

Possible Existence of K^{bar} -Hyperon Resonances and the origin of K^{bar} -Hadron Attractions



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INTRODUCTION

Low-Energy Hadron-Hadron Interactions

A Long-standing problem since Yukawa Theory

Experimental Knowledge

- NN, π N, KN, $\pi\pi$, $K\pi$: Phase Shift Analyses are available
- YN, YY : Cross sections, Hypernuclear Properties
- K^{bar} N : Cross sections, Scattering Lengths
- π Y, K^{bar} Y, KK : Unknown (Not well known)

Theoretical Models:

- Hadron-Exchange Models: The SU(3) symmetry+Physical Hadron masses
- Quark Models (with Meson-Exchange) the SU(6) Symmetry + OGE
- Effective Field Theory : Chiral perturbation

First-Principle Calculations:

Hadron-Hadron potentials derived from Lattice QCD calculations

mB potential model

*p-space potential

Long-range part of potential: One Hadron Exchange

SU(3) symmetric Interaction Lagrangian
(mBB coupling constants are predetermined in BB potential model)
Gaussian Form factor with a common range
(Cutoff range is the same with the range of short-range potential.)

Short-range part of potential : Phenomenological

The SU(3)-symmetric Strengths

Common range for all mB pairs

We consider two cases of range

$$V = \frac{\text{pot I}}{r_G} \frac{\text{pot II}}{0.4 \quad 0.45 \text{ (fm)}} \exp(-q^2/L^2) + V(\text{one-hadron-exchange potential}) \times \exp(-q^2/L^2)$$

where, $L=2/r_G$

t-channel exchange

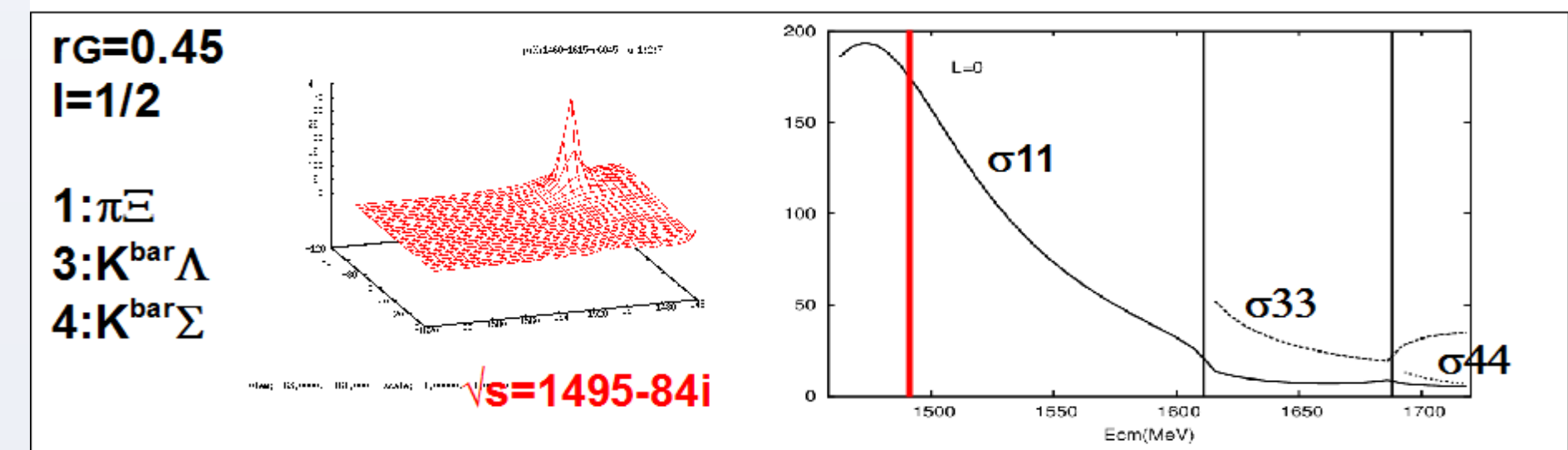
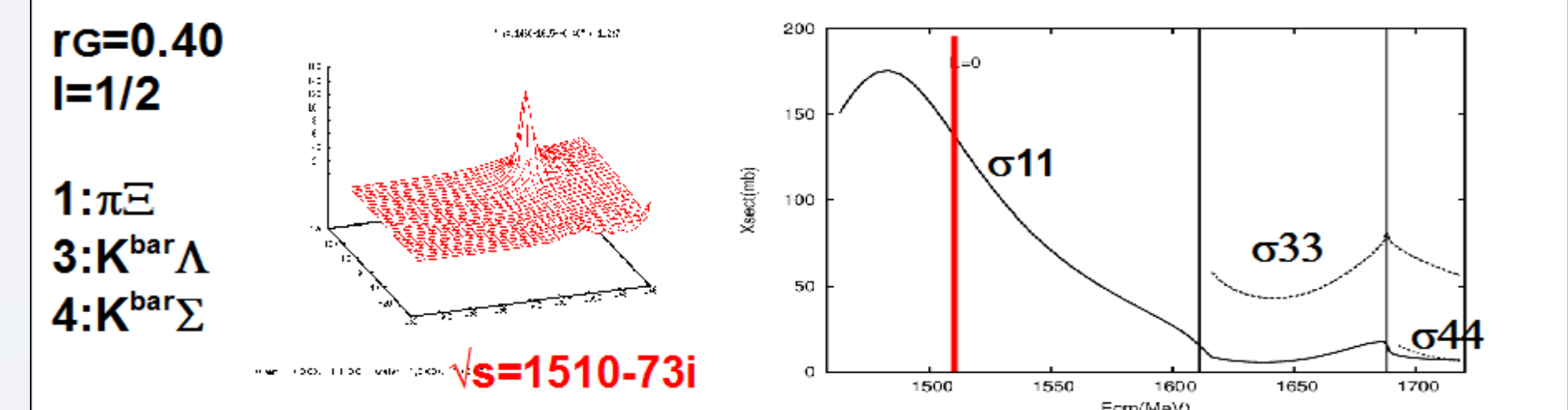
u-channel exchange

