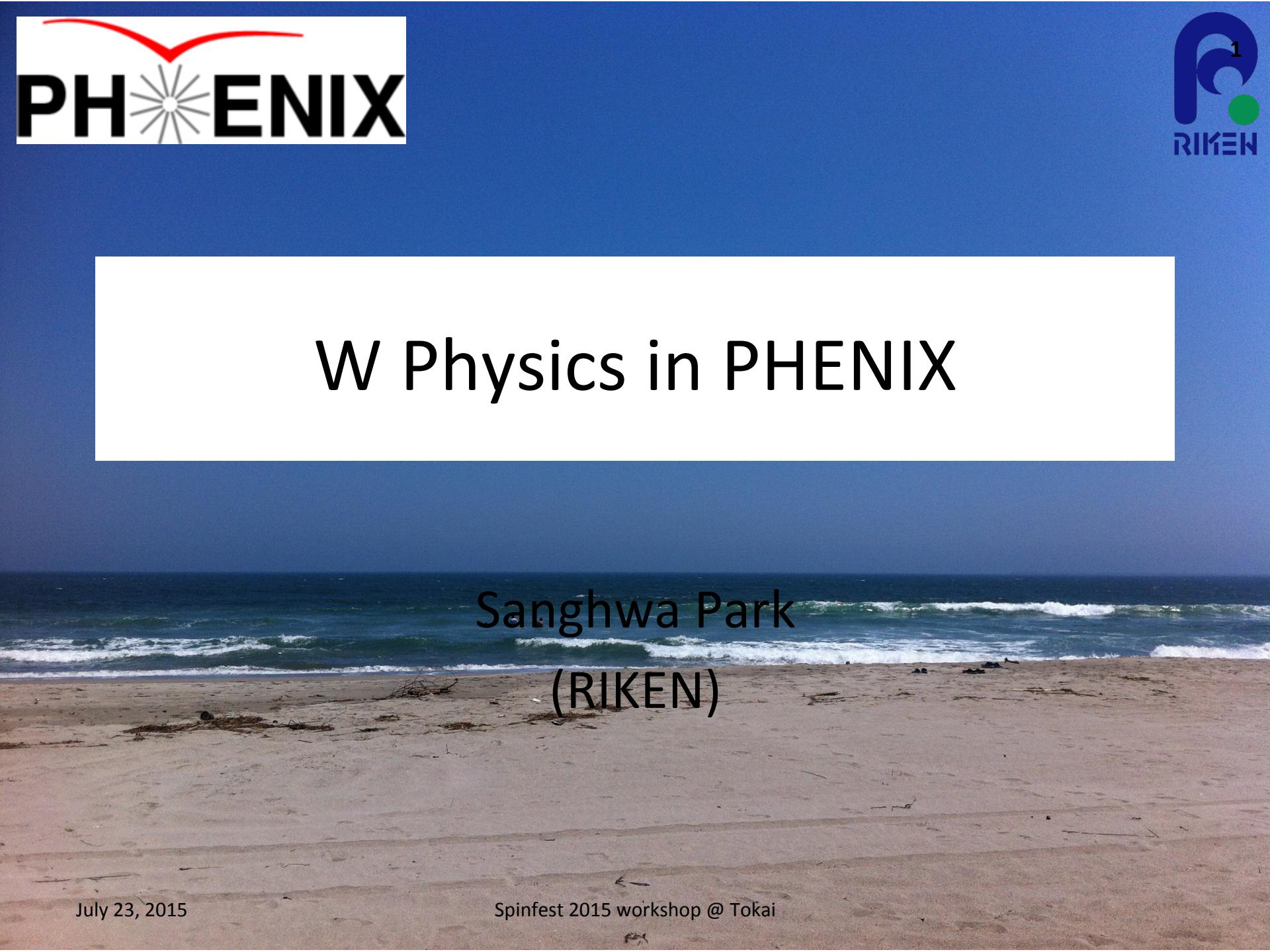


W Physics in PHENIX



Sanghwa Park
(RIKEN)

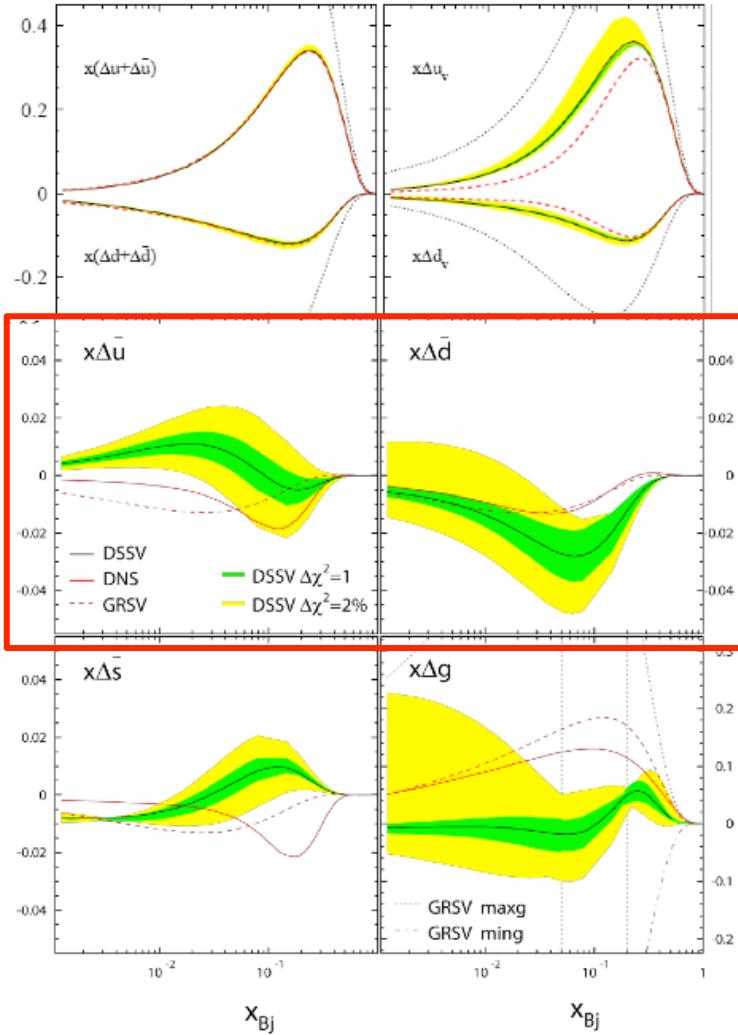
Outline

- Introduction
 - Physics motivation
 - W measurement
- PHENIX Experiment
 - Data
 - Detector configuration
- Analysis
- Results
- Summary

Motivation



De Florian et al. PRL 101, 072001 (2008)



$$\frac{1}{2} = \frac{1}{2} \Delta\Sigma + \Delta G + L_z$$

Quarks +
Anti-quarks

Gluon contributions

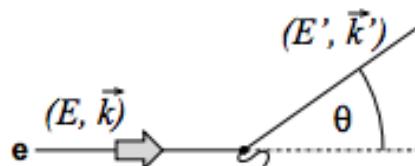
Quark & gluon orbital
angular momentum

$$\Delta\Sigma = (\Delta u + \Delta \bar{u}) + (\Delta d + \Delta \bar{d}) + (\Delta s + \Delta \bar{s})$$

- Well known combined quark PDFs by polarized DIS experiment.
- SIDIS sensitive to flavor separated quark and anti-quark PDFs
 - Limited by large uncertainties of fragmentation functions

What and How to Measure?

- Single Spin Asymmetry: $A(x, Q^2) = \frac{\sigma^+ - \sigma^-}{\sigma^+ + \sigma^-}$
- Semi-Inclusive Deep Inelastic Scattering (SIDIS):

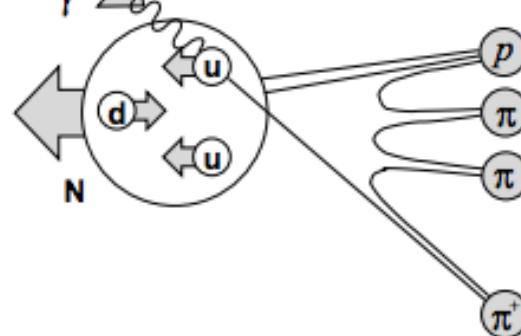
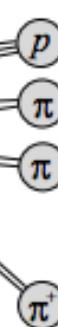


$$A_1^h(x, Q^2, z) = \frac{\sum_q e_q^2 \Delta q(x, Q^2) D_q^h(z, Q^2)}{\sum_{q'} e_{q'}^2 q'(x, Q^2) D_{q'}^h(z, Q^2)}$$

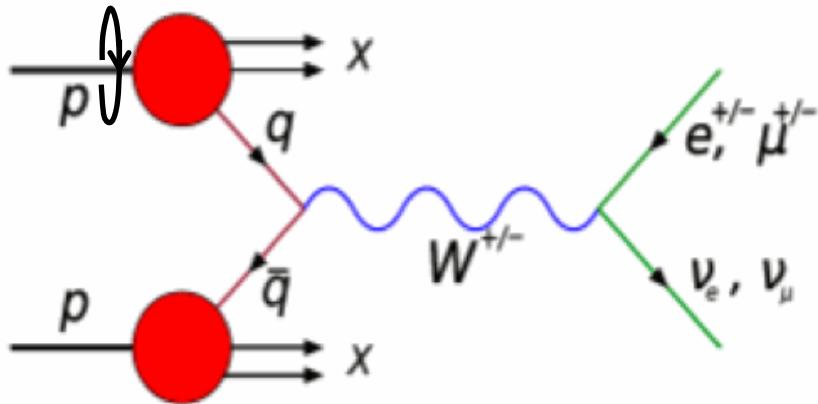
Fragmentation
Functions (FFs)

$u\bar{d} \rightarrow \pi^+$
$\bar{u}d \rightarrow \pi^-$
$u\bar{s} \rightarrow K^+$
\vdots

Flavor
tagging



W Measurement in polarized p+p collisions



$$A_L^{W^+} = \frac{\Delta \bar{d}(x_1)u(x_2) - \Delta u(x_1)\bar{d}(x_2)}{\bar{d}(x_1)u(x_2) + u(x_1)\bar{d}(x_2)}$$

$$A_L^{W^-} = \frac{\Delta \bar{u}(x_1)d(x_2) - \Delta d(x_1)\bar{u}(x_2)}{\bar{u}(x_1)d(x_2) + d(x_1)\bar{u}(x_2)}$$

- High scale set by W mass
- Maximum parity violation of weak interaction.
→ Fixed helicity of incoming quark and antiquark.

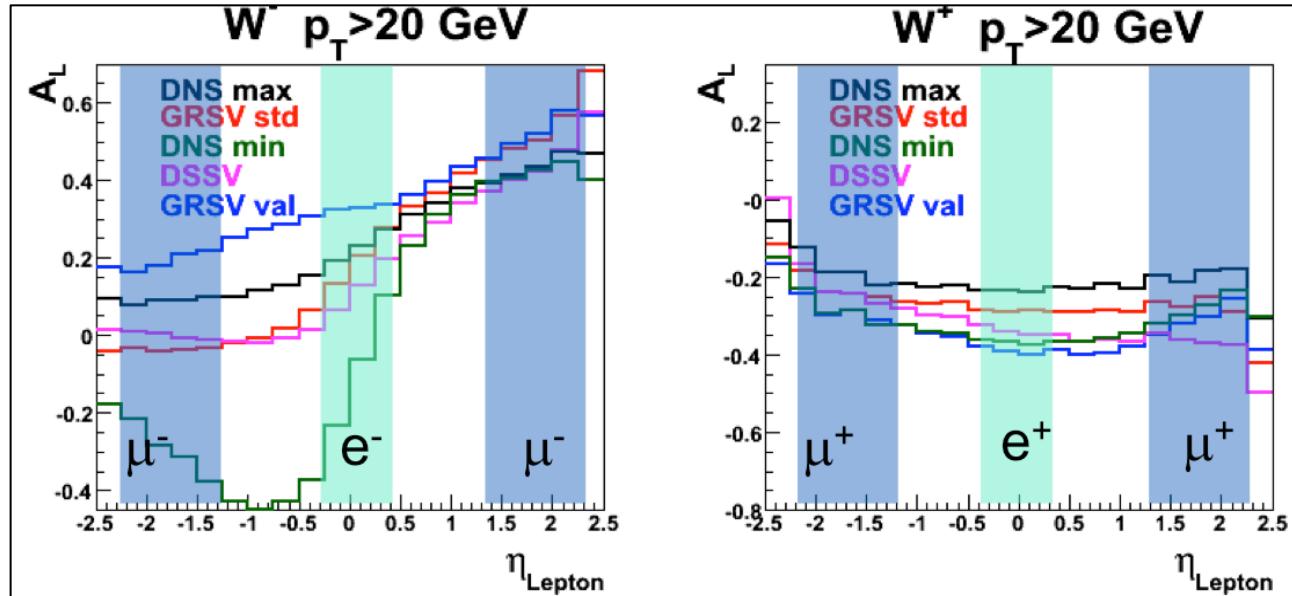
$$u_L \bar{d}_R \rightarrow W^+$$

$$d_L \bar{u}_R \rightarrow W^-$$

→ Independent from FFs

- Direct probe of the flavor-separated PDFs $\Delta u, \Delta \bar{u}, \Delta d, \Delta \bar{d}$

W Measurement in polarized p+p collisions



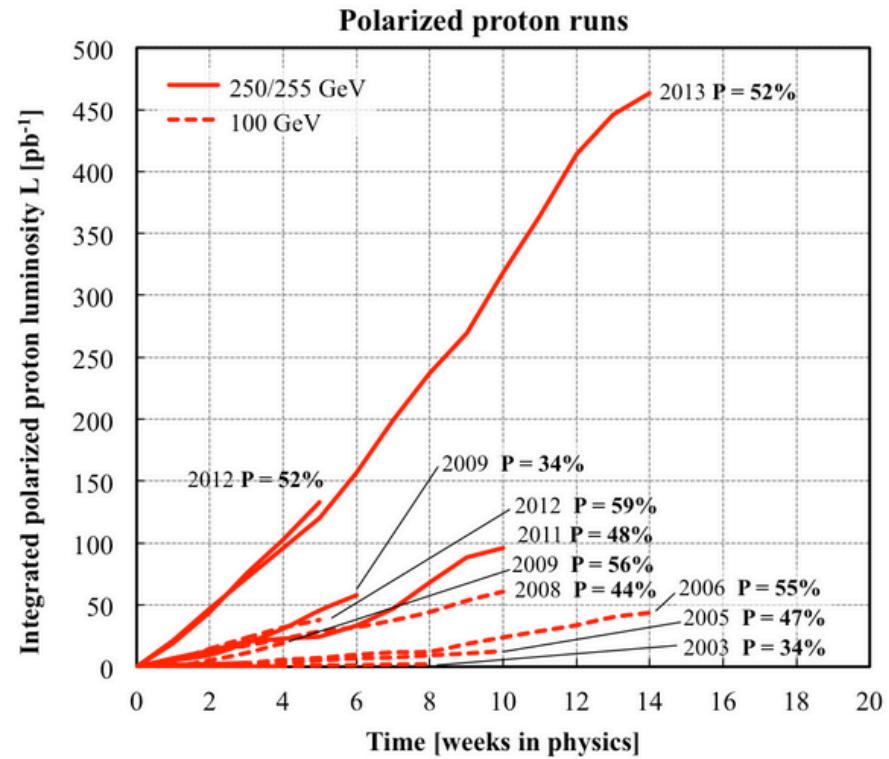
$$A_L^{W^-} \approx \frac{\Delta \bar{u}(x_1) d(x_2)(1-\cos\theta)^2 - \Delta d(x_1) \bar{u}(x_2)(1+\cos\theta)^2}{\bar{u}(x_1) d(x_2)(1-\cos\theta)^2 + d(x_1) \bar{u}(x_2)(1+\cos\theta)^2}$$

$$A_L^{W^+} \approx \frac{\Delta \bar{d}(x_1) u(x_2)(1+\cos\theta)^2 - \Delta u(x_1) \bar{d}(x_2)(1-\cos\theta)^2}{\bar{d}(x_1) u(x_2)(1+\cos\theta)^2 + u(x_1) \bar{d}(x_2)(1-\cos\theta)^2}$$

