

# Extremely Heavy Neutron Stars and the Equation of State

T. Takatsuka

(RIKEN; Iwate Univ.( Prof. Emeritus)) ,

- Background and **motivation**
- Too-soft EOS due to  $\Lambda$  ; **"Hyperon Crisis"**
- Massive NSs with **universal 3-body force**
- Massive NSs with **hadron-quark crossover**
- Too-rapid cooling and **necessity of  $\Lambda$ -super**

# NEUTRON STAR

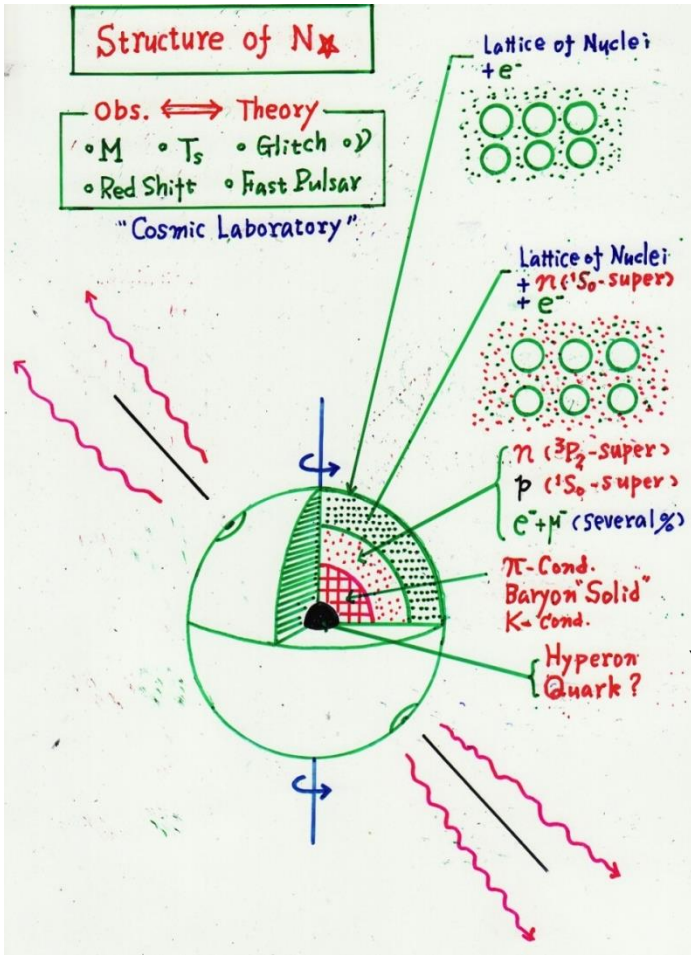
Huge NUCLEUS  
Y-mixed NSs → "HyperNSs"  
"Cosmic Laboratory"

New paradigm  
is coming!

# NUCLEUS

Y-mixed nuclei  
→ Hypernuclei

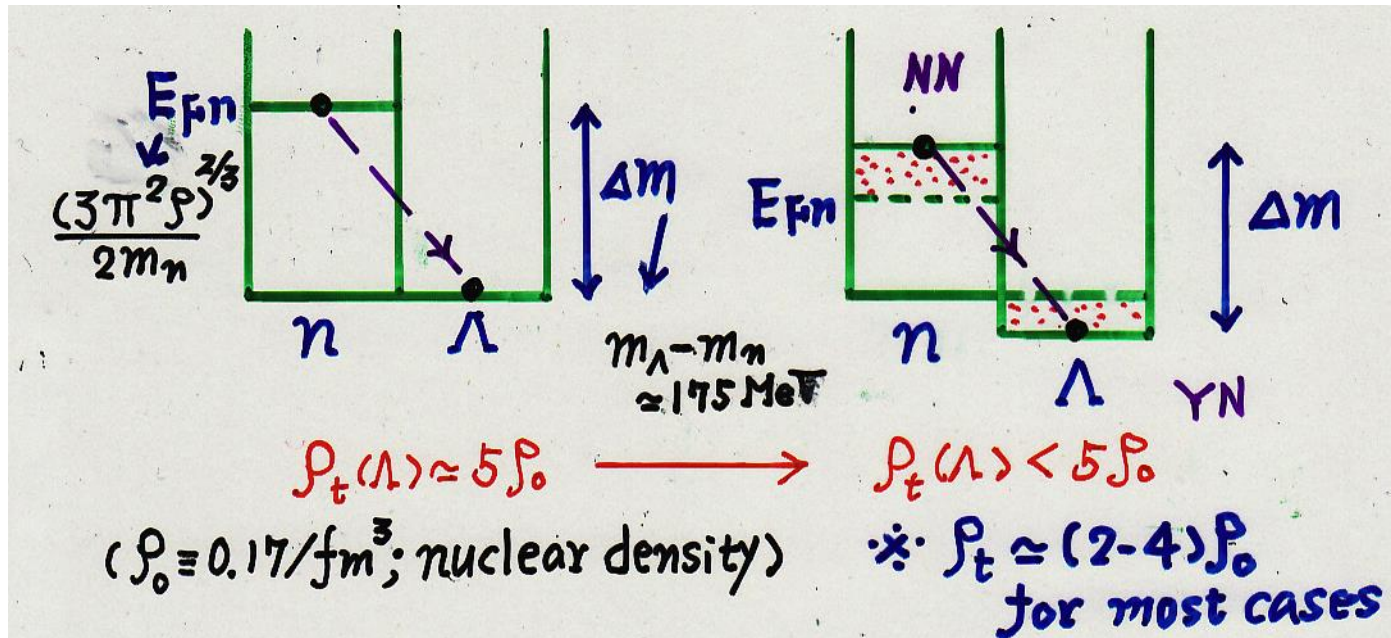
Terrestrial Laboratory  
(JPARK etc.)



# □ Hyperon Mixing in NS cores

< K.E. only >

< with interactions >



- Hyperon (Y) surely participate in Neutron Star (NS) Cores
- Standard picture for NS constituents:  
Old (n, p, e<sup>-</sup>, μ<sup>-</sup>) → Now (n, p, Y, e<sup>-</sup>, μ<sup>-</sup>)

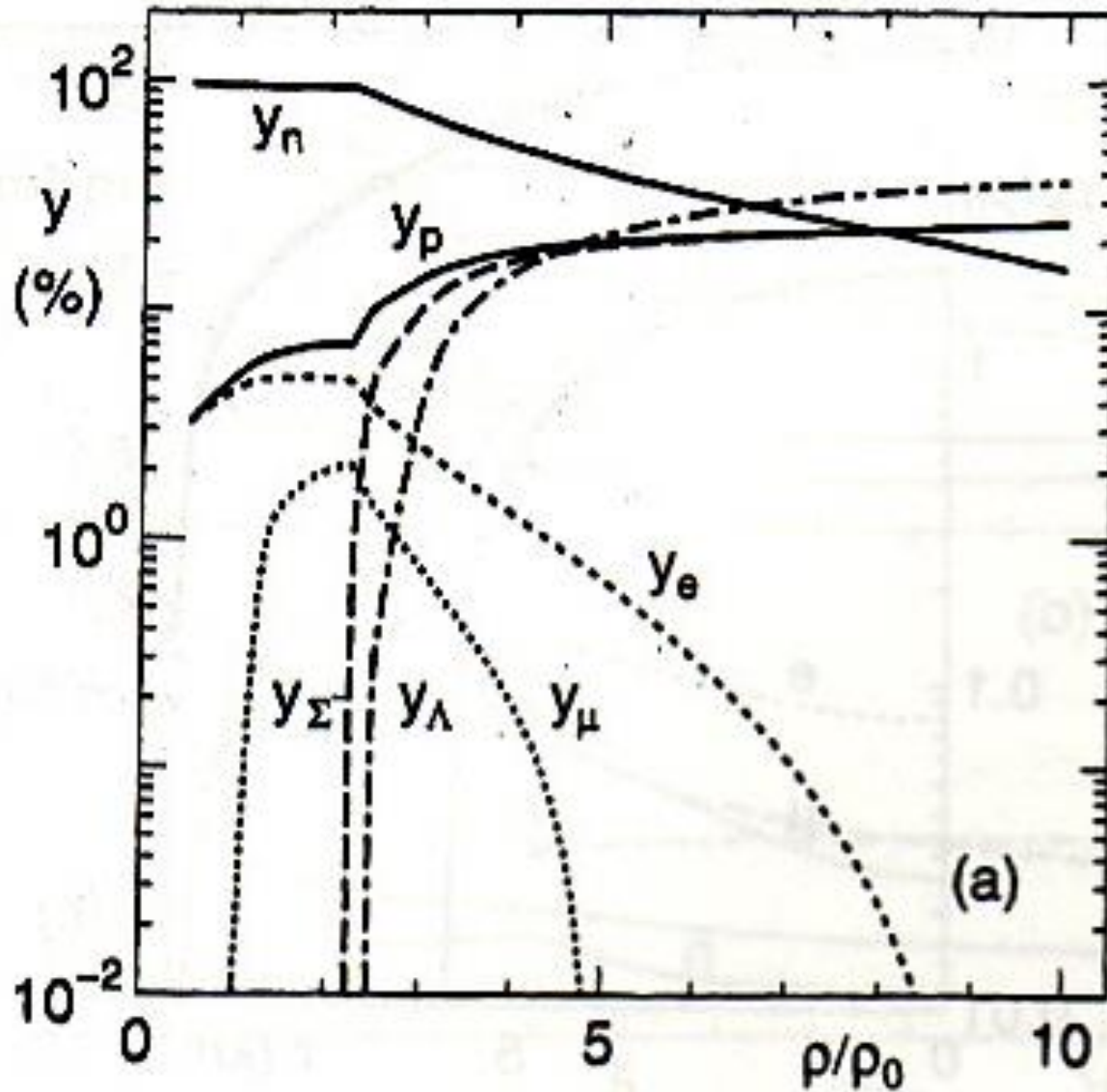
# □ Our approach to NS-matter with $\Lambda$ -mixing

- Matter composed of N (n, p),  $\Lambda$ ,  $\Sigma^-$  and Leptons ( $e^-$ ,  $\mu^-$ )
- effective interaction approach based on G-matrix calculations, (effective int. V for NN, N $\Lambda$ ,  $\Lambda\Lambda$ )  
Introduction of 3-body force U (TNI, phenomenological Illinois-type, expressed as effective 2-body force)
- V+U satisfy the saturation property and symmetry energy at nuclear density
- (hard, soft) is classified by the incompressibility  $\kappa$  ;  
 $\kappa=300, 280, 250$  MeV for TNI3,TNI6,TNI2

[1] S. Nishizaki, Y. Yamamoto and T. Takatsuka, Prog.Theor. Phys.105 (2001) 607; 108 (2002) 703

[2] T. Takatsuka, Prog. Theor. Phys. Suppl. No. 156 (2004) 84

- Hyperons appear at  $\rho_t \sim (2-2.5)\rho_0$



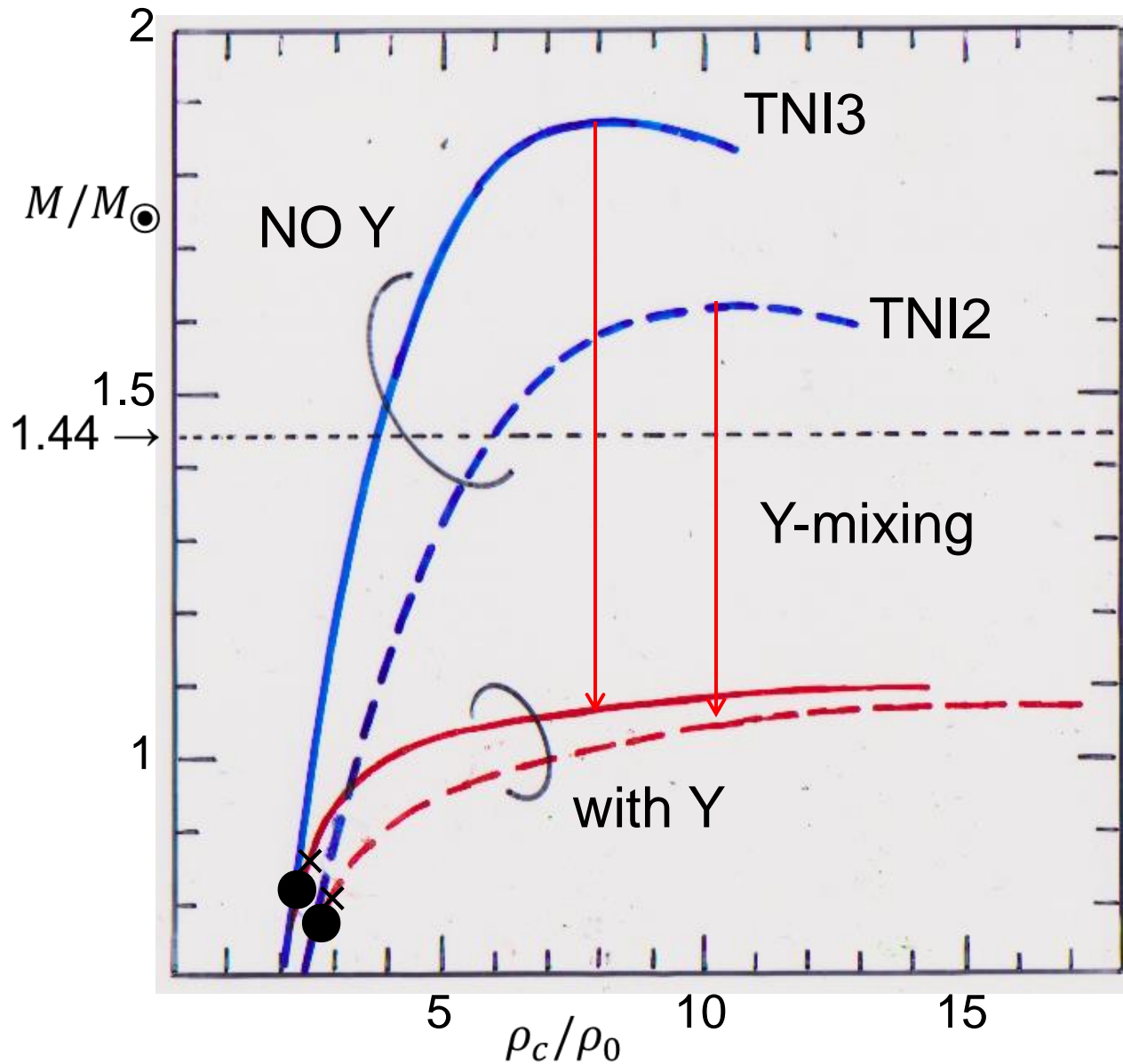
Then, What happens?

