

# Meson Properties at Finite Density from Meson-Nucleus systems

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*KEK*

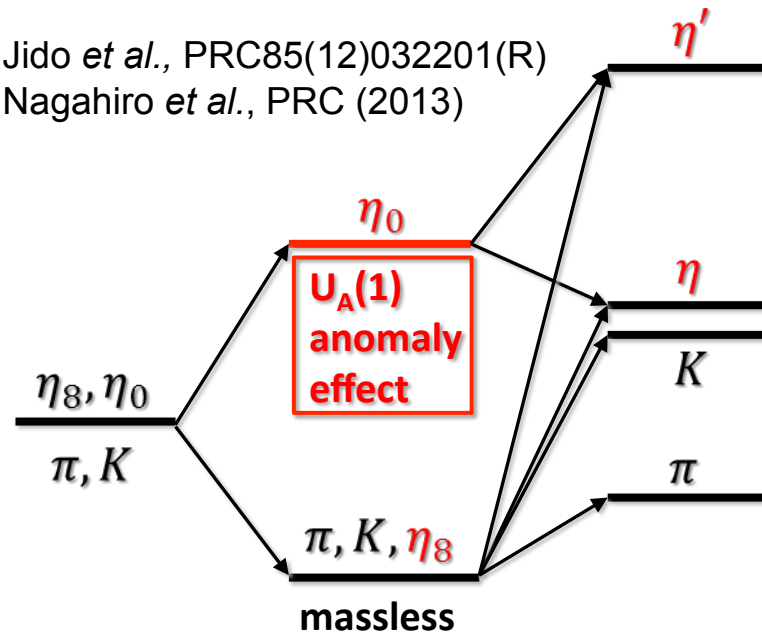


**Workshop on J-PARC Hadron Physics in 2014,  
Tokai, Ibaraki, Japan, Feb. 10 - 12, 2014**

# Meson mass spectrum and Symmetry Breaking Pattern (PS)

## schematic view of the mass of $\pi, K, \eta$ & $\eta'$

Jido *et al.*, PRC85(12)032201(R)  
Nagahiro *et al.*, PRC (2013)



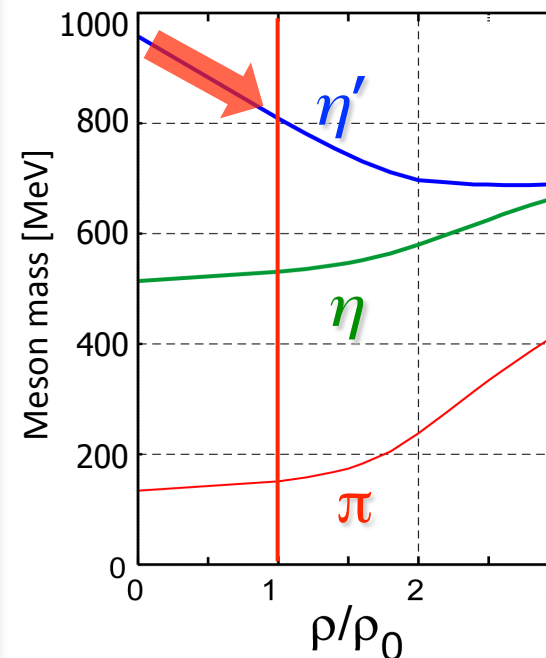
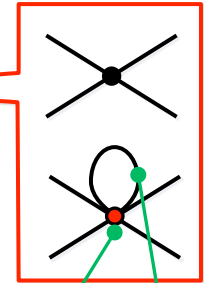
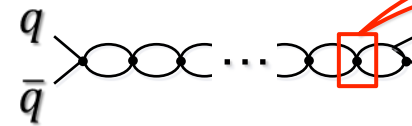
|                                |                                   |                                   |
|--------------------------------|-----------------------------------|-----------------------------------|
| $m_q, m_s = 0$                 | $m_q, m_s = 0$                    | $m_q, m_s \neq 0$                 |
| $\langle \bar{q}q \rangle = 0$ | $\langle \bar{q}q \rangle \neq 0$ | $\langle \bar{q}q \rangle \neq 0$ |

ChS  
manifest

dynamically  
broken

dyn. & explicitly  
broken

## cf.) NJL model with KMT



$U_A(1)$  breaking  
(KMT term<sup>[1,2]</sup>)

$$\langle \bar{q}q \rangle \rightarrow 0$$

[1] Kobayashi-Maskawa  
PTP44(70)1422  
[2] G. 't Hooft,  
PRD14(76)3432

$$\Delta m \sim -150 \text{ MeV} @ \rho_0$$

Costa *et al.*, PLB560(03)171,  
Nagahiro-Takizawa-Hirenzaki, PRC74(06)045203

## ■ *Recent Activities on Pionic Atoms*

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= N. Ikeno, H. Nagahiro . . .

= K. Itahashi, T. Nishi, Y. Watanabe . . .

= GSI  $\longrightarrow$  RIBF/RIKEN

N. Ikeno , J. Yamagata-Sekihara, H. Nagahiro and S. Hirenzaki, PTEP(2013) 063D01

N. Ikeno, H. Nagahiro and S. Hirenzaki, EPJA47 (2011) 161

N. Ikeno, R. Kimura, J. Yamagata-Sekihara, H. Nagahiro, D. Jido, K. Itahashi, L. S. Geng and S. Hirenzaki, PTP126 (2011) 483

# Introduction

## Deeply bound pionic atom

... Useful system to study pion properties at finite density and partial restoration of chiral symmetry

## Current status

- (d,<sup>3</sup>He) reaction in <sup>116, 120, 124</sup>Sn:  
Observation of pionic 1s states

- Pion-Nucleus optical potential

$$2\mu V_{\text{opt}}^s = -4\pi[\varepsilon_1\{b_0\rho(r) + b_1\delta\rho(r)\} + \varepsilon_2 B_0\rho^2(r)]$$

- GOR relation + Tomozawa-Weinberg

$$\frac{\langle \bar{q}q \rangle_\rho}{\langle \bar{q}q \rangle_0} \simeq \frac{f_\pi^{*2}}{f_\pi^2} \simeq \frac{b_1^{\text{free}}}{b_1^*(\rho)} = 0.78 \pm 0.05 @ \rho \simeq 0.6\rho_0$$

