eV)	591	$541 \pm 89 \pm 22$
threshold branching ratios		(SIDDHARTA)
$\frac{\Gamma(K^-p \rightarrow \pi^+\Sigma^-)}{\Gamma(K^-p \rightarrow \pi^-\Sigma^+)}$	2.37	2.36 ± 0.04
$\frac{\Gamma(K^-p \rightarrow \pi^+\Sigma^-, \pi^-\Sigma^+)}{\Gamma(K^-p \rightarrow \text{all inelastic channels})}$	0.66	0.66 ± 0.01
$\frac{\Gamma(K^-p \rightarrow \pi^0\Lambda)}{\Gamma(K^-p \rightarrow \text{neutral states})}$	0.19	0.19 ± 0.02
scattering length (fm)	$\text{Re } a(K^-p) = -0.65 \pm 0.10$	$\text{Im } a(K^-p) = 0.81 \pm 0.15$

best fit achieved with $\chi^2/d.o.f. \simeq 0.9$



UPDATED ANALYSIS of K^-p THRESHOLD PHYSICS with SIDDHARTA constraints

Y. Ikeda, T. Hyodo, W.W.

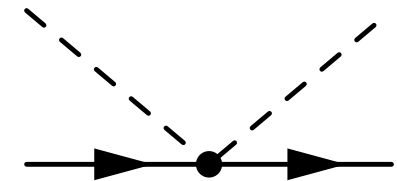
Phys. Lett. B 706 (2011) 63

Nucl. Phys. A (2012), in print

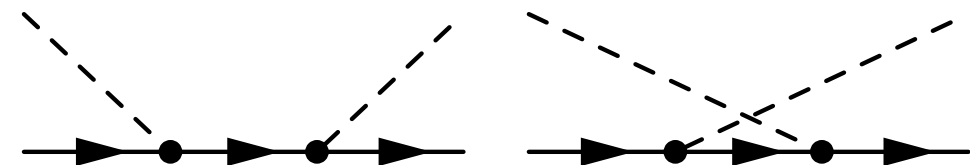
- Non-trivial result:
best NLO fit prefers **physical** values of **decay constants**:

f_K (MeV)	110.0	$(f_\pi = 92.4 \text{ MeV})$
f_η (MeV)	118.8	

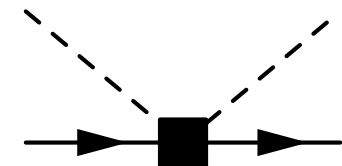
- Tomozawa-Weinberg** terms **dominant**



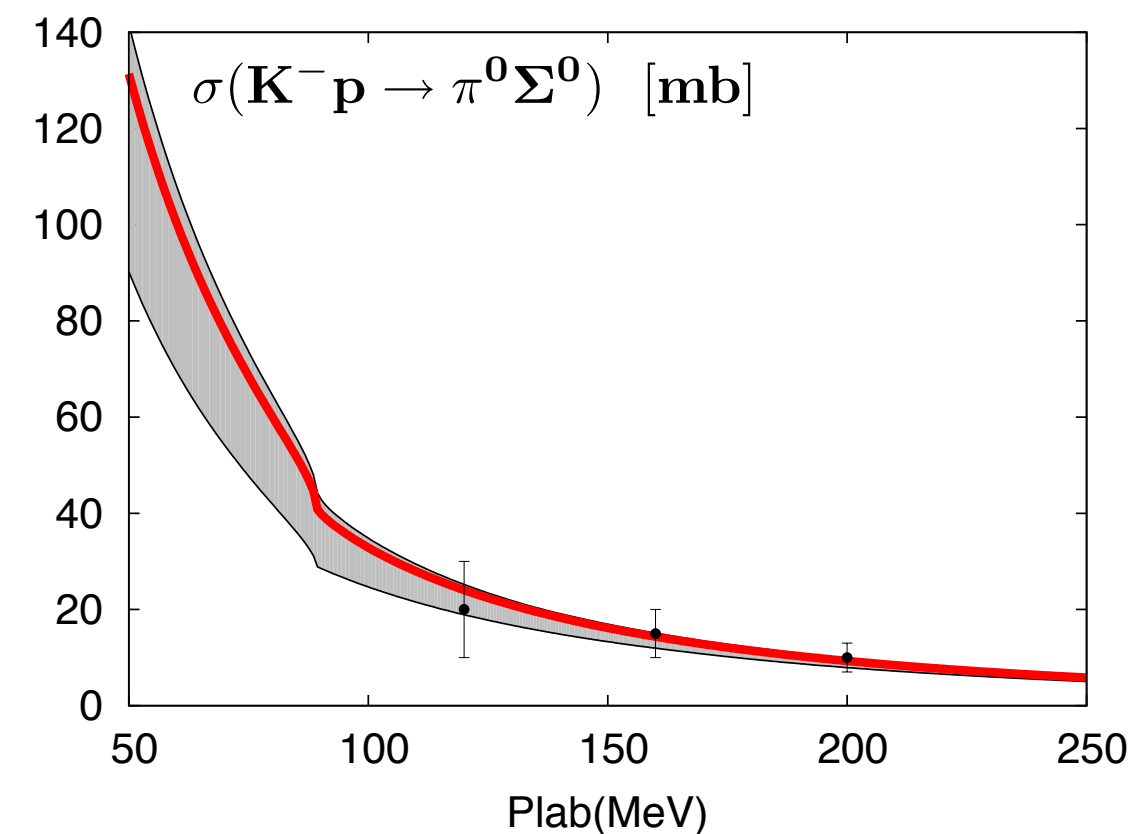
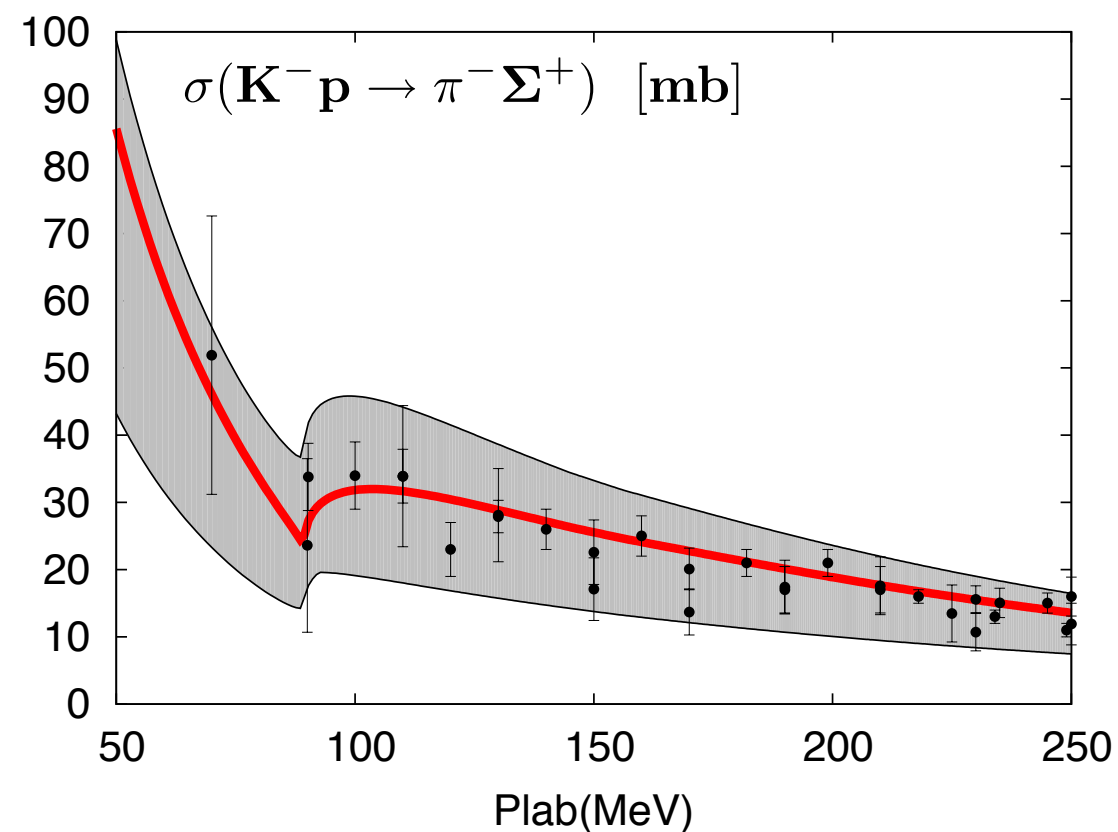
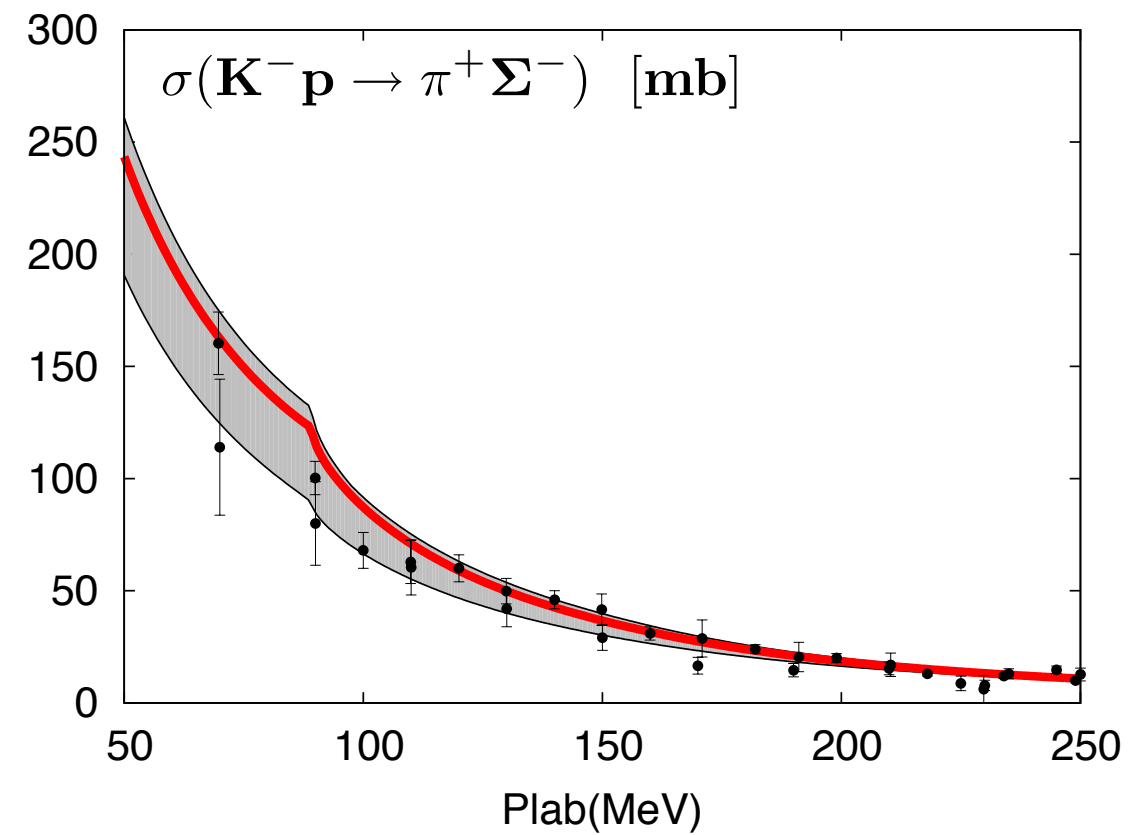
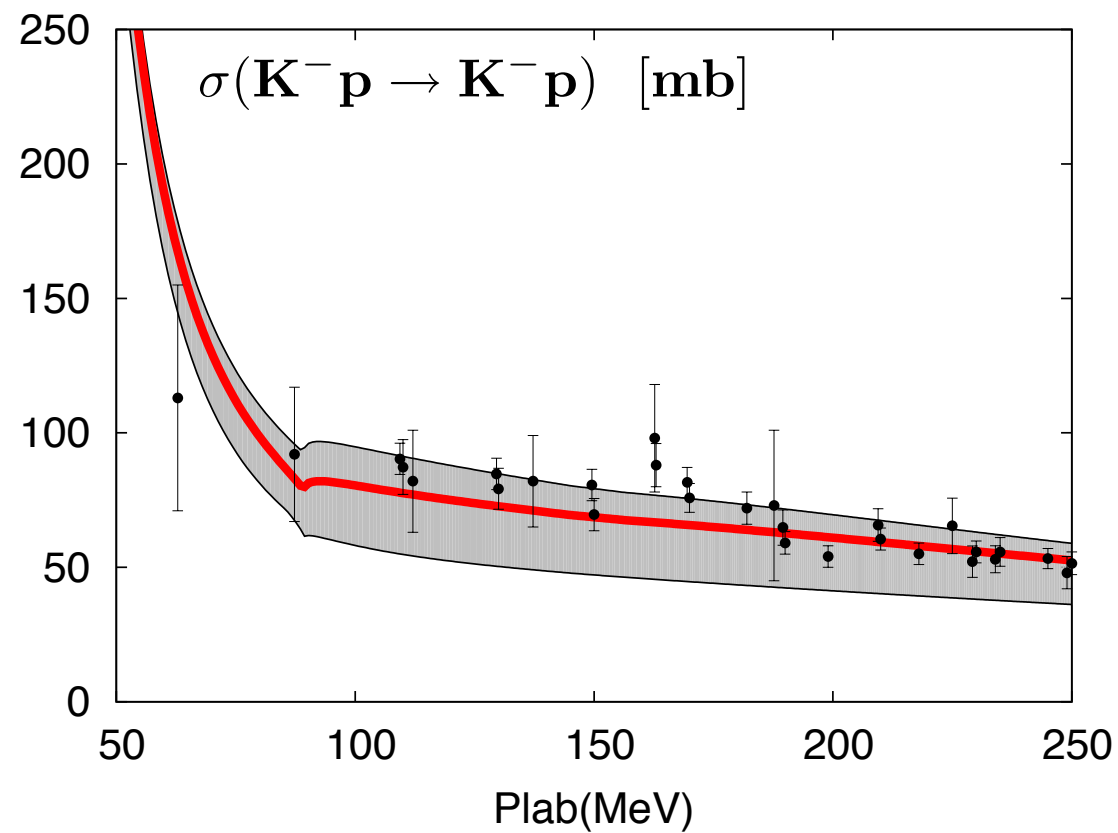
- Born** terms **significant**