→ Serious problems

I . Too-softened EOS

II . Too-rapid cooling

$M_{max} < M_{obs}$  (Softened EOS by Y)



Strong Softening  
of the EOS

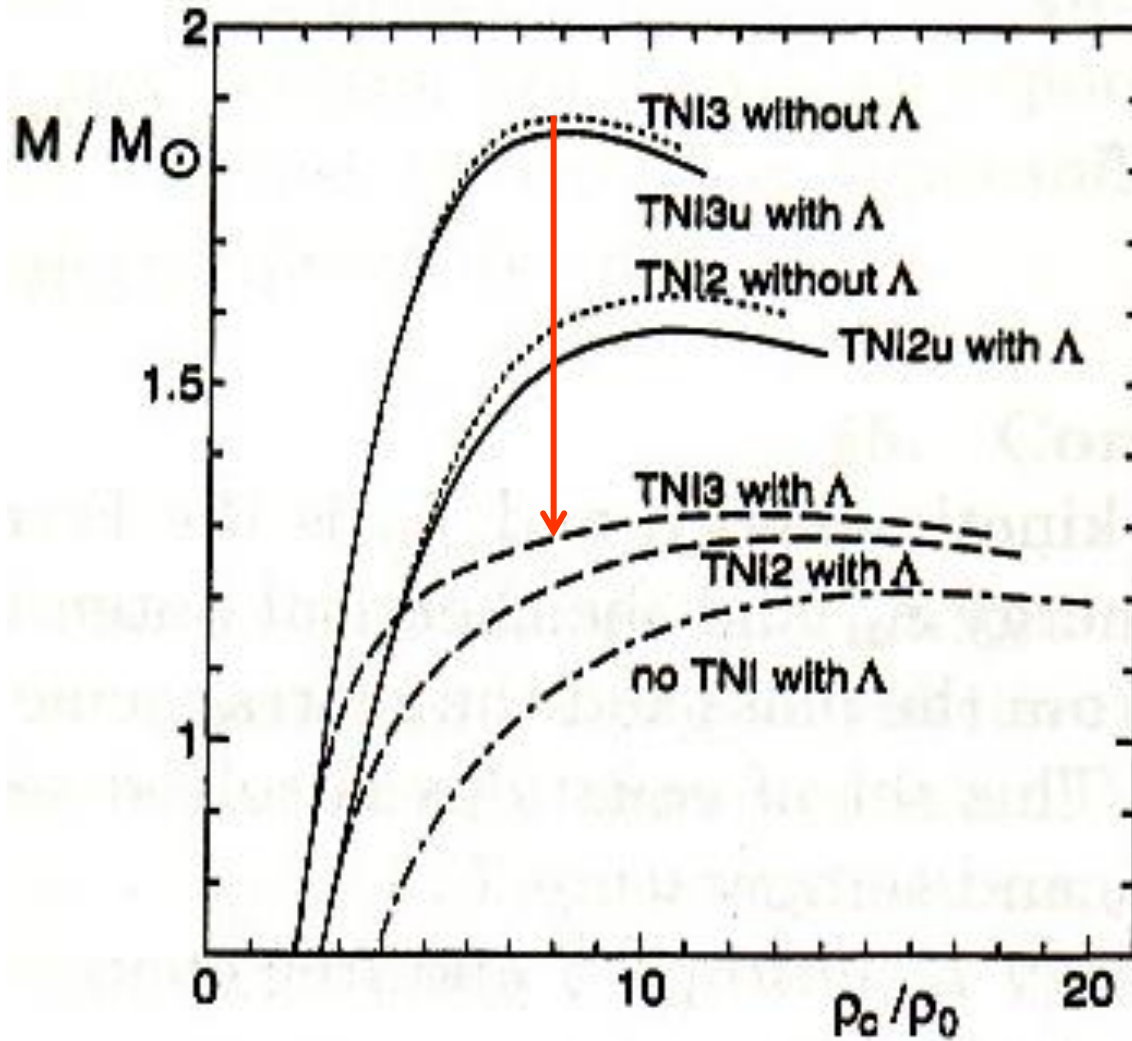


After  $2M_{\text{sun}}$   
observations

**Hyperon Crisis**  
(by T. Hatsuda)

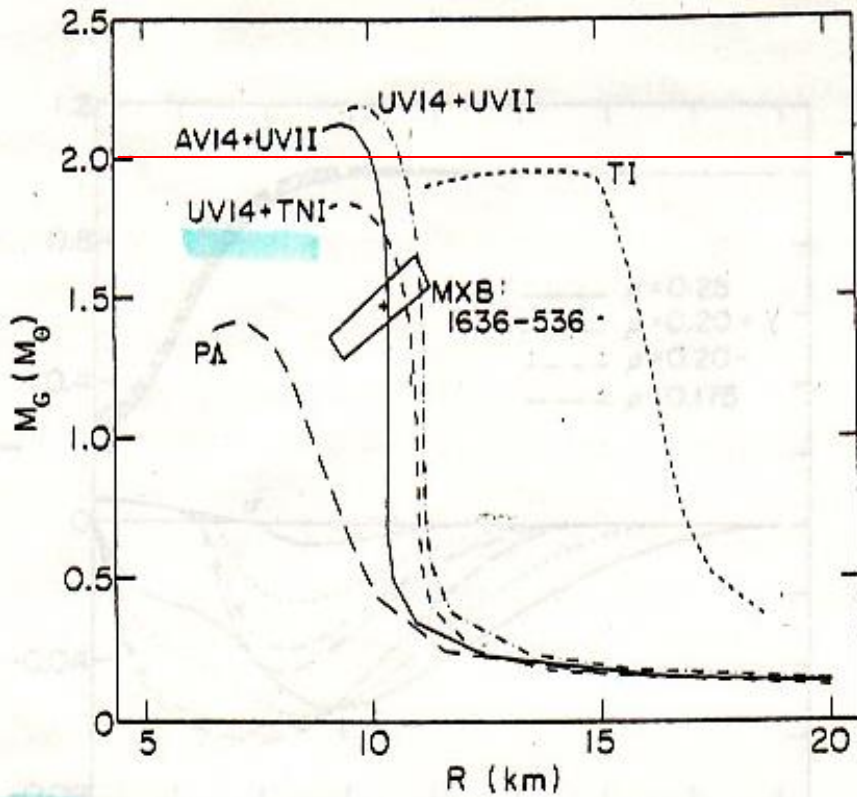


Even  $\Lambda$ -only mixing, situation is the same!

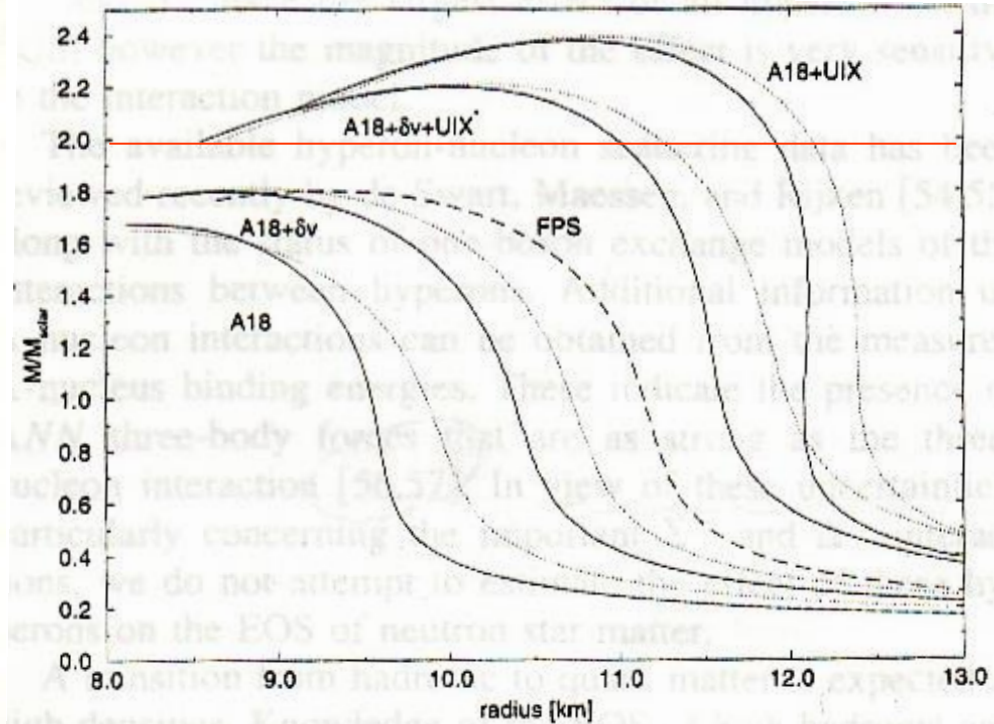




If no exotics,  $M \geq 2M_{\odot}$  is possible



R.B. Wiringa, V. Fiks and A. Fabrocini,  
PR C38 (1988) 1010.



A. Akmal, V.R. Pandharipande and D.G.  
Ravenhall, PR C58 (1998) 1804.

# Observation of Massive NSs

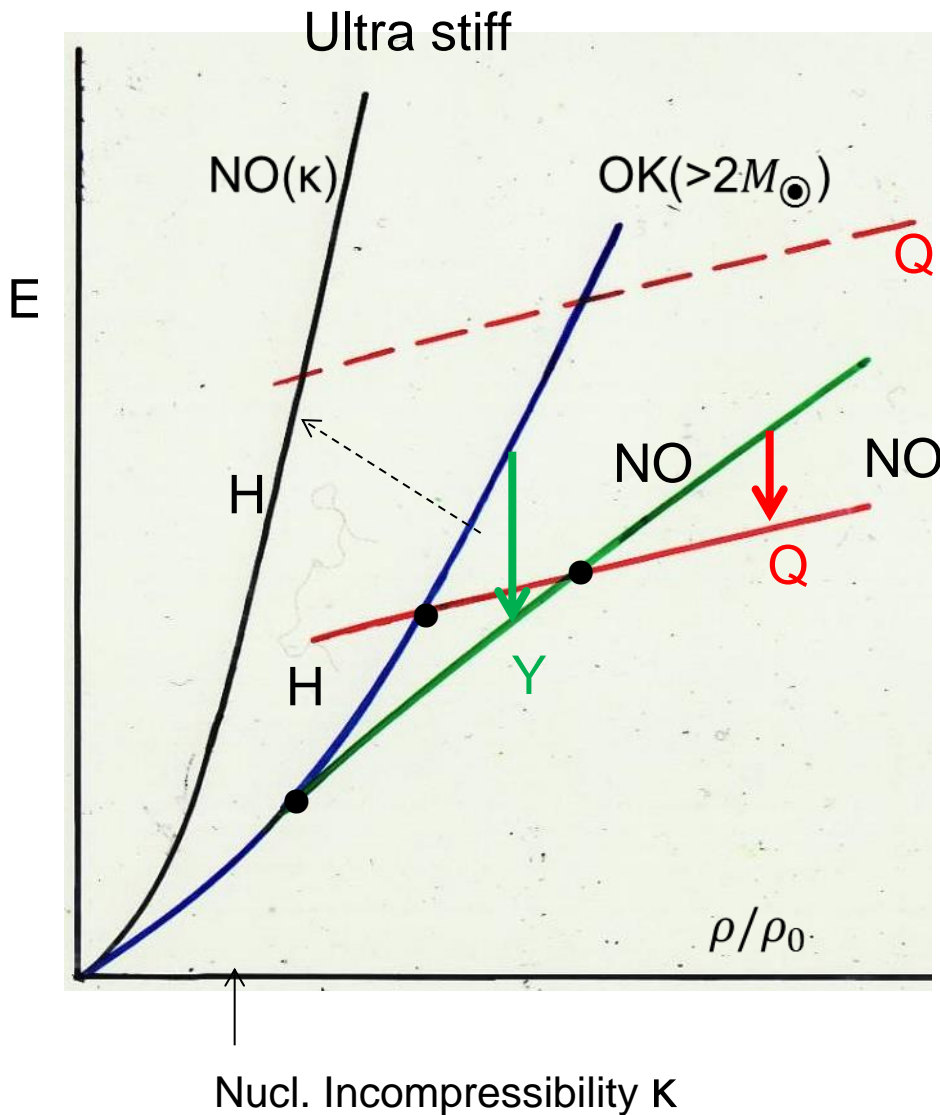
(2-solar-mass NSs)



- How to explain such massive NS, **with Y** ?
- NO Q-matt. (Q-deg. of freedom) in NSs?