s-channel exchange

Resonance Poles

$\Xi^*(I=1/2, J_p=1/2^-)$

Cross sections $\sigma_{11}, \sigma_{33}, \sigma_{44}$



BB potential model

*r-space potential

Long-range part of potential : One Boson Exchange potential

SU(3) symmetric Interaction Lagrangians

Physical masses, retardation effects

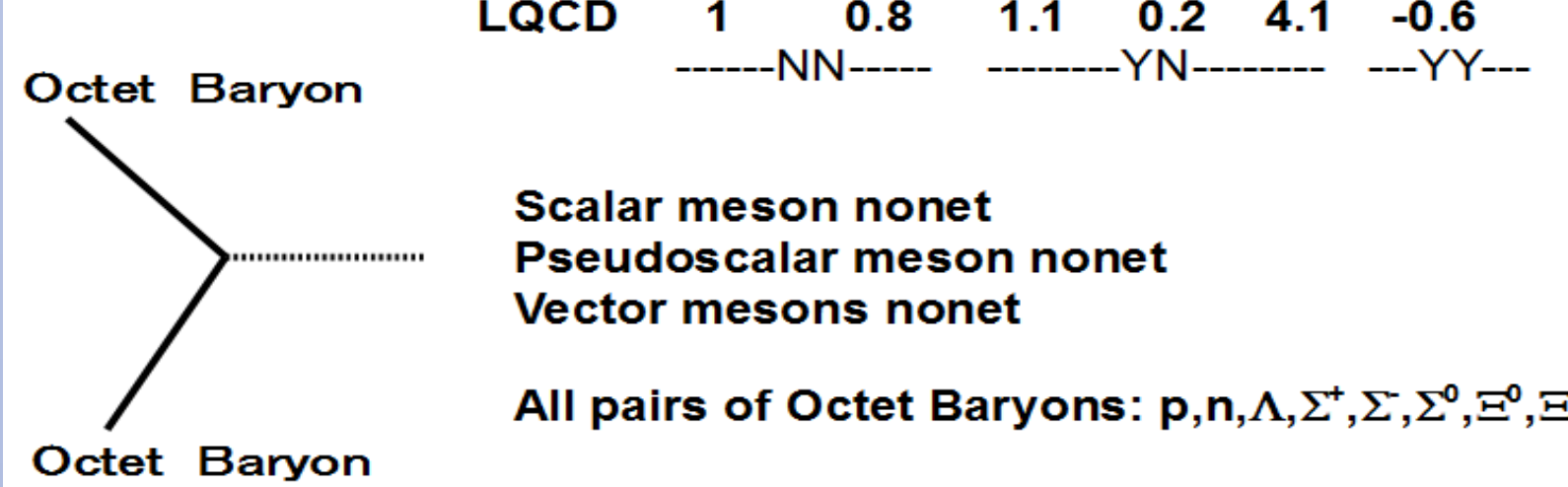
Smoothly cutoff by $[1-\exp(-(r/r_0)^2)]^4$, $r_0=0.4\text{fm}$