- NLO** parameters are non-negligible but **small**



UPDATED ANALYSIS of K^-p LOW-ENERGY CROSS SECTIONS

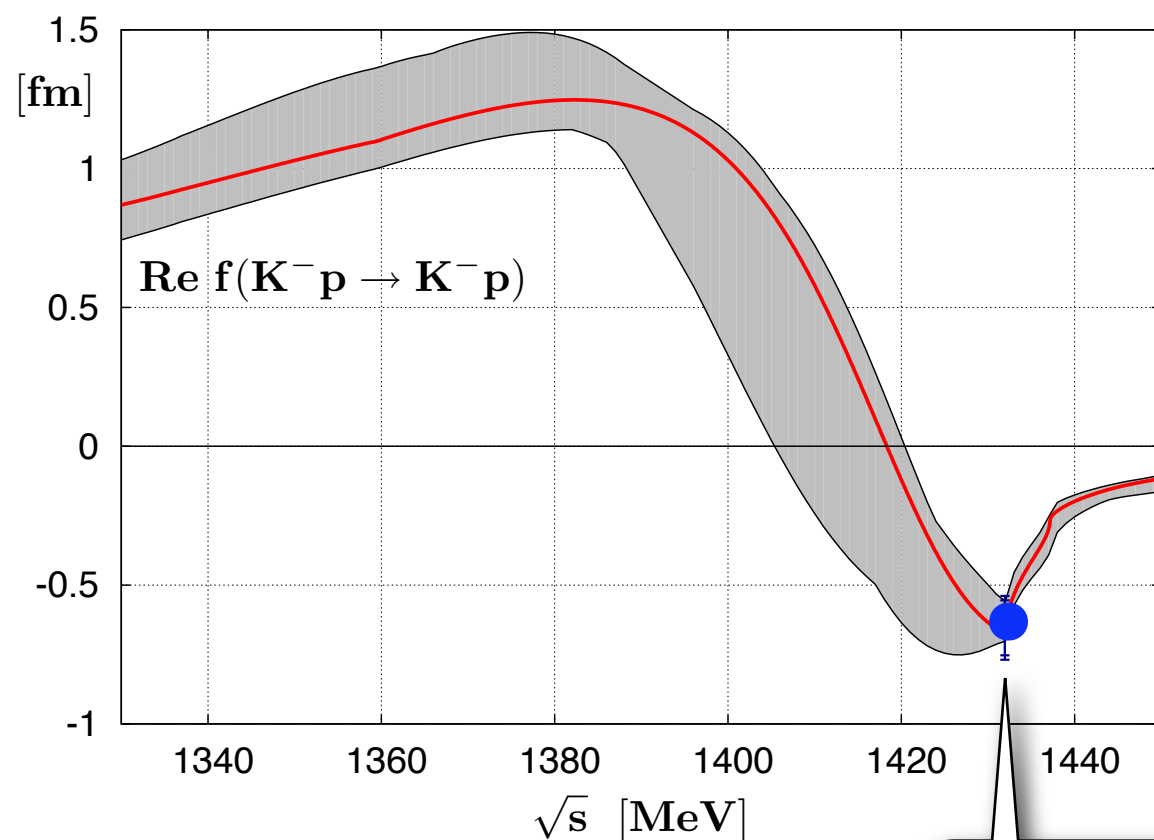


$K^- p$ SCATTERING AMPLITUDE

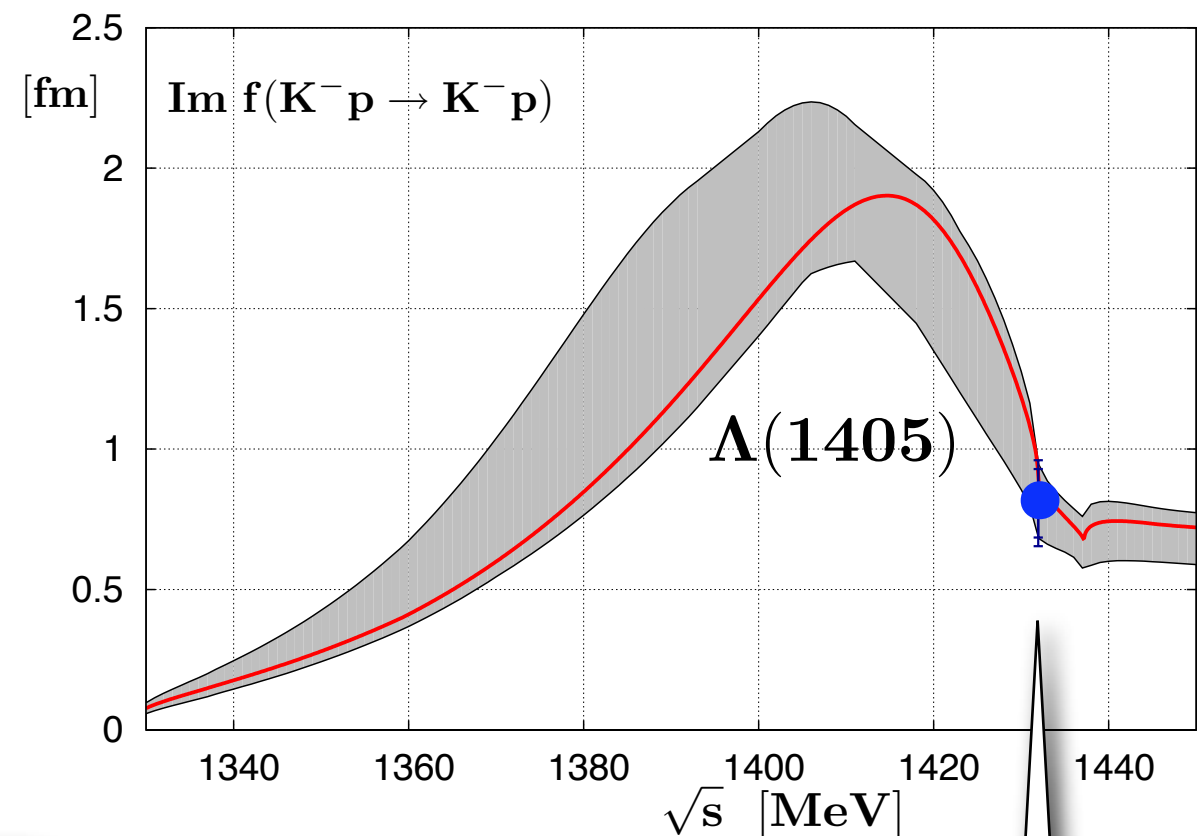
$$f(K^- p) = \frac{1}{2} [f_{\bar{K}N}(I=0) + f_{\bar{K}N}(I=1)]$$

- threshold region and subthreshold extrapolation:

$\Lambda(1405)$: $\bar{K}N$ ($I=0$) quasibound state embedded in the $\pi\Sigma$ continuum



$\text{Re } a(K^- p)$



$\text{Im } a(K^- p)$

- complex scattering length (including Coulomb corrections)