↓

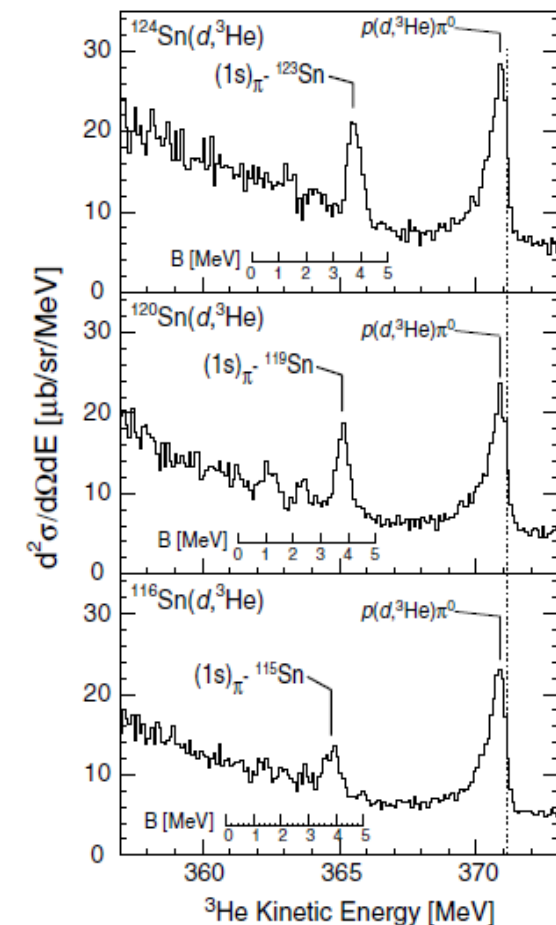
~ 0.67 @  $\rho = \rho_0$

Theoretical basis

Kolomeitsev, Kaiser, Weise, PRL90(2003)092501

Jido, Hatsuda, Kunihiro, PLB 670(08)109

K. Suzuki *et al.*, PRL92(2004)072302



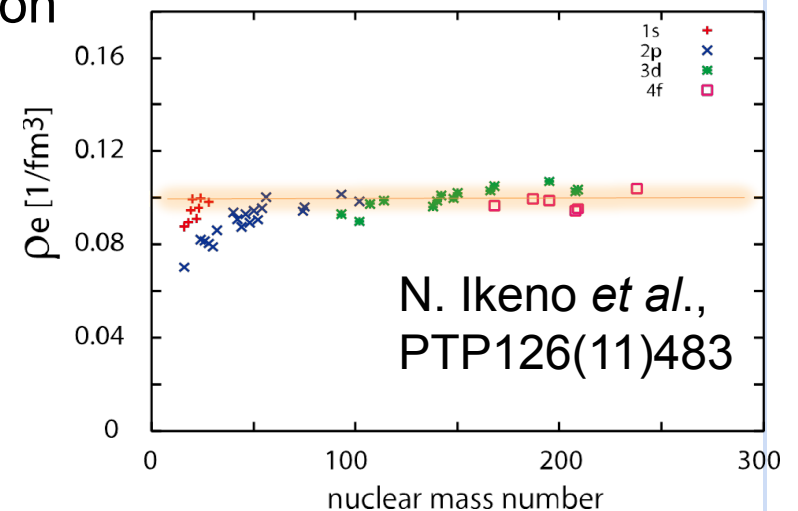
# What's next ?

## Interests

- $\bar{q}q$  condensate: beyond the linear density approx. (Goda, Jido)
  - : in asymmetric (n or p rich) Nuclear Matter
- Aspects of symmetry in “various extreme conditions”

## Difficulties for precise studies

- = Limited sensitivity of known atomic pion to  $\rho \simeq 0.6\rho_0$  (Seki-Masutani)
- = Uncertainties of Neutron density distribution
- = Residual Interaction effects



# What's next ?

## Interests

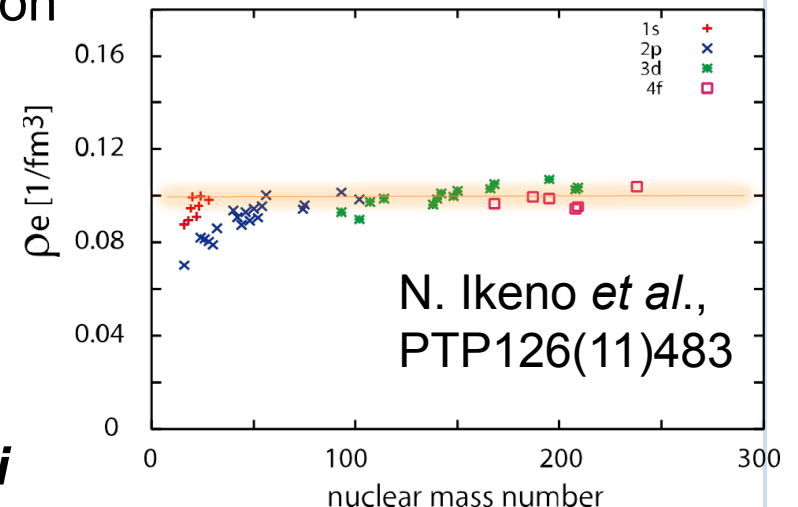
- $\bar{q}q$  condensate: beyond the linear density approx. (Goda, Jido)
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## How we can..

- = Several atomic states data (ex. 1s, 2s, 2p) in each nucleus  
(=> reduction of  $\rho_n$  ambiguities)
- = Systematic ‘precise’ observation for various nucleus **including unstable nuclei**  
(=> observation of various effective  $\rho$  and p/n ratio)



It will be

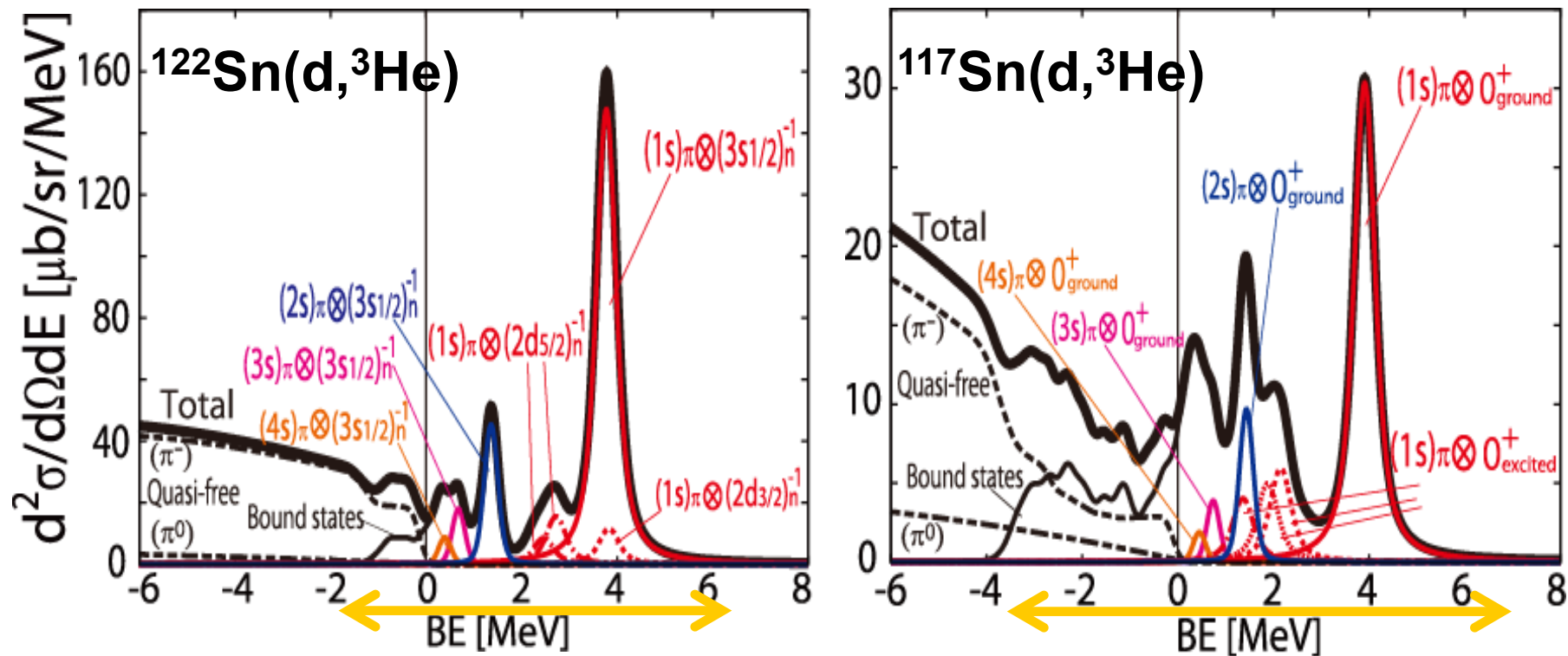
Study of Quark condensate by Hadronic atoms in Nuclear chart