- Quark flavor mixed at mid-rapidity
- Sensitive to anti-quark polarization at forward/backward measurement

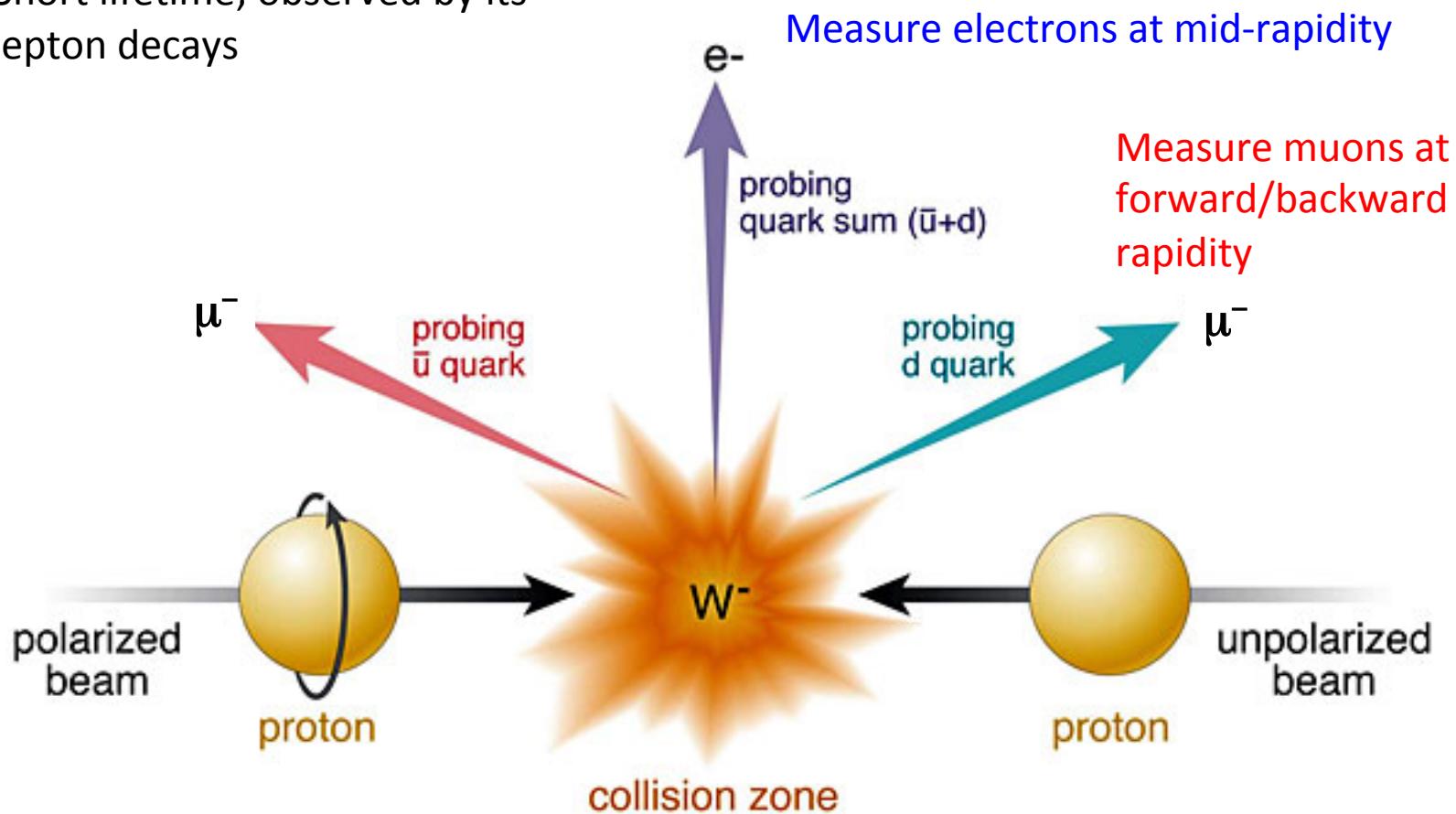
Polarized p+p data @ RHIC

- Longitudinally polarized p+p data taking 2009 - 2013 at $\sqrt{s} = 510$ (500) GeV.
- Accumulated data over 300pb^{-1} (multiple collision corrected)

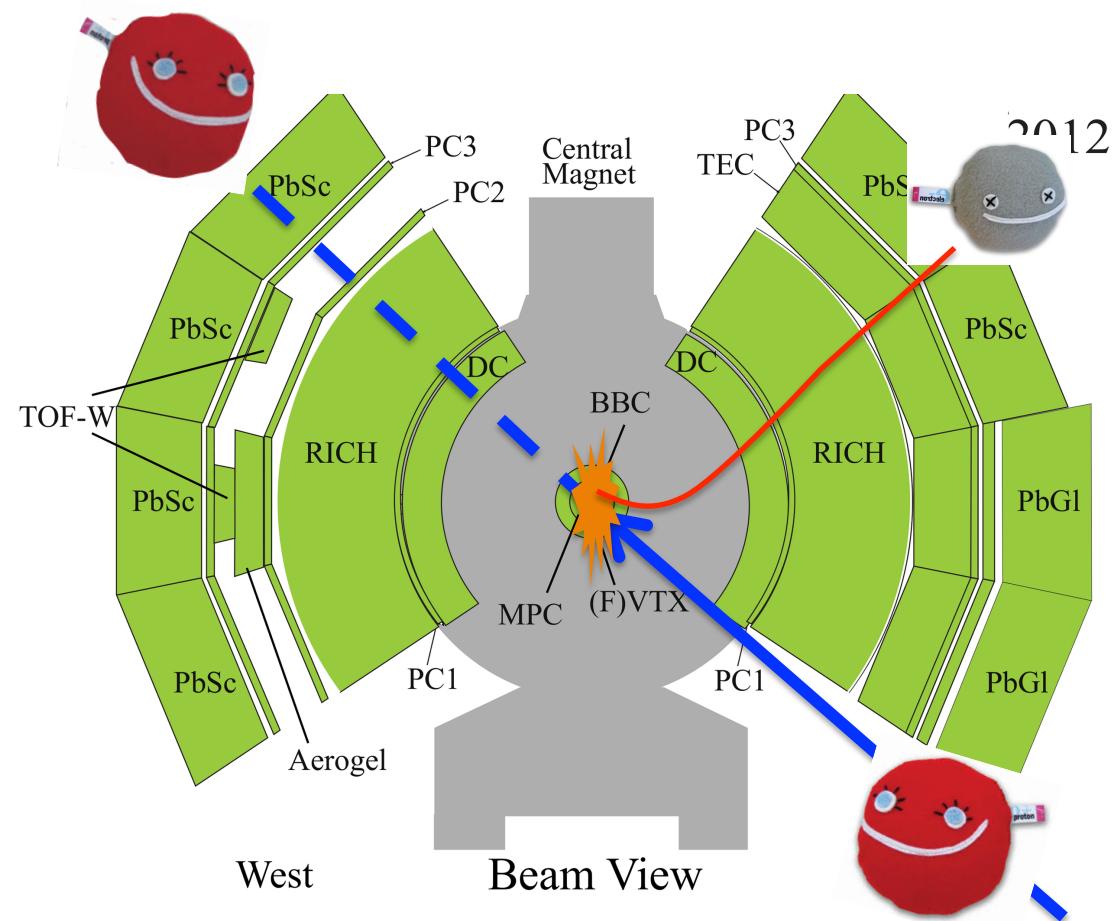
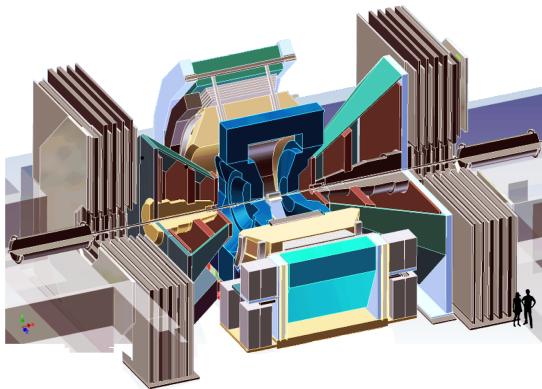


W Measurement @ PHENIX

- W is massive (~ 80 GeV)
- Short lifetime; observed by its lepton decays



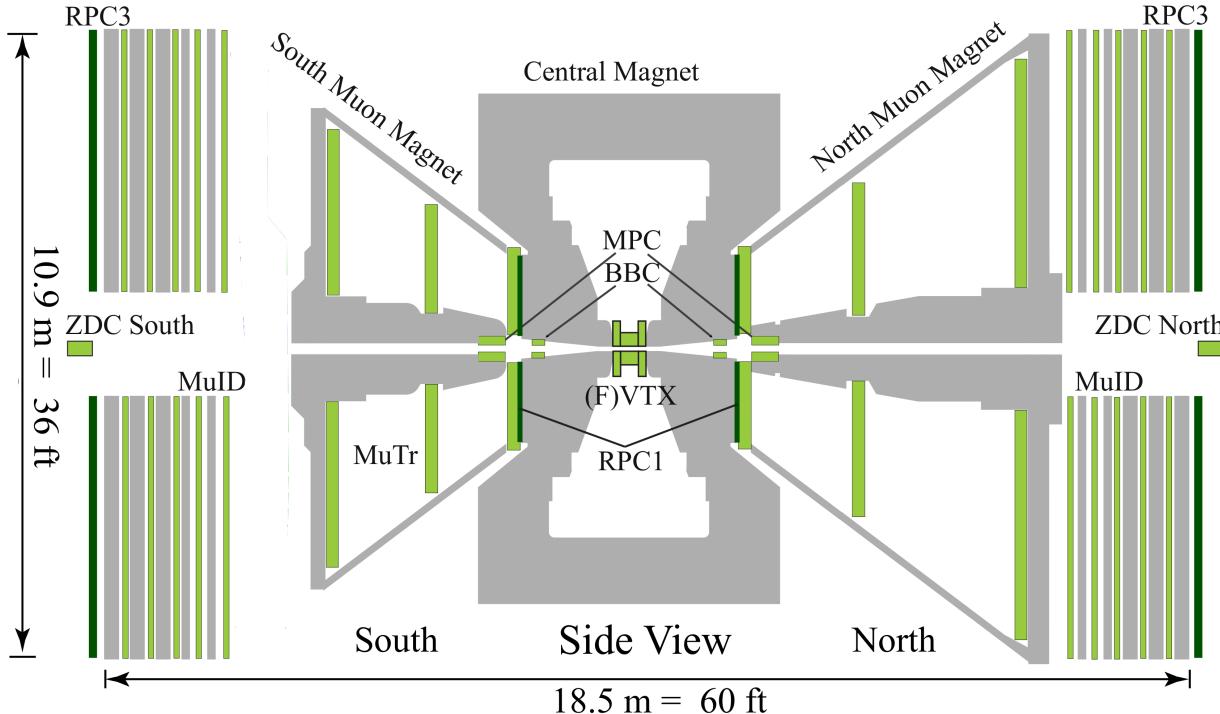
PHENIX Central Arm Detector



- **Measure $W \rightarrow e$**
- $|\eta| < 0.35$
- $\Delta\phi = \pi$
- **Electromagnetic Calorimeter**
- **DC and PC for tracking and charge separation**

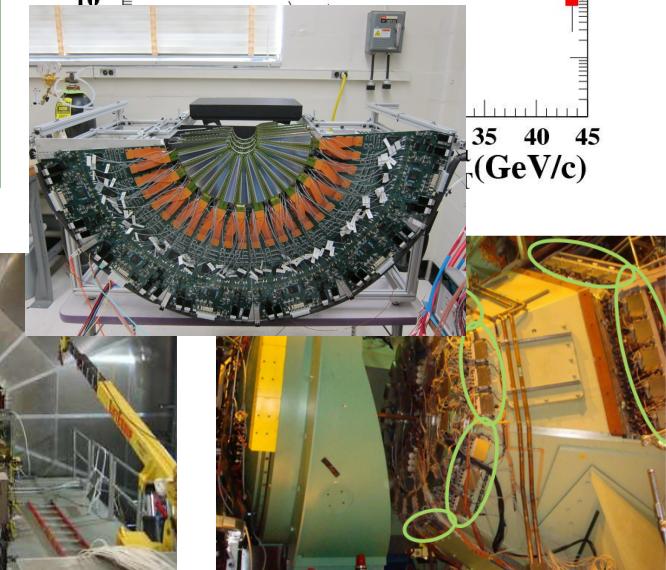
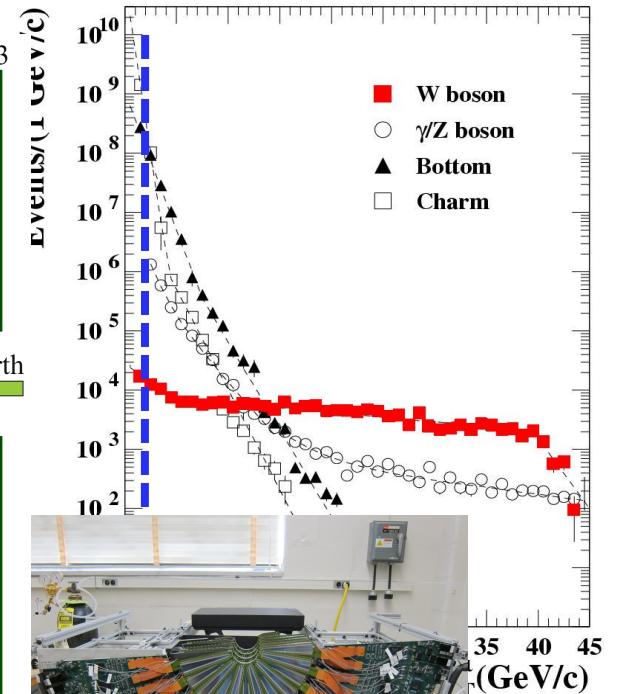
PHENIX Forward Arm Detector

- Forward upgrade

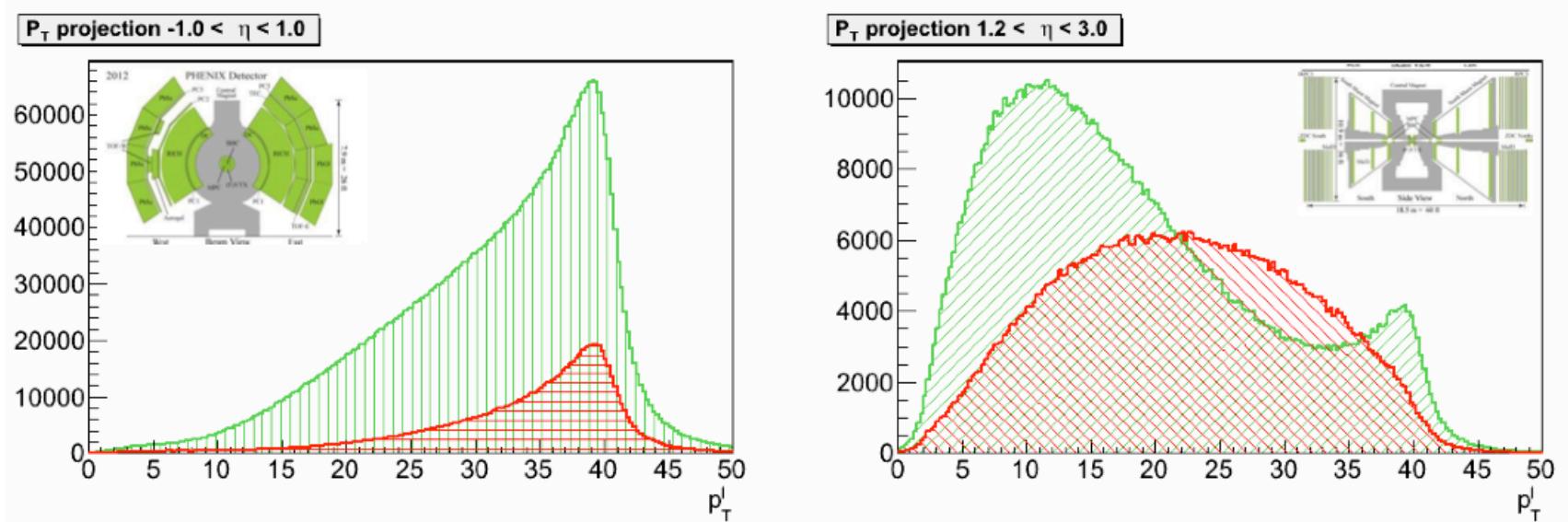


- $1.2 < |\eta| < 2.4, \Delta\phi = 2\pi$
- Fully upgraded in 2012
- MuTr, MuID
- High- p_T trigger:
small bending in magnetic field
+ timing (BBC / RPC)
- RPCs, FVTX: Additional BG rejection