$$\text{Re } a(K^- p) = -0.65 \pm 0.10 \text{ fm}$$

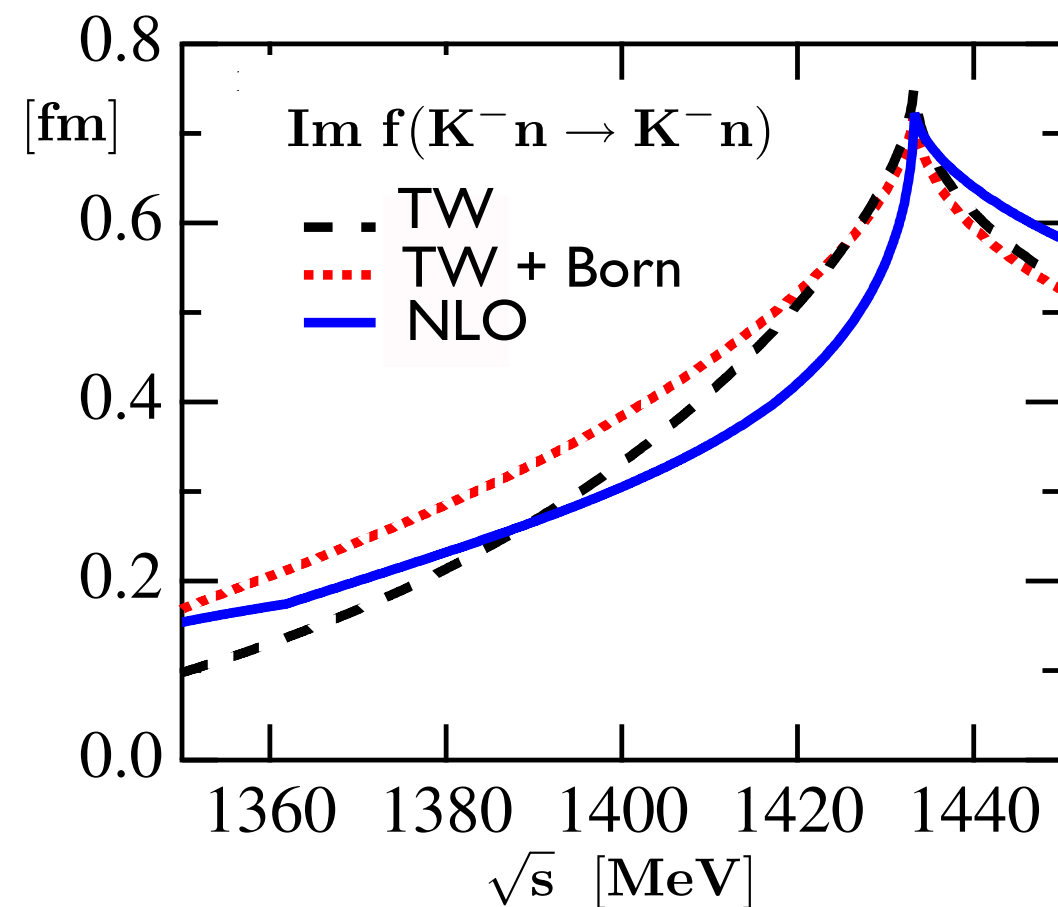
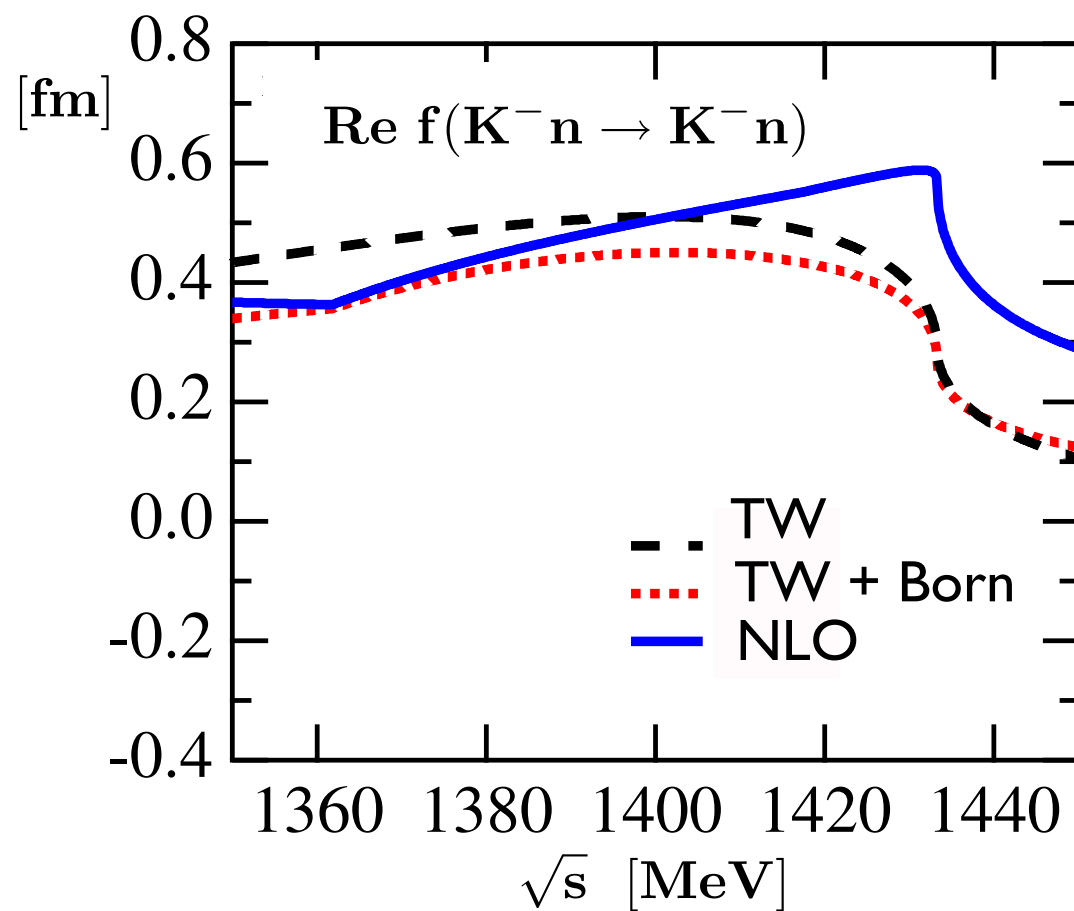
$$\text{Im } a(K^- p) = 0.81 \pm 0.15 \text{ fm}$$



K^-n SCATTERING AMPLITUDE

$$f(K^-n) = f_{\bar{K}N}(I = 1)$$

- threshold region and subthreshold extrapolation



- complex scattering length

$$\text{Re } a(K^-n) = 0.57^{+0.1}_{-0.2} \text{ fm}$$

$$\text{Im } a(K^-n) = 0.72^{+0.3}_{-0.4} \text{ fm}$$

Implications & Comments

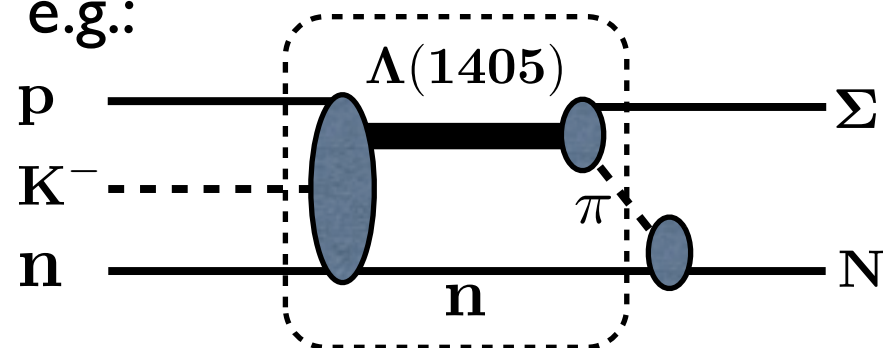
- $K^- p$ scattering length more accurately determined than $K^- n$ (SIDDHARTA constraints vs. uncertainties in $I = 1$ channels)
- **Kaonic deuterium** measurements important for providing further constraints on $K^- n$ interaction

- $B = 2$ systems - key issue:

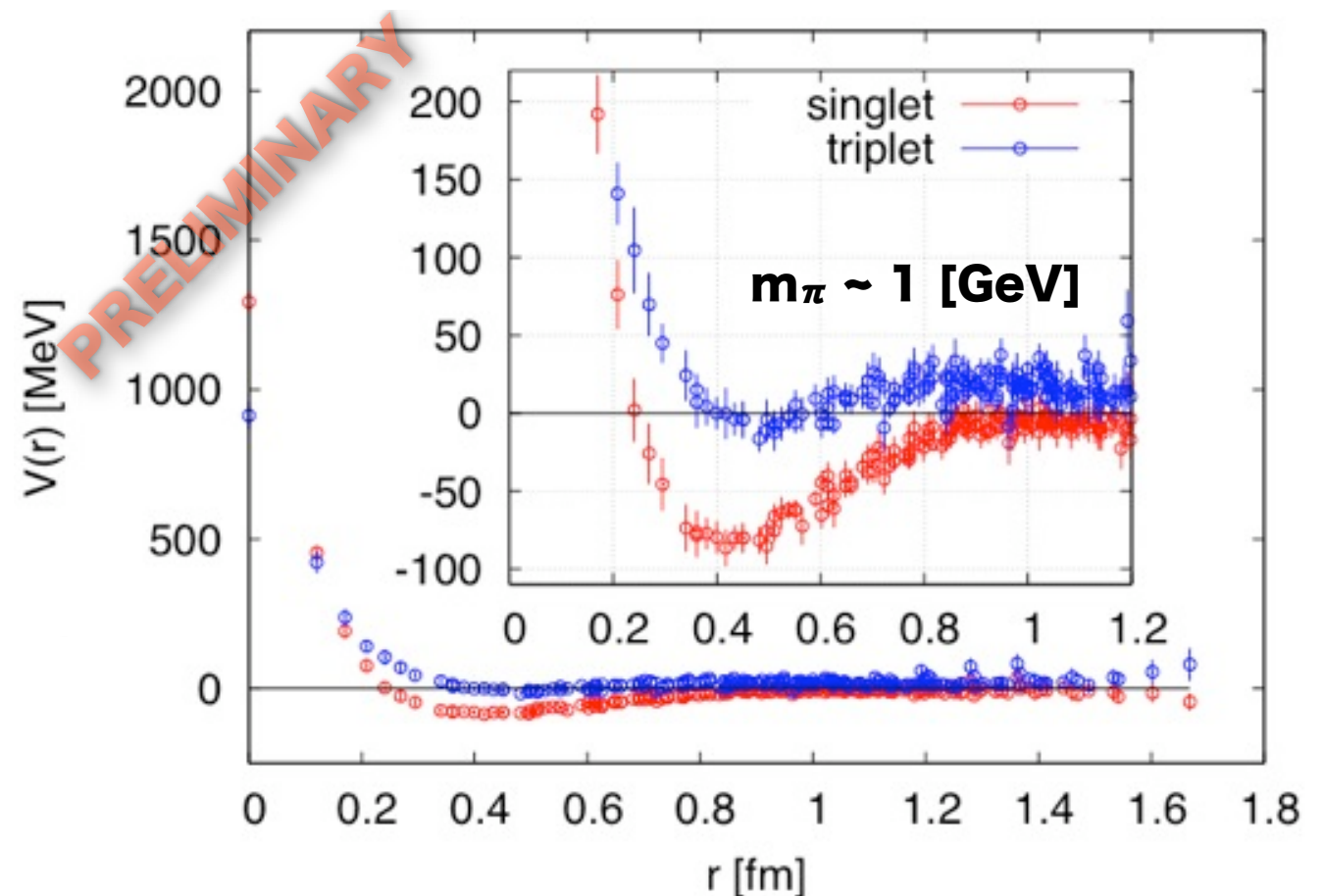


absorption into non-mesonic
hyperon - nucleon final states

e.g.:



Repulsive short-distance
 $\Lambda^*(uds) N$ **interaction ?**



Lattice QCD

Y. Ikeda et al.
(HAL QCD collaboration)



PART 2.