# Some Numerical Results (by N. Ikeno)

## 0 degree

Even target:  $^{122}\text{Sn}$  ( $0^+$ )

Odd target:  $^{117}\text{Sn}$  ( $1/2^+$ )



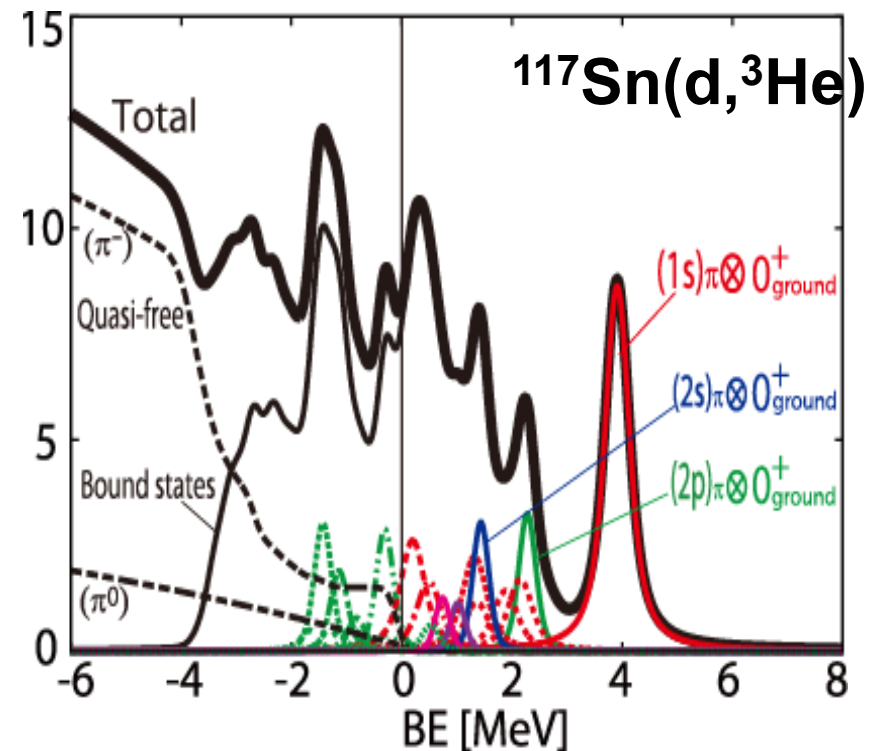
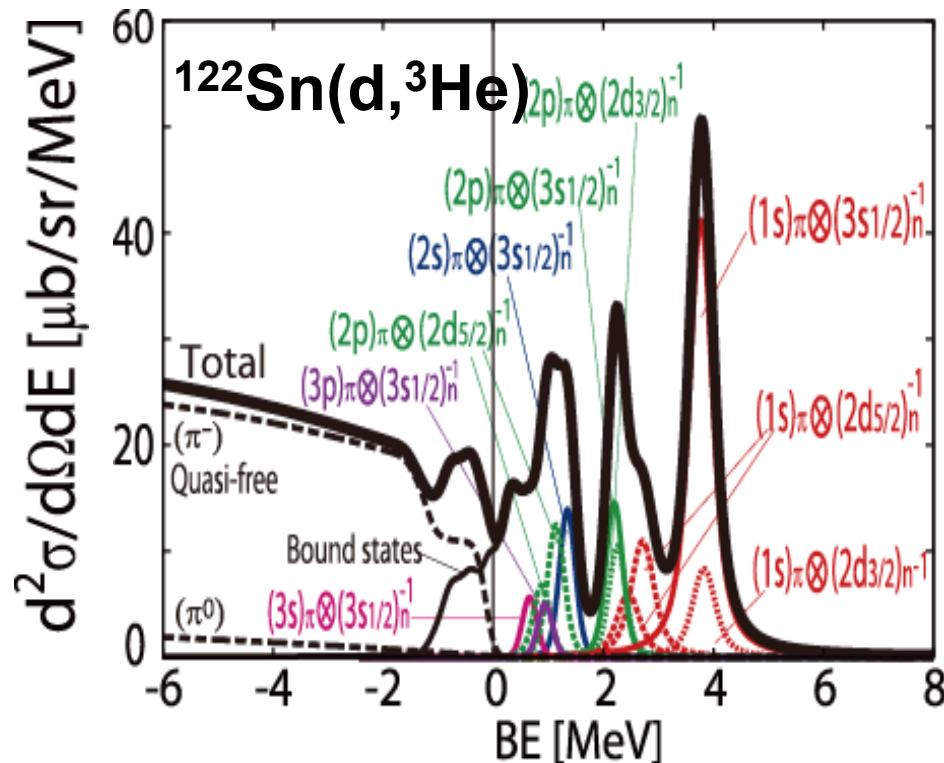
- Pionic 1s state formation with neutron s-hole state
- Spectrum of  $^{117}\text{Sn}(d, ^3\text{He})$  is spread over wider energy range.
- Cross section of  $^{117}\text{Sn}(d, ^3\text{He})$  is smaller.
- Pionic 1s and 2s states can be observed

# Some Numerical Results (by N. Ikeno)

## 2 degree

Even target:  $^{122}\text{Sn}$  ( $0^+$ )

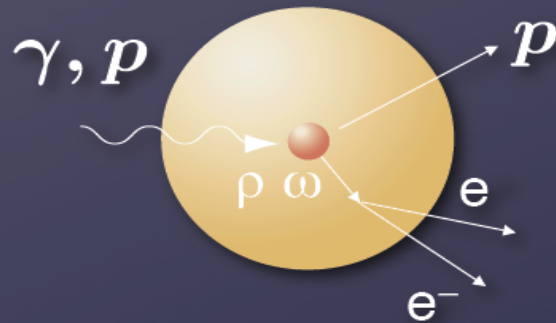
Odd target:  $^{117}\text{Sn}$  ( $1/2^+$ )



- Pionic  $2p$  state contributions become relatively larger.