Inclusive μ Production, 500 GeV/c



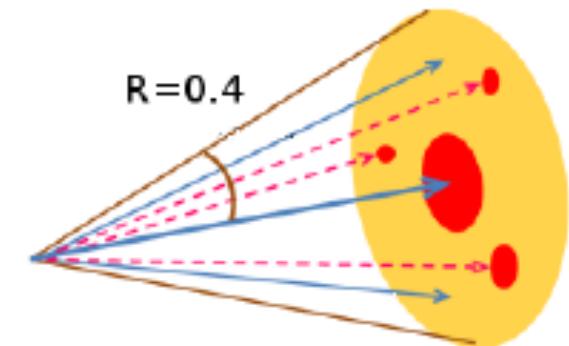
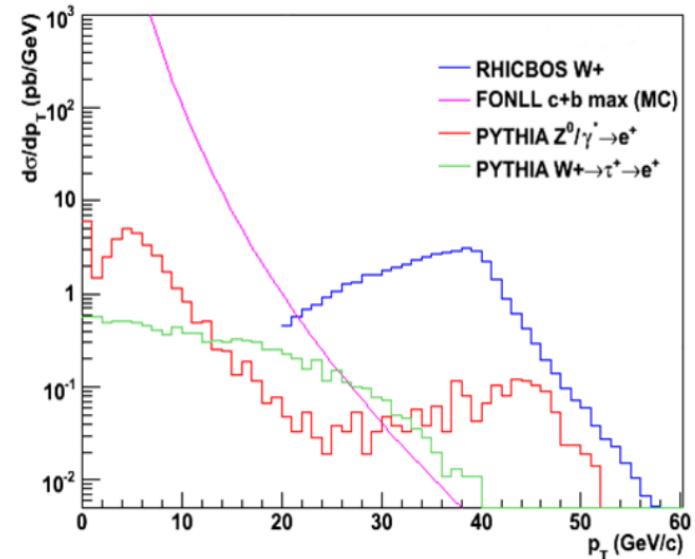
W Kinematics



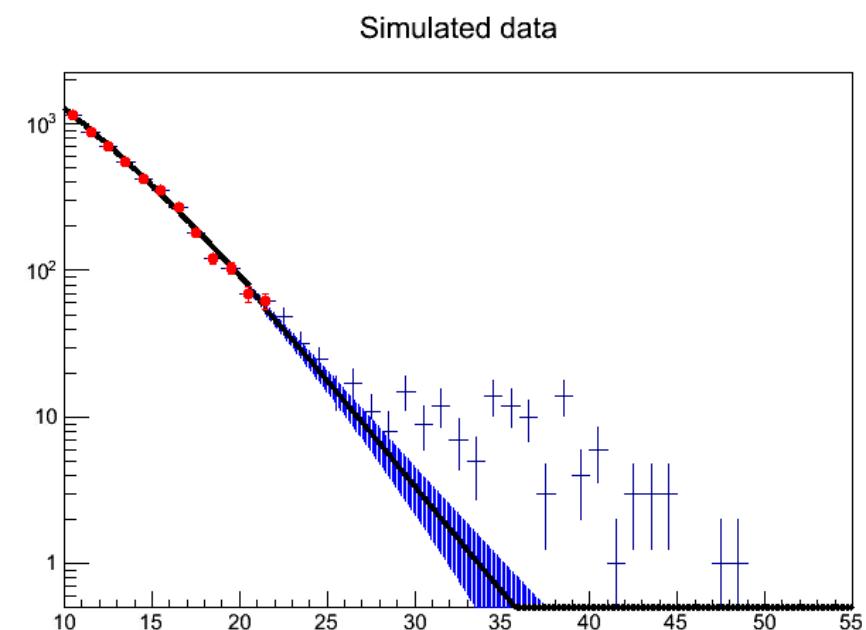
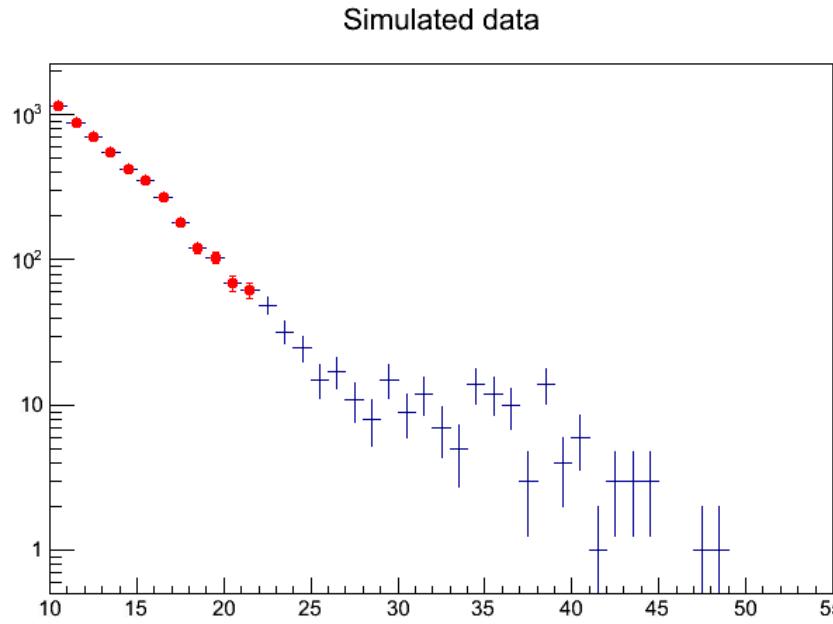
- Different kinematics at mid-rapidity and forward rapidity
- Jacobian peak is only visible at mid-rapidity
- Different analysis approach to identify W

Mid-rapidity Measurement

- Background:
 - Photons from neutral pion/eta decays followed by e^\pm pair production
 - Cosmic rays
 - Beam related backgrounds
 - Z, charm and bottom, other W decays
- Reduce background and estimate contribution between 30 and 50 GeV
 - Measure high pT electrons using EMCAL
 - DC-EMCAL matching ($\Delta\varphi < 0.01$ rad)
- Relative isolation cut:
 - Main background discriminator
 - Energy in a cone of $R=0.4$ divided by energy of the candidate
 - reduces background by a factor of 10

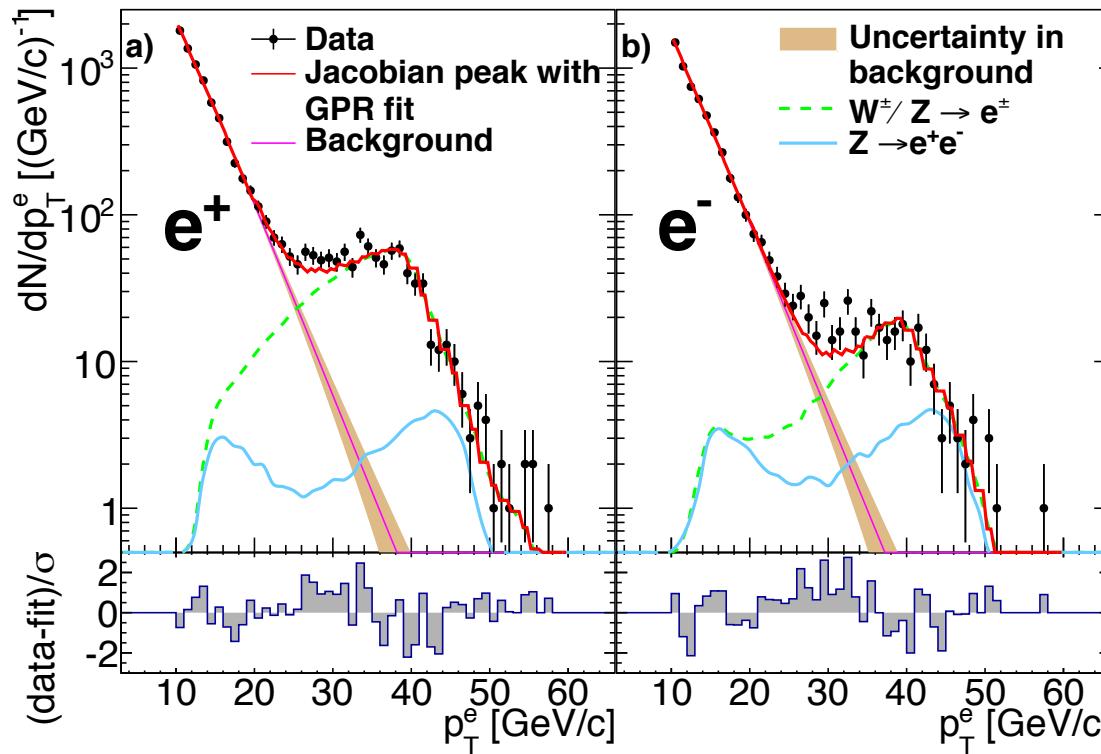


Gaussian Process Regression



- Use background control region to extrapolate a shape in the 30 to 50 GeV region
- The GPR will give a background contribution and uncertainty
- Cross check with a classical functional form (modified power law) showed good agreement

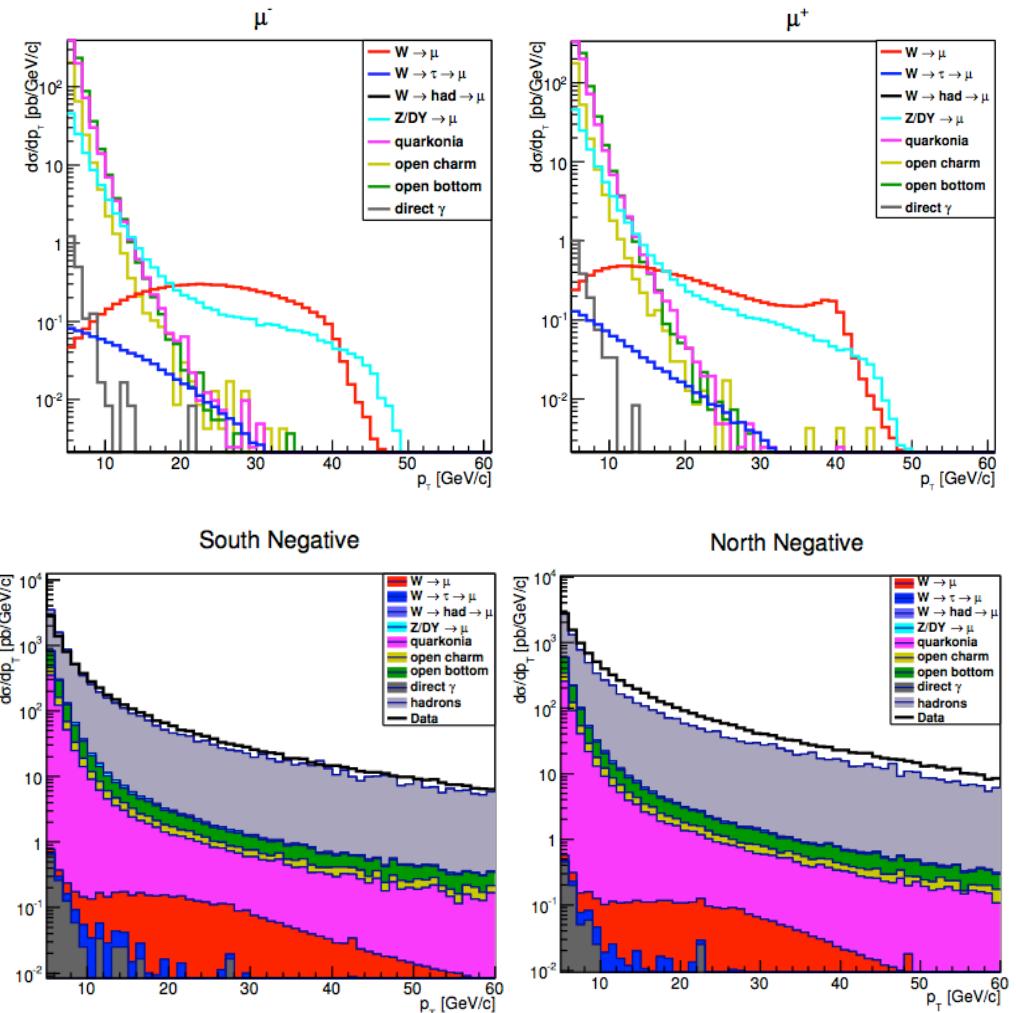
p_T Spectra



- Fitting with simulated Jacobian peak and GPR background shape
- Estimate the signal-to-background ratio in the signal region (30-50 GeV)
- 97% (94%) of positron signal remains for e^+ (e^-)

Forward Rapidity Measurement

- Real muon background:
 - Open heavy flavor, quarkonium, DY/Z
 - Get smeared into high pT region
- Looking for W at $p_T > 16 \text{ GeV}/c$
- Large Hadron BG contamination: low pT charged kaons, pions.
- Careful signal identification required.

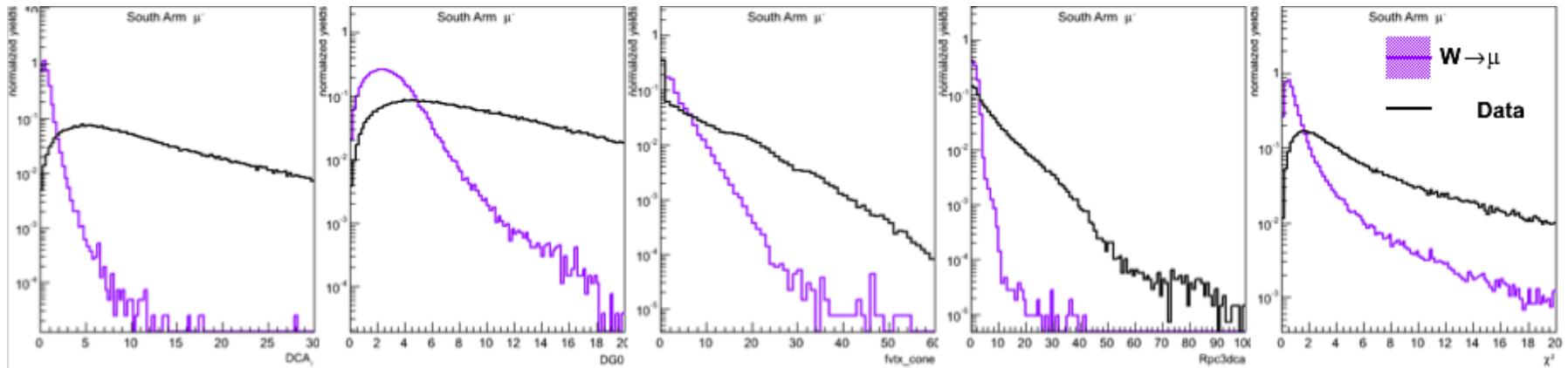


Background reduction

- Multivariate analysis using likelihood approach
- Signal purity < 1%: use data as background shape at the initial stage
- Define likelihood ratio (Wness) based on signal (MC) and BG shapes (data):

$$W_{\text{ness}} \equiv \frac{\lambda_{\text{sig}}(x)}{\lambda_{\text{sig}}(x) + \lambda_{\text{BGs}}(x)}$$

$\lambda = p(\text{DG0}, \text{DDG0})p(\text{chi2}, \text{DCAr})$
 $p(\text{RPC_DCA})p(\text{FVTX_match})p(\text{FVTX_cone})$