Short-range part of potential : LQCD

SU(3) symmetric strengths and common range

Gaussian form : $\exp(-(r/r_0)^2)$, $r_0=0.476\text{fm}$

Relative strengths are determined by LQCD results (within $\pm 10\%$)



Results for π N, KN scattering lengths

π N scattering lengths

	calc	exp
rG	0.40	0.45
S11	+0.2458	+0.2482
S31	-0.1496	-0.1466
P11	-0.2359	-0.2340
P31	-0.1375	-0.1290
P13	-0.0862	-0.0894
P33	+0.6238	+0.6235

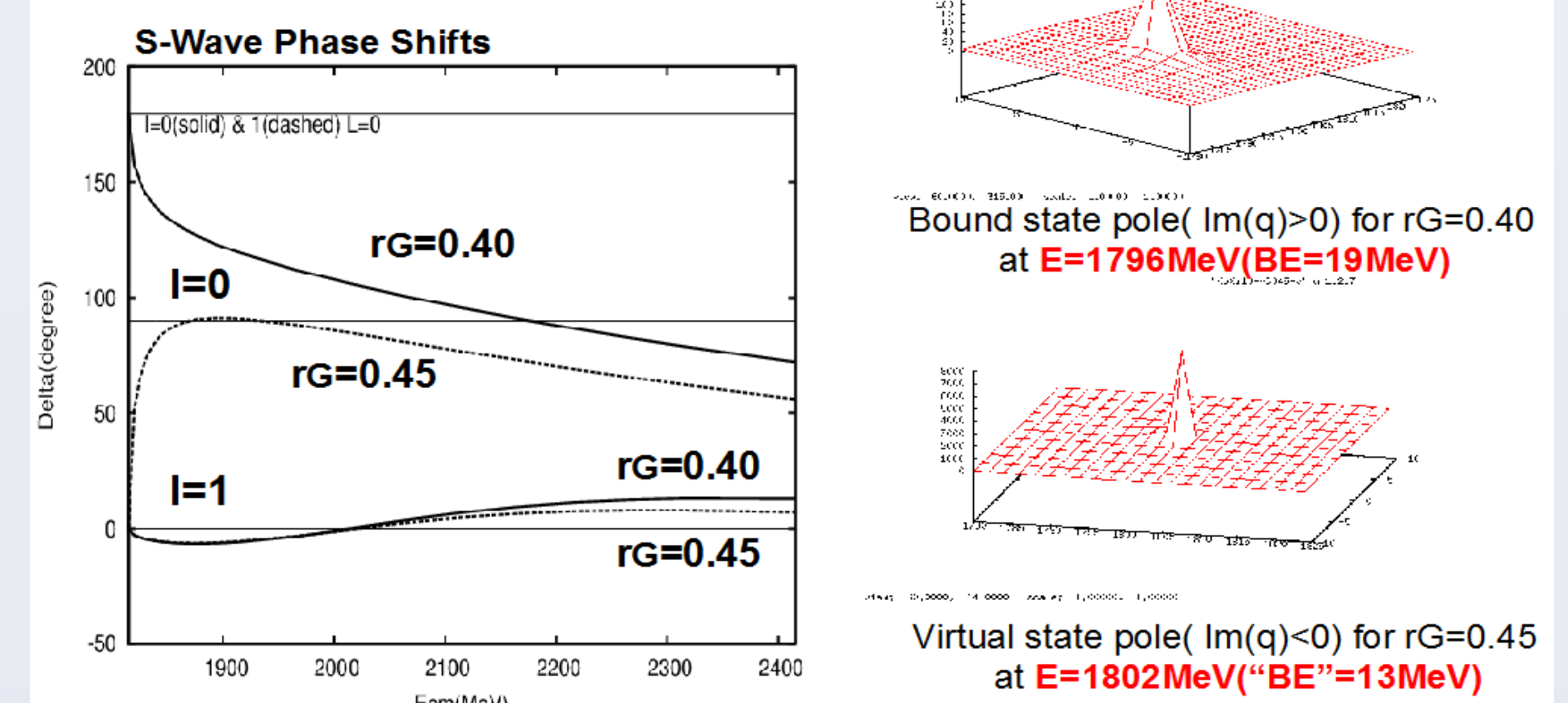
KN scattering lengths

	calc	exp
rG	0.40	0.45
S01	-0.008	-0.013
S11	-0.365	-0.369
P01	+0.166	+0.179
P11	-0.106	-0.103
P03	-0.058	-0.071
P13	+0.047	+0.040