We consider the possibility in two frameworks:

- ① Pure hadronic (H) matter
- ② With Q-degrees of freedom



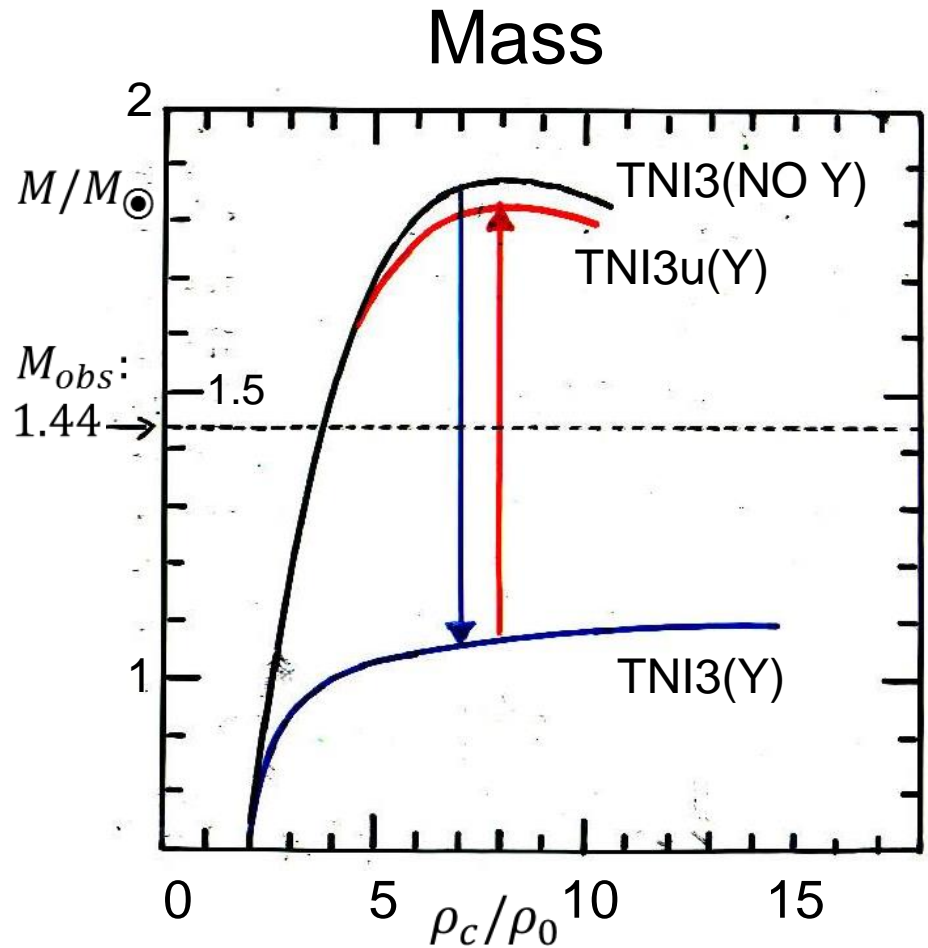
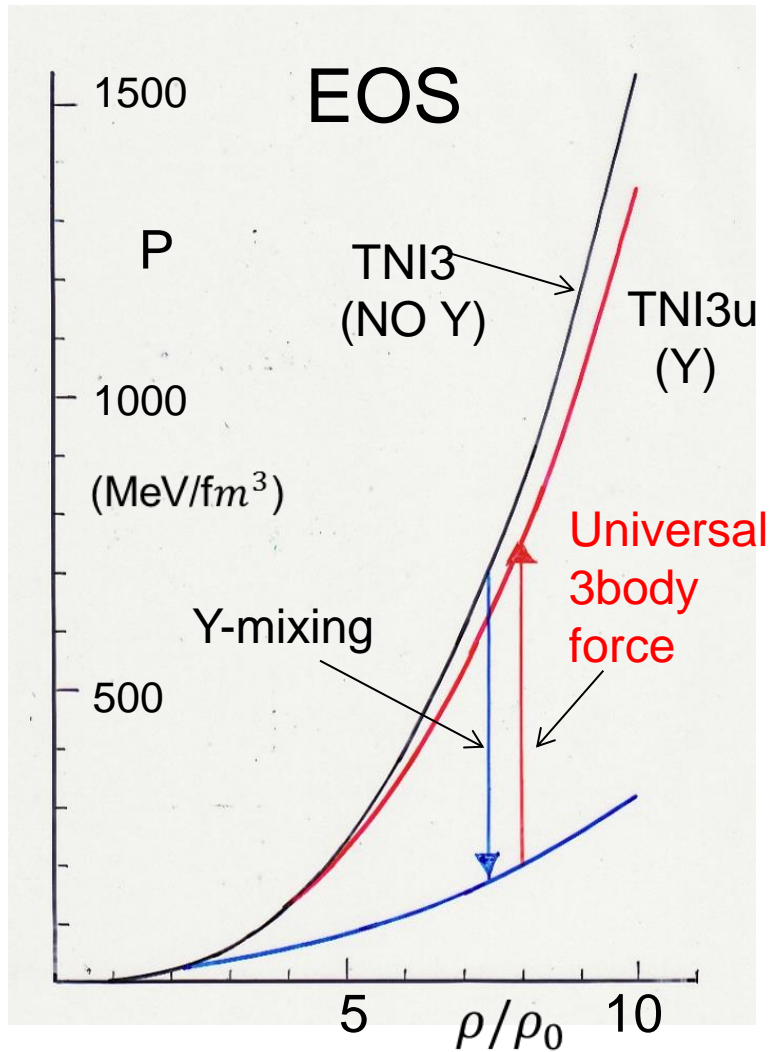
Possible candidate to solve the problem

□ **Universal 3-body force**

an extended use of the phenomenological 3-body force  $U$  of Illinois's type (Friedman-Pandharipande) :

**NNN**  $\longrightarrow$  **BBB**

Dramatic softening of EOS  $\longrightarrow$  Necessity of “Extra Repulsion”



As a review  $\longrightarrow$  T.Takatsuka, Prog.Theor.Phys.Suppl.No.156 (2004) 84.

A step forward to the origin of the Universal 3-Body Force,  
we consider at short  $d$

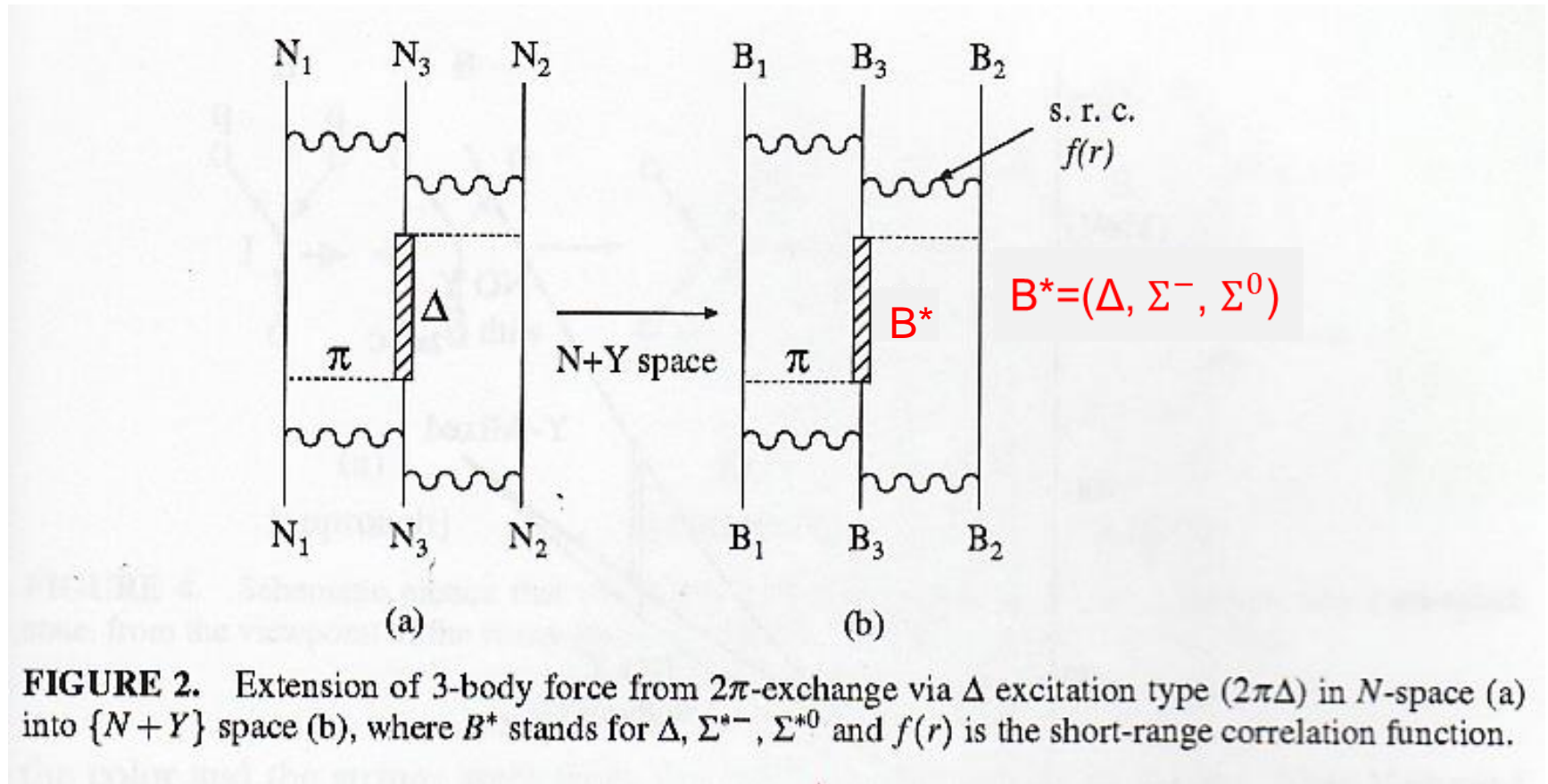
## SJM 3-Body Force (Tamagaki)

from the **string-junction quark model** of baryons, which  
is based on the confinement (color degrees of freedom)  
and **flavor-independent** (namely, **universal**),  
and also for intermediate and long distances, an extended

## $2\pi\Delta$ 3-Body Force (Fujita-Miyazawa type)

# Extended $2\pi\Delta$ -Type 3-body Force

; not universal

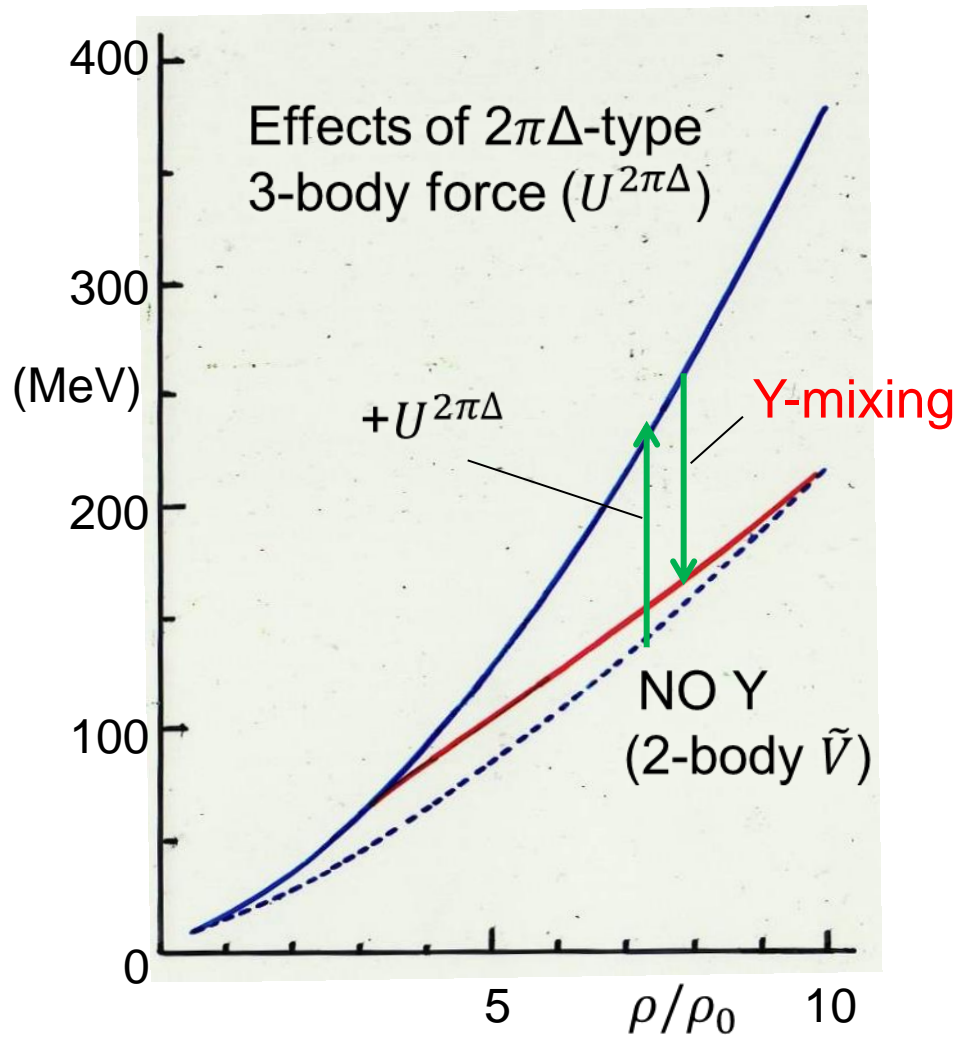


**FIGURE 2.** Extension of 3-body force from  $2\pi$ -exchange via  $\Delta$  excitation type ( $2\pi\Delta$ ) in  $N$ -space (a) into  $\{N+Y\}$  space (b), where  $B^*$  stands for  $\Delta, \Sigma^{*-}, \Sigma^{*0}$  and  $f(r)$  is the short-range correlation function.