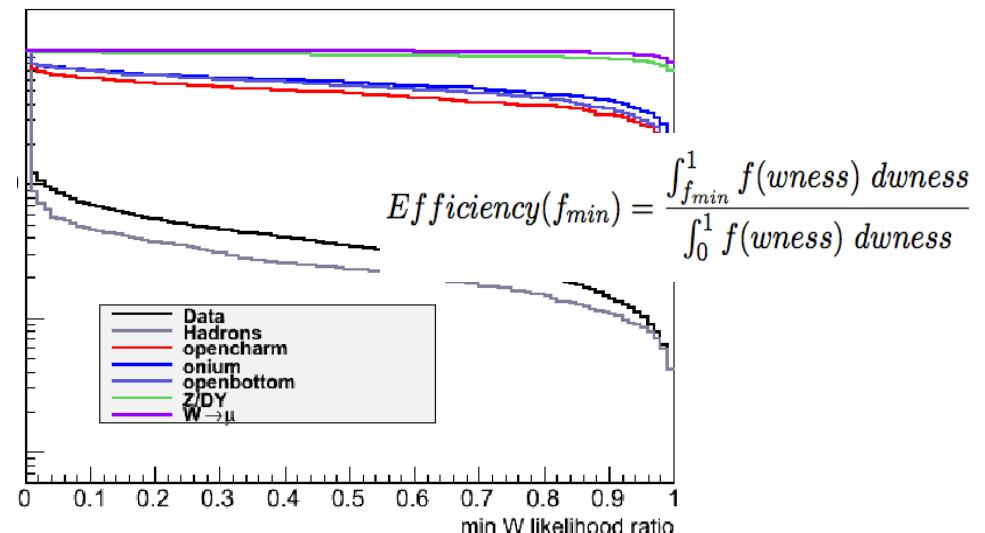
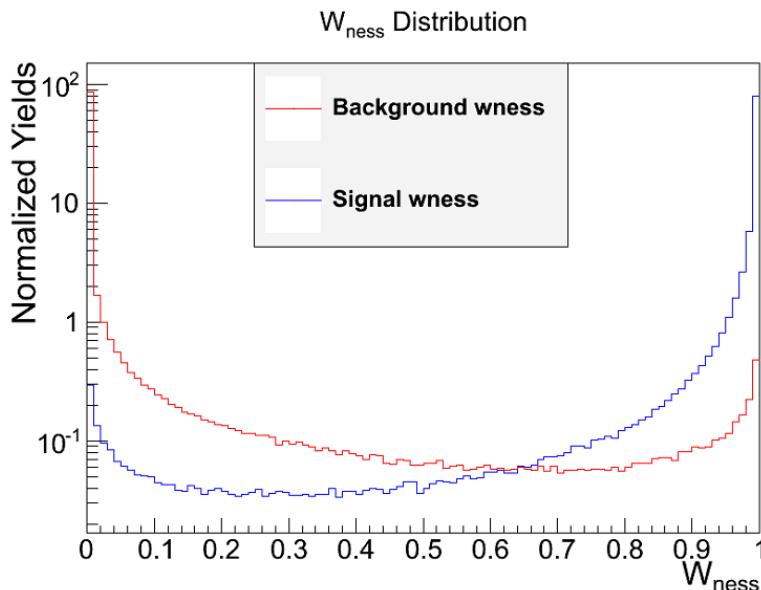


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- Define likelihood ratio (W_{ness}) based on signal (MC) and BG shapes (data):

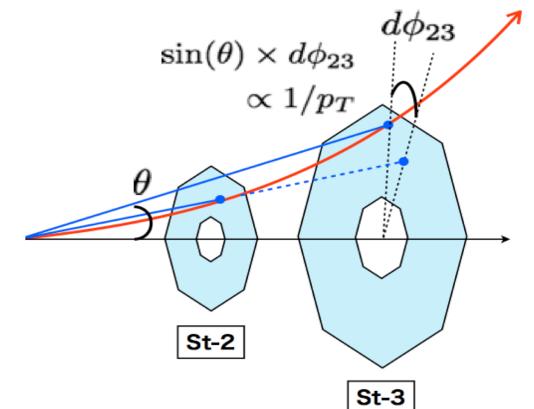
$$W_{\text{ness}} \equiv \frac{\lambda_{\text{sig}}(x)}{\lambda_{\text{sig}}(x) + \lambda_{\text{BGs}}(x)}$$

wness [wness → 1: signal-like event
wness → 0: background-like event

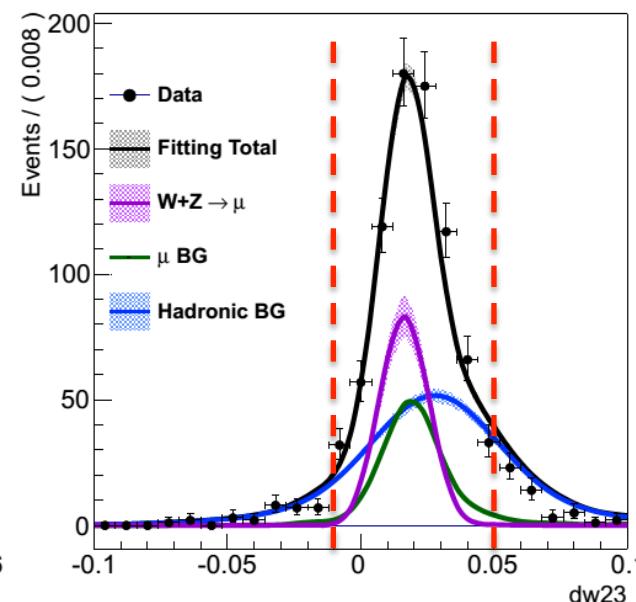
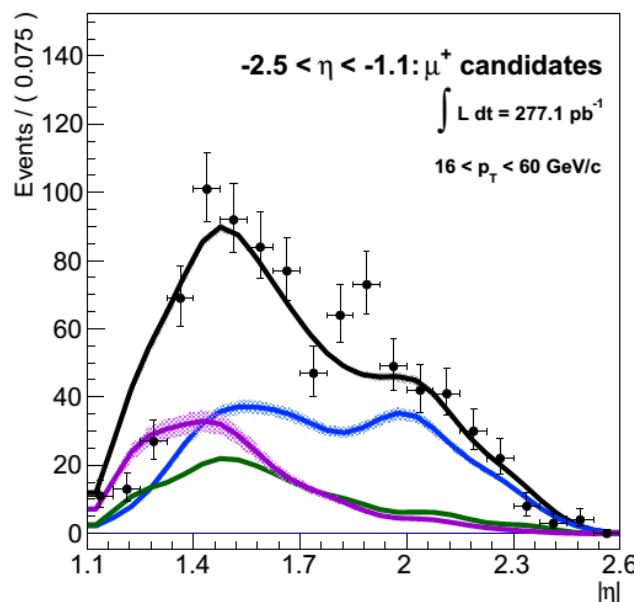


W Signal Fit

- After the pre-selection, perform 2D unbinned maximum likelihood fit in independent variables: rapidity, effective bending angle (dw_{23})

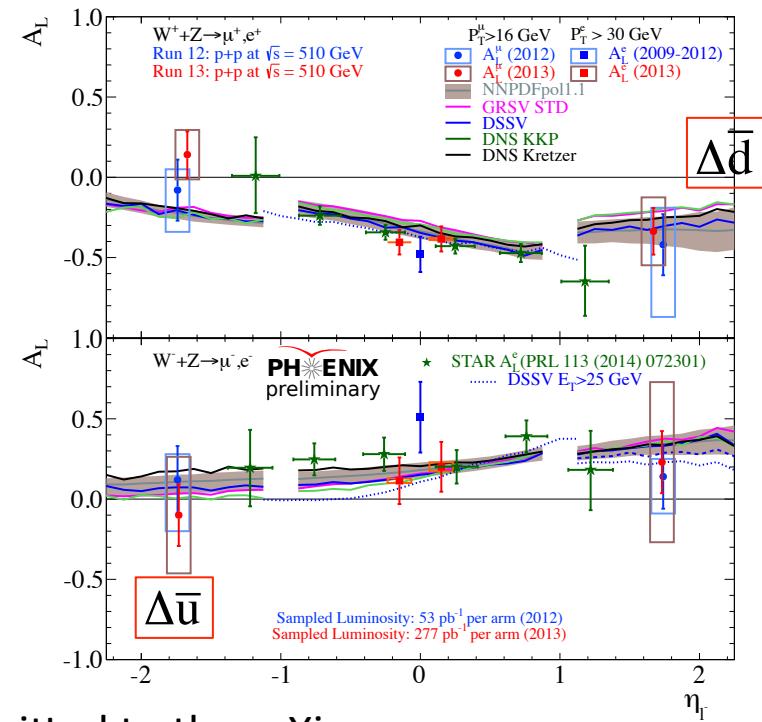
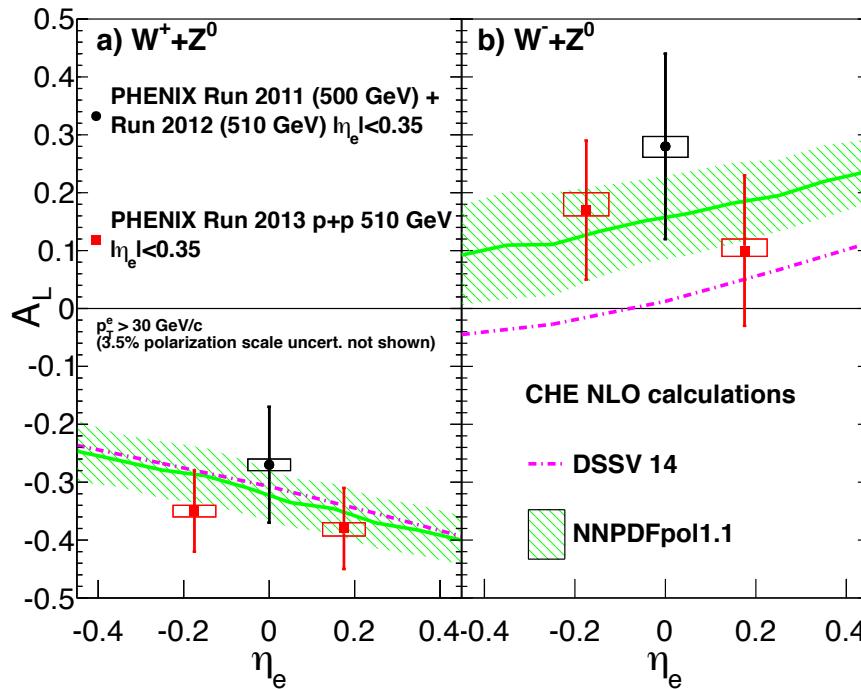


$$dw_{23} = p_T \times \sin \theta \times d\phi_{23}$$



A_L Results

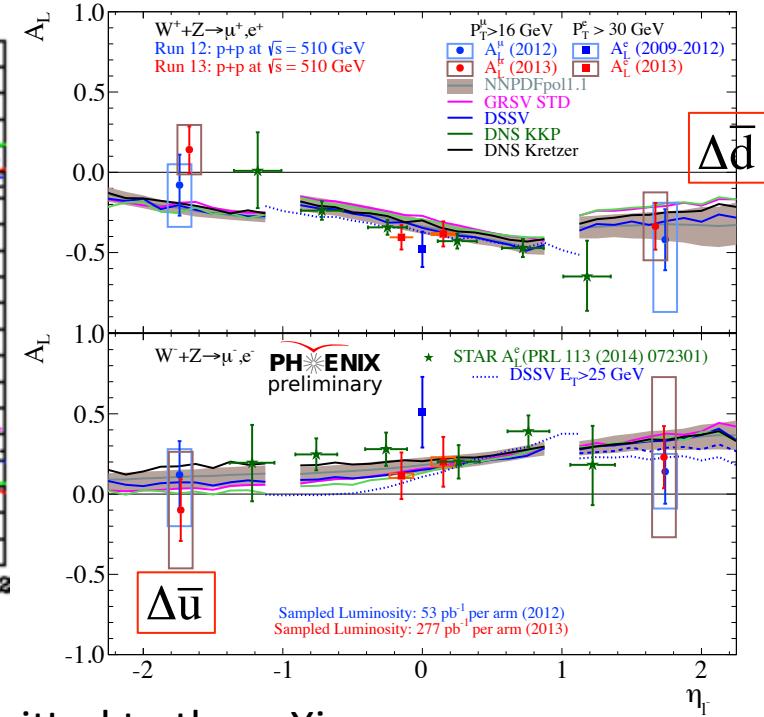
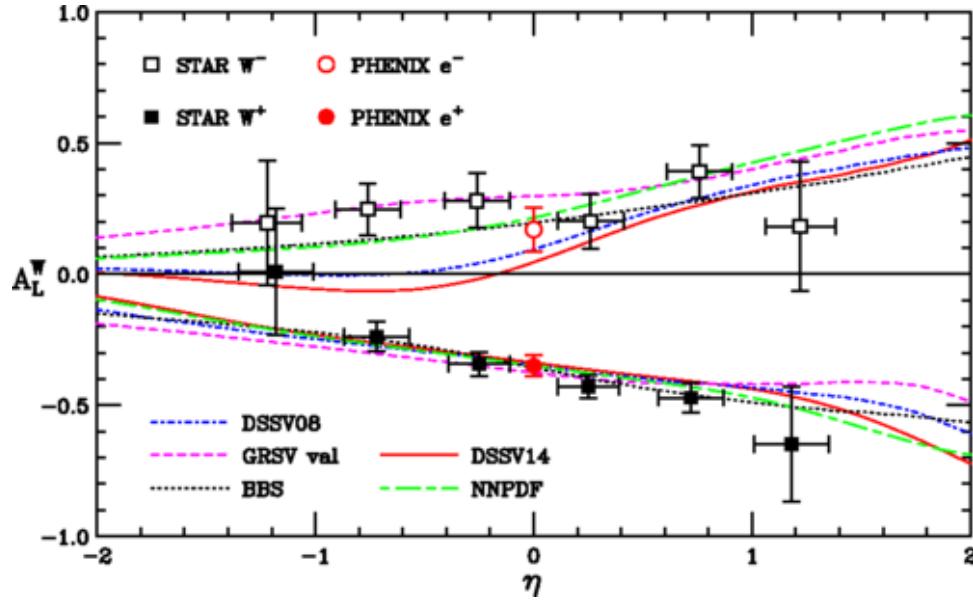
arXiv:1504.07451v1 [hep-ex]



- Mid-rapidity results has been recently submitted to the arXiv
 - included in the recent global analysis
- Preliminary results at forward/backward rapidities
- Mid-rapidity and forward rapidity results show good agreement with theory predictions
- AL at backward rapidity tends to be smaller/positive

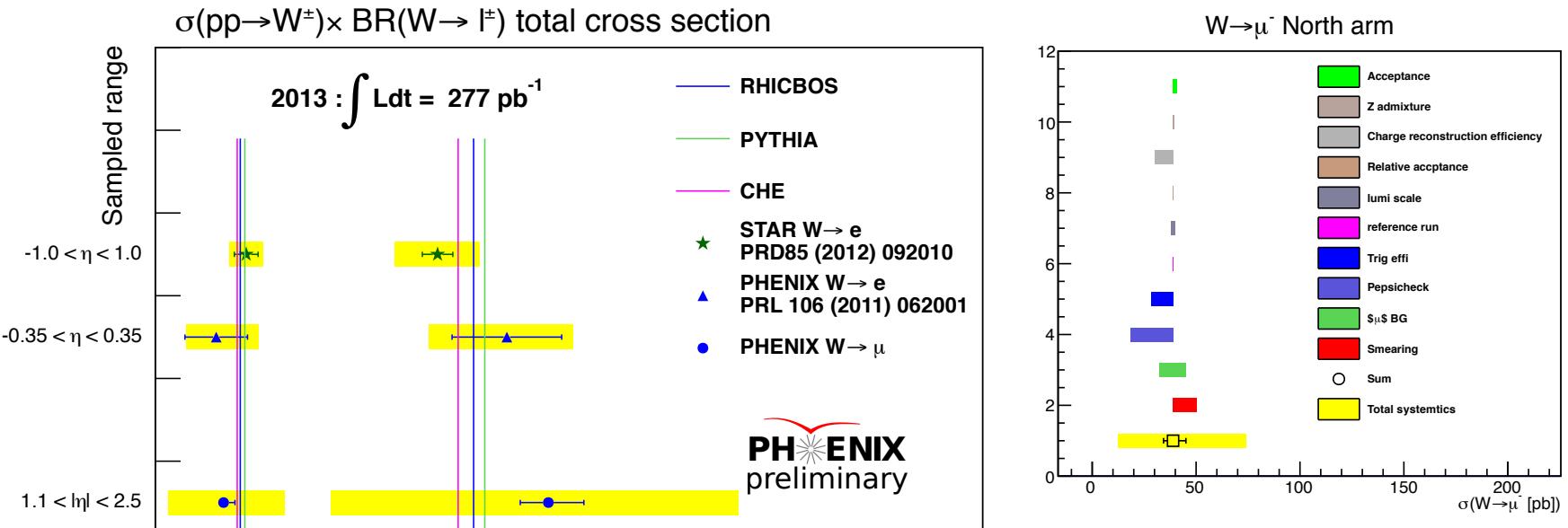
A_L Results

Phys. Rev. D 91, 094033 (2015)