S=-3 and I=0
 $K^{\text{bar}}\Xi$
(1815)

S=-3 and I=1
 $K^{\text{bar}}\Xi$
(1815)

Isospin=0 state



Results for K^{bar} N scattering quantities

K⁻p threshold data:

	calc	exp
rG	0.40	0.45
γ	2.35	2.36
R_c	0.660	0.700
R_0	0.189	0.172
Re(a)	-0.666	-1.019
Im(a)	0.462	0.398

If isospin-symmetric masses are used

Re(a)	-0.354	-0.639
Im(a)	0.453	0.440

$a(K-p) \neq (a(I=0) + a(I=1))/2$ (not so simple!)

New parameters are only two!

	{27}	{10 ⁺ }	{10}	{8-1}+5/9 {8-2}	{8-2}	{1}
π N	○	○	○	○	—	—
KN	○	○	○	○	—	—
K^{bar} N	○	○	○	○	●	●

The origin of the K^{bar} -Baryon Attractions in S-states

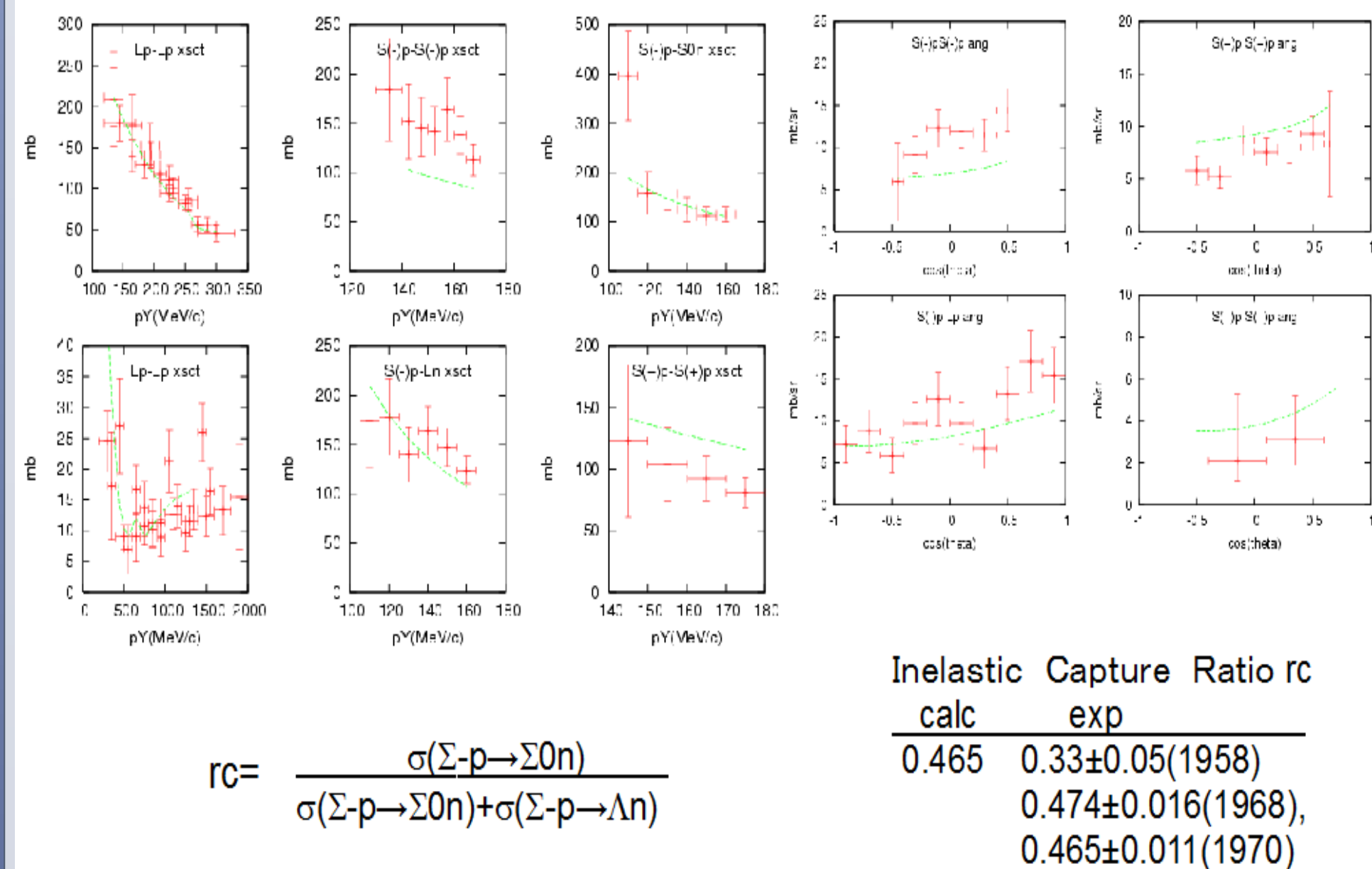
= Isospin-dependent ρ -contribution + large attractive ω contribution