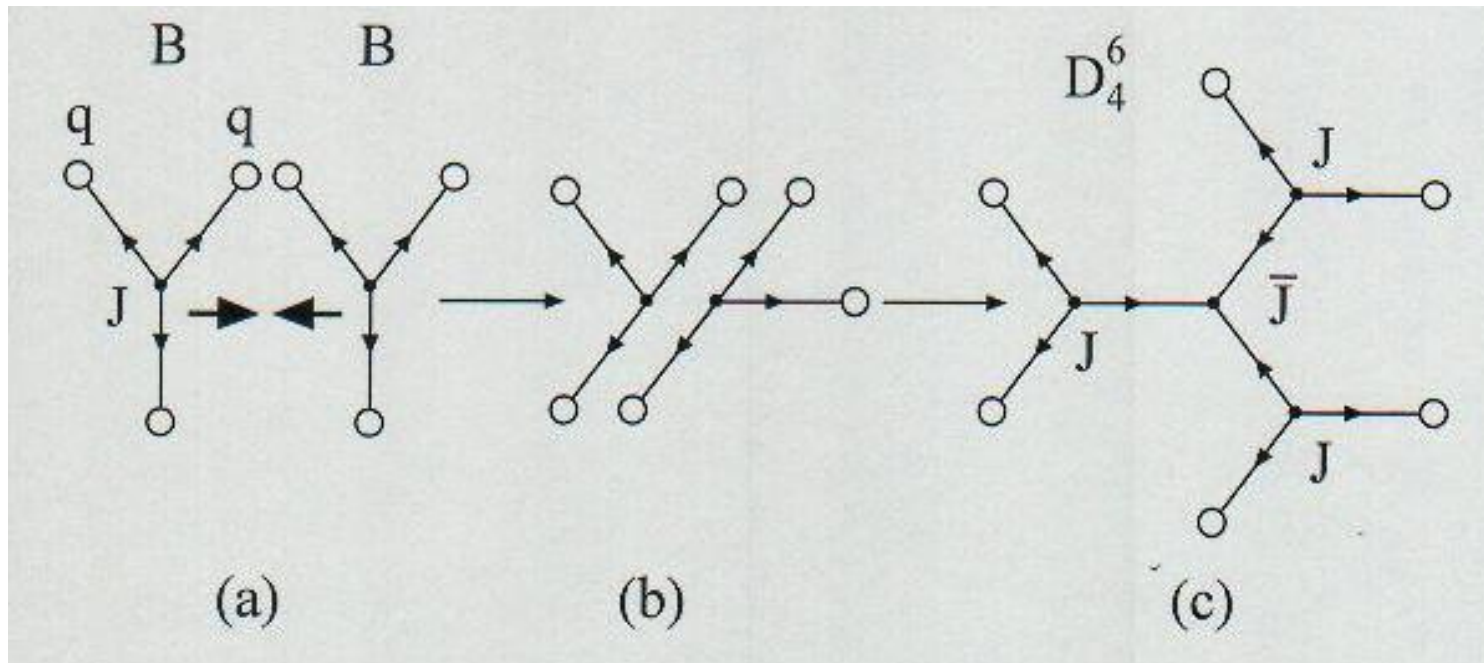
- Short-range correlations among  $N_1, N_2$  and  $N_3$  are duly taken into account ; T.Kasahara, Y.Akaishi and H.Tanaka, PTP Suppl.No.56(1974)96



# EOS of Neutron Star Matter



# Repulsion from SJM-----**flavor independent**

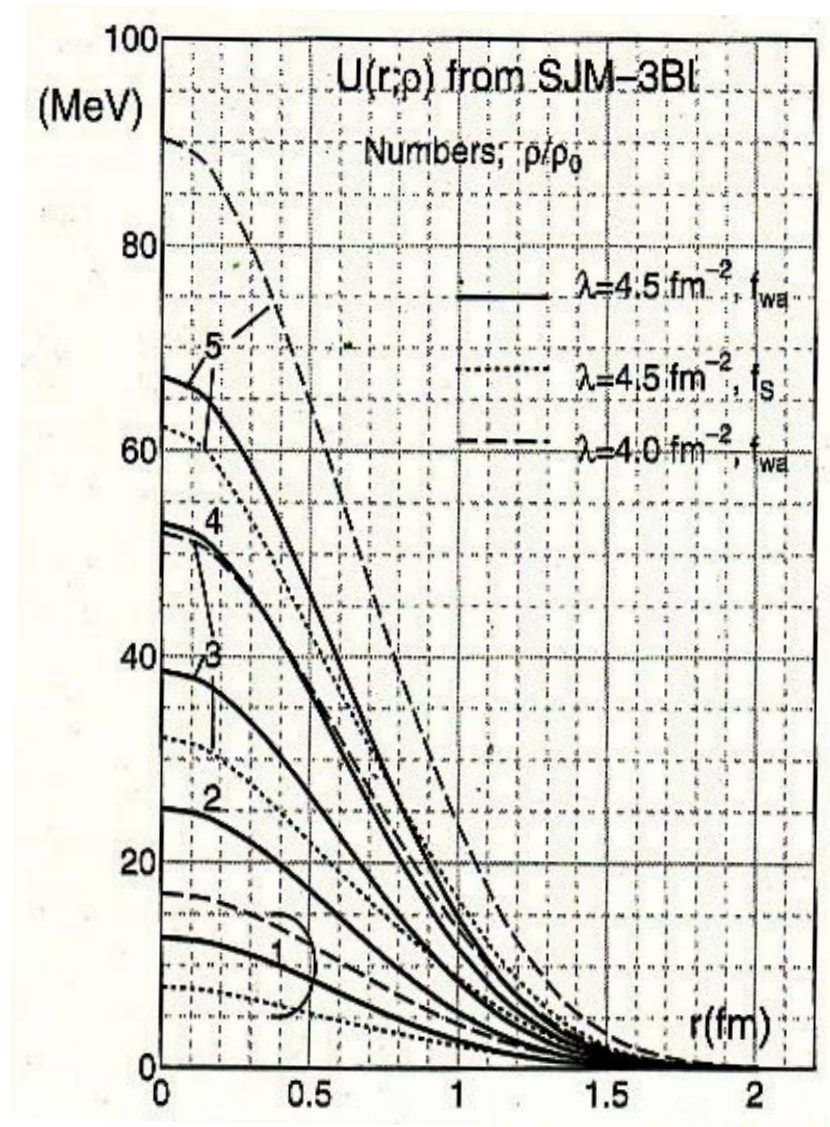


- (a) 2B come in short distance
- (b) Deformation (resistance)
- (c) Fusion into 6-quark state

(by R. Tamagaki)

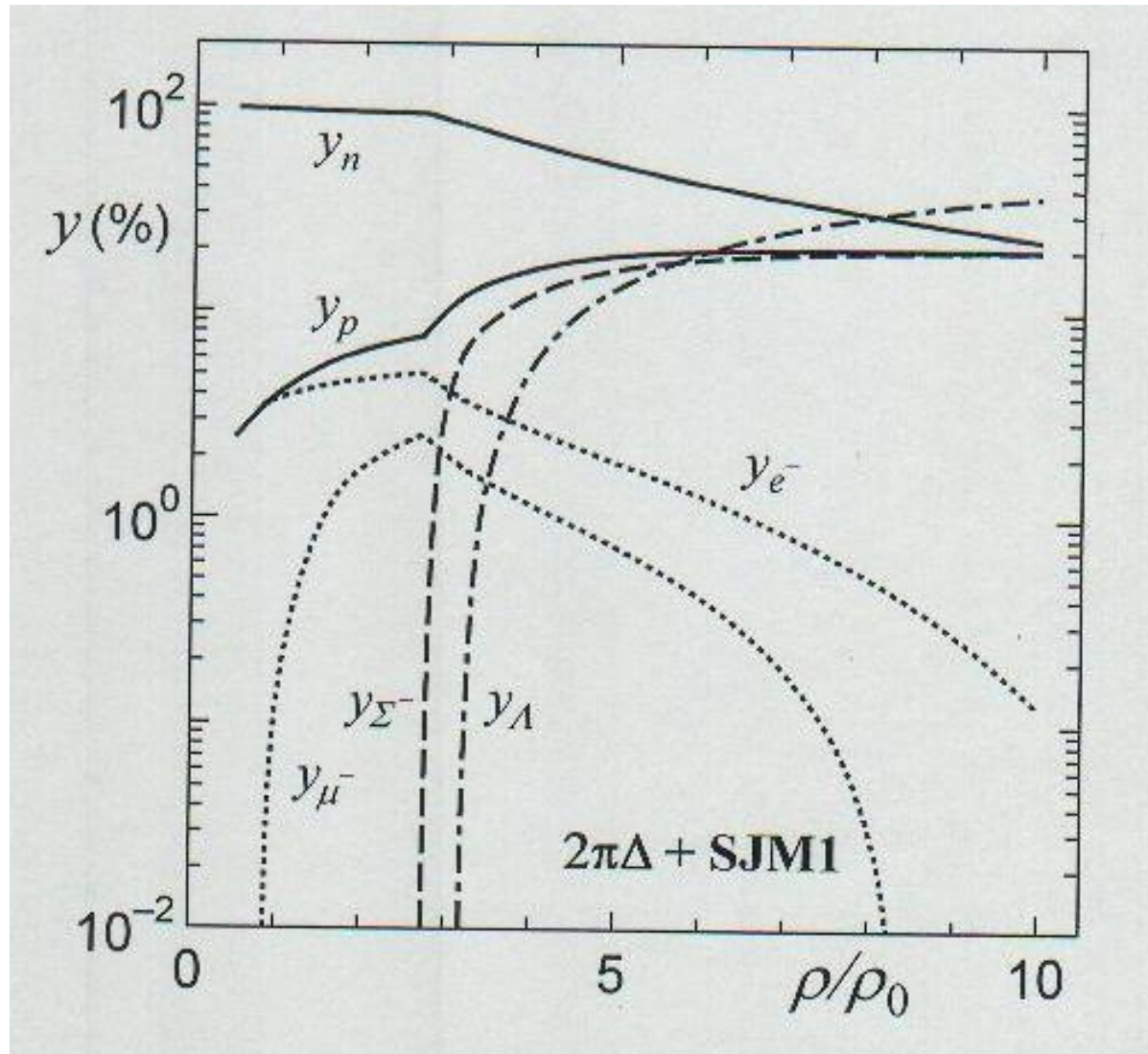
Prog. Theor. Phys. 119  
(2008) 965.

○ **Energy barrier ( $\sim 2\text{GeV}$ ) corresponds to repulsive core of BB interactions**

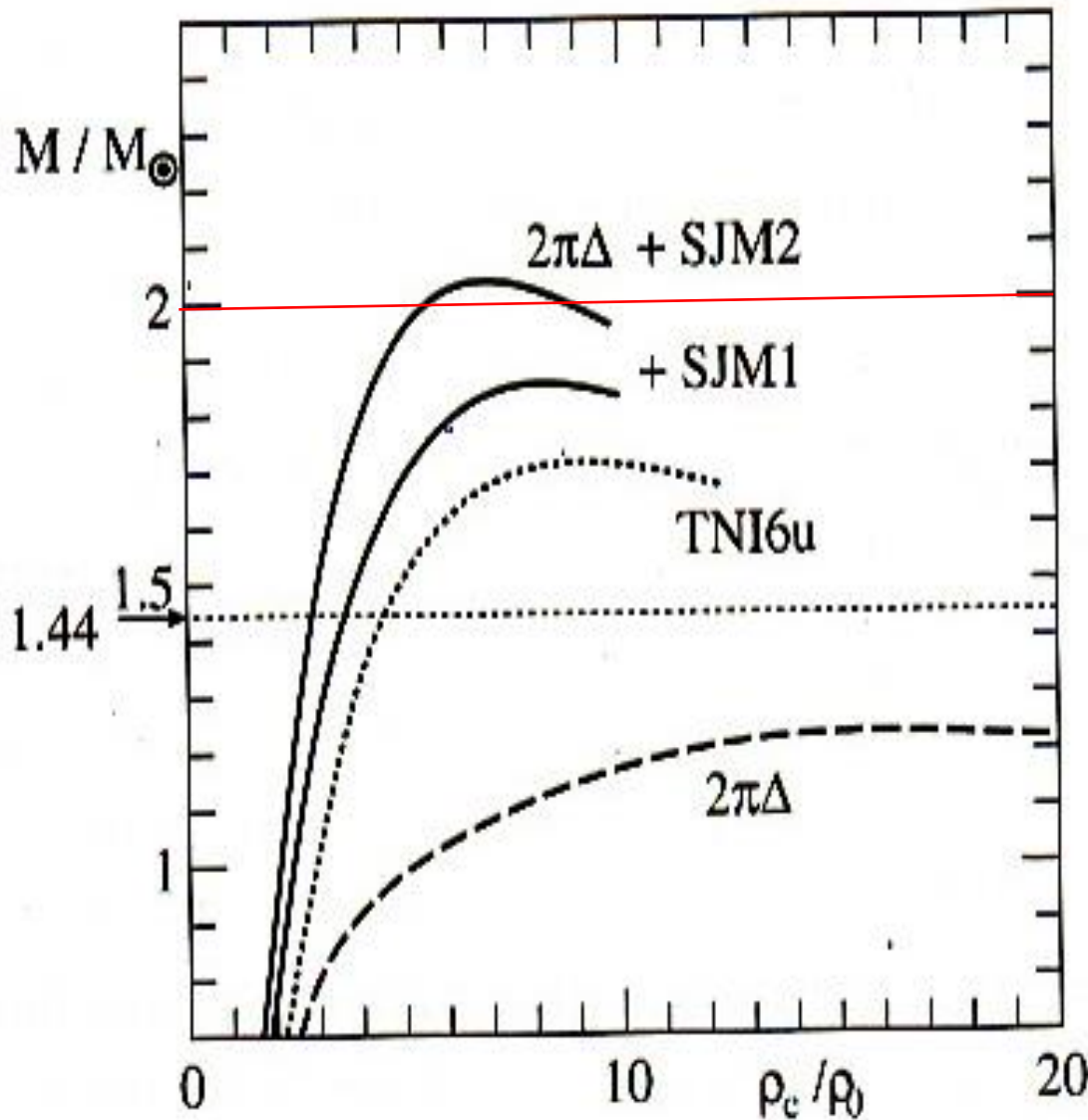


R. Tamagaki, Prog. Theor. Phys. 119 (2008) 965.

# Fraction of constituents in Y-mixed NSs



# Mass v.s. Central Density



NS-mass from 2-body force + "universal" 3-body force ( $2\pi\Delta$ -type + SJM).