# Vector Meson Mass Shift by Invariant mass

**$M_{e^+e^-}$**



KEK E325  $p+A \rightarrow V + X$   
J-LAB g7  $\gamma+A \rightarrow V + X$

$$m_{\rho,\omega} = \sqrt{(p_{e^+} + p_{e^-})^2}$$

- ▶ small FSI
- ▶ rare decay
- ▶ fast  $\omega$ ,  $\phi$  decay outside

TABLE I. Properties of vector mesons (Amsler *et al.*, 2008).

|          | Mass<br>(MeV/ $c^2$ ) | $\Gamma$<br>(MeV/ $c^2$ ) | $c\tau$<br>(fm) | Main<br>decay                 | $\frac{\Gamma_{e^+e^-}}{\Gamma_{\text{tot}}}$ <sup>a</sup><br>( $\times 10^{-5}$ ) |
|----------|-----------------------|---------------------------|-----------------|-------------------------------|------------------------------------------------------------------------------------|
| $\rho^0$ | $775.49 \pm 0.34$     | $149.4 \pm 1.0$           | 1.3             | $\pi^+\pi^-$ ( $\sim 100\%$ ) | 4.7                                                                                |
| $\omega$ | $782.65 \pm 0.12$     | $8.49 \pm 0.08$           | 23.2            | $\pi^+\pi^-\pi^0$ (89%)       | 7.2                                                                                |
| $\phi$   | $1019.455 \pm 0.020$  | $4.26 \pm 0.04$           | 46.2            | $K^+K^-$ (49%)                | 29.7                                                                               |

<sup>a</sup>These branching ratios are at the pole mass.

## Observation of 『mass shift』

1, Mass reduction will be equivalent to attractive  $V$  in Eq. of Motion..

$$m_{\eta'}^2 \rightarrow m_{\eta'}^2(\rho) = (m_{\eta'} + \Delta m_{\eta'}(\rho))^2 \sim m_0^2 + 2m_0\Delta m(\rho)$$

$$\Delta m(\rho) \rightarrow V(\rho(r)) = V_0 \frac{\rho(r)}{\rho_0}$$

2, But “ Attractive  $\rightarrow$  Mass reduction ” is wrong. Ex.) Coulomb case.  
Origin of the attraction is important.

$$p^2 + (m - \Delta m)^2 = (E + V)^2$$

$$\rightarrow M_{\text{inv}}^2 = E^2 - p^2 \sim m^2 \left( 1 - \frac{2}{m}(\Delta m + V) \right) \quad \begin{array}{l} \text{Invariant mass data ONLY} \\ \text{at small kinetic energy} \end{array}$$

3, Thus, “exclusive” and/or “systematic” are important !

==> \* Bound state spectroscopy

(Quantum number selection rules, No vacuum background)

\* Systematic info. on invariant mass  
(Not simply ‘mass’, ‘width’)

# Vector Meson Mass Shift by Invariant mass

Ryugo S. Hayano and Tetsuo Hatsuda: Hadron properties in the nuclear medium

TABLE IV. Compilation of experimental results on the in-medium mass and width of the  $\rho$ ,  $\omega$ , and  $\phi$  mesons produced with elementary reactions, measured in different experiments. This is based on updating the table prepared by [Metag \(2008a\)](#).

|          | Invariant mass                                                               |                                         | Attenuation                    |                                                                                                       |
|----------|------------------------------------------------------------------------------|-----------------------------------------|--------------------------------|-------------------------------------------------------------------------------------------------------|
|          | E325 @ KEK                                                                   | CLAS-g7 @ JLab                          | CBELSA/TAPS                    | LEPS @ SPring-8                                                                                       |
| Reaction | $pA$ 12 GeV                                                                  | $\gamma A$ 0.6–3.8 GeV                  | $\gamma A$ 0.7–2.5 GeV         | $\gamma A$ 1.5–2.5 GeV                                                                                |
| Momentum | $p > 0.5$ GeV/ $c$                                                           | $p > 0.8$ GeV/ $c$                      | $p < 0.5$ GeV/ $c$             | $1.1 < p < 2.2$ GeV/ $c$                                                                              |
| $\rho$   | $\uparrow$<br>$\Delta m(\rho_0)/m = -9\%$                                    | $\Delta m \approx 0$<br>Some broadening |                                |                                                                                                       |
| $\omega$ | $\downarrow$<br>No broadening                                                |                                         | $\Delta m(\rho_0)/m = -14\%^a$ | $\Gamma_\omega(\rho_0) = 130\text{--}150$ MeV/ $c^2$<br>$\rightarrow \sigma_{\omega N} \approx 70$ mb |
| $\phi$   | $\Delta m(\rho_0)/m = -3.4\%$<br>$\Gamma_\phi(\rho_0) \approx 15$ MeV/ $c^2$ |                                         |                                | $\sigma_{\phi N} = 35$ mb<br>$\rightarrow \Gamma_\phi(\rho_0) \approx 80$ MeV/ $c^2$                  |

<sup>a</sup>This may change as a result of the ongoing reanalysis ([Metag, 2008b](#)).

.....Various data. Not consistent.

- 
- Precise/High statistics data at JPARC ... Necessary !!
  - Momentum dependence of  $\Phi$  data (as expected in E16) is important as Systematic info.
  - On the other hand,  $\Phi$  mass shift could be small.  
(Philipp Gubler, Poster yesterday. )

==>

- Experimental determination of  $\langle N | \bar{s} s | N \rangle$  by in-medium  $\Phi$  . Important quantity !

# $\eta'(958)$ mesic nucleus

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H.Nagahiro, S.Hirenzaki, Phys.Rev.Lett.94 (2005)232503

H.Nagahiro, M.Takizawa, S.Hirenzaki, Phys.Rev.C74 (2006)045203

D. Jido, H. Nagahiro, S. Hirenzaki, Phys.Rev.C 85, 032201 (R) (2012)

H. Nagahiro, S. Hirenzaki, E. Oset, A. Ramos, Phys. Lett. B 709 (2012) 87-92

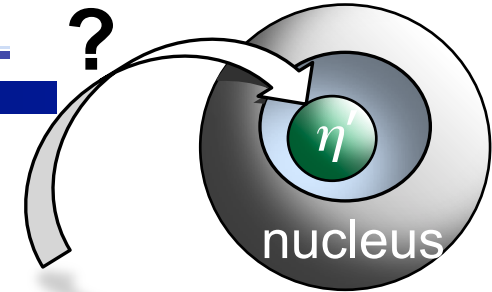
K. Itahashi, H. Fujioka, H. Geissel, R. S. Hayano, S Hirenzaki, S. Itoh, D. Jido, V. Metag, H. Nagahiro, M. Nanova, T. Nishi, K. Okochi, H. Outa, K. Suzuki, Y. K. Tanaka, H. Weick, Prog. Theor. Phys. 128 (2012) 601-613.