- Mid-rapidity results has been recently submitted to the arXiv
- Preliminary results at forward/backward rapidities
- Mid-rapidity and forward rapidity results show good agreement with theory predictions
- AL at backward rapidity tends to be smaller/positive

Cross Section Results



Contributions to systematic uncertainty for $W \rightarrow \mu$

- Cross section for the $W \rightarrow e$ using 2009 data (Phys.Rev.Lett. 106:062001)
- Preliminary for the $W \rightarrow \mu$ using 2013 data: consistent with prediction within large systematic uncertainty

Summary

- W cross section, single spin asymmetry A_L are measured using all available data collected at PHENIX
- Mid-rapidity measurement ($W \rightarrow e$):
 - Final A_L result has been submitted to the arXiv
 - Work in progress on the cross section measurement using 2013 data
- Forward rapidity measurement ($W \rightarrow \mu$):
 - Preliminary results
 - Ongoing analysis efforts to reduce systematics

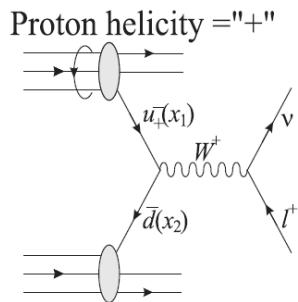


Backup

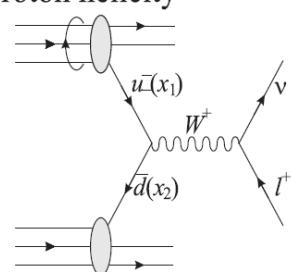


W measurement

(a)



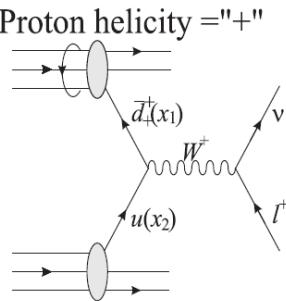
Proton helicity = "+"



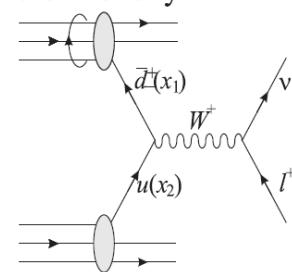
$$A_L^{W+}(y) = \frac{-u^+(x_1)\bar{d}(x_2) - (-u^-(x_1))\bar{d}(x_2)}{u^+(x_1)\bar{d}(x_2) + u^-(x_1)\bar{d}(x_2)}$$



(b)



Proton helicity = "+"

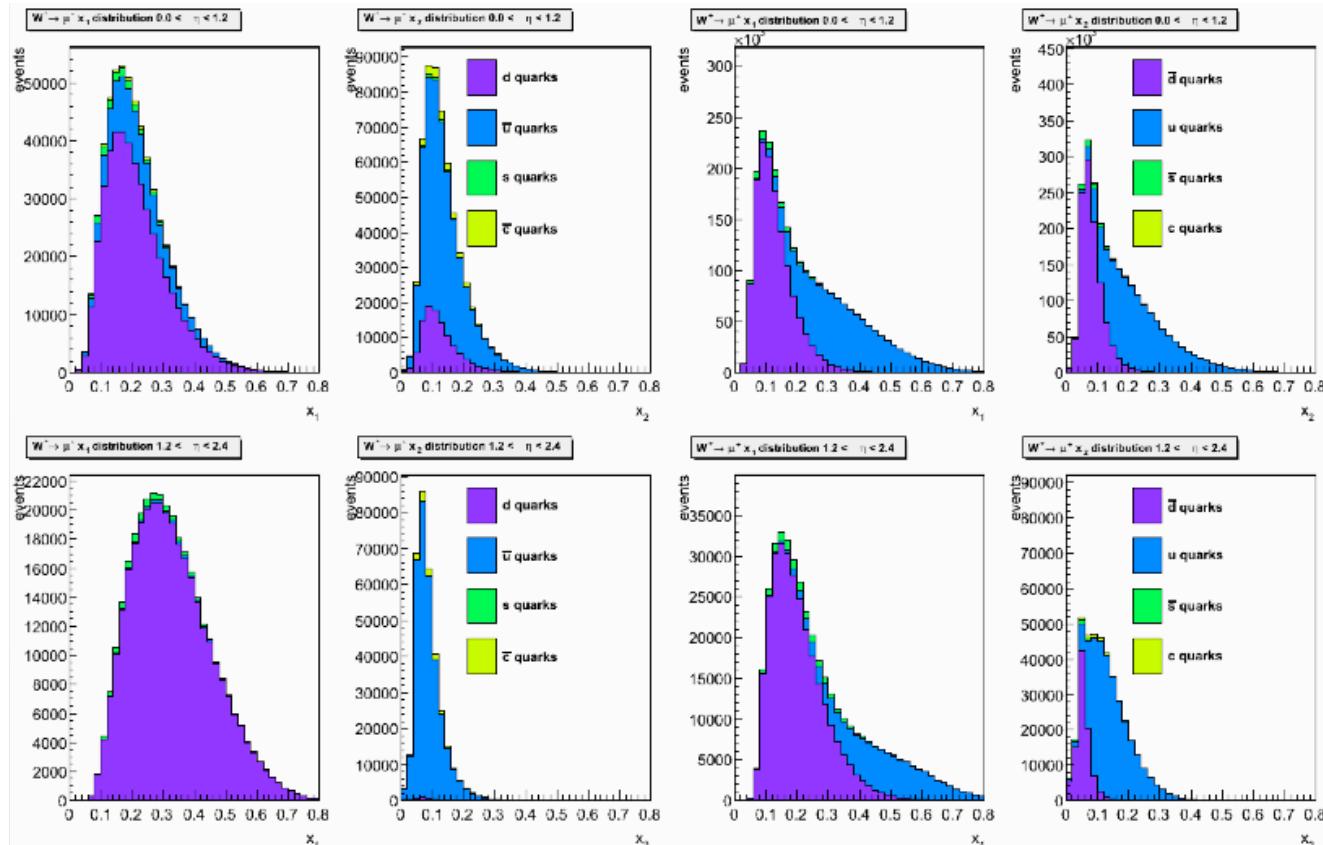


$$A_L^{W+}(y) = \frac{\bar{d}^+(x_1)u(x_2) - \bar{d}^-(x_1)u(x_2)}{\bar{d}^+(x_1)u(x_2) + \bar{d}^-(x_1)u(x_2)}$$



$$A_L^{W+}(y) = \frac{\Delta\bar{d}(x_1)u(x_2) - \Delta u(x_1)\bar{d}(x_2)}{\bar{d}(x_1)u(x_2) + u(x_1)\bar{d}(x_2)}$$

PYTHIA: x_1, x_2

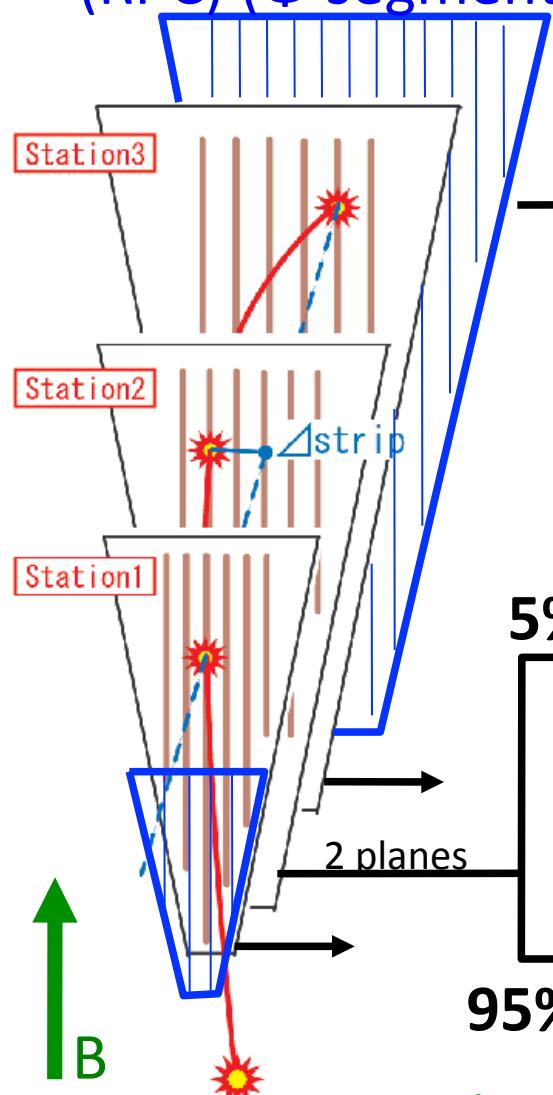


$$A_L^{e+} = \frac{\Delta \bar{d}(x_1)u(x_2)(1 + \cos \theta_l)^2 - \Delta u(x_1)\bar{d}(x_2)(1 - \cos \theta_l)^2}{\bar{d}(x_1)u(x_2)(1 + \cos \theta_l)^2 + u(x_1)\bar{d}(x_2)(1 - \cos \theta_l)^2}$$

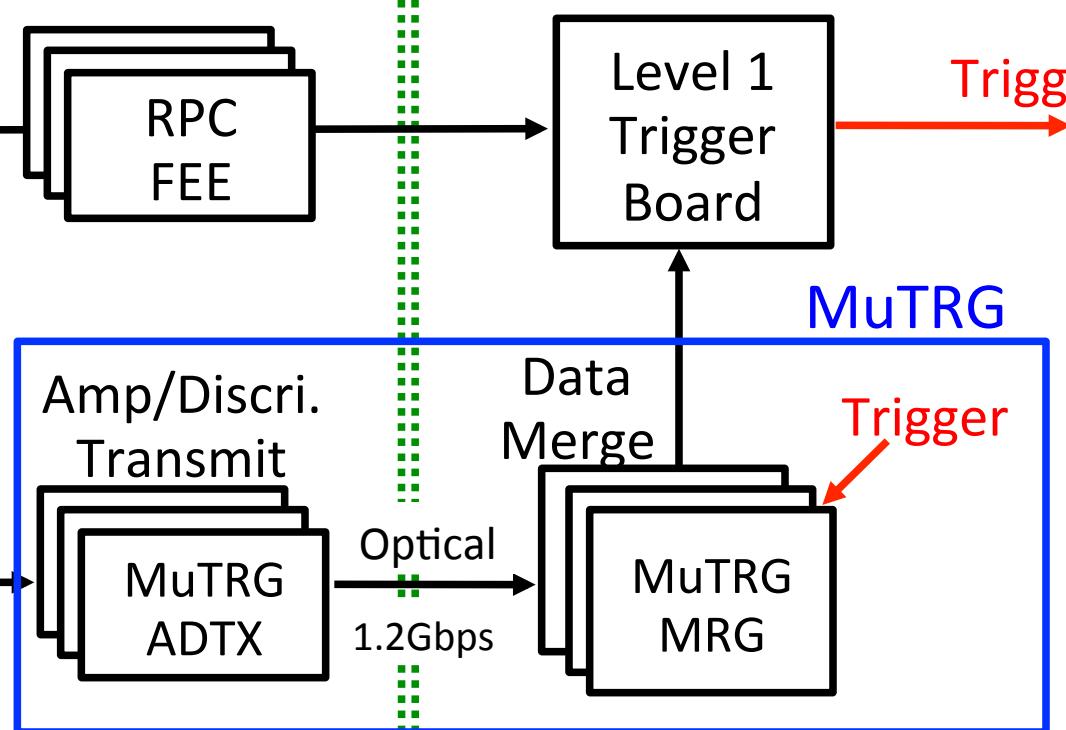
$$A_L^{e-} = \frac{\Delta \bar{u}(x_1)d(x_2)(1 - \cos \theta_l)^2 - \Delta d(x_1)\bar{u}(x_2)(1 + \cos \theta_l)^2}{\bar{u}(x_1)d(x_2)(1 - \cos \theta_l)^2 + d(x_1)\bar{u}(x_2)(1 + \cos \theta_l)^2}.$$

W Trigger System

Resistive Plate Counter
(RPC) (Φ segmented)



Trigger events with straight track
(e.g. Δ strip ≤ 1)

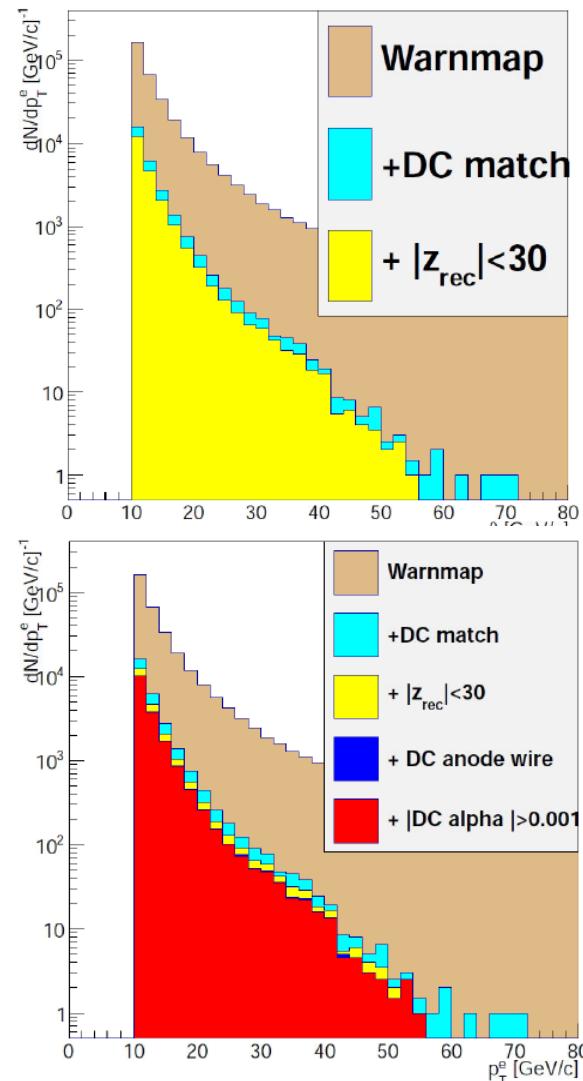


RPC / MuTRG data are also recorded on disk.