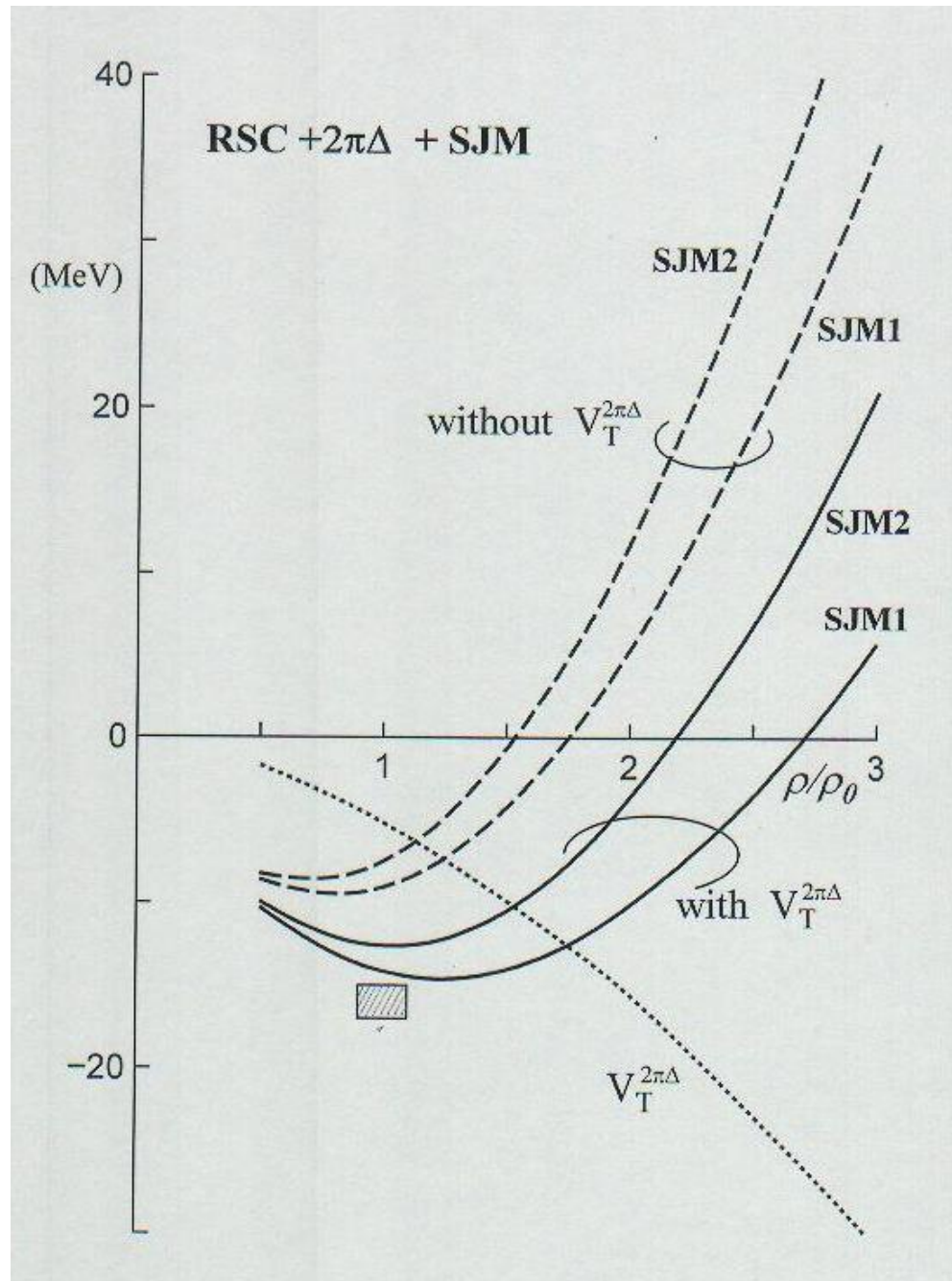
$M_{max} > 2M_{\odot}$   
is possible.

(Before observations)

T.Takatsuka, S.Nishizaki and R.Tamagaki, AIP Conference Proceedings 1011 (2008) 209.



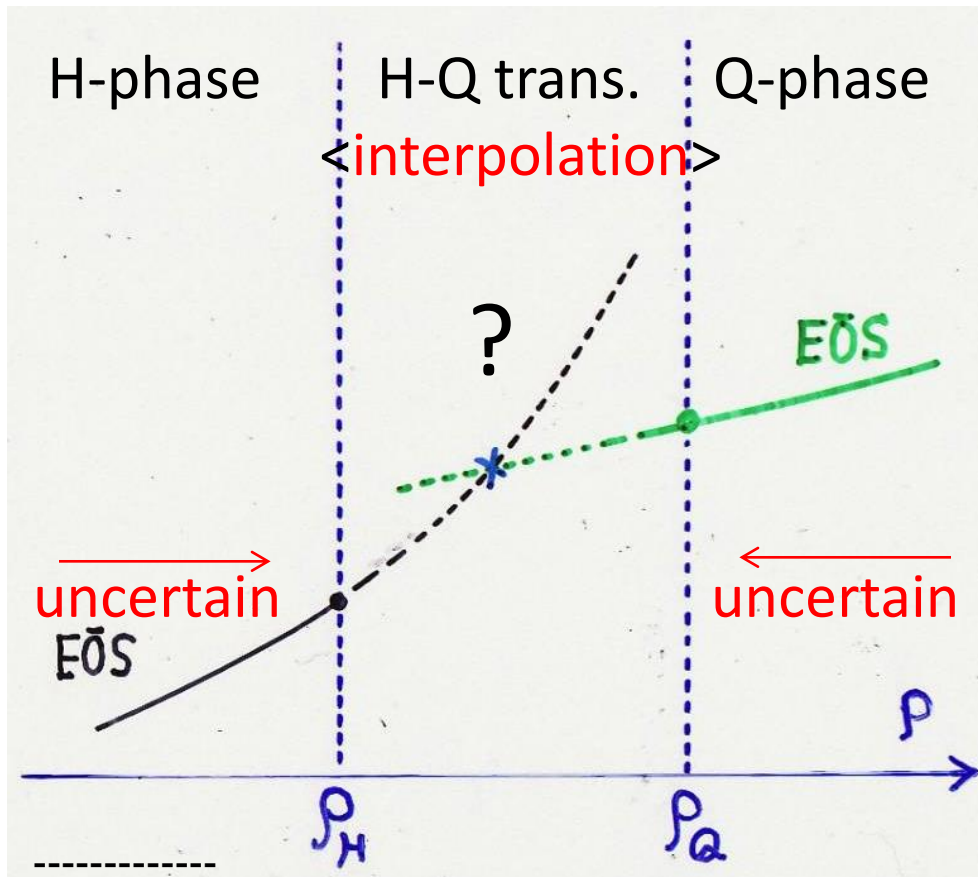
# Symmetric Nuclear Matter





# □ Possibility of quark matter in NSs <sup>\*</sup>)

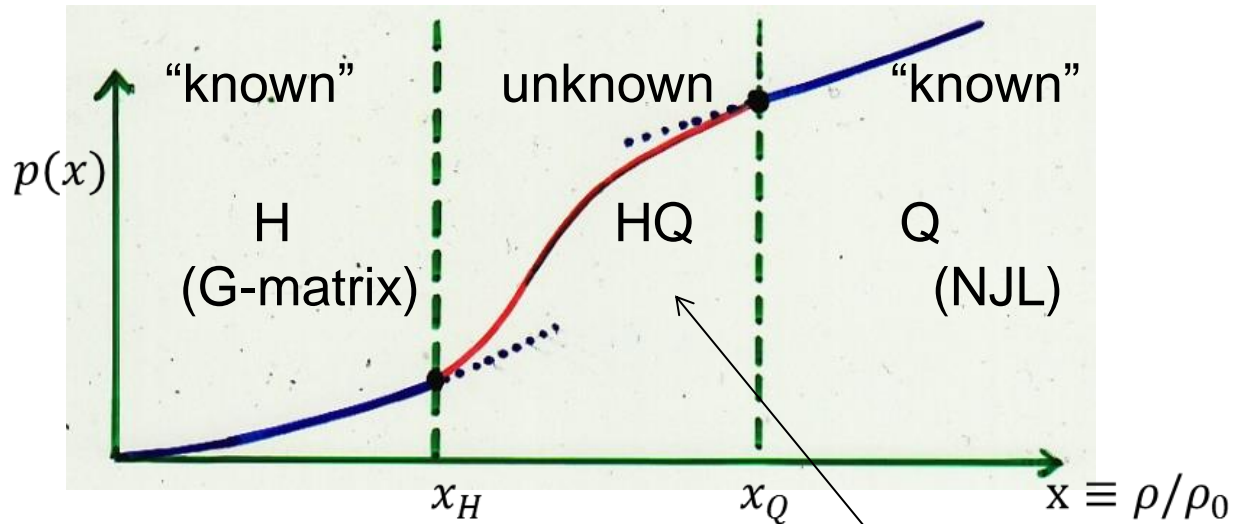
## A way of approach



- H: point particle + interaction  
→ G-Matrix, Variational
- Q: q-matter + asymptotic freedom
- HQ Phase transition  
Cross point (Maxwell, Gibbs) → not necessarily reliable
- **Need new strategy**

- T. Takatsuka, T. Hatsuda and K. Masuda, AIP Conference Proceedings 1484 (Melville, N.Y. 2012) 406.
- K. Masuda, T. Hatsuda and T. Takatsuka, ApJ 794 (2013) 12.

# (1) “3-window model”



①  $p(x) = a^m + bx^n + c \quad \left( p = x^2 \frac{\partial(\varepsilon)}{\partial x} \right)$

②  $\varepsilon(x) = \frac{a}{m-1} x^m + \frac{b}{n-1} x^n - c + dx$

③ Conditions

(i) thermodynamic stability:  $\frac{\partial p}{\partial x} > 0$

(ii) sound velocity:  $v_z \leq c$

④ Determination of  $(a, b, c, d)$

$$p(x_H) = p_H, \quad p(x_Q) = p_Q$$

$$\varepsilon(x_H) = \varepsilon_H, \quad \varepsilon(x_Q) = \varepsilon_Q$$

not by Gibbs condition,  
but by phenomenological  
interpolation

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• T. Takatsuka, “Genshikaku Kenkyu”  
Vol.57 (2013) 270.

# ○ Quark Matter phase <sup>\*)</sup>

- (2 + 1)-flavor NJL model with vector interaction

$$L_{NJL} = \bar{q}(i\not{\partial} - m)q + \frac{1}{2}G_S \sum_{\alpha=0}^8 \{(\bar{q}\lambda^\alpha q)^2 + (\bar{q}\lambda^\alpha i\gamma_5 q)^2\} \\ + G_D \{ \det \bar{q}(1 + \gamma_5)q + h.c. \} - \frac{1}{2}g_V(\bar{q}\gamma^\mu q)^2$$

with  $q \equiv \{q_i; i = u, d, s\}$      $m \equiv \{m_i\}$

- Hatsuda-Kunihiro parameter set (Phys. Rep - 247 (1994) 221)

$$\Lambda = 631.4 \text{ MeV}, G_S \Lambda^2 = 1835, G_D \Lambda^2 = 9.29$$

$$m_u = m_d = 5.5 \text{ MeV}, m_s = 135.7 \text{ MeV}$$

- $g_V$  is not well determined, but it is suggested that  $g_V$  can be comparable or even larger than  $g_S$

→ we take

$$\frac{g_V}{g_S} \sim (0 - 1.5)$$

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\*) K.Masuda, T.Hatsuda and T.Takatsuka, ApJ 794 (2013) 12

## Some results for NS models

JEOS	$x_H$	$x_S$	H-EOS	Q-EOS	m	n	$M_{max}/M_{\odot}$	$R/k_m$	$\rho_c/\rho_0$
1	1.5	5.5	TNI2u	$g_v = 0.5G_S$	0.2	-2.6	2.61	13.38	3.99
2	1.5	6.0	"	"	"	"	2.59	13.27	3.90
3	1.5	7.0	"	"	"	"	2.53	12.08	4.52
4	1.5	8.0	"	"	"	"	2.48	12.56	4.35
5	1.5	7.0	"	$g_v = 1.5G_S$	"	"	3.08	13.73	3.34
6	1.5	7.0	"	$g_v = 1.0G_S$	"	"	2.86	13.28	3.94
7	1.5	7.0	"	$g_v = 0.$	"	"	1.99	12.30	4.85
8	1.5	7.0	"	$g_v = 0.5G_S$	2.6	-0.2	2.62	13.44	4.05
9	1.5	7.0	"	"	1.2	-1.2	2.61	13.44	3.73

## (2) Hadron-Quark Crossover Model

From a viewpoint of quark percolation through hadrons, we construct a phenomenological EOS by assuming a smooth crossover transition from hadron matter to quark matter

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K.Masuda, T.Hatsuda and T.Takatsuka, ApJ 794(2013)12

K.Masuda, T.Hatsuda and T.Takatsuka, PTEP (2013)073D01

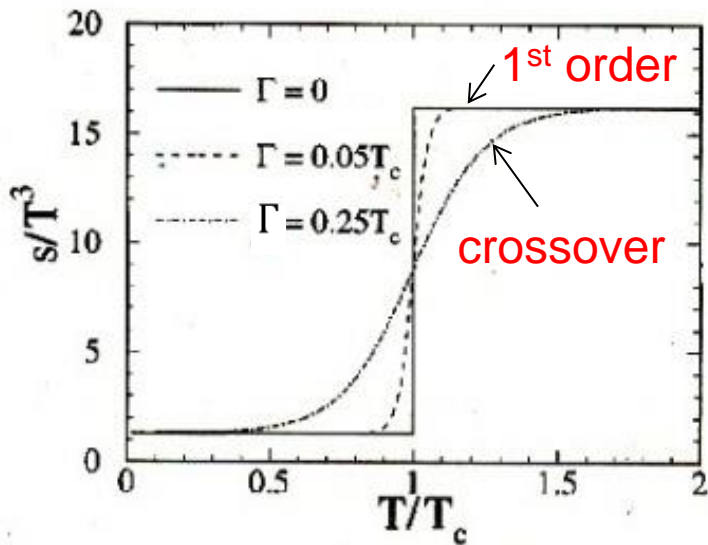
# □ Motivation

## ○ QCD Phase diagram:

$\mu=0, T \neq 0 \rightarrow$  aspect of H-Q crossover transition at  $T_c \sim 200$  MeV  
 $\rightarrow$  well described by the parameterization (\*)

$$s(T) = s_H(T)\omega_H(T) + s_Q(T)\omega_Q(T)$$

$\omega_H(T) + \omega_Q(T) = 1$ , e.g.,  $\omega_Q(T) = \{1 + \tanh(T - T_c)/\Gamma\}/2$   
 $\rightarrow p(T) = \int_0^T s(t)dt, e(T) = T_s(T) - p(T)$