On-shell Potential Values (V/4pi) at 50MeV above each K^{bar} -Baryon threshold

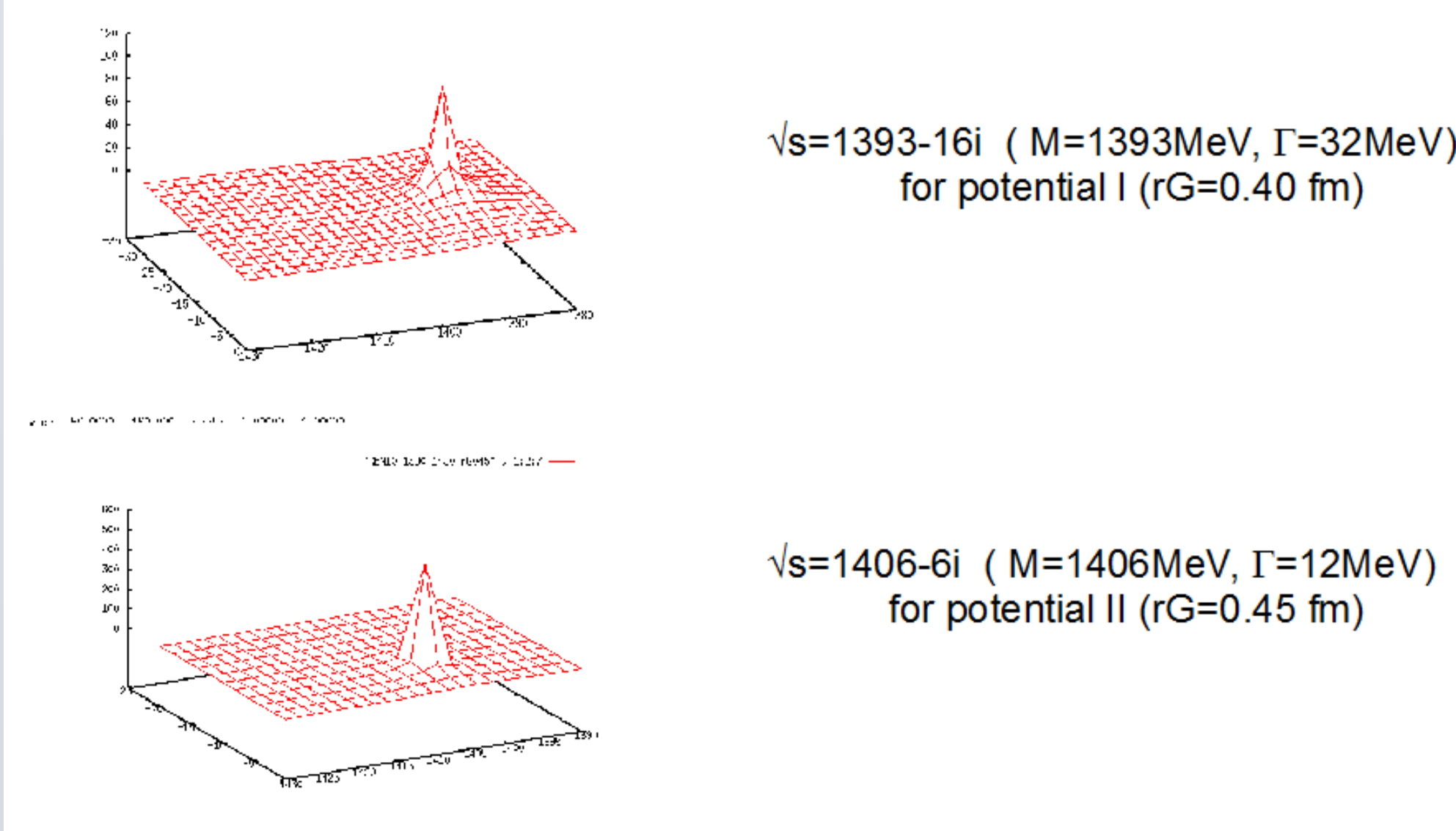
K^{bar} -B	Isospin	ρ	ω	ϕ	scalar	Baryon	Short	Total	
K^{bar} N	0	-42.4	-91.7	20	-25.0	22.4	-44.9	-161.5	$\Lambda^*(1405)$
K^{bar} N	1	14.1	-91.7	20	-25.3	156.5	11.5	85.2	
K^{bar} Λ	1/2	0	-84.7	49.6	-28.7	6.5	-12.1	-69.4	
K^{bar} Σ	1/2	-78.4	-87.5	55.9	-27.1	30.7	18.5	-87.9	$\Xi^*(1510)$
K^{bar} Σ	3/2	39.2	-87.5	55.9	-30.0	0	-2.2	-24.6	
K^{bar} Ξ	0	-69.4	-70.3	90.7	-28.7	14.2	7.1	-56.4	$\Omega^*(1796)$
K^{bar} Ξ	1	23.1	-70.3	90.7	-32.7	5.2	14.2	30.4	