Interaction Region Rack Room

Event selection and basic cuts

- Select high EMCal clusters
- Match to DC tracks
- Reconstruct the z vertex position
- Remove problem areas in the DC
- Remove tracks that have a very small bending angle to increase purity



Gaussian Process Regression

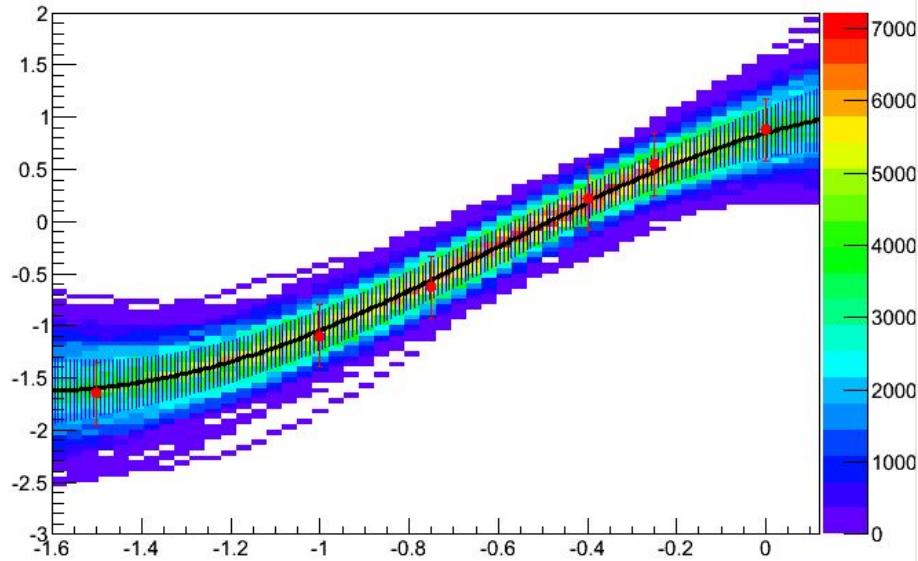
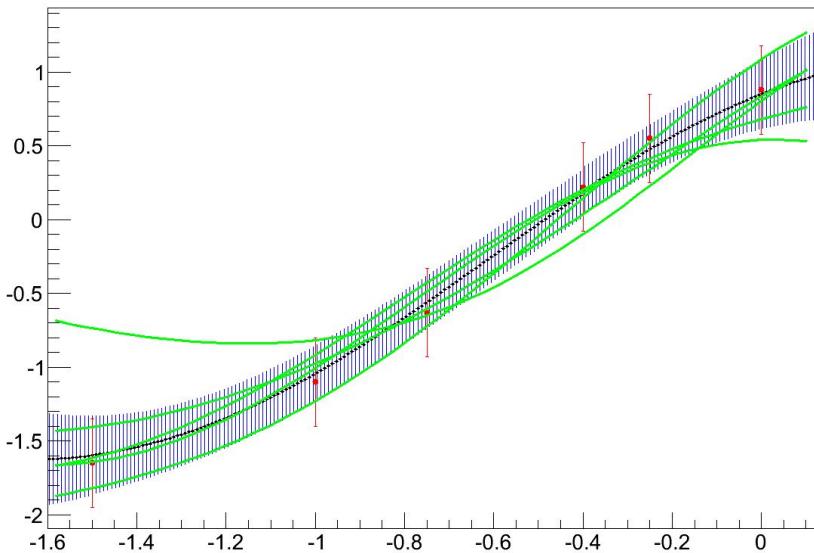
- When functional form is not known apriori
- Shift focus from prior knowledge over parameters to prior over functions (with some minimal constraints)

$$k(x, x') = \sigma_f^2 \exp\left[\frac{-(x - x')^2}{2l^2}\right] + \sigma_n^2 \delta(x, x')$$

- Correlation function encodes how much each data point influences the neighboring points
- Hyperparameters are determined through minimization over data

Function Extraction

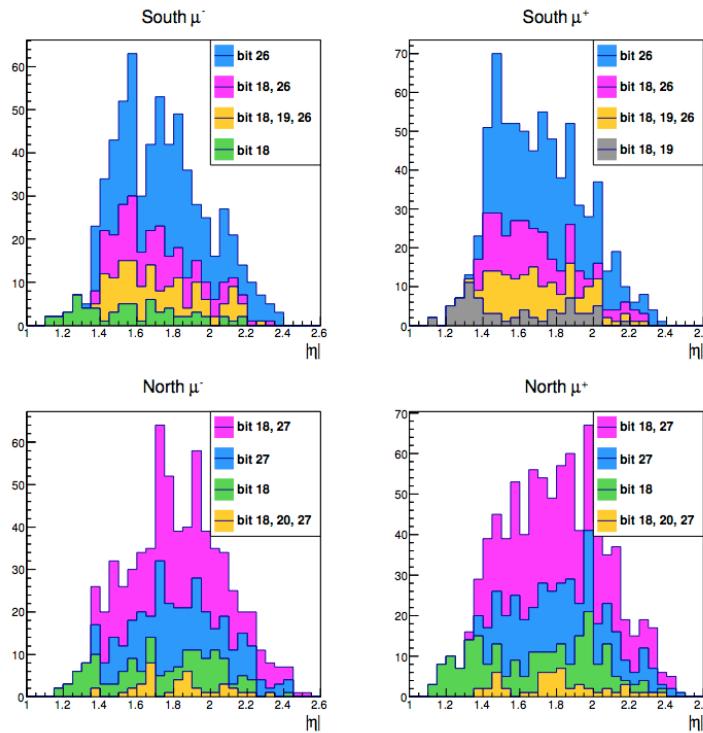
All sampled functions



- Sampling over these functions and filling a 2D histogram (as on the right) will give a Gaussian distribution for each prediction point
- The mean of the Gaussian distribution is the prediction and the sigma is the uncertainty
- *The GPR we use does this mathematically through the equations I presented in the PWG and in the Group meeting but basically this is the only way I can think of to present this information in a couple of slides*

Trigger Efficiency

1. Scanned contributions of each trigger combination within the muon data



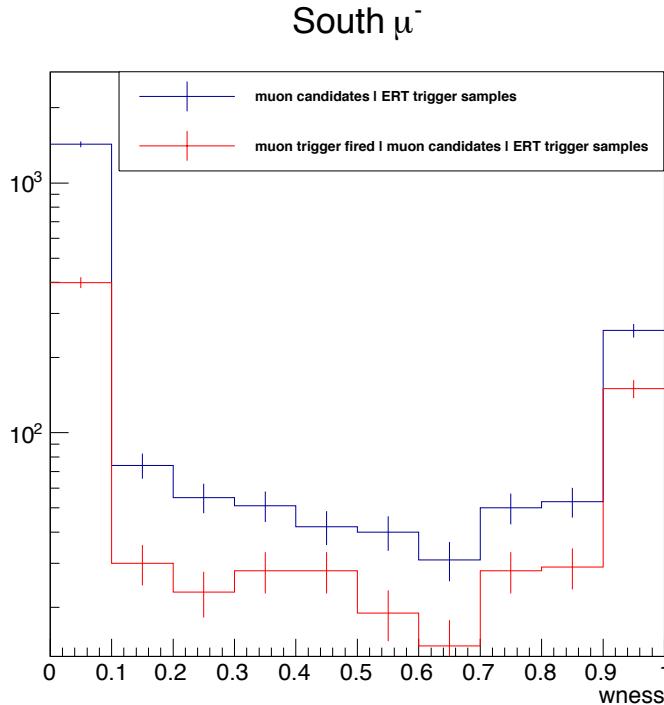
< PHENIX physics triggers >

Trigger bit	Name
0	BBCLL1(> 0 tubes)
1	BBCLL1(> 0 tubes) novertex
2	ZDCLL1wide
3	BBCLL1(noVtx)&(ZDCN ZDCS)
4	BBCLL1(> 0 tubes) narrowvtx
5	ZDCNS
6	ERTLL1_4x4b
7	
8	
9	
10	
11	
12	
13	
14	MPC_C&ERT_2x2
15	(MPCS_C & MPCS_C & MPCN_C)
16	((MUIDLL1_N2D S2D) N1D&N2D)&BBCLL1(noVtx)
17	(MUIDLL1_N1D S1D)&BBCLL1(noVtx)
18	(MUON_S_SG1&MUIDLL1_S1D) (MUON_N_SG1&MUIDLL1_N1D)&BBCLL1(noVtx)
19	MUON_S_SG3&MUIDLL1_S1D&BBCLL1(noVtx)
20	MUON_N_SG3&MUIDLL1_N1D&BBCLL1(noVtx)
21	(MUON_N_SG3&MUIDLL1_N1H) (MUON_S_SG3&MUIDLL1_S1H)&BBCLL1(noVtx)
22	MUON_S_SG3&BBCLL1(noVtx)
23	MUON_N_SG3&BBCLL1(noVtx)
24	MUON_S_SG1&BBCLL1(noVtx)
25	MUON_N_SG1&BBCLL1(noVtx)
26	MUON_S_SG1_RPC3_1_A B C&BBCLL1(noVtx)
27	MUON_N_SG1_RPC3_1_A B C&BBCLL1(noVtx)

Used all muon arm triggers to maximize statistics

Trigger Efficiency

2. Measure the trigger efficiencies for each trigger combination using electron trigger samples



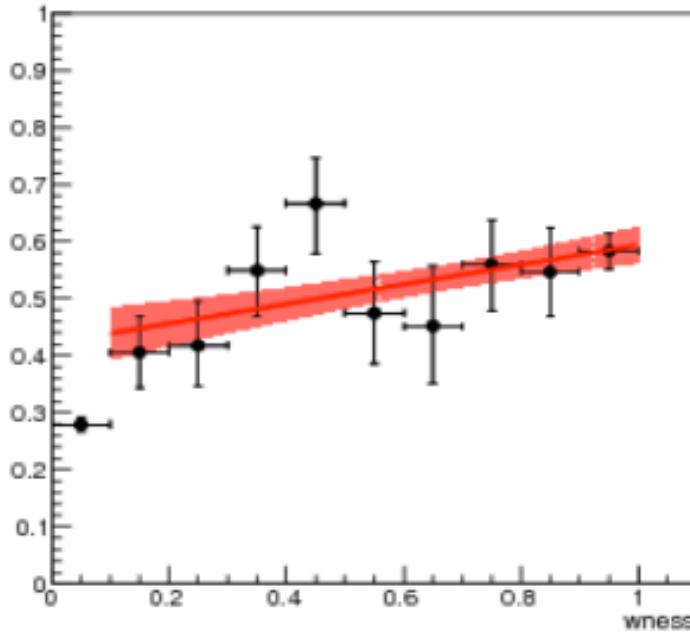
< PHENIX physics triggers >

Trigger bit	Name
0	BBCLL1(> 0 tubes)
1	BBCLL1(> 0 tubes) novertex
2	BBCLL1 ..
3	ZDCNS
4	ERTLL1_4x4b
5	ERTLL1_4x4a&BBCLL1
6	ERTLL1_4x4c&BBCLL1(narrow)
7	ERTLL1_E
8	ERTLL1_E&BBCLL1(narrow)
9	CLOCK
10	MPC_B
11	MPC_A
12	MPC_C&ERT_2x2
13	(MPCS_C & MPCS_C & MPCN_C)
14	((MUIDLL1_N2D S2D) ((N1D&N2D))&BBCLL1(noVtx)
15	(MUIDLL1_N1D S1D)&BBCLL1(noVtx)
16	(MUON_S_SG1&MUIDLL1_S1D) ((MUON_N_SG1&MUIDLL1_N1D)&BBCLL1(noVtx)
17	MUON_S_SG3&MUIDLL1_S1D&BBCLL1(noVtx)
18	MUON_N_SG3&MUIDLL1_N1D&BBCLL1(noVtx)
19	(MUON_N_SG3&MUIDLL1_N1H) ((MUON_S_SG3&MUIDLL1_S1H)&BBCLL1(noVtx)
20	MUON_S_SG3&BBCLL1(noVtx)
21	MUON_N_SG3&BBCLL1(noVtx)
22	MUON_S_SG1&BBCLL1(noVtx)
23	MUON_N_SG1&BBCLL1(noVtx)
24	MUON_S_SG1&BBCLL1(noVtx)
25	MUON_N_SG1&BBCLL1(noVtx)
26	MUON_S_SG1_RPC3_1_A B C&BBCLL1(noVtx)
27	MUON_N_SG1_RPC3_1_A B C&BBCLL1(noVtx)

Trigger Efficiency

2. Measure the trigger efficiencies for each trigger combination using electron trigger samples

South μ^-



< PHENIX physics triggers >

Trigger bit	Name
0	BBCLL1(> 0 tubes)
1	BBCLL1(> 0 tubes) novertex
2	BBCLL1 ..
3	ZDCNS
4	ERTLL1_4x4b
5	ERTLL1_4x4a&BBCLL1
6	ERTLL1_4x4c&BBCLL1(narrow)
7	ERTLL1_E
8	ERTLL1_E&BBCLL1(narrow)
9	CLOCK
10	MPC_B
11	MPC_A
12	MPC_C&ERT_2x2
13	(MPCS_C & MPCS_C & MPCN_C)
14	((MUIDLL1_N2D S2D) ((N1D&N2D))&BBCLL1(noVtx)
15	(MUIDLL1_N1D S1D)&BBCLL1(noVtx)
16	(MUON_S_SG1&MUIDLL1_S1D)
17	(MUON_N_SG1&MUIDLL1_N1D)&BBCLL1(noVtx)
18	(MUON_S_SG3&MUIDLL1_S1D&BBCLL1(noVtx)
19	MUON_N_SG3&MUIDLL1_N1D&BBCLL1(noVtx)
20	(MUON_N_SG3&MUIDLL1_N1H)
21	(MUON_S_SG3&MUIDLL1_S1H)&BBCLL1(noVtx)
22	MUON_S_SG3&BBCLL1(noVtx)
23	MUON_N_SG3&BBCLL1(noVtx)
24	MUON_S_SG1&BBCLL1(noVtx)
25	MUON_N_SG1&BBCLL1(noVtx)
26	MUON_S_SG1_RPC3_1_A B C&BBCLL1(noVtx)
27	MUON_N_SG1_RPC3_1_A B C&BBCLL1(noVtx)

Trigger Efficiency

3. Calculate the total trigger efficiency for all trigger combinations

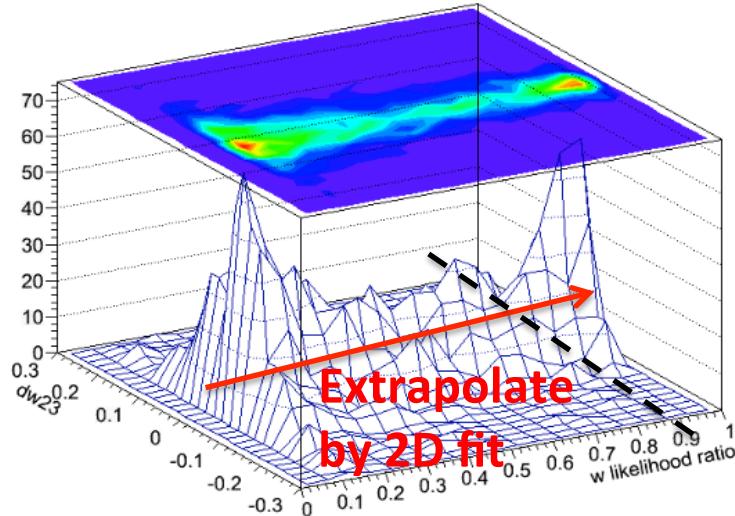
$$\epsilon_{total} = \sum_{trigger} \epsilon_{trigger} \times f_{trigger}$$

Arm	Charge	ϵ_{total}
South	Negative	0.450 ± 0.016
South	Positive	0.463 ± 0.015
North	Negative	0.573 ± 0.019
North	Positive	0.557 ± 0.016