## ○ Correspondence

T increase  $\rightarrow$  K.E. increase  
 $\mu$  (or  $\rho$ ) increase  $\rightarrow$  K.E. increase ] **common**  
of constituent particles

## ○ Taking analogy, assume for $\mu \neq 0$ crossover case

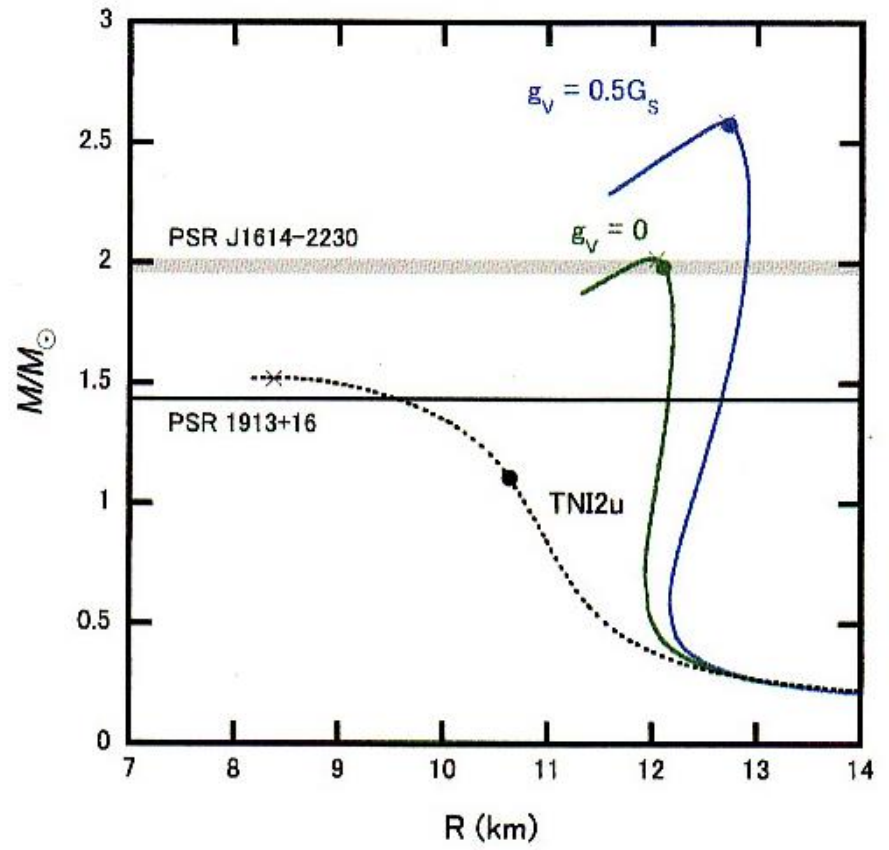
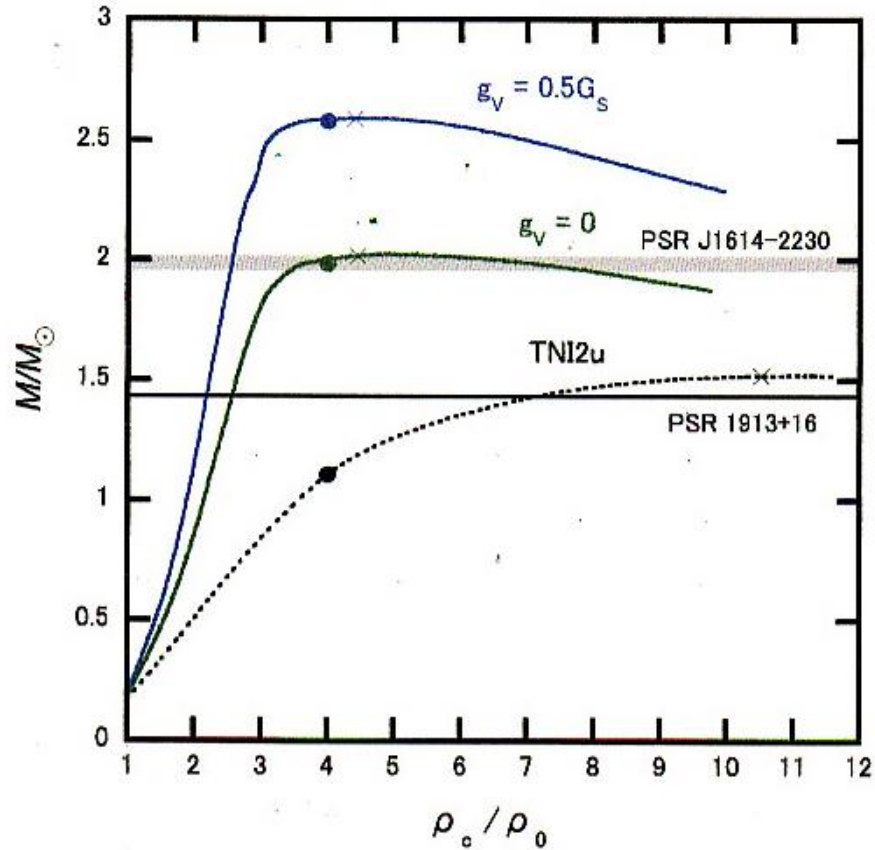
$$\hat{F}(\rho, T; Y_l) = \hat{F}_{HL}(\rho, T; Y_l)w_-(\rho, T) + \hat{F}_{QL}(\rho, T; Y_l)w_+(\rho, T).$$

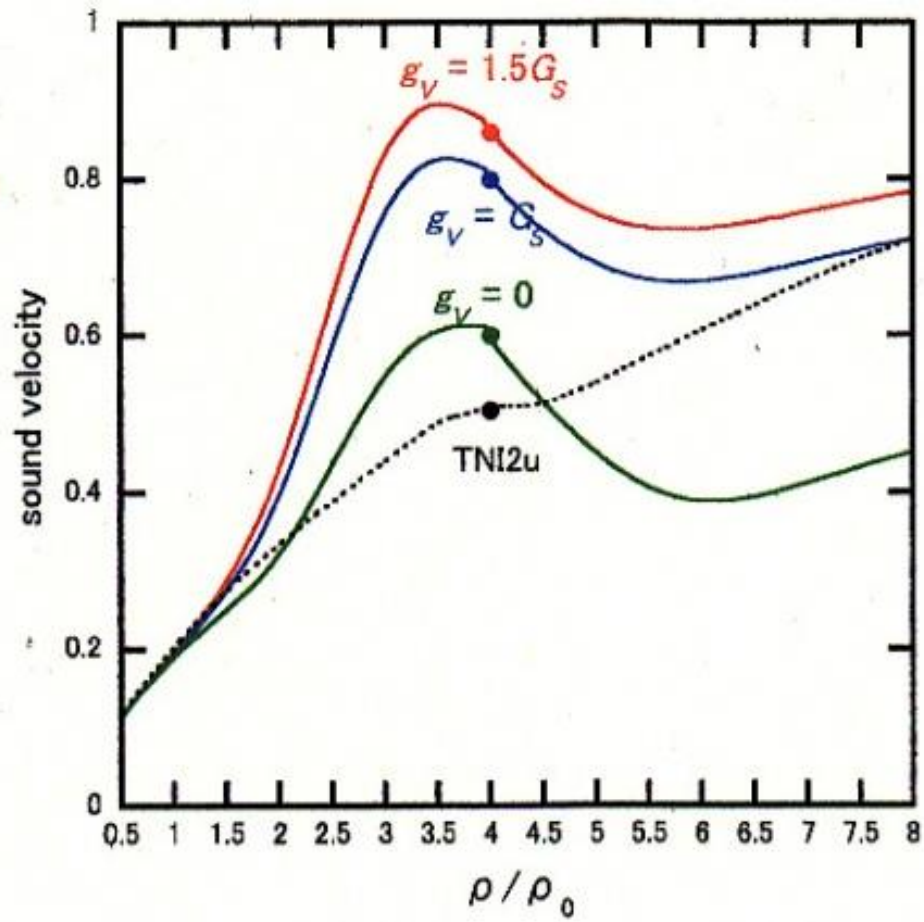
$$w_{\pm}(\rho, T) \rightarrow w_{\pm}(\rho) = \frac{1}{2} \left( 1 \pm \tanh \left( \frac{\rho - \bar{\rho}}{\Gamma} \right) \right),$$

(\*) M. Asakawa and T. Hatsuda, Phys. Rev. D55 (1997) 4488.



# 2-solar –mass NSs are possible



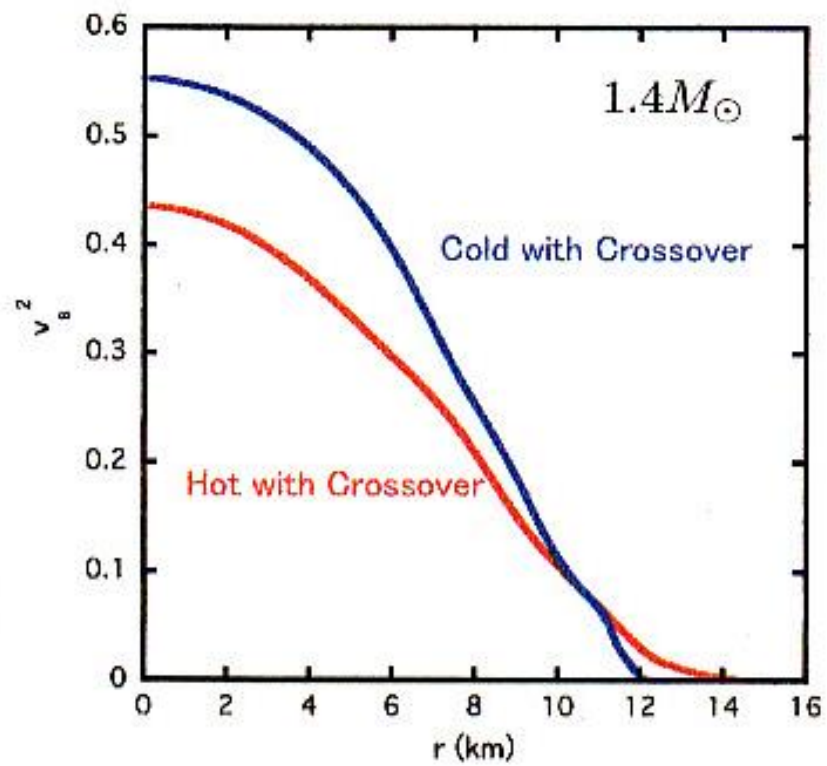
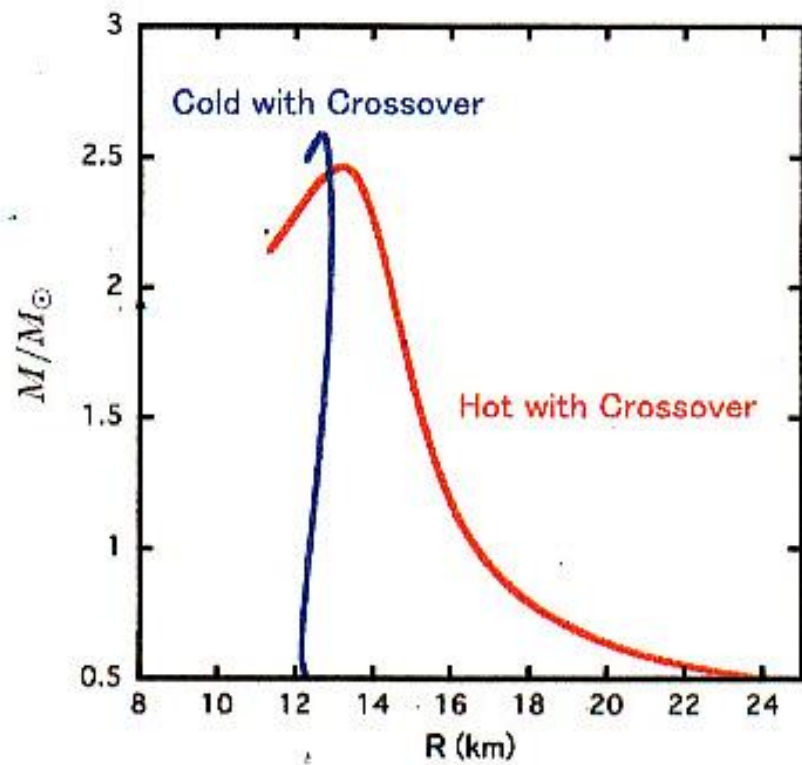