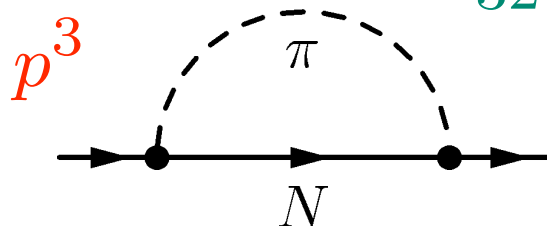
The **SIGMA TERM** and **STRANGENESS** in the **NUCLEON**

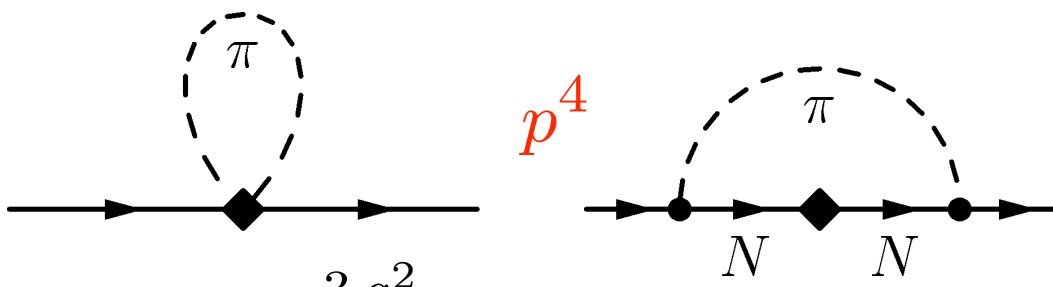
- **Mass** and **scalar density of quarks** in the **nucleon**
- Pion - nucleon **phase shifts** and **sigma term**
- Chiral extrapolations and **Lattice QCD**
- Implications: **chiral condensate** in a **nuclear medium**



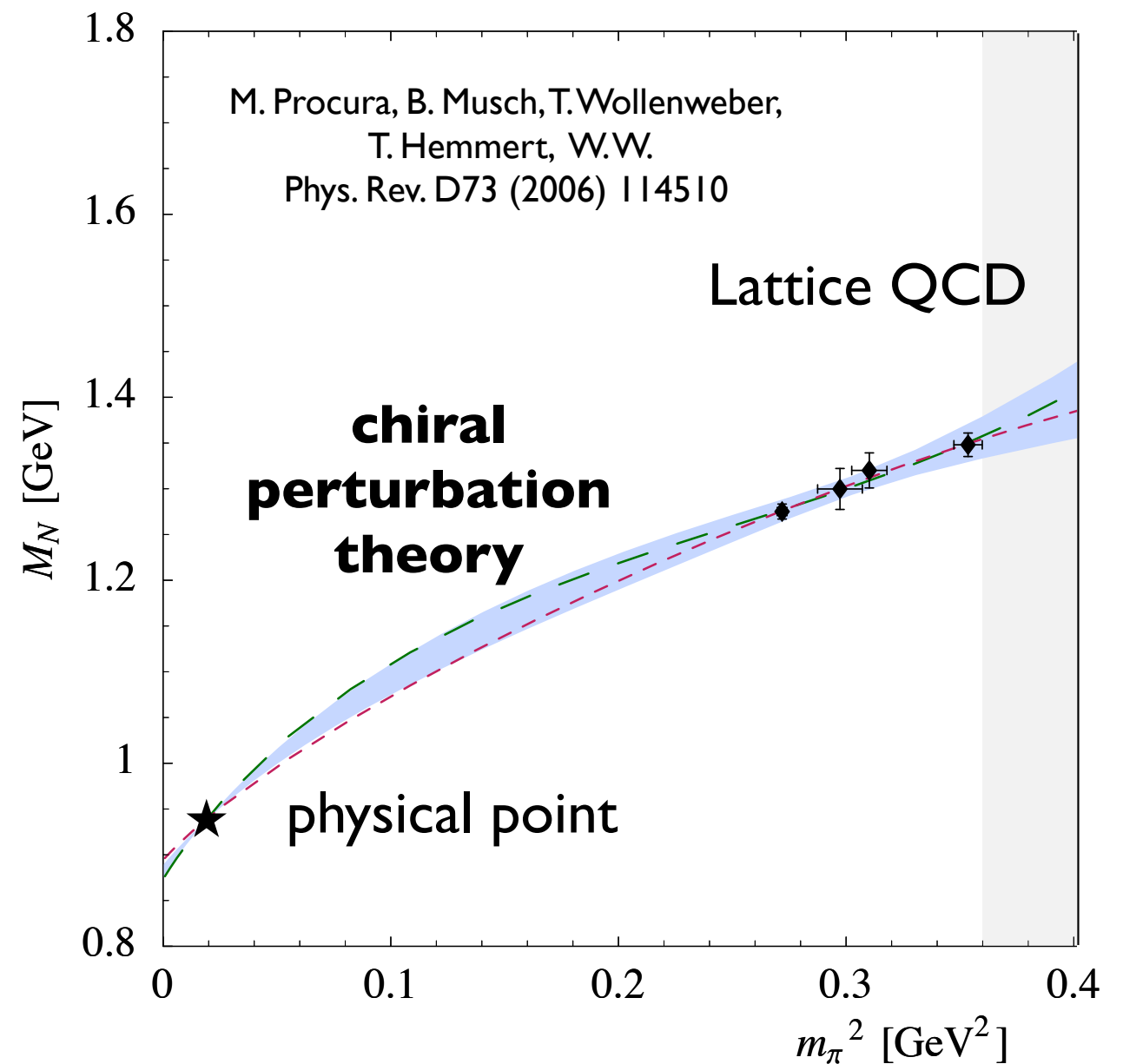
MASS of the NUCLEON: LATTICE QCD + CHIRAL PERTURBATION THEORY

$$M_N = \langle N | \frac{\beta(g)}{2g} \text{Tr}(G_{\mu\nu} G^{\mu\nu}) + \sum_i m_i \bar{q}_i q_i | N \rangle = M_0 + \Delta M(m_\pi)$$

$$M_N = M_0 - 4c_1 m_\pi^2 - \frac{3g_A^2}{32\pi f_\pi^2} m_\pi^3$$


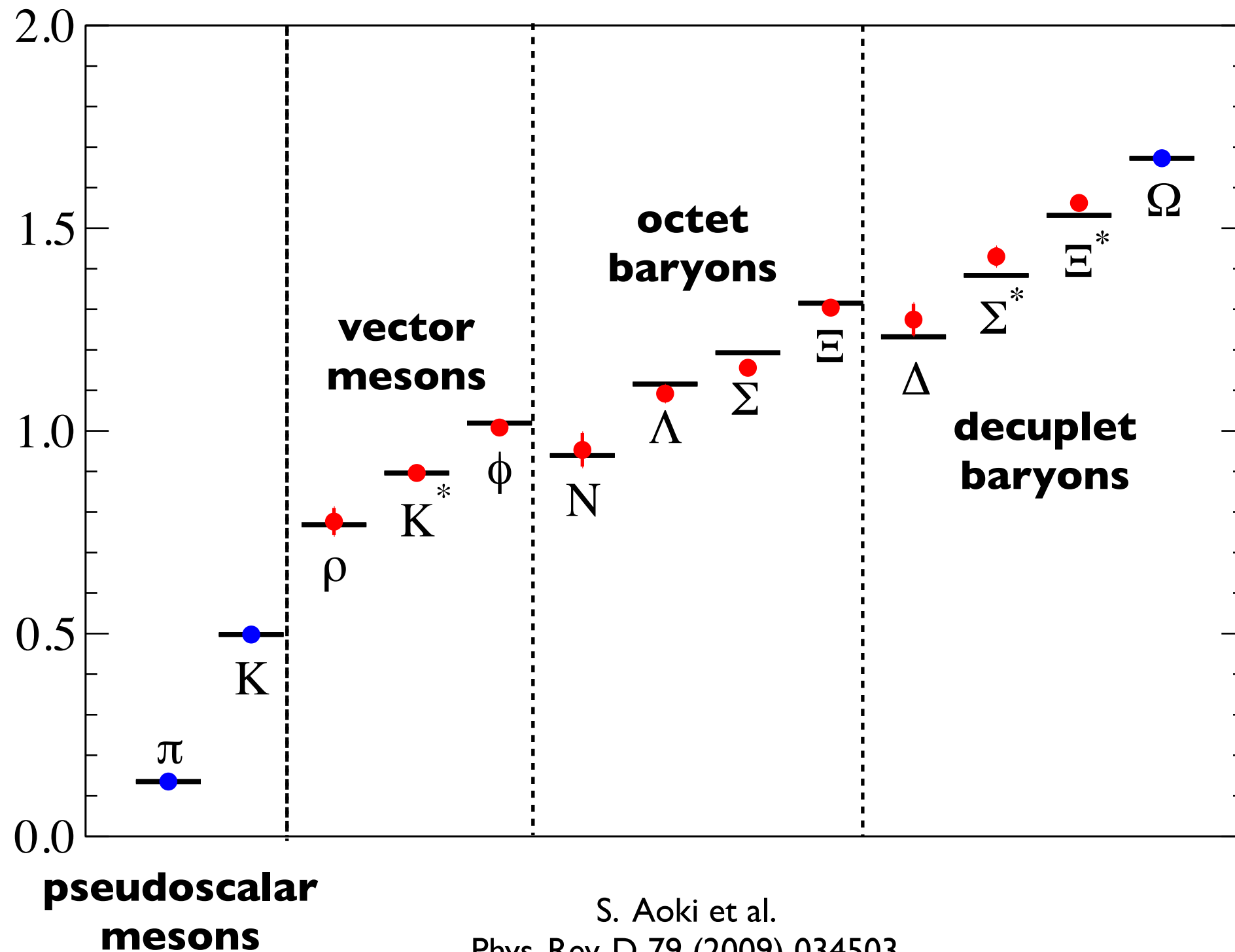
$$+ \left[4e_1^r(\lambda) + \frac{3c_2}{128\pi^2 f_\pi^2} - \frac{3g_A^2}{64\pi^2 f_\pi^2} M_0 \right. \\ \left. - \frac{3}{32\pi^2 f_\pi^2} \left(\frac{g_A^2}{M_0} - 8c_1 + c_2 + 4c_3 \right) \ln \frac{m_\pi}{\lambda} \right] m_\pi^4$$


$$+ \frac{3g_A^2}{256\pi f_\pi^2 M_0^2} m_\pi^5 + \mathcal{O}(m_\pi^6)$$



HADRON MASSES from LATTICE QCD

- Full QCD with 2+1 flavors and physical quark masses



S. Aoki et al.
Phys. Rev. D 79 (2009) 034503
Phys. Rev. D 81 (2010) 074503



SIGMA TERMS

- Pion-nucleon **sigma term**:

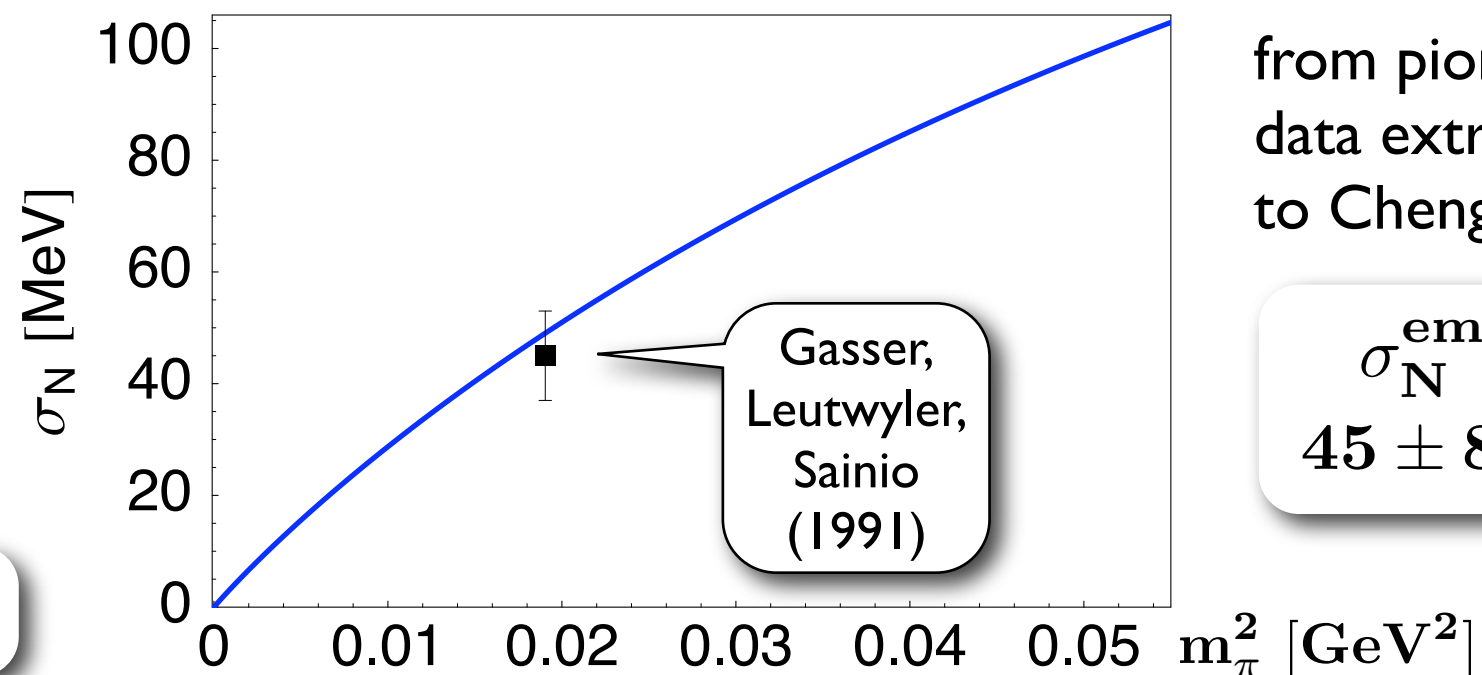
$$\sigma_N = \bar{m} \langle N | \bar{u}u + \bar{d}d | N \rangle = \bar{m} \frac{\partial M_N}{\partial \bar{m}} \simeq m_\pi^2 \frac{\partial M_N}{\partial m_\pi^2} \quad \left(\bar{m} = \frac{m_u + m_d}{2} \right)$$