H. Nagahiro, D. Jido, H. Fujioka, K. Itahashi, S. Hirenzaki,  
Phys. Rev. C 87, 045201 (2013).

# Introduction

- $\eta'(958)$  meson ...close connections with  $U_A(1)$  anomaly
  - » Theoretical works
    - › the effects of the  $U_A(1)$  anomaly on  $\eta'$  properties
    - › at finite temperature/density
      - T. Kunihiro, PLB219(89)363
      - R.D.Pisarski, R.Wilczek, PRD29(84)338
      - Y. Kohyama, K.Kubodera and M.Takizawa, PLB208(1988)165
      - K.Fukushima, K.Onishi, K.Ohta, PRC63(01)045203
      - P. Costa *et al.*, PLB560(03)171, hep-ph/0408177
    - etc...
    - › the possible character changes of  $\eta'$  at  $\rho \neq 0$
  - » Poor experimental information  
on the  $U_A(1)$  anomaly at finite density
- Proposal for the study of the  $\eta'$ -mesic nuclei
  - »  $U_A(1)$  anomaly effect in medium from the “mesic nuclei”
  - » the  $\eta'$  properties at finite density

# $\eta'$ property in medium



## ✓ small scattering length ?

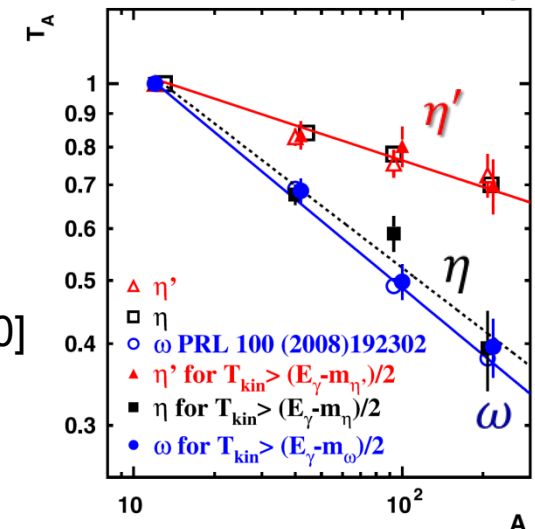
$|\text{Re } a_{\eta'N}| < 0.8 \text{ fm}$ , [ $pp \rightarrow pp\eta'$ @ COSY, Moscal *et al.*, PLB474(00)416]

$|a_{\eta'N}| \sim 0.1 \text{ fm}$ , [ ... , Moscal *et al.*, PLB482(00)356]

## ✓ smaller absorption width in medium ?

CBELSA/TAPS [M.Nanova *et al.*, PLB710(12)600]

[estimated transparency ratio  $\gamma A \rightarrow \eta' X$ ]



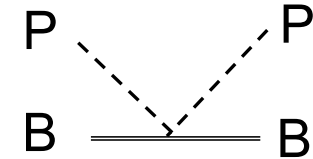
## ✓ mass reduction in finite T/ρ?

$\langle \bar{q}q \rangle \rightarrow 0$  [NJL model w/ KMT interaction]

[experimentally observed enhanced production of soft pions]

Interpreted as mass reduction of  $\eta'$  in the hot medium [Csorgo *et al.*, PRL105(10)182301]

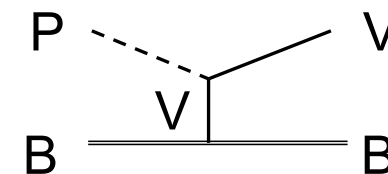
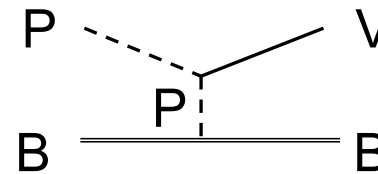
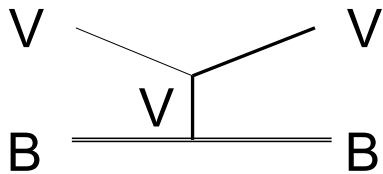
pseudoscalar-baryon (PB) : Weinberg-Tomozawa interaction



$\pi N, \eta N, K\Lambda, K\Sigma + \eta' N$  by the  $\eta - \eta'$  mixing

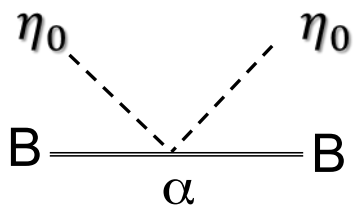
their result :  $|a_{\eta' N}| = 0.01 \text{ fm} \iff |a_{\eta' N}| \sim 0.1 - 0.8 \text{ fm}$  [PLB'00]

vector-baryon channels : through PB-VB interaction



their result :  $|a_{\eta' N}| = 0.03 \text{ fm}$

coupling of the singlet component of pseudoscalar to baryons



$$\mathcal{L}_{\eta_0 B} \propto \eta_0^2 \langle \partial_\mu \bar{B} \gamma^\mu B - \bar{B} \gamma^\mu \partial_\mu B \rangle$$

$\alpha \dots$  free parameter

Borasoy , PRD61(00)014011

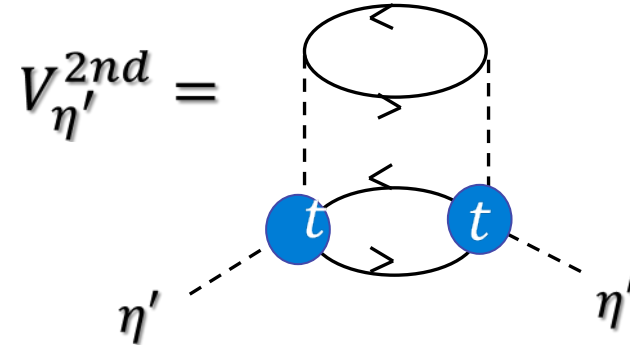
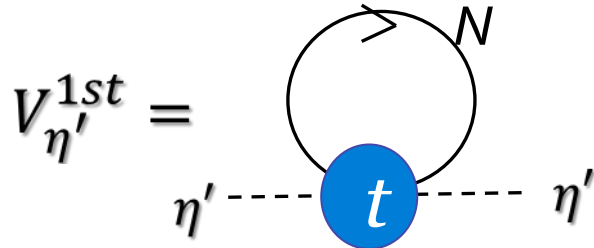
S. Bass, Phys.Lett. B463 (1999) 286

Kawarabayashi-Ohta, PTP66(81)1789

their result :  $|a_{\eta' N}| = 0.1 \text{ fm}$  can be reproduced

# phenomenological estimation for $V_{\eta'}^{opt}$

Optical potential  $V_{\eta'}$  [H.Nagahiro, S. Hirenzaki, E. Oset, A. Ramos, PLB709(12)87]



We consider only the **attractive** case & **energy-independent** potential.