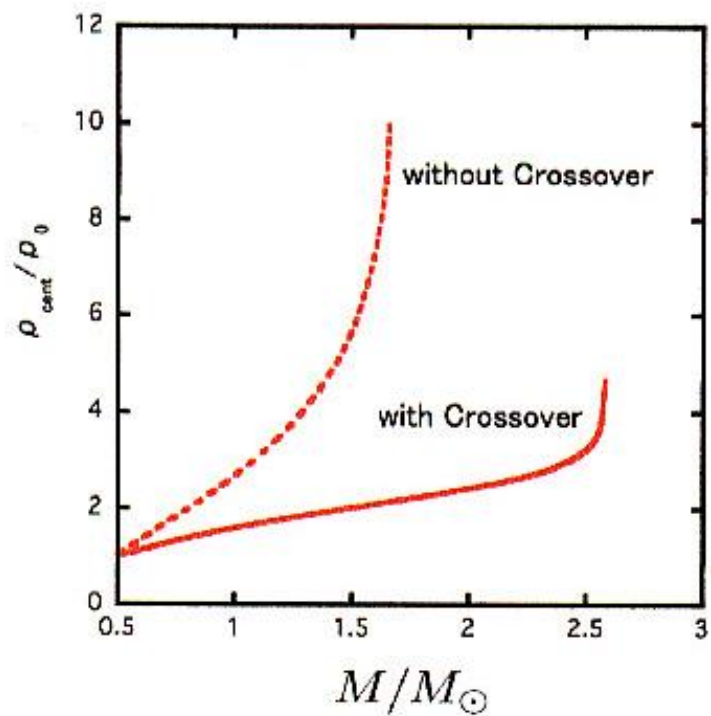
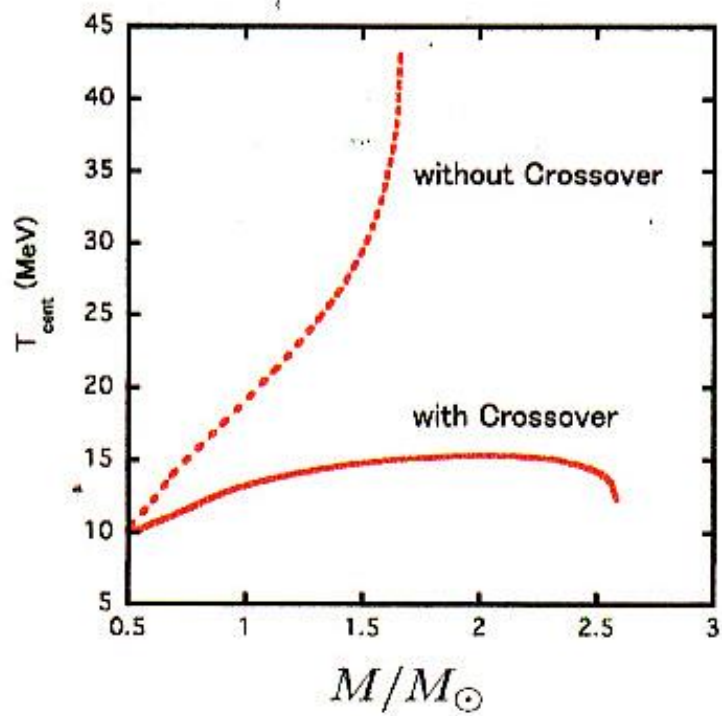
Sound velocity

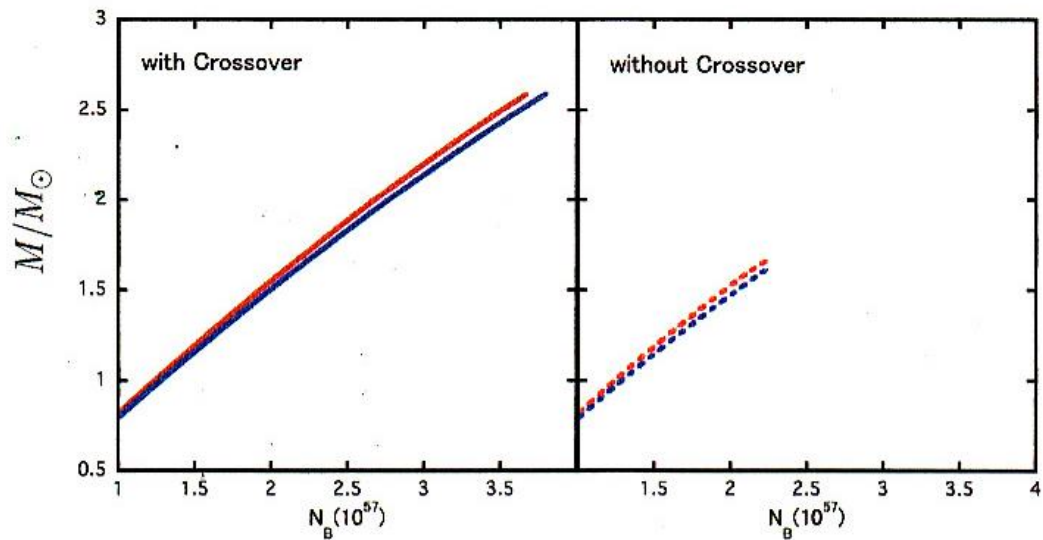
Application of our EOS with crossover  
(named “**CRover**”) to **hot** NSs at birth

It is found that the H-Q crossover plays important roles not only to generate a stiff EOS compatible with extremely heavy NSs but also to lower the internal temperature of hot NSs

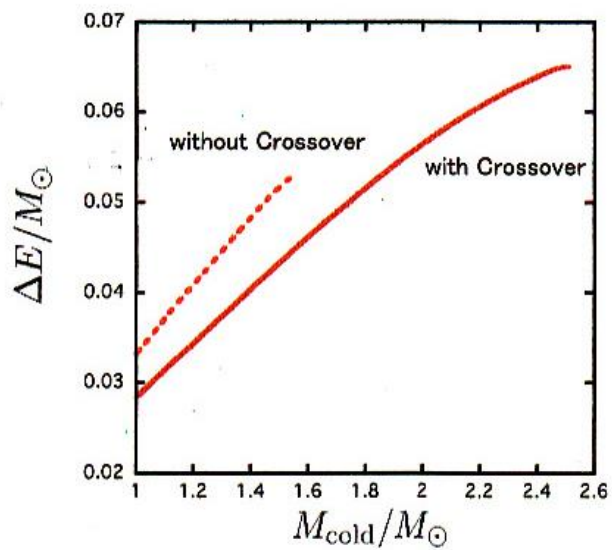
It is noteworthy that hot NSs interestingly constrain  
The maximum mass of cold NSs.







(a)





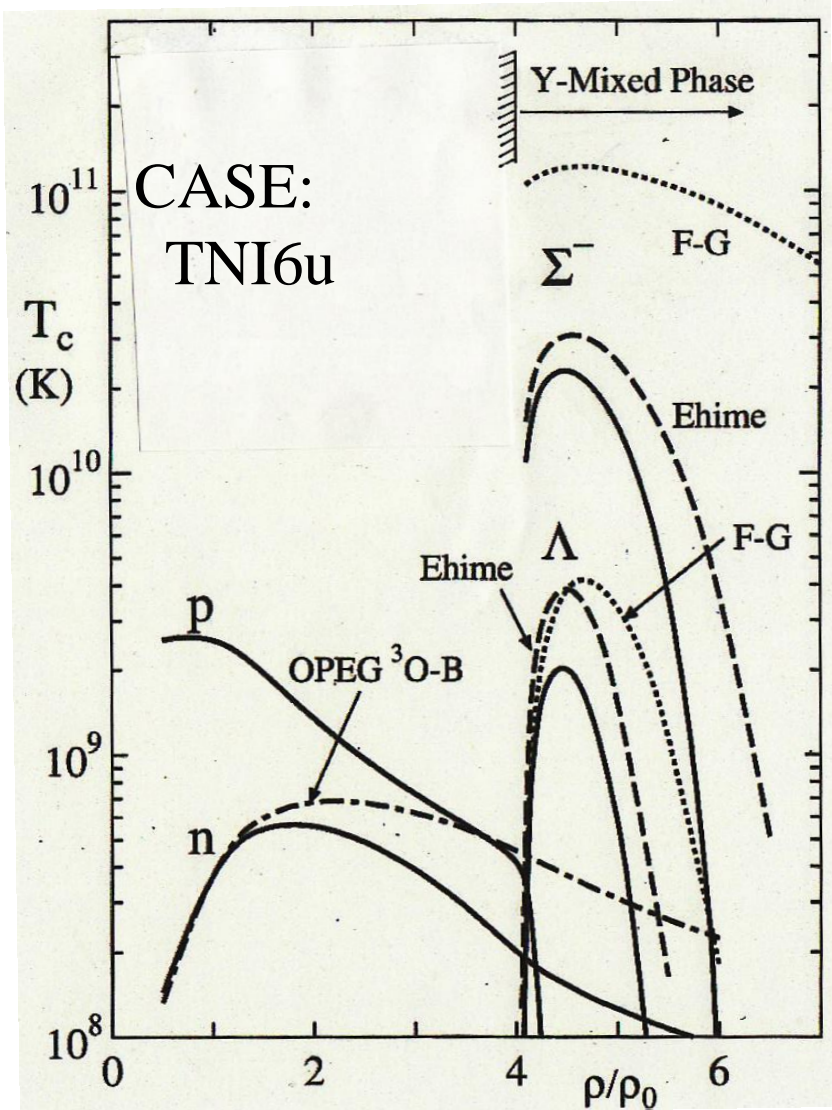
## Too-rapid cooling of NSs with $\Upsilon$ -mixing

Direct URCA is made possible by  $\Upsilon$  (YDurca, e.g.,

$$\Lambda \longrightarrow p + e^- + \bar{\nu}, \quad p + e^- \longrightarrow \Lambda + \nu$$

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c.f.) Durca :  $n \rightarrow p + e^- + \bar{\nu}$ , and inverse process  
Murca:  $n + N \rightarrow p + N + e^- + \bar{\nu}$ , and inv. pro.



Critical Temperature  $T_c$   
versus Density  $\rho$

□ Pairing type:

$n \rightarrow 3P2$

$p, \Lambda, \Sigma^- \rightarrow 1S0$

□ Pairing interactions:

$n, p \rightarrow$  OPEG-A pot.

$\Lambda, \Sigma^- \rightarrow$  ND-Soft

for solid lines

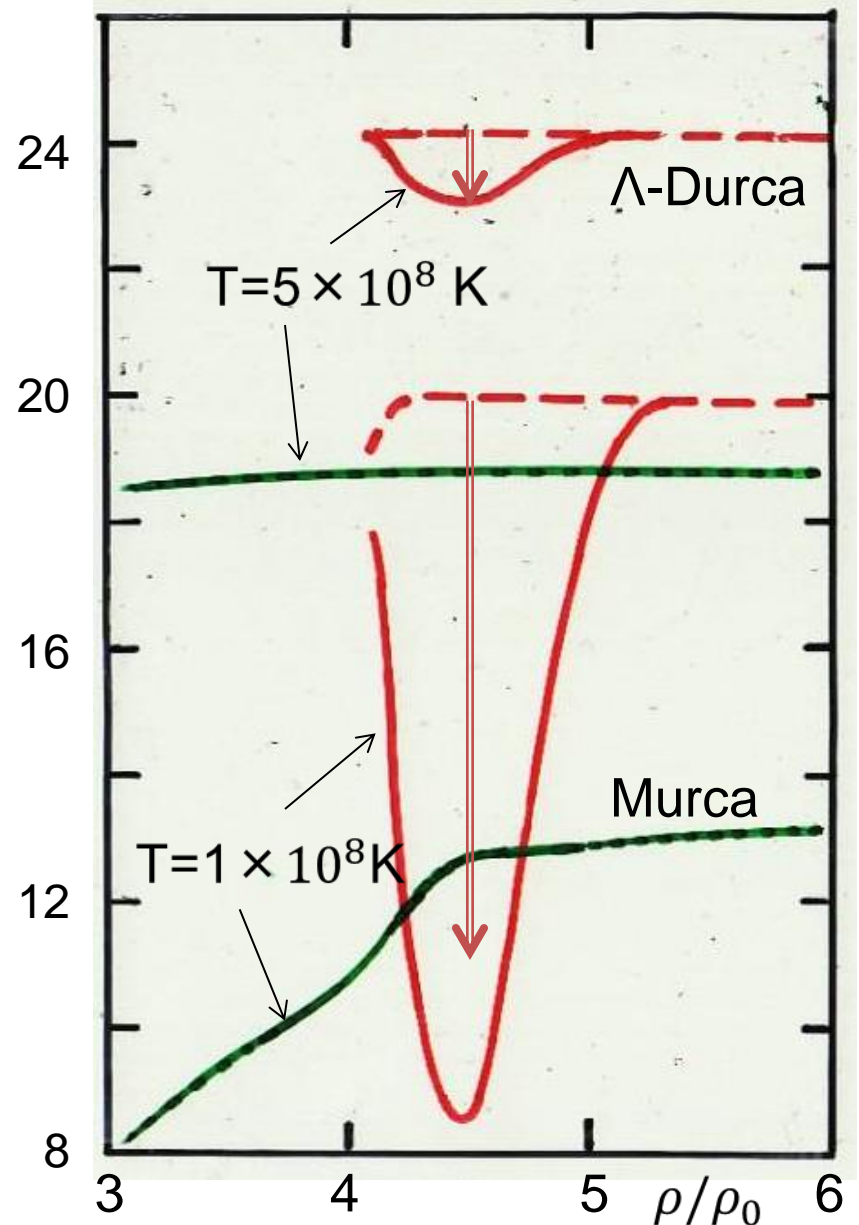
# Suppression by $\Lambda$ -Superfluidity

○  $\varepsilon$ :  $\nu$ -emissivity due to  
 $\Lambda$ -Durca (Red)  
 Murca (Green)  
 dashed line: No suppression

○  $T$ : internal temperature of  
 NSs

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 T.Takatsuka, S.Nishizaki, Y.Yamamoto  
 and R.Tamagaki,  
 Prog.Theor.Phys.115(2006)355

Log  $\varepsilon$  (erg/cm<sup>3</sup>·s)



# With and without Y core depends on M

Too -rapid cooling → **Hyperon superfluidity**

NSs with  $M > 1.35 M_{\text{sun}}$  have a Y-mixed core. If Y-superfluidity is realized, it suppresses the efficient  $\nu$ -emission by Y-Durca ( $\exp(-\Delta/T)$ )