< PHENIX physics triggers >

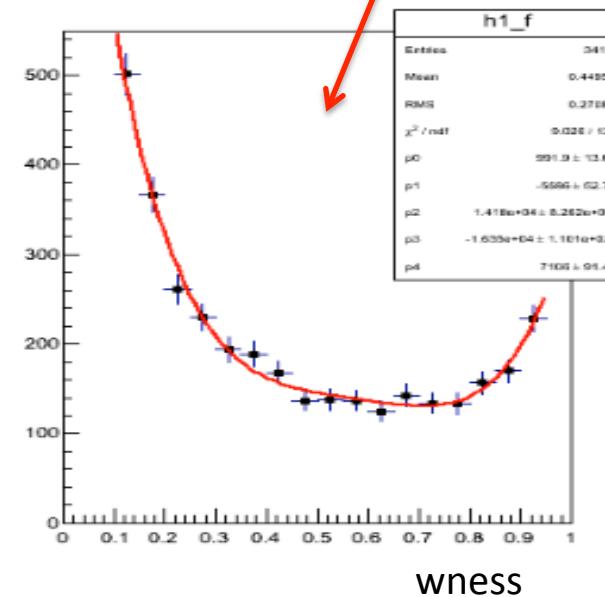
Trigger bit	Name
0	BBCLL1(> 0 tubes)
1	BBCLL1(> 0 tubes) novertex
2	BBCLL1 ..
3	ZDCNS
4	ERTLL1_4x4b
5	ERTLL1_4x4a&BBCLL1
6	ERTLL1_4x4c&BBCLL1(narrow)
7	ERTLL1_E
8	ERTLL1_E&BBCLL1(narrow)
9	CLOCK
10	MPC_B
11	MPC_A
12	MPC_C&ERT_2x2
13	(MPCS_C & MPCS_C & MPCN_C)
14	((MUIDLL1_N2D S2D) ((N1D&N2D))&BBCLL1(noVtx)
15	(MUIDLL1_N1D S1D)&BBCLL1(noVtx)
16	((MUON_S_SG1&MUIDLL1_S1D)
17	(MUON_N_SG1&MUIDLL1_N1D)&BBCLL1(noVtx)
18	MUON_S_SG3&MUIDLL1_S1D&BBCLL1(noVtx)
19	MUON_N_SG3&MUIDLL1_N1D&BBCLL1(noVtx)
20	(MUON_N_SG3&MUIDLL1_N1H)
21	(MUON_S_SG3&MUIDLL1_S1H)&BBCLL1(noVtx)
22	MUON_S_SG3&BBCLL1(noVtx)
23	MUON_N_SG3&BBCLL1(noVtx)
24	MUON_S_SG1&BBCLL1(noVtx)
25	MUON_N_SG1&BBCLL1(noVtx)
26	MUON_S_SG1_RPC3_1_A B C&BBCLL1(noVtx)
27	MUON_N_SG1_RPC3_1_A B C&BBCLL1(noVtx)

dw23 for Hadron Background

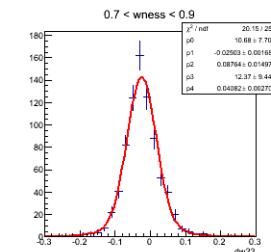
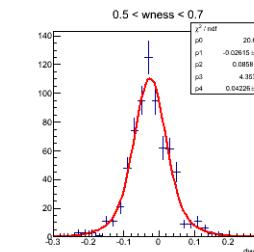
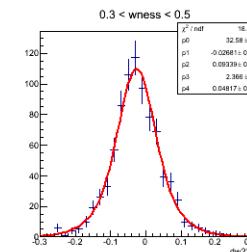
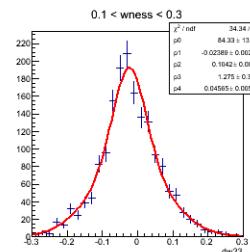
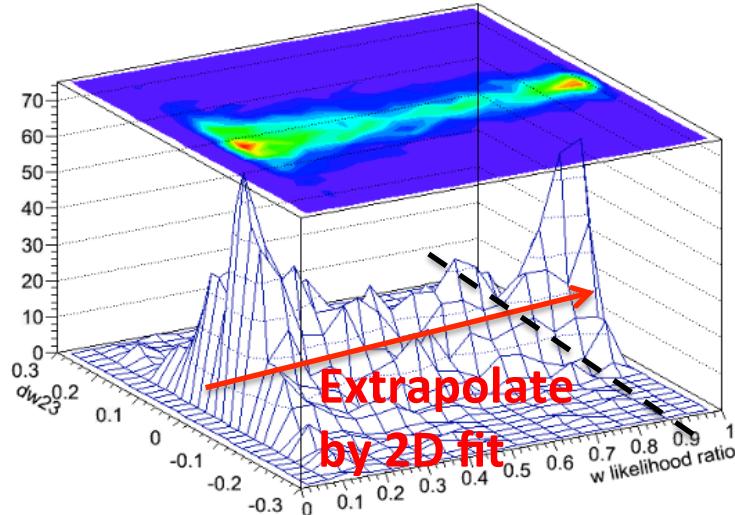


2D model of dw23-wness

$$p(\text{wness}, \text{dw23}) = p(\text{wness}) \cdot p(\text{dw23} | \text{wness})$$



dw23 for Hadron Background



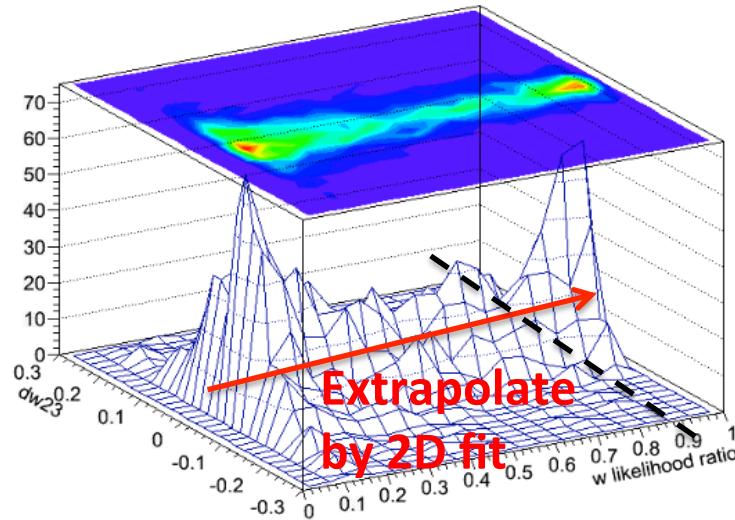
2D model of dw23-wness

$$p(\text{wness}, \text{dw23}) = p(\text{wness}) \cdot p(\text{dw23} | \text{wness})$$

- Fit model: Coaxial double gaussian
- Vary parameters linearly

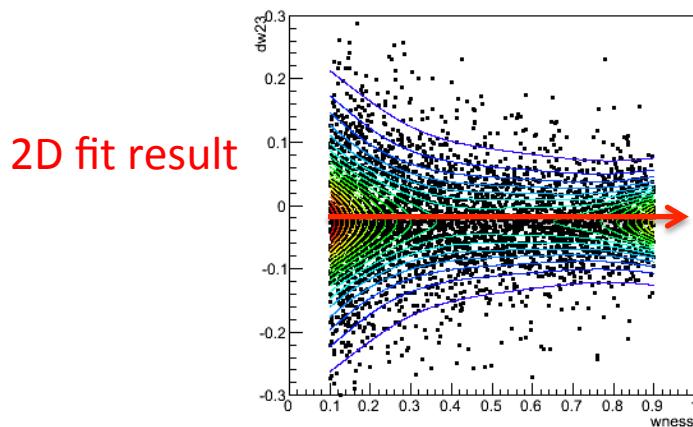
Slice of dw23 distributions

dw23 for Hadron Background

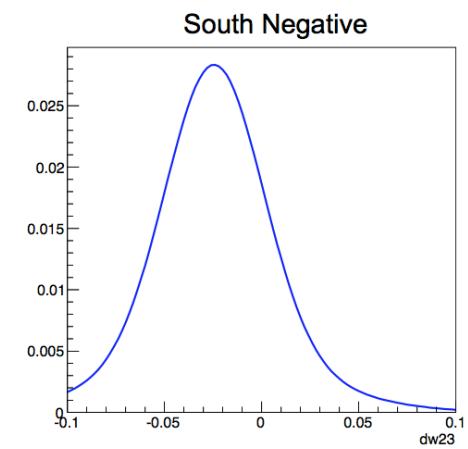


2D model of dw23-wness

$$p(\text{wness}, \text{dw23}) = p(\text{wness}) \cdot p(\text{dw23} | \text{wness})$$



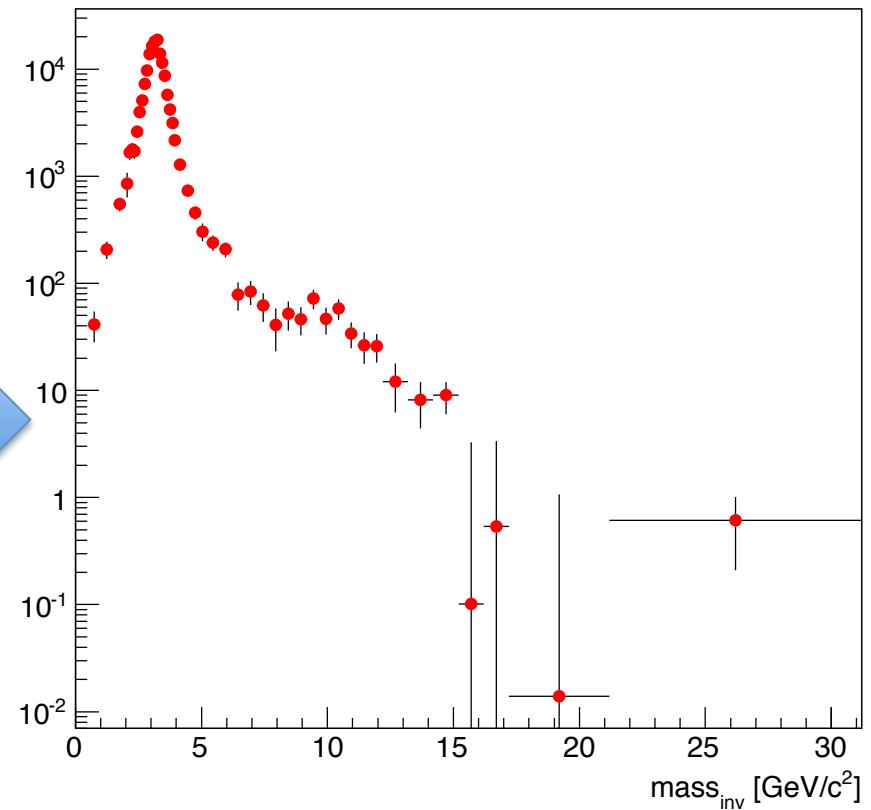
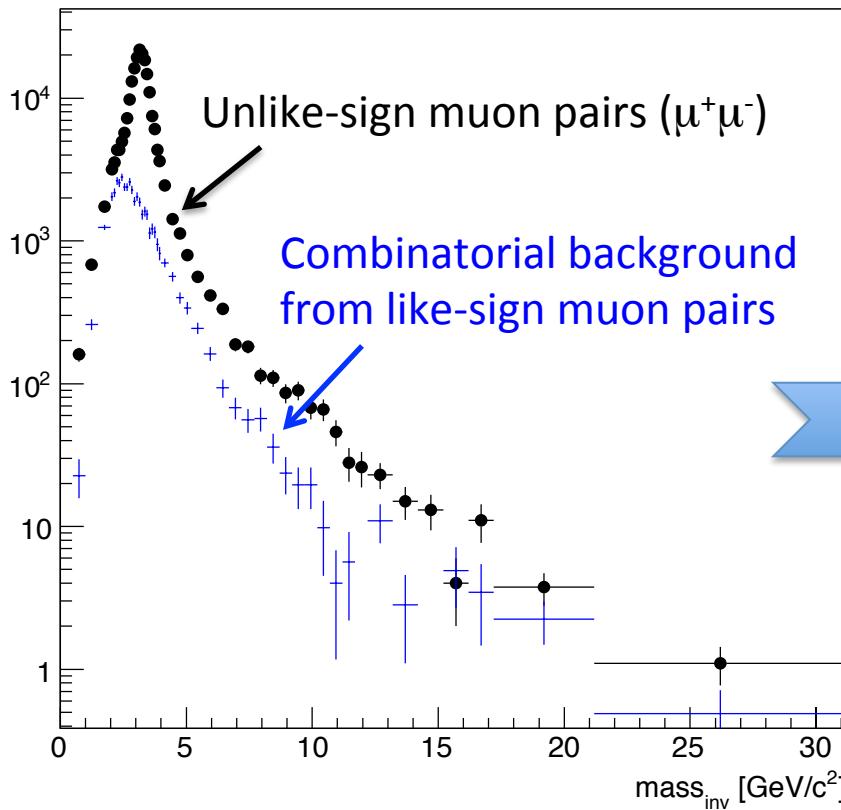
Extrapolate the fit function to the target wness region.



Muon Background Estimation

- Real muon background is fixed in the signal fit
- Muon background is estimated by di-muon events

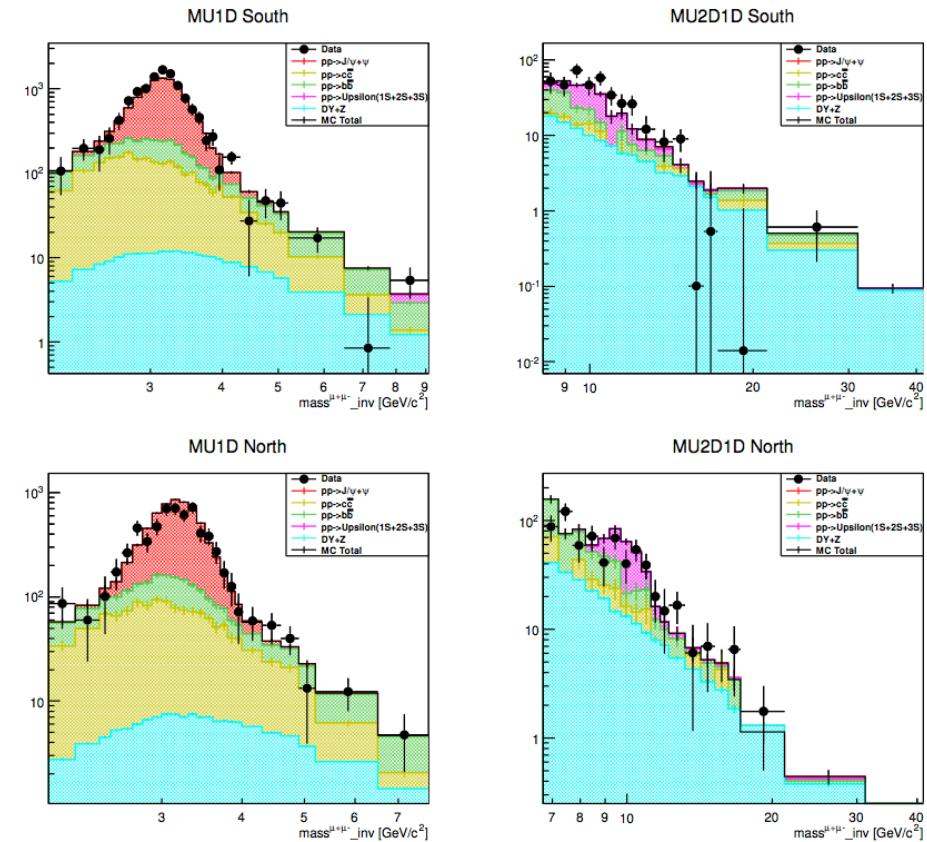
Invariant mass (real collision data)



Muon Background Estimation

- Muon background: Open heavy flavor, quarkonia, Drell-Yan/Z
- Various muon background processes are combined together before constructing probability density functions.
- Relative contributions → scale factors.