Re  $V_{\eta'}$  and Im  $V_{\eta'}$  with various  $\alpha$  values

in unit of MeV

| $\alpha$ | $ a_{\eta'N} $ fm | $V_{\eta'}^{1st}(\rho_0)$ | $V_{\eta'}^{2nd}(\rho_0)$ | $V_{\eta'}^{total}(\rho_0)$       |
|----------|-------------------|---------------------------|---------------------------|-----------------------------------|
| -0.193   | 0.1               | $-8.6 - 1.7i$             | $-0.1 - 0.1i$             | <b><math>-8.7 - 1.8i</math></b>   |
| -0.834   | 0.3               | $-26.3 - 2.1i$            | $-0.6 - 0.9i$             | <b><math>-26.8 - 3.0i</math></b>  |
| -1.79    | 0.5               | $-43.8 - 3.0i$            | $-1.3 - 2.5i$             | <b><math>-44.1 - 5.5i</math></b>  |
| -9.67    | 1.0               | $-87.7 - 6.9i$            | $-4.1 - 10.4i$            | <b><math>-91.8 - 17.2i</math></b> |

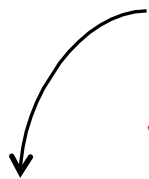
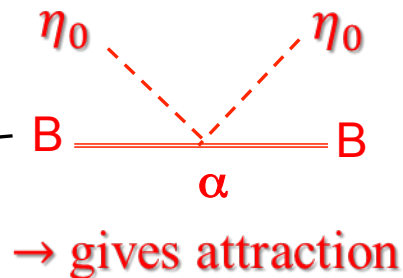
**Re  $V \gg$  Im  $V$**

# phenomenological estimation for $V_{\eta'}^{opt}$

## The reason why $\text{Re } V \gg \text{Im } V$ in the chiral unitary calculation

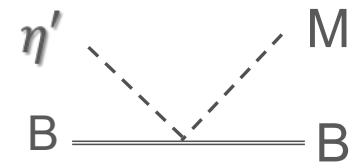
Kawarabayashi-Ohta, PTP66(81)1789

Borasoy, PRD61(00)014011



This interaction ...

WT interaction for  $\eta'$



$\rightarrow$  width [small]

- ✓ *resembles* that of the anomaly effect discussed by D. Jido PRC85(12)
- ✓ seems to **dominate** the  $\eta' N$  interaction
- ✓ contributes mostly to the  **$\eta'$  elastic channel** & barely to the **inelastic channel**

# Formation by (p,d) reaction

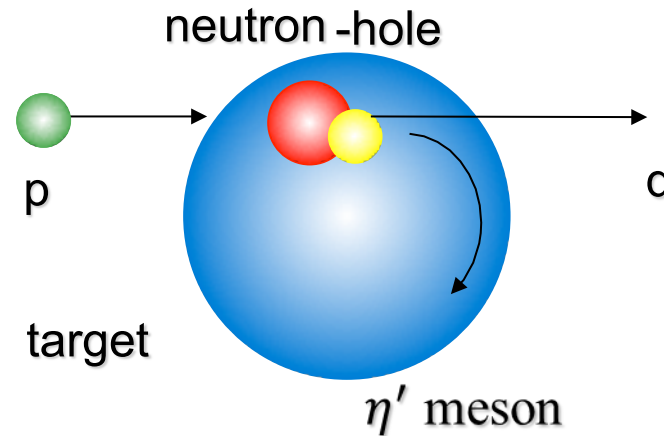
missing mass spectroscopy

K. Itahashi, H. Fujioka *et al.*, PTP128(12)601

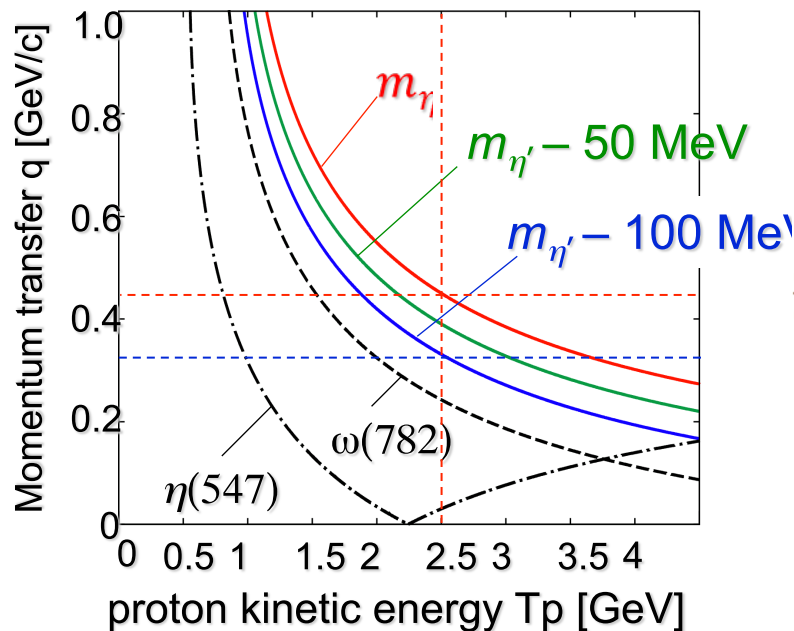
proton kinetic energy  $T_p = 2.5$  GeV

target :  $^{12}\text{C}$ , ( $^{16}\text{O}$ ,  $^{40}\text{Ca}$ )

forward reaction :  $\theta_d = 0$  deg.