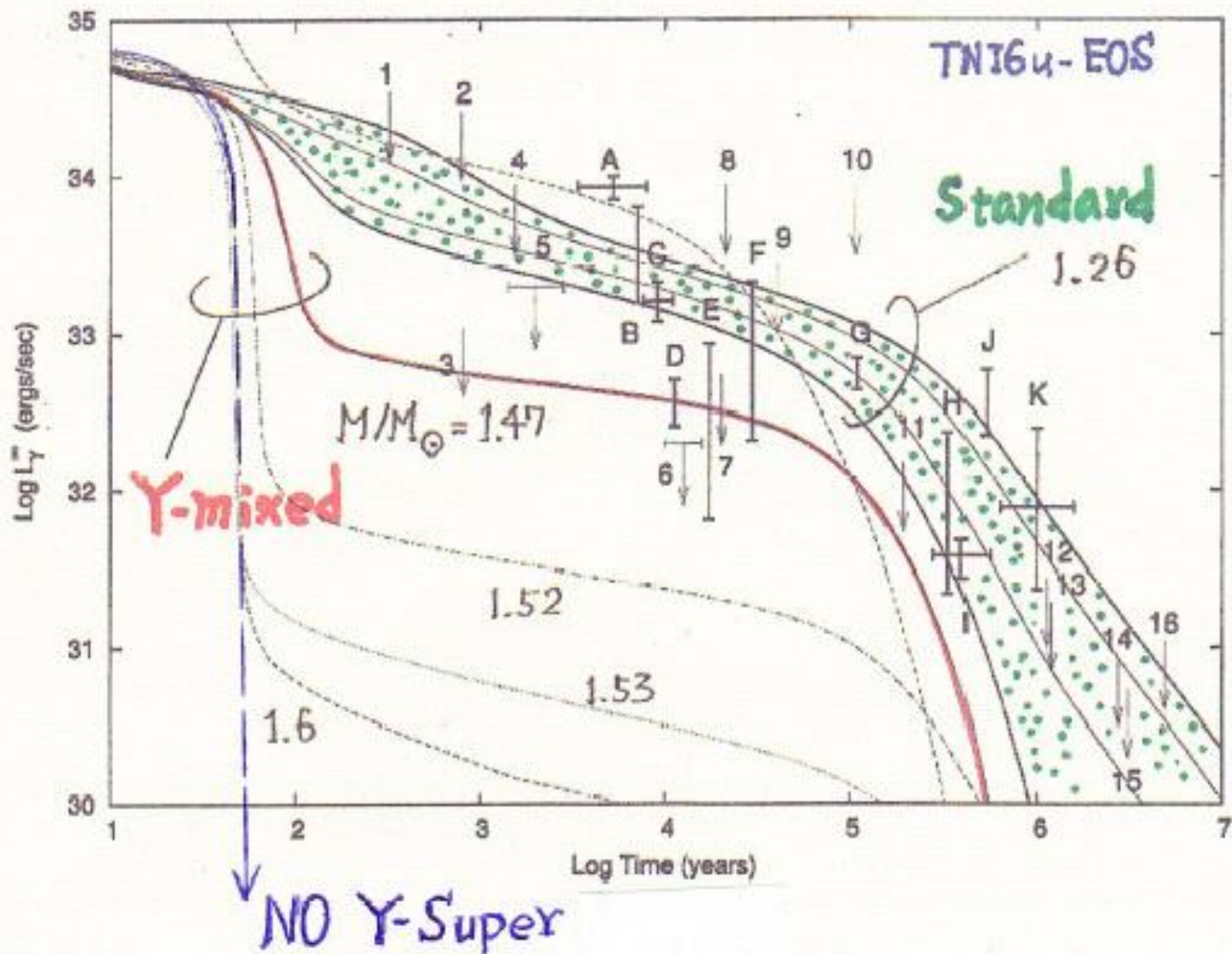
→ moderate cooling consistent with colder class NSs

That is, a new scenario is

Lighter NSs → Warm (standard slow cooling of Murca)

Heavier NSs → Cool (nonstandard fast cooling of YDurca (“hyperon cooling”) + Y-super)

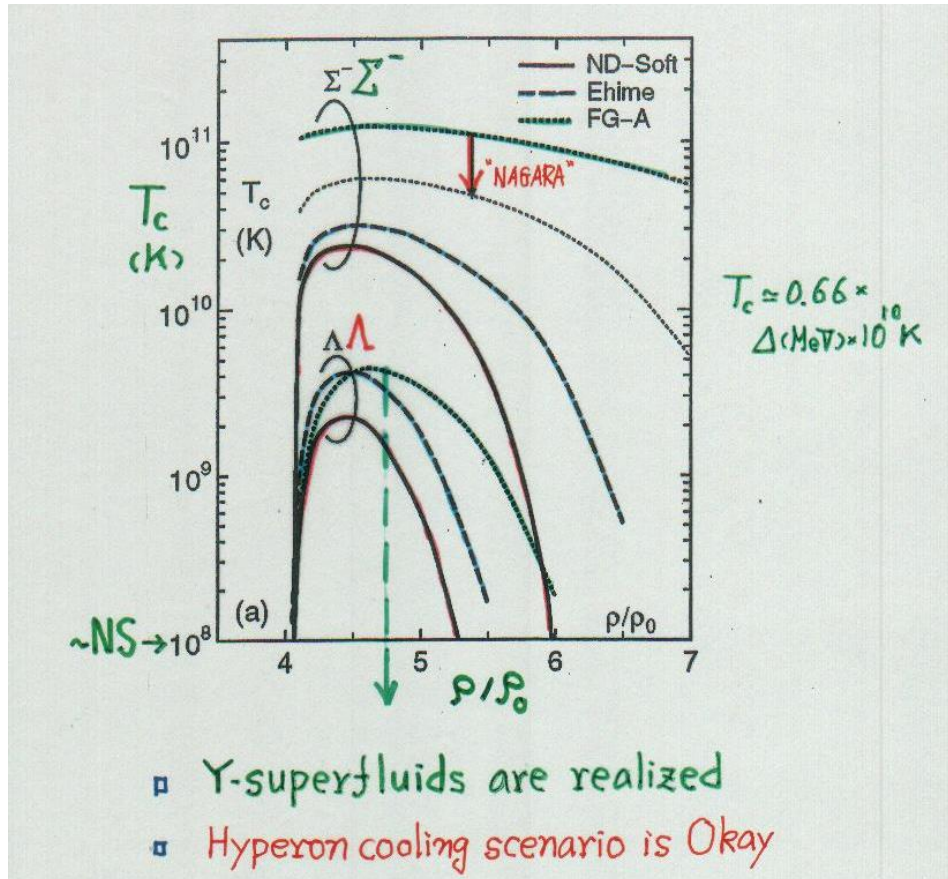
Massive NSs → Very Cold (“hyperon cooling”)



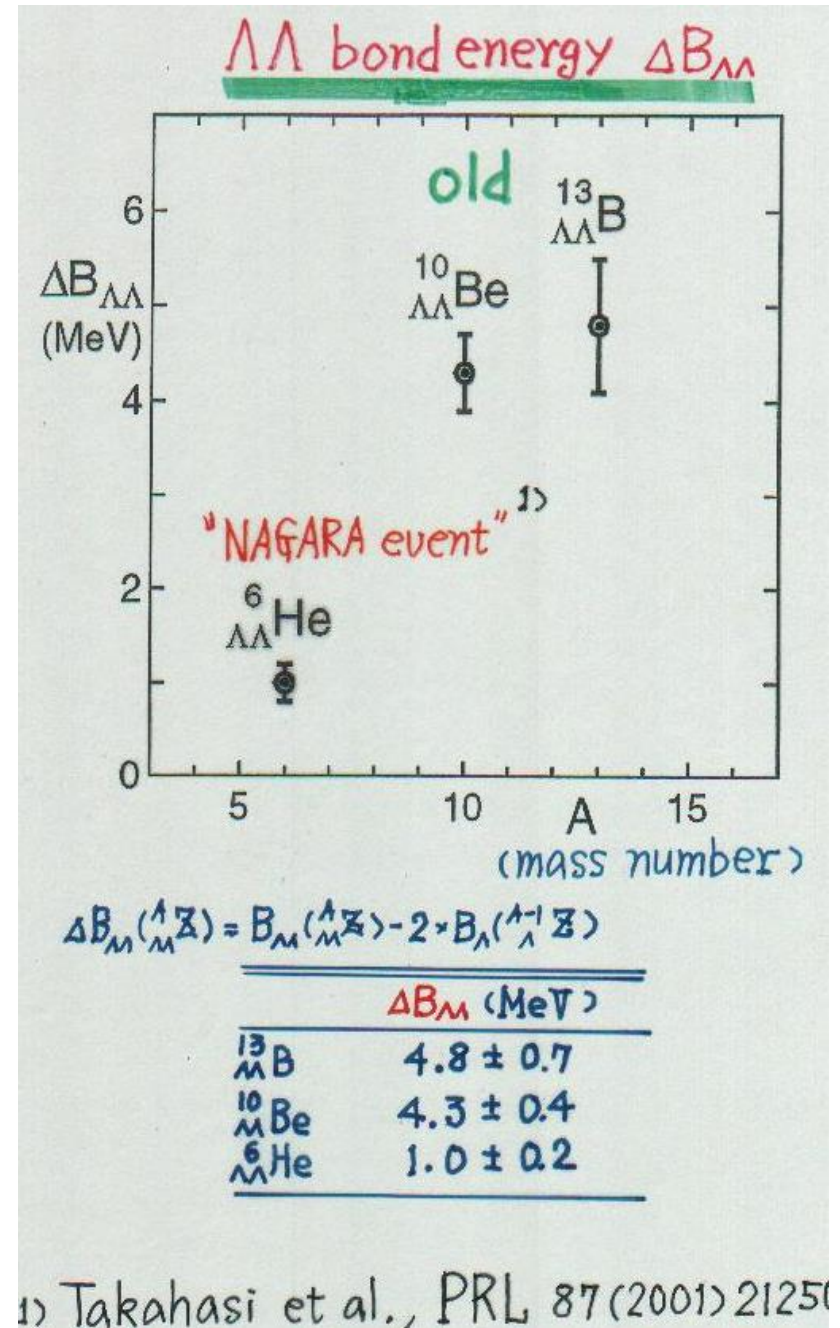


# NO $\Lambda$ -super due to "NAGARA"

$A$ -dependence ?  $\rightarrow$



- ▣  $\Upsilon$ -superfluids are realized
- ▣ Hyperon cooling scenario is Okay





# NAGARA event

**NO  $\Lambda$ -super !**  $\Rightarrow$  Too-rapid cooling  $\rightarrow$  break down of the hyperon cooling scenario

**Need more careful investigations**

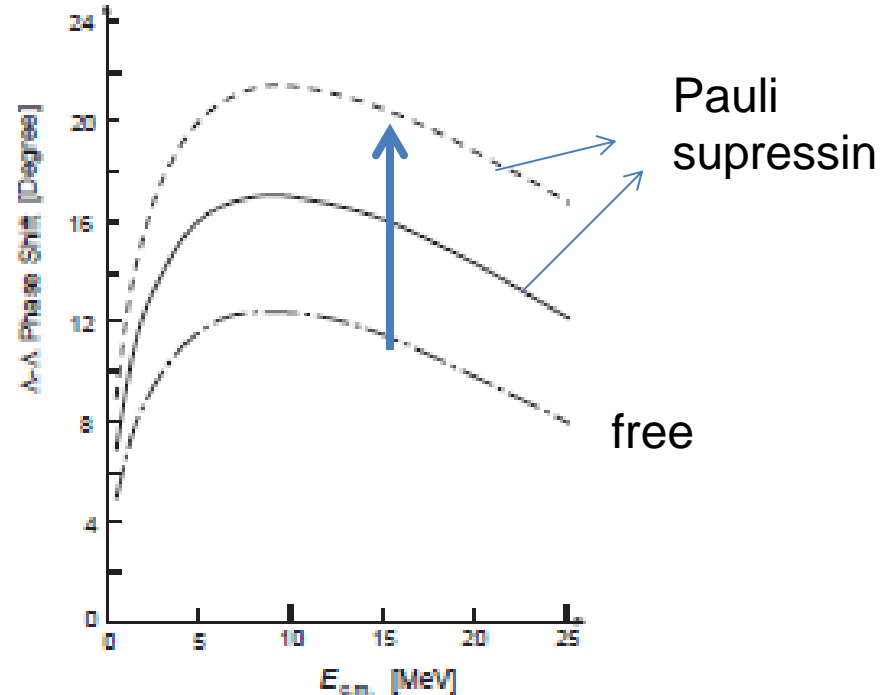
- sensitivity to  $\Lambda\Lambda$  int.  $\rightarrow$  rearrangement effect, dependence on “ $\alpha$ -core” ?
- mechanism to enhance  $\Lambda\Lambda$  attraction
- How about the **A-dependence** of  $\Lambda\Lambda$  bond energy? (J-PARC exp. is highly expected)
- Especially, Lattice cal. study for  $\Lambda\Lambda$  int.

We need further investigations, i.e.,

- a) A-dependence
- b) Checking the validity of  $\Lambda\Lambda$ -bond energy extraction
- c) Including other missing effects to enhance  $\Lambda\Lambda$  attraction

e.g.

$\Lambda\Lambda-\Xi N$  coupling effects in medium



K.S.Myint ,S.Shinmura and Y.Akaishi,  
Eur.Phys.J.A16 (2003) 21

# Summary

Due to the  $\Upsilon$ -mixing sure to occur in NS cores, we are faced to the serious problems, too-softened EOS and too-rapid cooling .

The former is so to speak , "hyperon crisis" , considering recent observations of very massive 2-solar-mass NSs. Possible solution would be , universal 3-body force in the case of pure hadronic framework , and hadron- quark crossover transition when quark degrees of freedom is taken into account.

To get out from the problem of too-rapid cooling, a central concern would be in the point how we revive the  $\Lambda$ -superfluidity ,reconciling  $\Lambda\Lambda$ -hypernuclear data.