- Previous status:

from chiral
interpolation using
older lattice data

M. Procura et al.
Phys. Rev.
D73 (2006) 114510

$$\sigma_N = 49 \pm 6 \text{ MeV}$$



from pion-nucleon
data extrapolated
to Cheng-Dashen p.

$$\sigma_N^{\text{emp}} = 45 \pm 8 \text{ MeV}$$

- Strangeness content:**

$$\sigma_N = \frac{\langle N | \bar{u}u + \bar{d}d - 2\bar{s}s | N \rangle}{1 - y}$$

$$y = \frac{2\langle N | \bar{s}s | N \rangle}{\langle N | \bar{u}u + \bar{d}d | N \rangle} \simeq 1 - \frac{\bar{m}}{m_s} \frac{M_\Xi + M_\Sigma - 2M_N}{\sigma_N} \sim 0.2 - 0.3$$

... but with large uncertainties

assuming flavour SU(3) symmetry

B. Borasoy, U.-G. Meißner
Ann. of Phys. 254 (1997) 192



SIGMA TERMS ... more recent

- Combined analysis of baryon octet (and decuplet)



$$\sigma_N = 47 \text{ (9)(1)(3) MeV}$$

\uparrow (statist.) \uparrow (lattice artifacts) \nwarrow (chiral extrap.)



consistent with earlier results
and with phenomenology

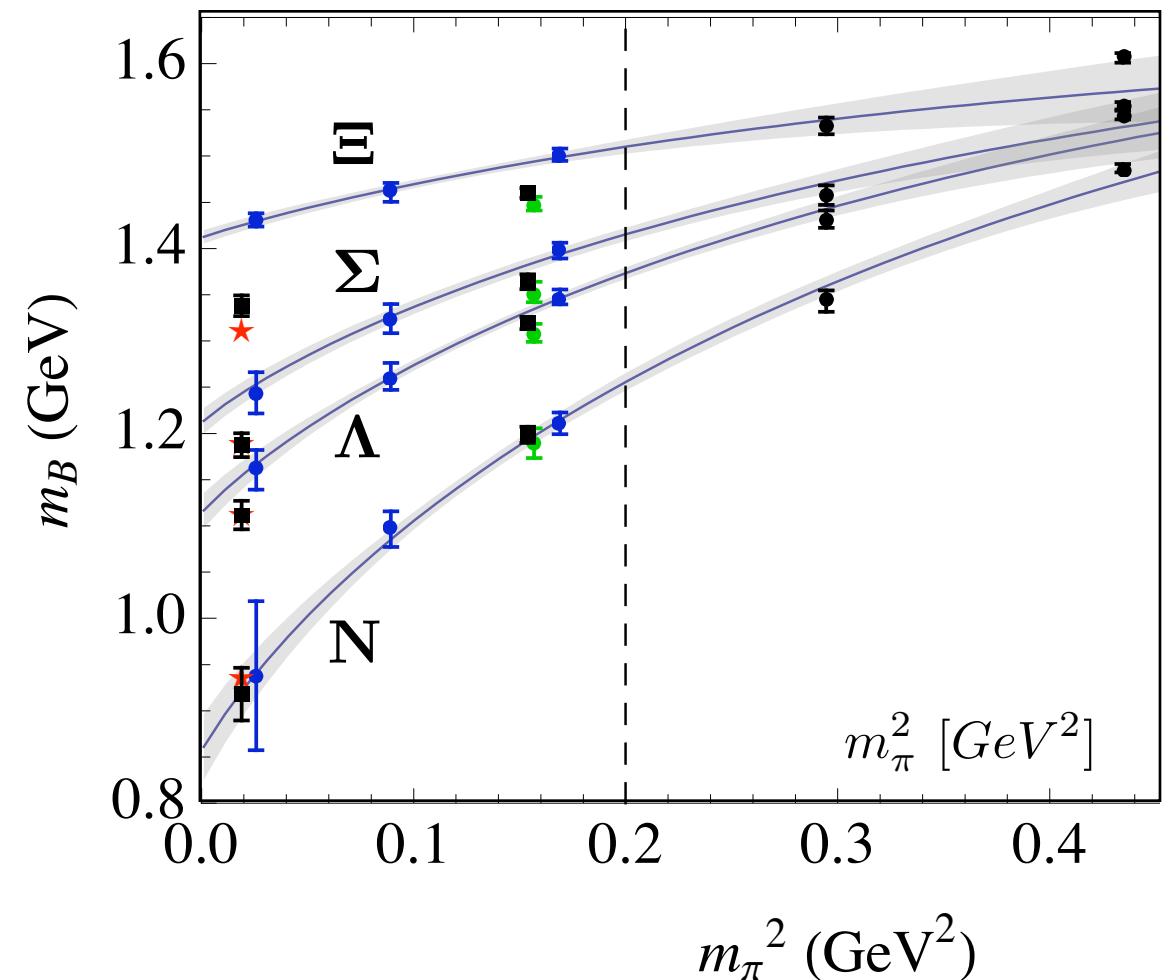
- Strange quark contribution**

$$\sigma_{Ns} = m_s \langle N | \bar{s}s | N \rangle = m_s \frac{\partial M_N}{\partial m_s}$$



$$\sigma_{Ns} = 31 \text{ (15)(4)(2) MeV}$$

R.D.Young, A.W.Thomas
Phys. Rev. D81 (2010) 014503



much smaller than previously expected ! $y \sim (5 \pm 4) \cdot 10^{-2}$



SIGMA TERM ... contd.

- M. M. Pavan, I. I. Strakovsky,
R. L. Workman, R. A. Arndt,
PiN Newslett. 16, 110-115 (2002)

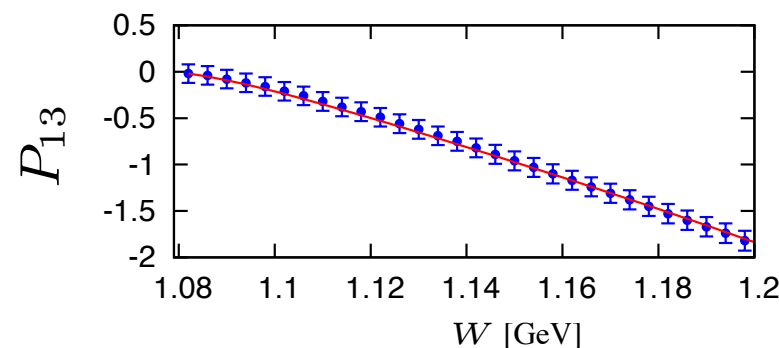
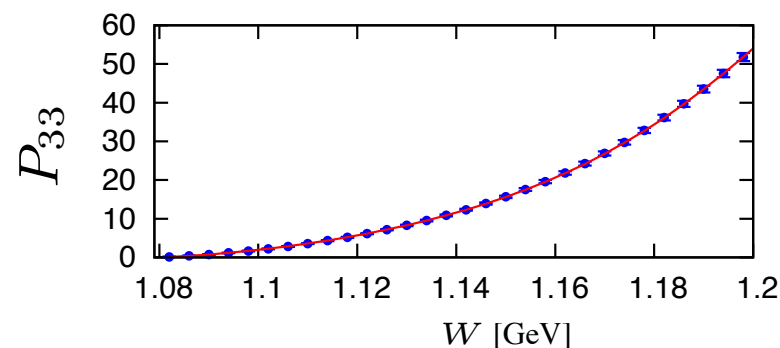
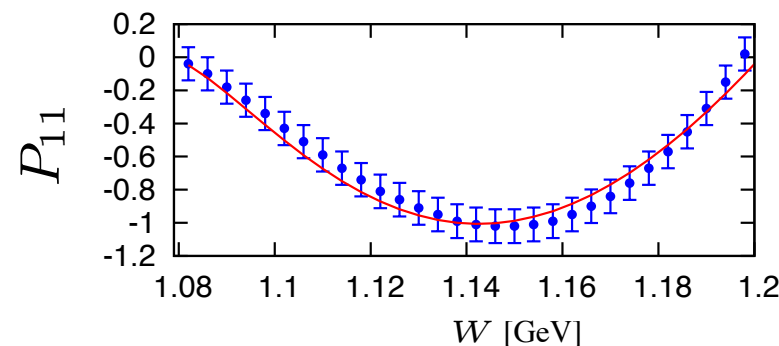
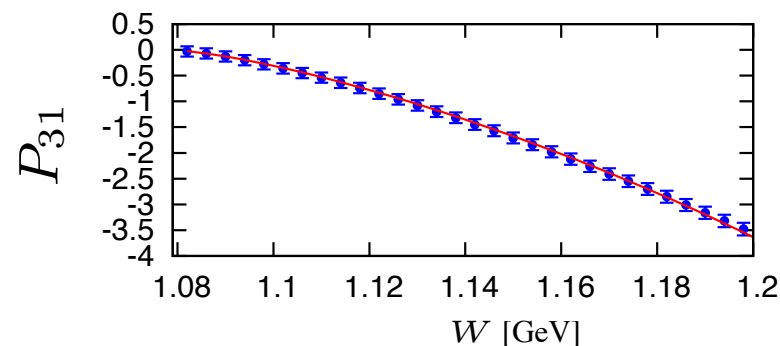
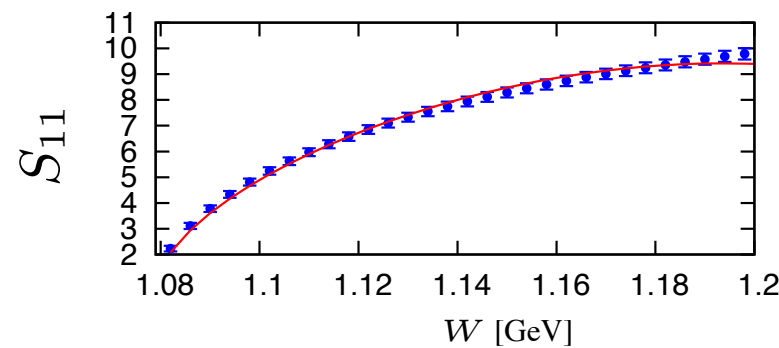
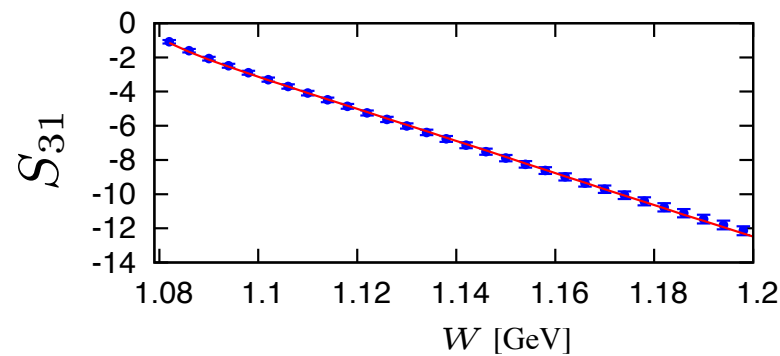
updated pion-nucleon phase shift analysis:

$$\sigma_N = 64 \pm 7 \text{ MeV} !$$

- covariant chiral perturbation theory with explicit $\Delta(1232)$

J.M.Alarcón, J. Martin Camalich, J.A. Oller; arXiv:1110.3797 [hep-ph]

phase
shift
[deg]



fix pion-nucleon
low-energy constants



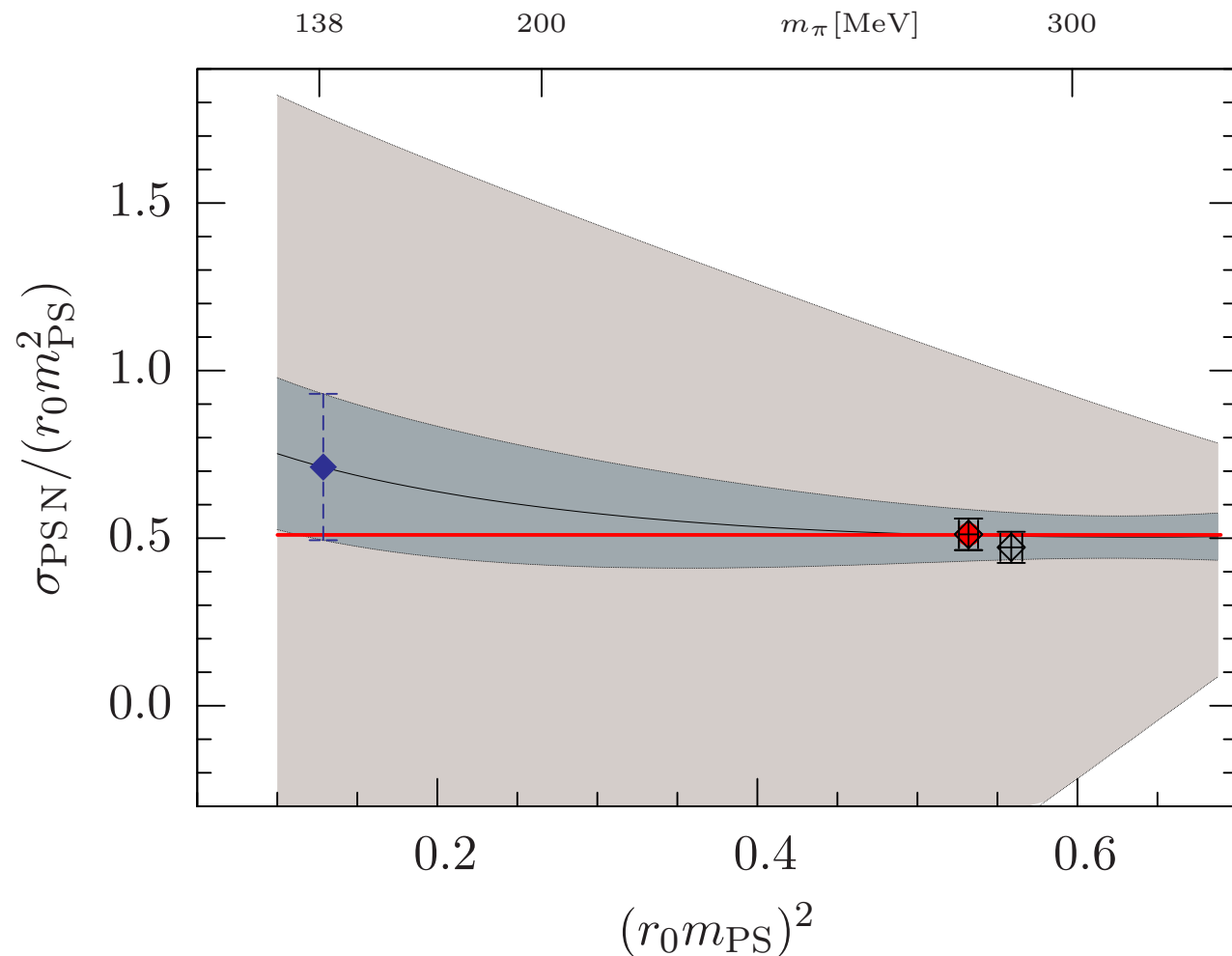
deduce (large)
sigma term:

$$\sigma_N = 59 \pm 7 \text{ MeV}$$



SIGMA TERM ... contd.

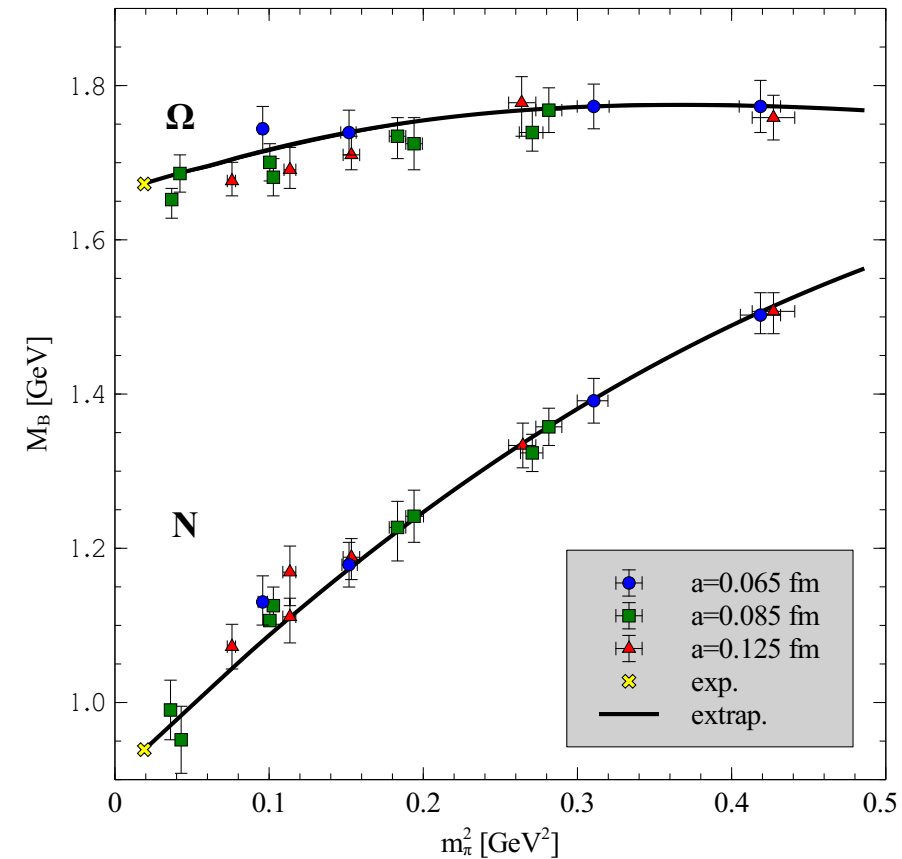
- Update of lattice QCD results and chiral extrapolations



G. Bali et al. (QCDSF) ; arXiv:1110.3797 [hep-ph]

$$\sigma_{\text{N}} = 38 \pm 12 \text{ MeV}$$

- Very small scalar strange sea component in the nucleon



lattice QCD
S. Dürer et al. (BMW)
Science 322 (2008) 1224

A. Simke, MFM Lutz ; arXiv:1111.0238 [hep-ph]

- Covariant $\text{SU}(3) \times \text{SU}(3)$ chiral perturbation theory to NNNLO with octet and decuplet baryons

$$\sigma_{\text{N}} \sim 40 \text{ MeV}$$

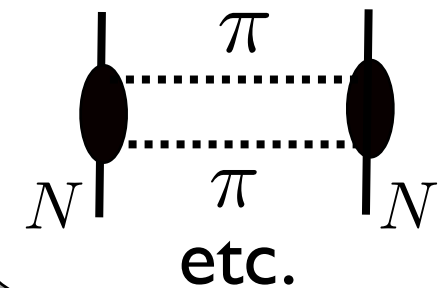
CHIRAL CONDENSATE at finite BARYON DENSITY

- Chiral (quark) condensate $\langle \bar{q}q \rangle$: $m_\pi^2 f_\pi^2 = -2 m_q \langle \bar{q}q \rangle$
Order parameter of spontaneously broken chiral symmetry in QCD
- Hellmann - Feynman theorem: $\langle \Psi | \bar{q}q | \Psi \rangle = \langle \Psi | \frac{\partial \mathcal{H}_{\text{QCD}}}{\partial m_q} | \Psi \rangle = \frac{\partial \mathcal{E}(m_q; \rho)}{\partial m_q}$

sigma term

$$m_q \frac{\partial M_N}{\partial m_q}$$

**in-medium
chiral
effective
field theory**



$$\frac{\langle \bar{q}q \rangle_\rho}{\langle \bar{q}q \rangle_0} = 1 - \frac{\rho}{f_\pi^2} \left[\frac{\sigma_N}{m_\pi^2} \left(1 - \frac{3 p_F^2}{10 M_N^2} + \dots \right) + \frac{\partial}{\partial m_\pi^2} \left(\frac{E_{\text{int}}(p_F)}{A} \right) \right]$$

(free) Fermi gas
of nucleons

nuclear interactions
(dependence on pion mass)



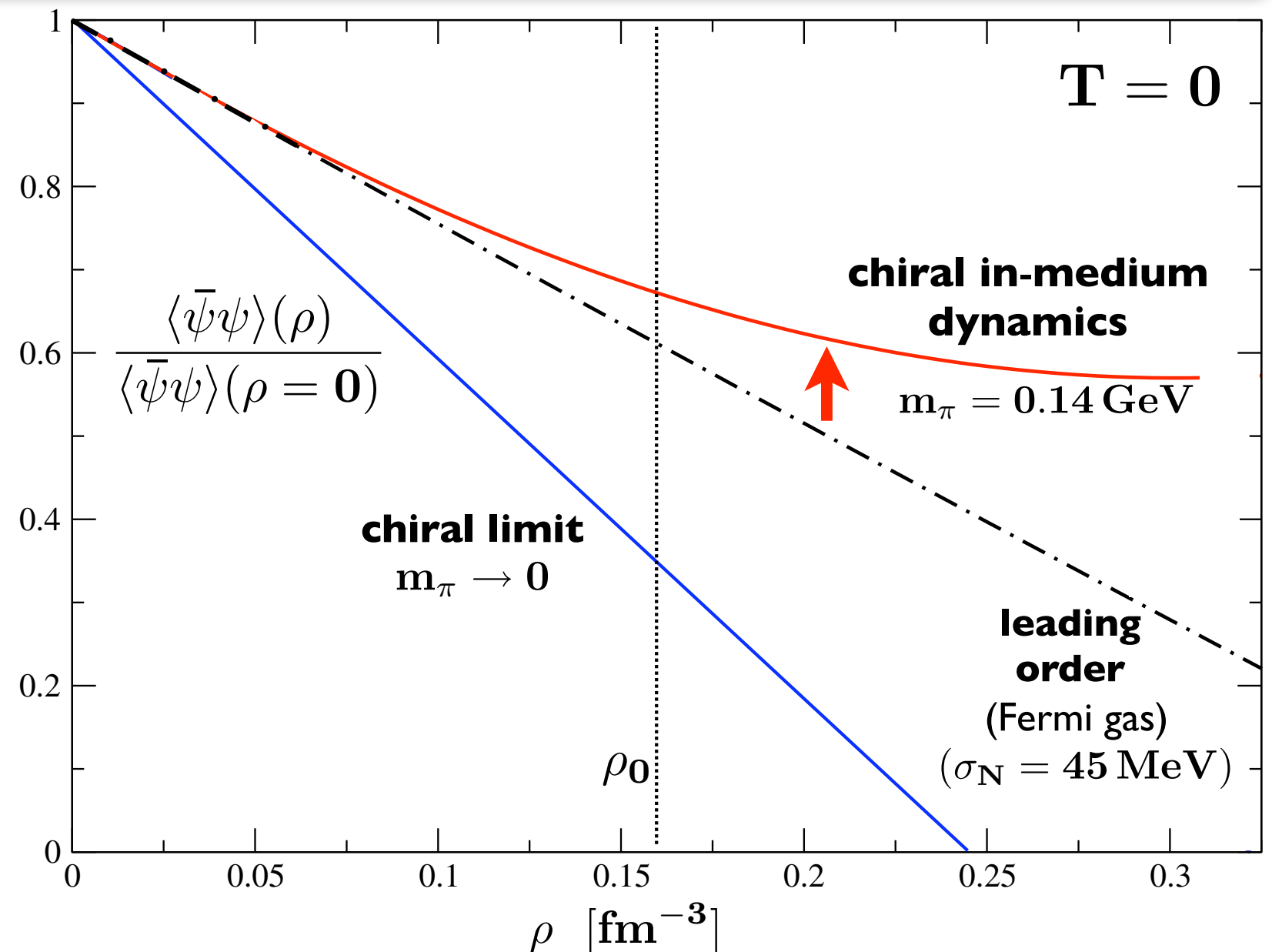
why the **SIGMA TERM** is so important: DENSITY DEPENDENCE of **CHIRAL CONDENSATE**