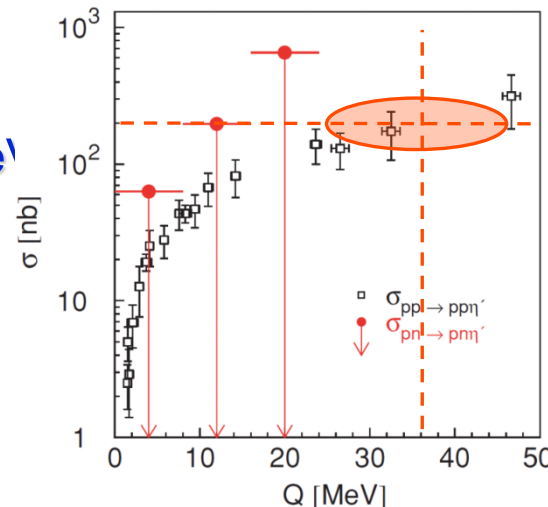
momentum transfer



elementary cross section  $pn \rightarrow \eta' d$

**No information**

J.Klaja *et al.*, PRC81(10)035209 (COSY)



$\sigma_{pp \rightarrow pp\eta'}$

**assumptions**

$$\left(\frac{d\sigma}{d\Omega}\right)_{pn \rightarrow \eta' d}^{lab} = 30 \mu b/sr$$