Process	Scale factors
$J/\Psi + \Psi$	0.317 ± 0.016
Open charm	2.605 ± 0.817
Open bottom	1.983 ± 0.934
$\Upsilon(1S + 2S + 3S)$	0.437 ± 0.093
Drell-Yan/Z	1.112 ± 0.446



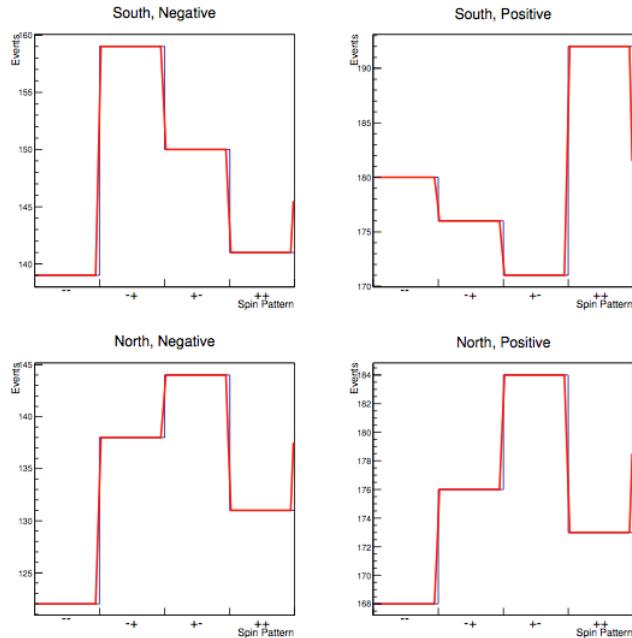
Single Spin Asymmetry

- Corrected Single Spin Asymmetry:

$$A_L = \frac{1}{P} \frac{N^+ - N^-}{N^+ + N^-} \times \left(1.0 + \frac{BG}{SIG} \right)$$

Background does not have asymmetry, but dilute the signal asymmetry

- Both beams are polarized → measure independently and combined



$$\begin{aligned}
 N_{++} &= \sigma_0 L_{++} \left(1 + A_L^{Blue} P_B + A_L^{Yellow} P_Y + A_{LL} P_1 P_2 \right) \\
 N_{+-} &= \sigma_0 L_{+-} \left(1 + A_L^{Blue} P_B - A_L^{Yellow} P_Y - A_{LL} P_1 P_2 \right) \\
 N_{-+} &= \sigma_0 L_{-+} \left(1 - A_L^{Blue} P_B + A_L^{Yellow} P_Y - A_{LL} P_1 P_2 \right) \\
 N_{--} &= \sigma_0 L_{--} \left(1 - A_L^{Blue} P_B - A_L^{Yellow} P_Y + A_{LL} P_1 P_2 \right)
 \end{aligned}$$

$$N_{\alpha,\beta} = \sigma_0 + \alpha \sigma_L^{Blue} + \beta \sigma_L^{Yellow} + \alpha \beta \sigma_{LL}$$

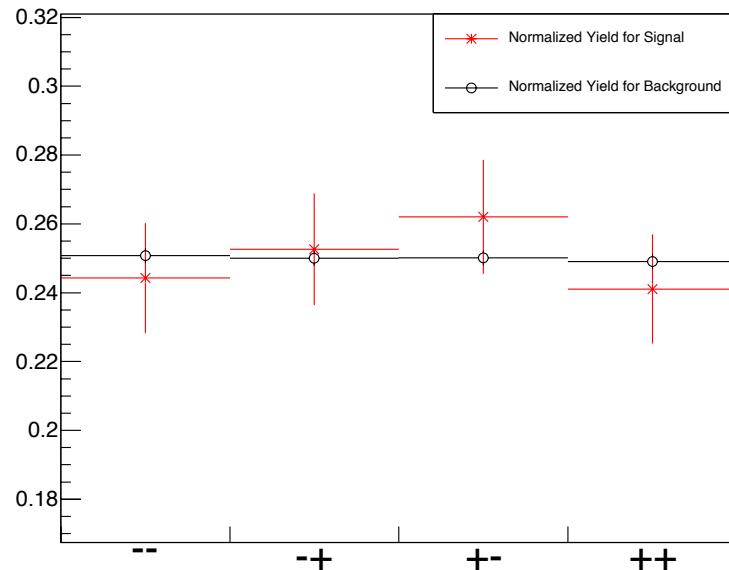
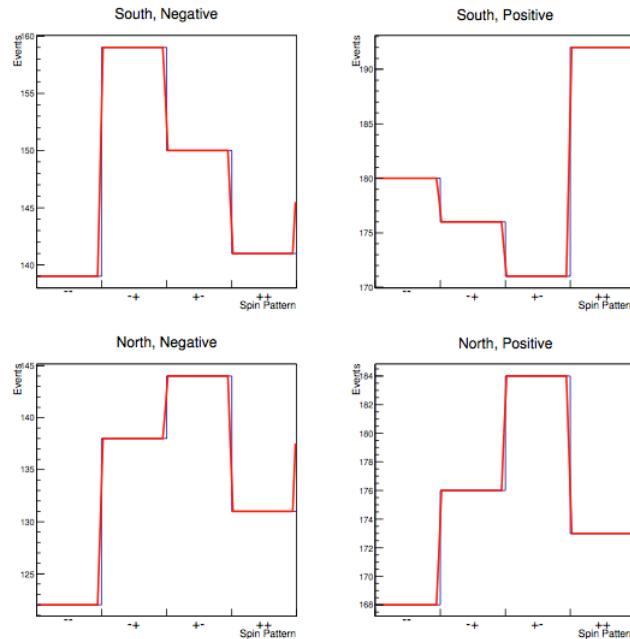
Single Spin Asymmetry

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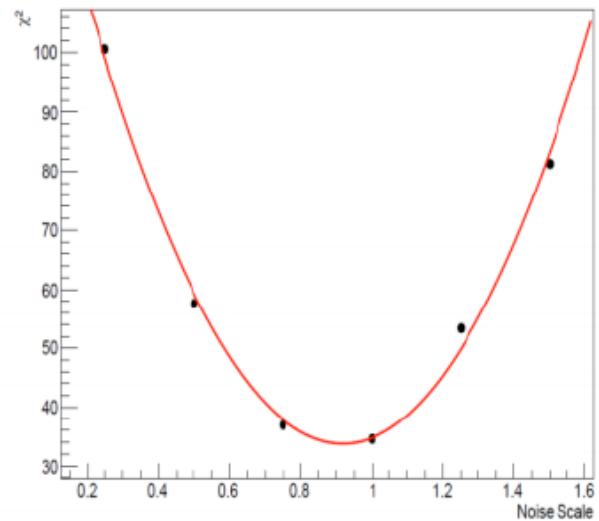
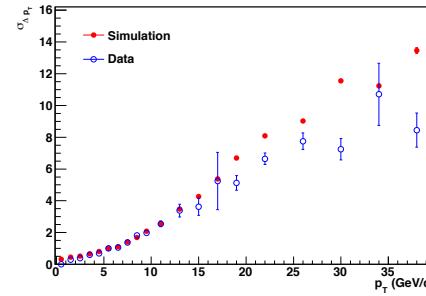
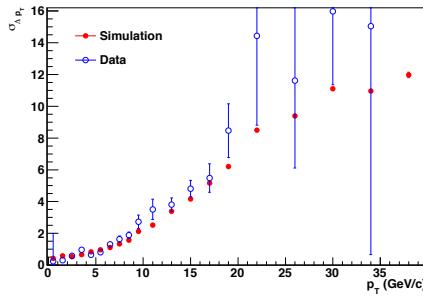
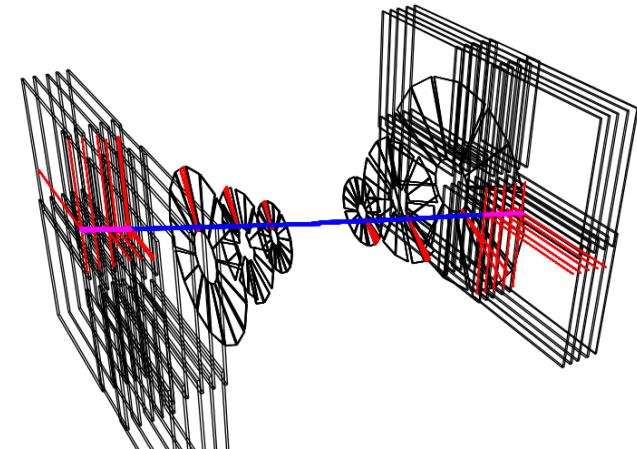
Background does not have asymmetry, but dilute the signal asymmetry

- Both beams are polarized → measure independently and combined



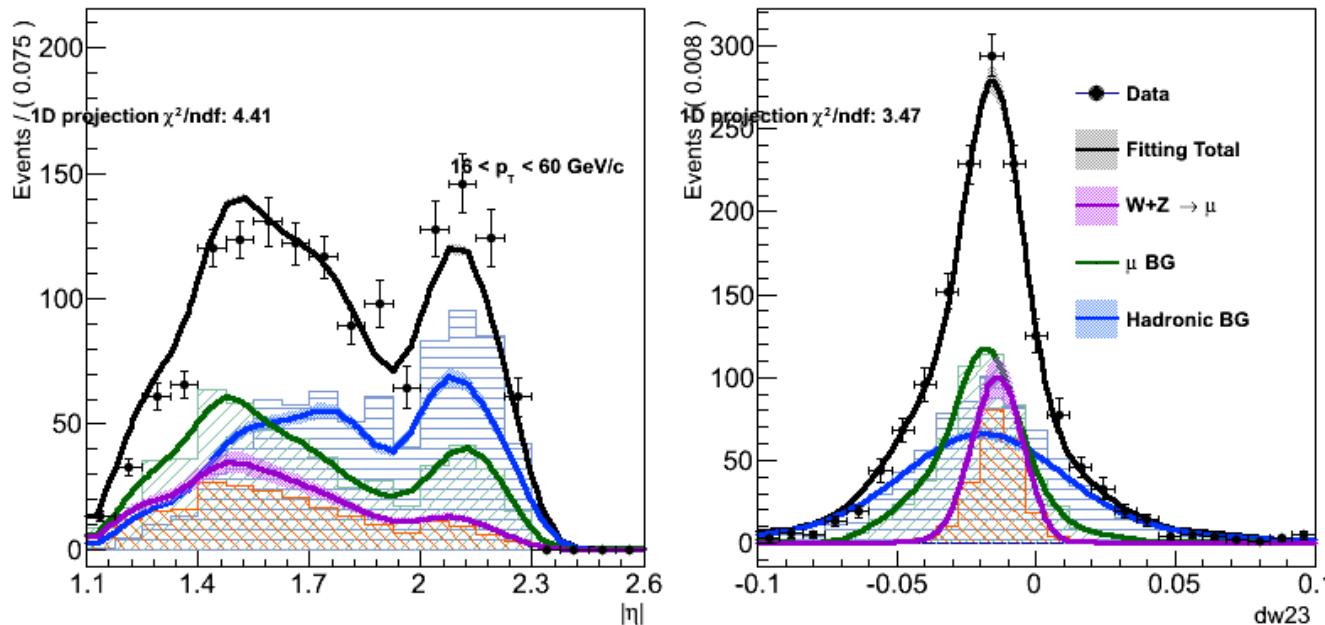
MuTr position resolution

- Using the cosmic data
 - Measure momentum for incoming and outgoing tracks
 - Compare data with MC
 - Noise RMS to be tuned



Cross Check of the Fit

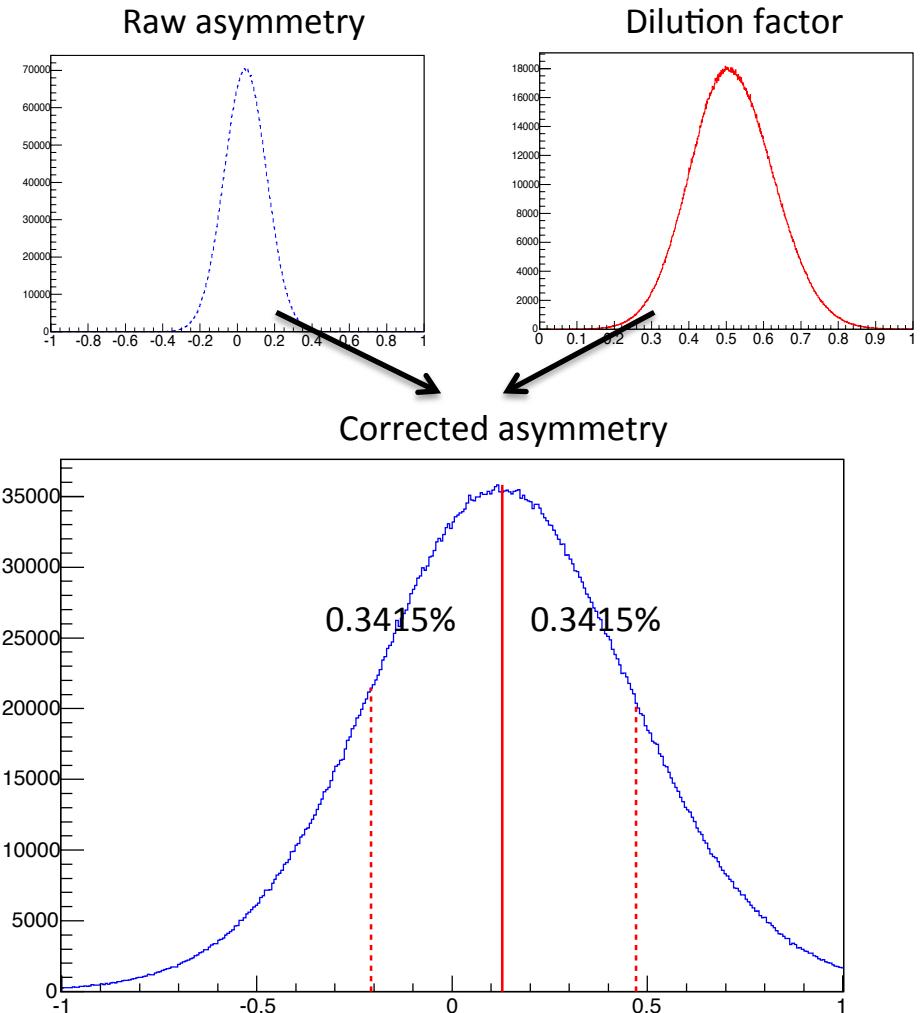
- Create a trial data set entirely of simulation.
- Signal, background contributions are known prior.
- Estimate the efficiency of the method used
 - predict possible over/under estimation
 - take the relative difference as systematic uncertainty



Systematic Uncertainty

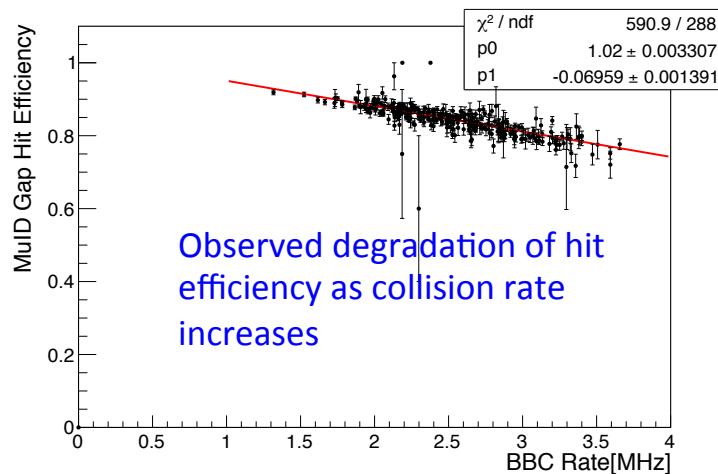
$$A_L = \frac{1}{P} \frac{N^+ - N^-}{N^+ + N^-} \times \left(1.0 + \frac{BG}{SIG} \right)$$

- Systematic uncertainty sources:
 - S/BG Fit
 - Trigger efficiency correction
 - Muon background
 - MuTr position resolution

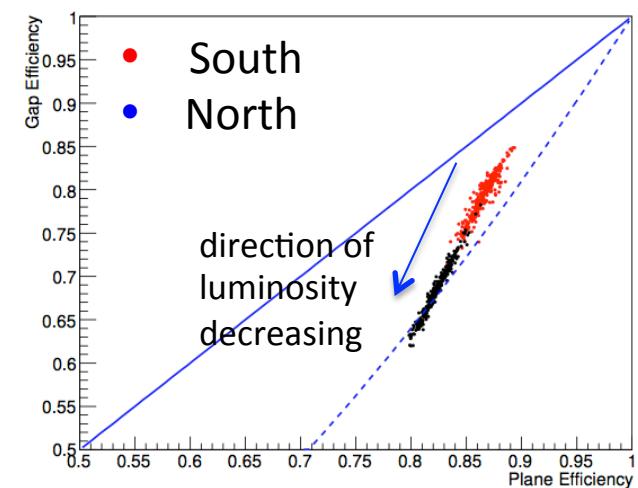


Simulation Tuning

- Produced W/Z signal and various background MC simulations to support the analysis (PYTHIA +GEANT3)
- Rate dependence of detector performance:



MuID detector hit efficiency



MuTr detector hit efficiency