In-medium Chiral Effective Field Theory

(NLO 3-loop)

constrained by
**realistic nuclear
equation of state**

N. Kaiser, Ph. de Homont, W.W.
Phys. Rev. C 77 (2008) 025204



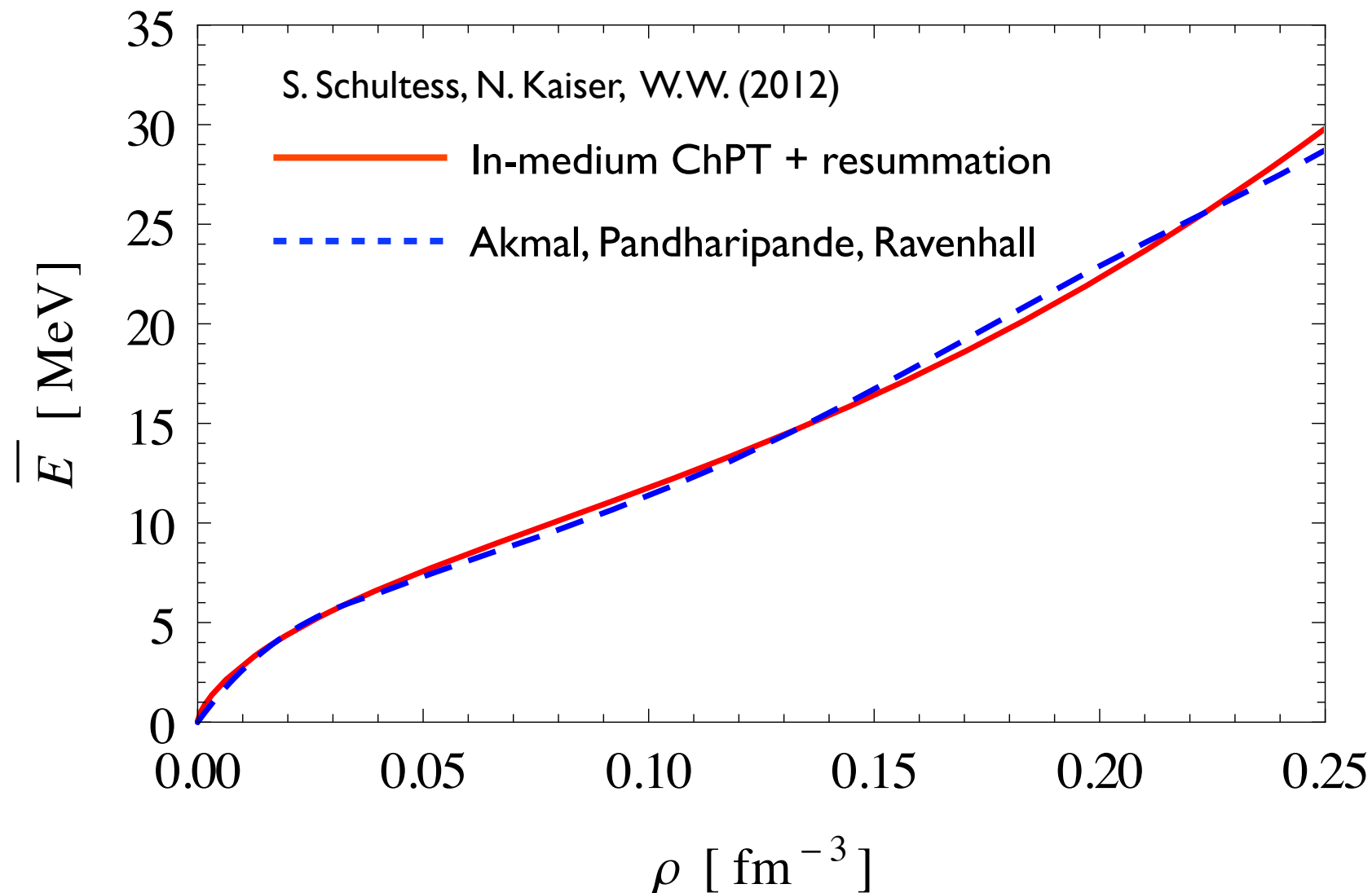
- Substantial **change** of **symmetry breaking scenario**
between chiral limit $m_q = 0$ and physical quark mass $m_q \sim 5 \text{ MeV}$
- Nuclear Physics** would be **very different** in the **chiral limit** !



NEUTRON MATTER

- **In-medium chiral effective field theory (3-loop)** with resummation of short distance contact terms (large nn scattering length, $a_s = 19$ fm)

N. Kaiser, Nucl. Phys.A 860 (2011) 370



- perfect agreement with sophisticated many-body calculations



Outlook:

**New Constraints
from
NEUTRON STARS**



A two-solar-mass neutron star measured using Shapiro delay

P. B. Demorest¹, T. Pennucci², S. M. Ransom¹, M. S. E. Roberts³ & J. W. T. Hessels^{4,5}

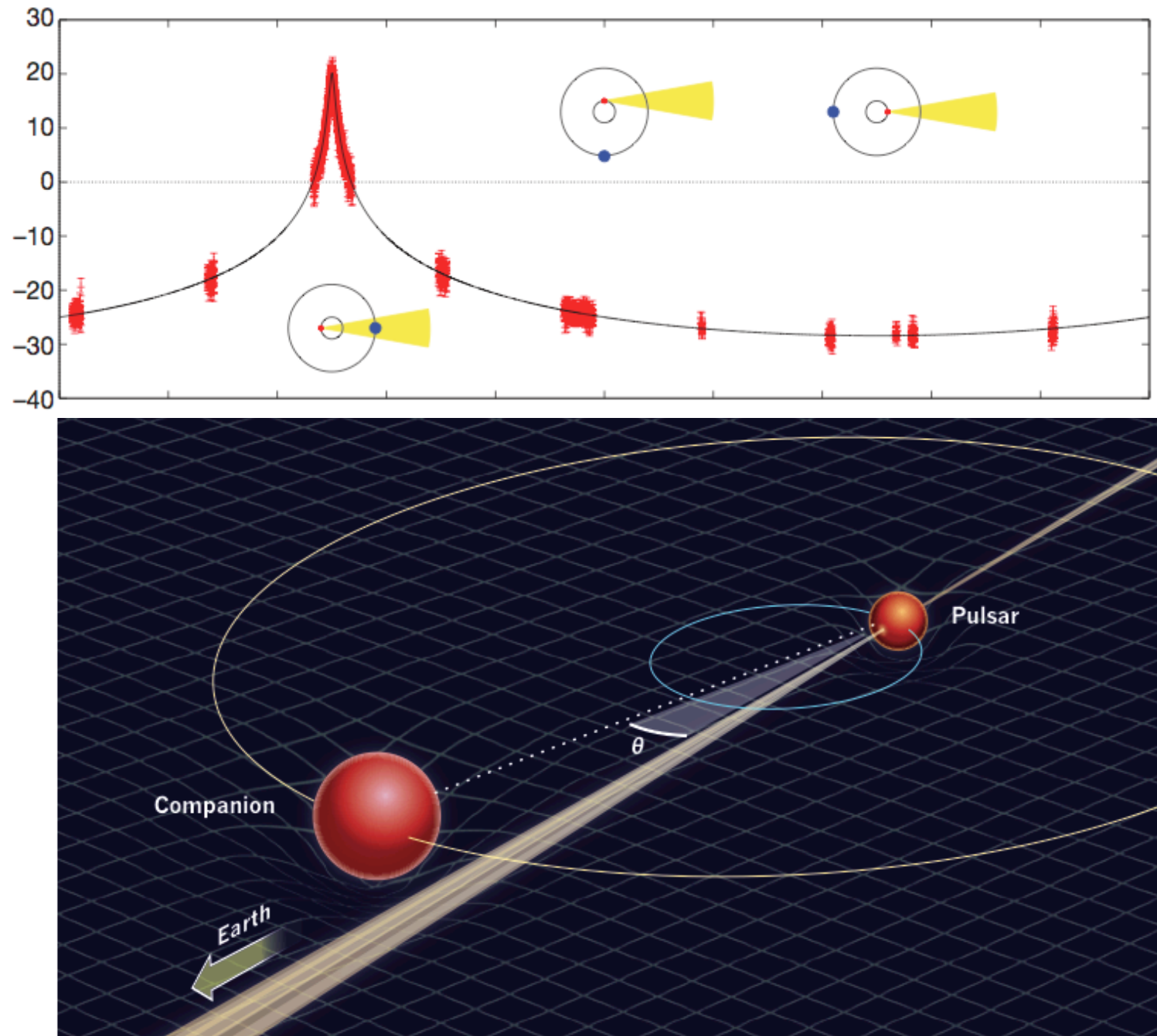
Nature, Oct. 28, 2010

direct measurement of
neutron star mass from
increase in travel time
near companion