K.Nakayama in private comm  
Itahashi *et al.*, PTP128(12)601

# $^{12}\text{C}(p,d)^{11}\text{C} \eta'$ : **strong attraction** $(V_0, W_0) = -(100, 10)$ MeV

light nucleus  $\longleftrightarrow$  heavy nucleus

less (shallow)  $\eta'$  bound states

less hole-states

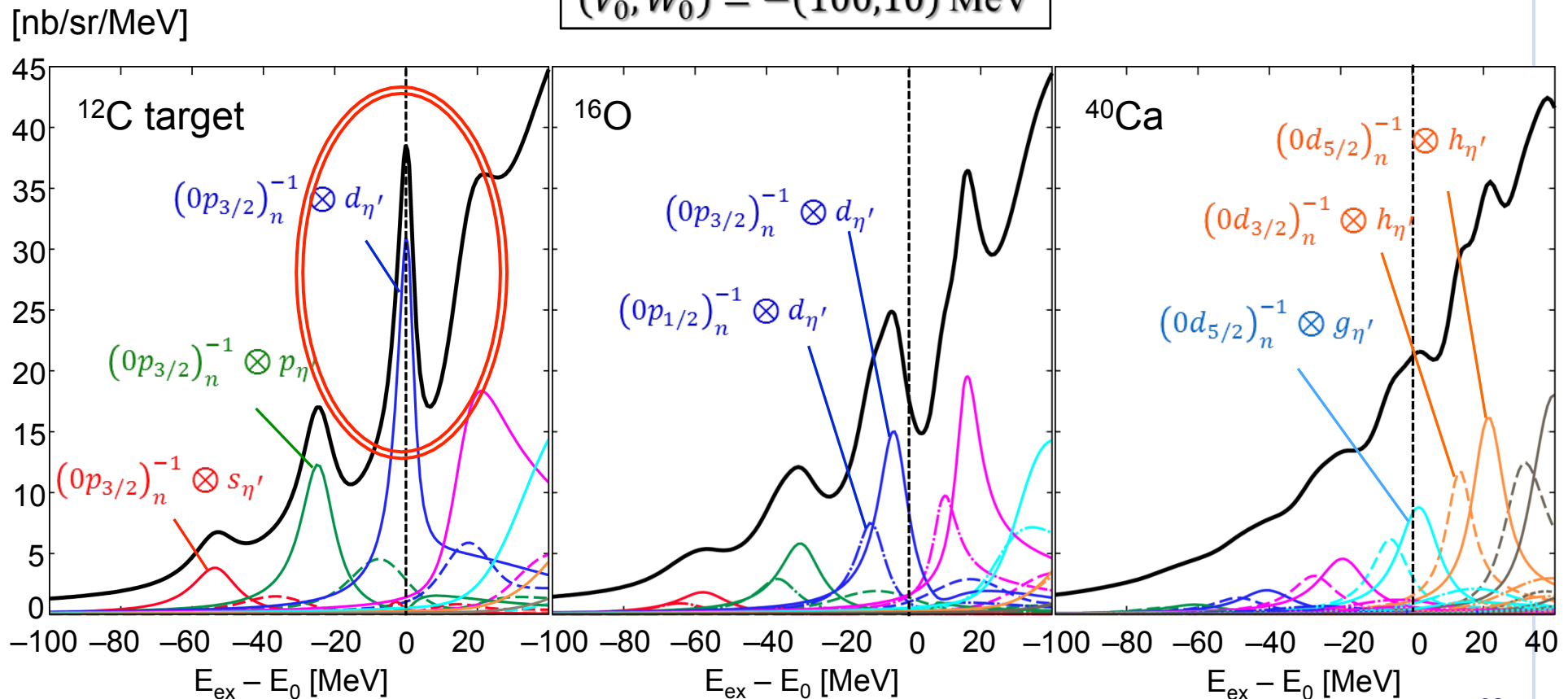
✓ simpler structure

many (deeper)  $\eta'$  bound states

many hole-states

✓ complex structure

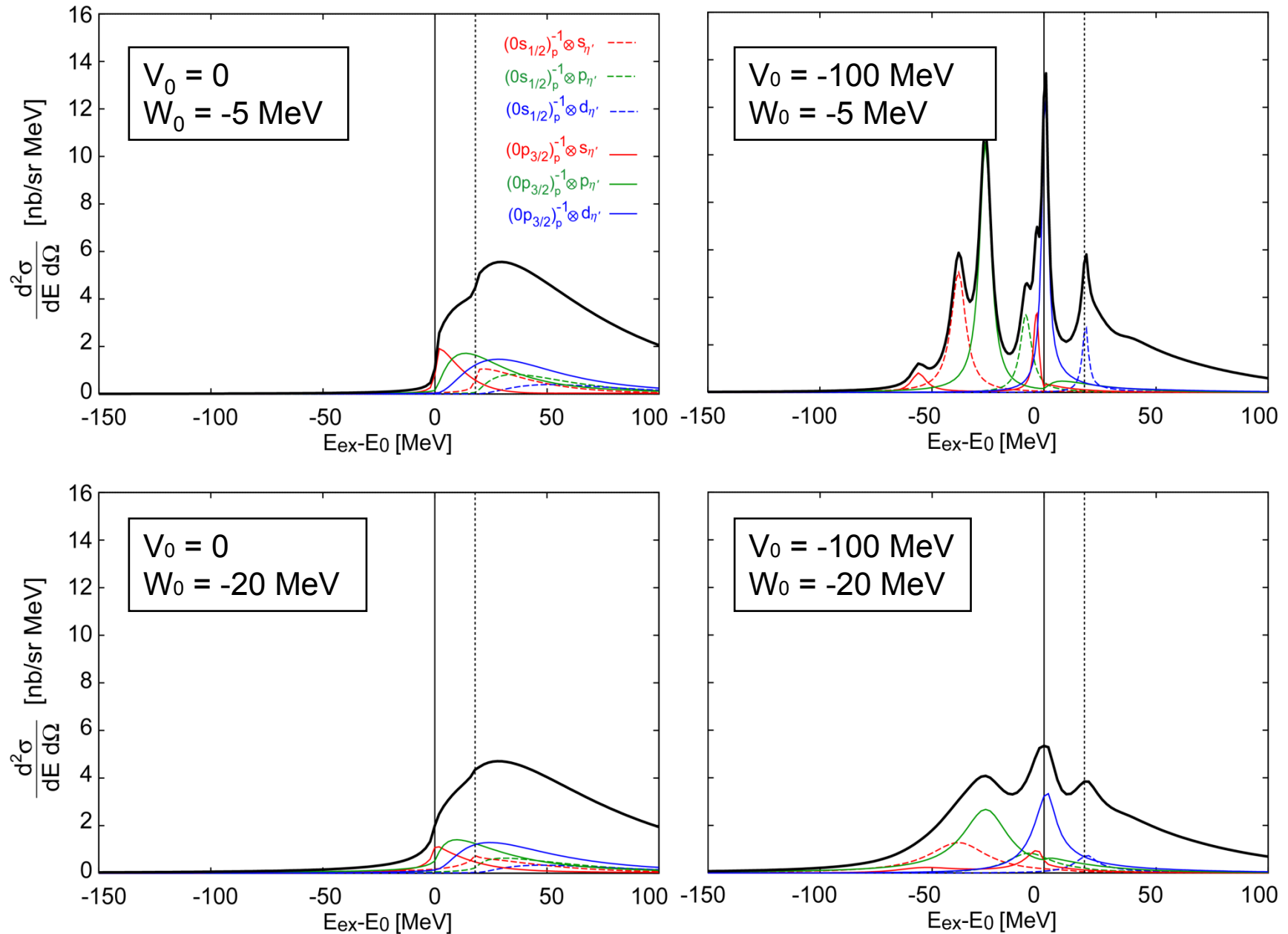
$(V_0, W_0) = -(100, 10)$  MeV



# Numerical Results : $^{12}\text{C}(\gamma, p)^{11}\text{B}_{\eta'}$

H.Nagahiro, S.Hirenzaki,

Phys.Rev.Lett.94 (2005)232503

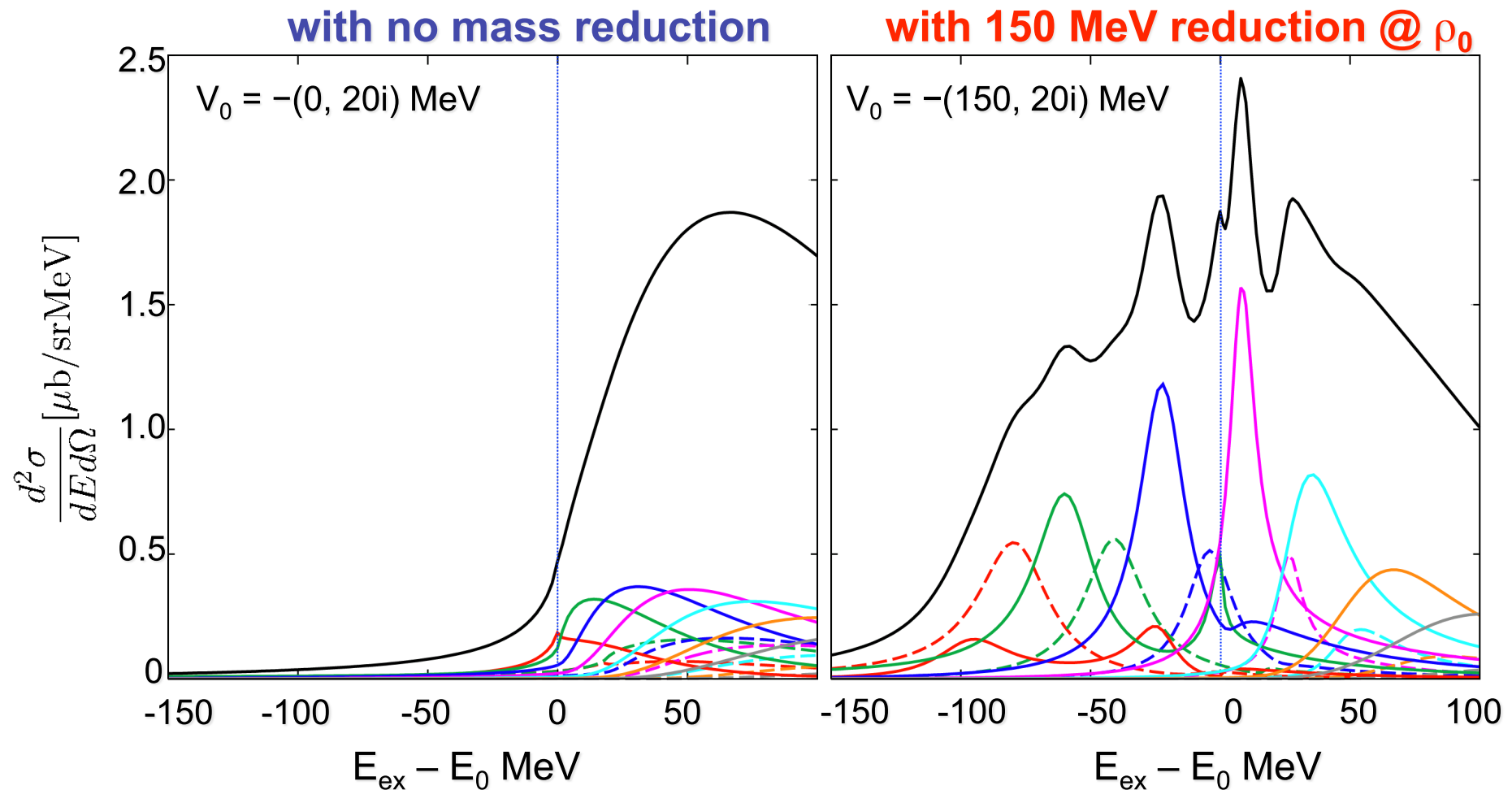


# $\eta'$ -mesic nuclei formation spectra : $^{12}\text{C}$ target : $(\pi^+, p)$ reaction @ JPARC

- $p_\pi = 1.8 \text{ GeV}/c$
- proton angle = 0 deg.

$$\left(\frac{d\sigma}{d\Omega}\right)^{Lab.} = 100 \mu\text{b/sr} \quad \text{case}$$

By H. Nagahiro  
PTP Suppl. 186(2010)316.



# $\eta'(958)$ -meson-nucleus bound system

Partial restoration of Chiral sym and  $U_A(1)$  anomaly effect  
in the viewpoint of mesic-nuclei

(possible) large mass reduction without large absorption

$$\text{Re}V \gg \text{Im}V$$

special feature of  $\eta'$

- ✓ attraction from 'elastic' interaction
- ✓ smaller inelastic channel

possibilities to observe bound state peaks

→ Experiment

# Summary

- Meson property at finite density,  
Meson-Nucleus systems
- Pionic atom: for getting deeper insights  
= information at various  $\rho$  and  $\rho_p / \rho_n$  ratio  
= Pionic atom in various nucleus including unstable nuclei
- $\eta'(958)$  : Anomaly effect at finite density  
(S. Sakai, Poster yesterday)
- Experimental determination of  $\langle N | \bar{s} s | N \rangle$   
by in-medium  $\Phi$  .