Scalar mesons provide almost constant attraction ($\sim -30\text{MeV}$)

We obtain a reasonable description of YN scattering data



Our potentials provide $\Lambda(1405)$ resonance as a single resonance



Property of our BB potential :
Single particle potentials in symmetric nuclear matter
at normal density ($K_F=1.36$ (1/fm))

Baryon	proton-part	neutron-part	total	0.8x
p	-24.7	-44.8	-69.4	-55.5
n	-44.8	-24.7	-69.4	-55.5
Λ	-18.3	-17.9	-36.3	-29.0
Σ^+	33.7	4.5	38.3	30.6
Σ^-	3.4	31.8	35.1	28.1
Σ^0	18.7	19.1	37.9	30.3
Ξ^0	18.2	3.4	21.5	17.2
Ξ^-	2.8	17.8	20.5	16.4

For all of $\Sigma^+, \Sigma^-, \Sigma^0, \Xi^0, \Xi^-$,
Repulsive interaction with nuclear matter (both proton part and neutron part)
(Especially, Σ^-, Ξ^- interact very repulsively with neutron matter)

We constructed a potential model describing simultaneously
Baryon-Baryon and Meson-Baryon Scattering.
Based on SU(3)-symmetry and
One-hadron-exchange mechanism

NN, YN, YY, π N, KN, K^{bar} N interactions at low energies,

We extend the potential to

S=-2 $\pi\Xi-K^{\text{bar}}\Lambda-K^{\text{bar}}\Sigma-\eta\Xi$
S=-3 $K^{\text{bar}}\Xi$

and discuss existence of S-wave resonances

Summary

- We constructed a potential model which describes consistently NN, YN, YY, π N, KN K^{bar} N scattering. One-hadron-exchange mechanisms with the SU(3) symmetric coupling constants, physical hadron masses and short-range cutoff. The SU(3)-symmetric short-range potential with We tried two ranges $r_G=0.4$ and 0.45 fm for mB potentials, SU(3)-symmetric strengths (BB: relative strengths by LQCD calculations HAL-QCD)
 - Using our potentials, we calculated S=-2 $\pi\Xi-K^{\text{bar}}\Lambda-K^{\text{bar}}\Sigma-\eta\Xi$ and S=-3 $K^{\text{bar}}\Xi$
 - We found an S-wave resonance and a bound or virtual state. $\Xi^*(I=1/2, J^*=1/2^-)$ at $\sqrt{s}=1495-1510\text{MeV}$ with width $\Gamma\sim 150\text{MeV}$ ($\Omega^*(I=0, J^*=1/2^-)$ at $\sqrt{s}=1789\text{MeV}$ (BE=19MeV) or 1802 ("BE"=13MeV))
- The results are still model-dependent. We need a careful refinement:
Full inclusion of Decouplet baryons : Ξ^*, Ω^*
Better fit to Kp cross sections, etc