J1614-2230

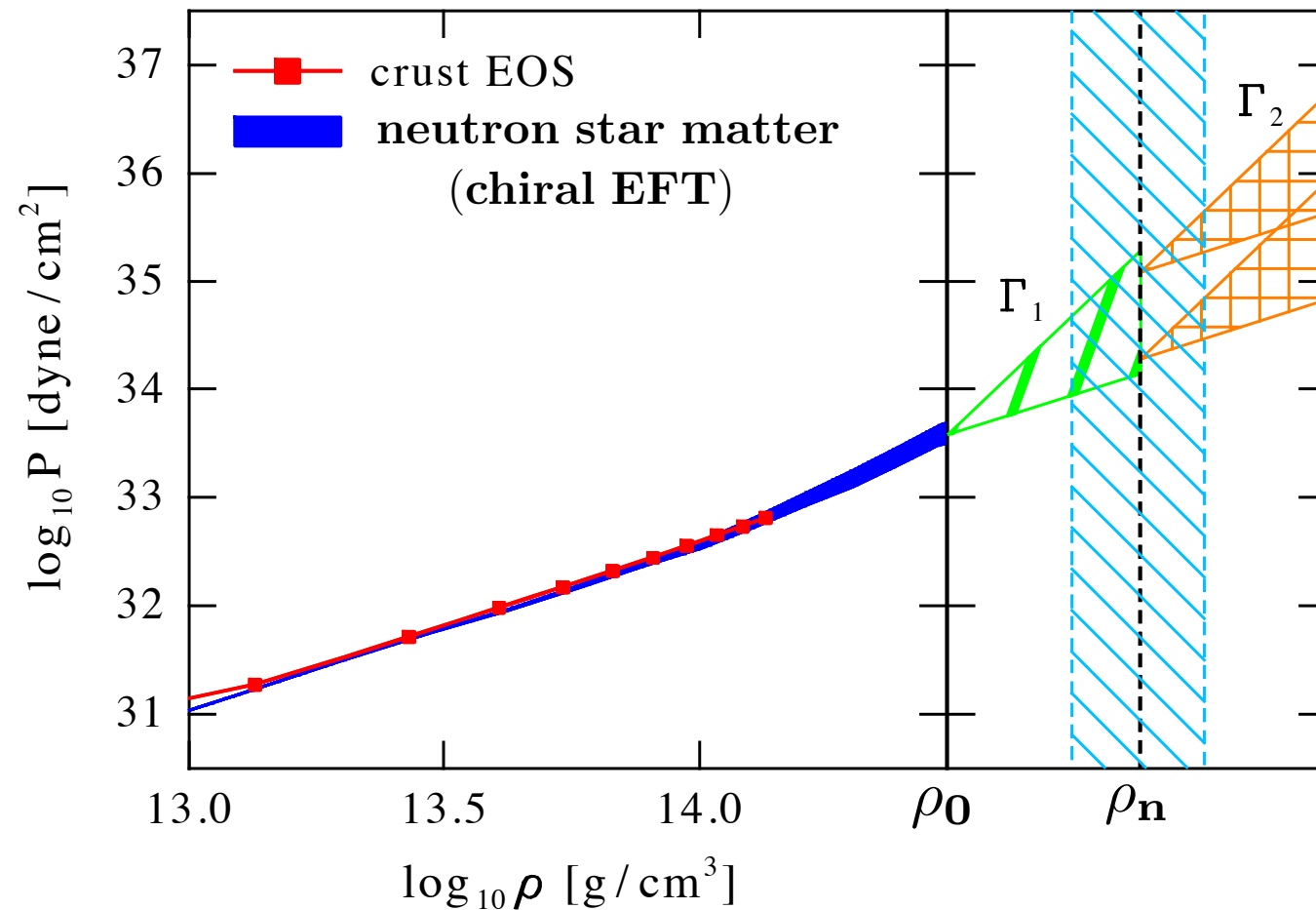
most edge-on binary
pulsar known (89.17°)
+ massive white dwarf
companion ($0.5 M_{\text{sun}}$)

heaviest neutron star
with $1.97 \pm 0.04 M_{\text{sun}}$



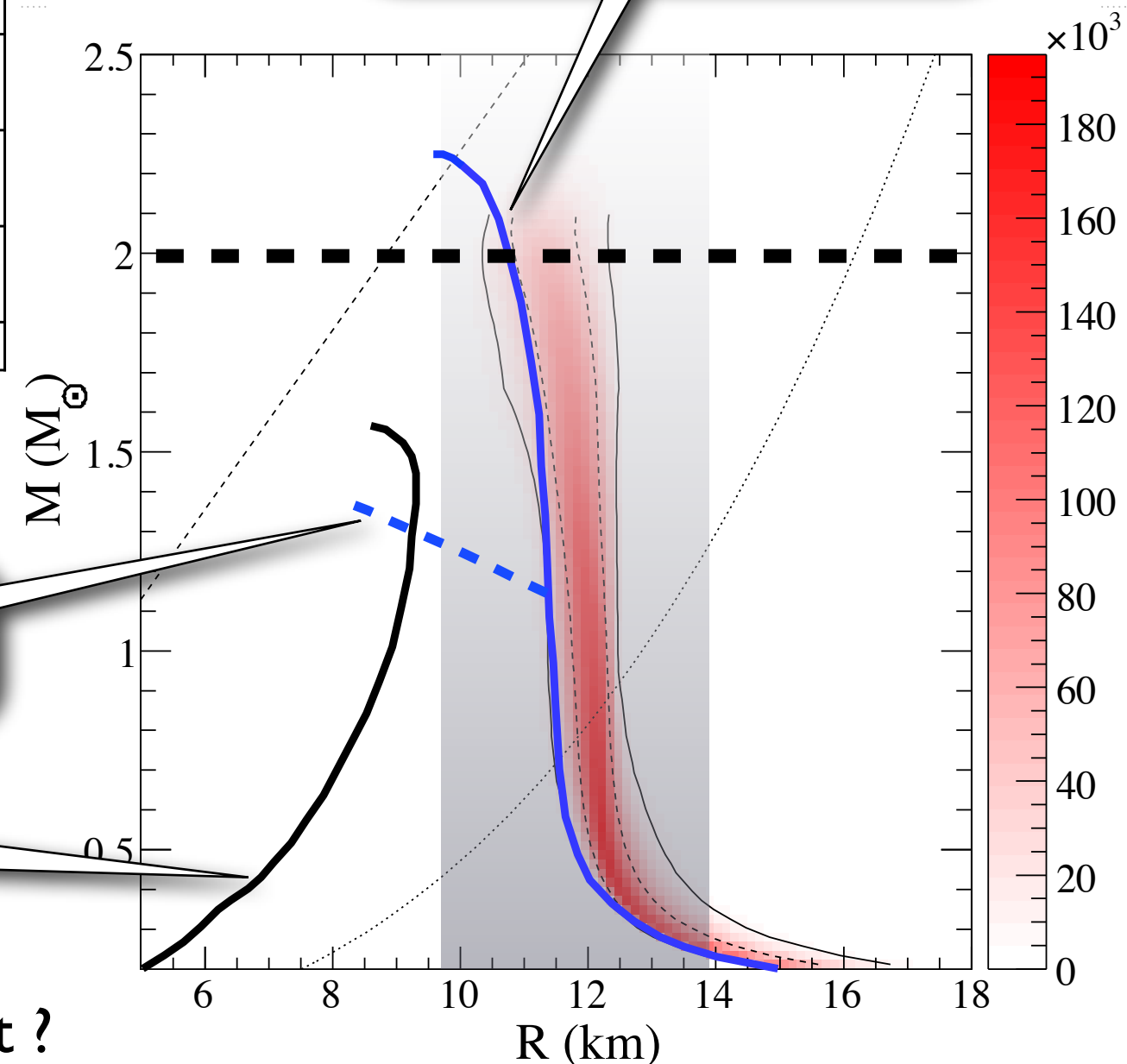
News from NEUTRON STARS

K. Hebeler, J. Lattimer, C. Pethick, A. Schwenk
PRL 105 (2010) 161102



A.W. Steiner, J. Lattimer, E.F. Brown
Astroph. J. 722 (2010) 33

realistic “**nuclear**” EoS
(Illinois 1998)



New constraints
from **EFT** and
neutron star
observables

kaon
condensate

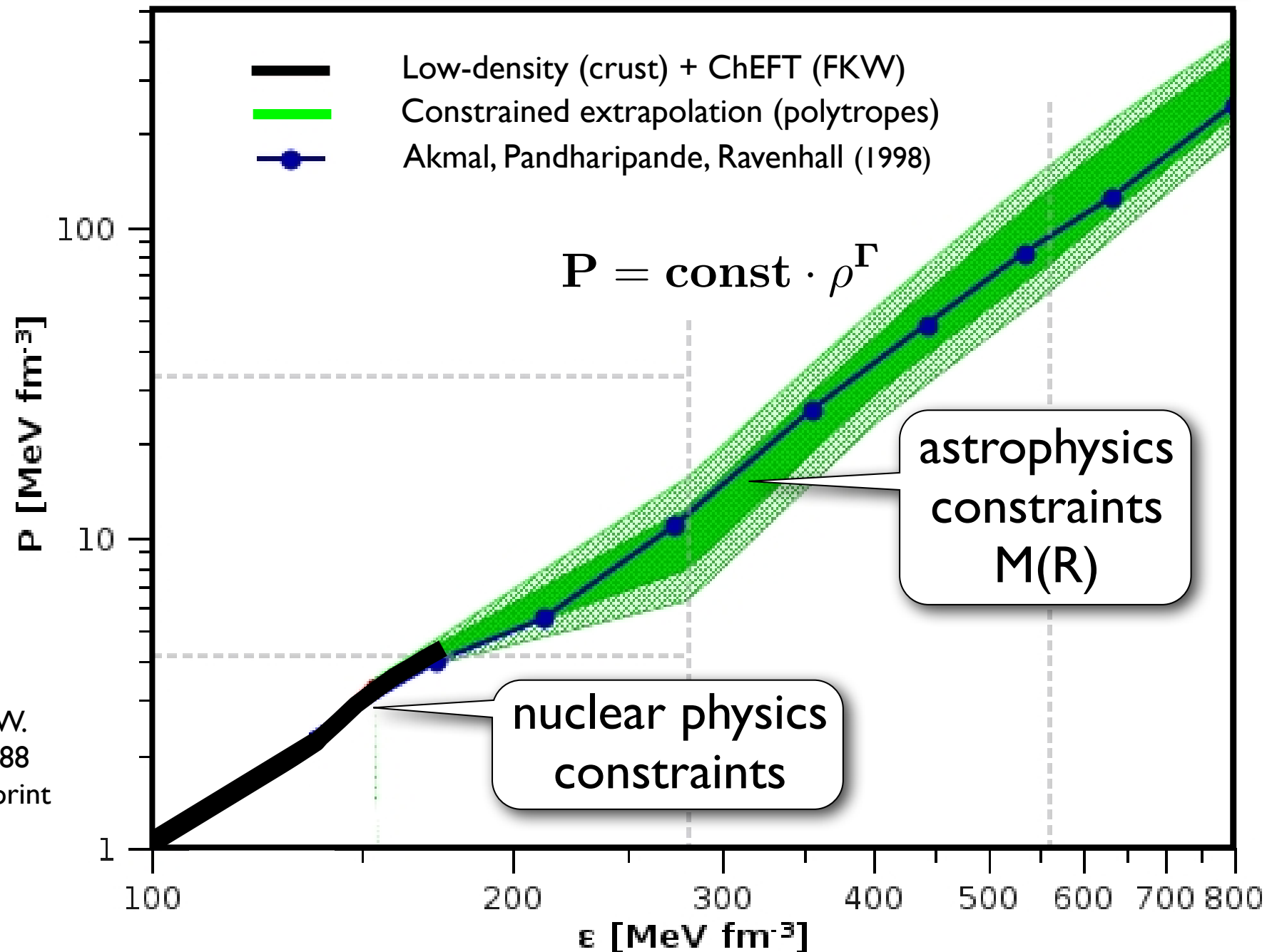
quark
matter

“**Exotic**” equations of state ruled out ?



NEUTRON STAR MATTER

Equation of State



S. Fiorilla,
N. Kaiser, W.W.
arXiv:1111.3688
NPA (2012) in print

B. Röttgers, W.W.
(2011)

Prog. Part. Nucl. Phys.
(2012) in print

- Including new neutron star constraints plus **Chiral Effective Field Theory** at lower density



SUMMARY

- **New**

consistent analysis of $\bar{K}N$ threshold physics and scattering data based on chiral SU(3) effective Lagrangian at next-to-leading order

- **New** evaluation of $K^- p$ scattering length:

$$a(K^- p) = -0.65 + 0.81 i \text{ [fm]} \quad (\sim 15 \% \text{ accuracy})$$

deduced: $a(K^- n) \simeq 0.6 + 0.7 i \text{ [fm]}$ (less accurate)

- Need kaonic deuterium to complete $\bar{K}N$ and set constraints for $\bar{K}NN$

- Nucleon **sigma term**:

Lattice QCD continuously improving towards $\sigma_N \sim 40 \text{ MeV}$

Very small sea of strange quarks in the nucleon

- **New** constraints from two-solar-mass neutron star and window of n-star radii:

conventional EoS works best - **kaon condensate** ruled out

