

# Mesons in nuclei and partial restoration of chiral symmetry

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mesons in nuclear matter in the context of chiral symmetry

- introduction
- $K^{\text{bar}}$  meson in nuclear medium
- $K^+$  nucleus scattering revisited
- $\pi^0 \rightarrow \gamma\gamma$  in nuclear medium
- $\eta$  mesonic nuclei
- $\eta'$  in nuclear medium and  $\eta'$ -N interaction



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# Motivation

## Why do we study the properties of hadron in nucleus ?

- as nuclear physics
  - interested in the nature of the strong interaction
  - study many-body systems governed by the strong force
  - discover new bound systems of the strong interaction
  - exotic states are interesting
- as hadron physics
  - in-medium change of hadron properties
  - more fundamental interpretation in terms of QCD
  - one of the key concept is partial restoration of **chiral symmetry**
- for other research areas
  - provide basic informations of high density physics
  - important constraints accessible in experiments on earth

# In-medium change of hadron properties

## medium effects on hadron

mass modification

mass is given by pole of propagator at rest

vertex correction

## wave function renormalization

$$Z = \left(1 - \frac{\partial \Sigma}{\partial p_0^2}\right)^{-1}$$

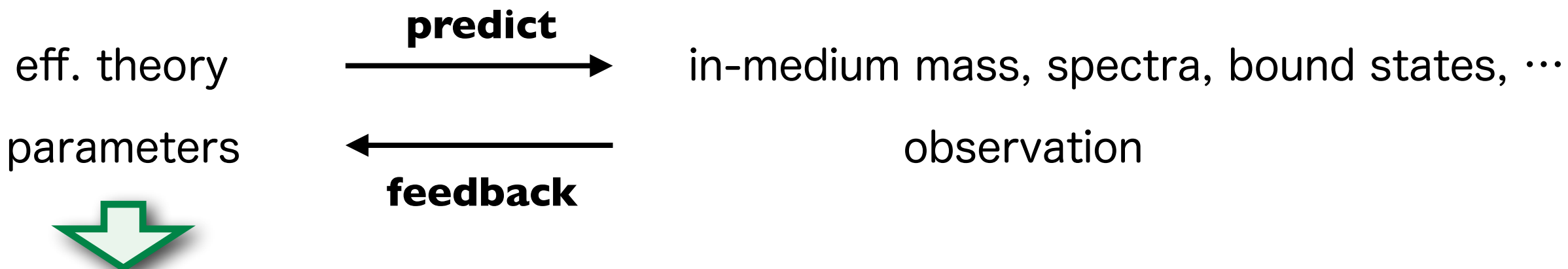
**in-medium self-energy  $\Sigma$**  

describes interaction between hadron and nuclear matter.

**effective theory, effective model** such as, in-medium ChPT

provides fundamental interactions between hadrons and nucleons

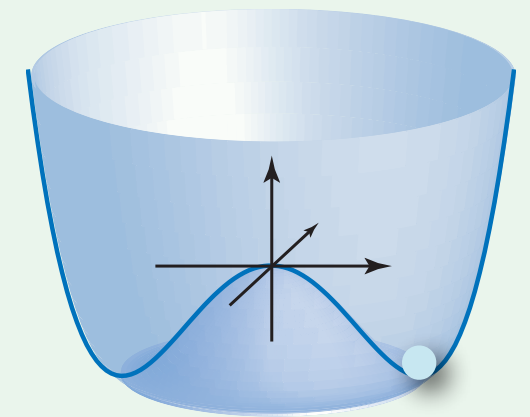
describes hopefully nuclear matter out of nucleon correlations (NN, NNN, ...)



more fundamental interpretation in terms of QCD

# Chiral Symmetry

- a fundamental symmetry in QCD,
- dynamically broken by physical states
- dynamical ChS breaking determines **vacuum property** and describes **low energy hadron dynamics**
  - most of light hadron properties is affected by ChSB
  - hadrons are excitation modes upon vacuum
- DChSB is a **phase transition phenomenon**
  - broken symmetry can be restored at extreme conditions, such as high density, high temp.
  - partial (incomplete) restoration takes in nuclear medium
  - pionic atom experiments and pion nucleus scattering with theoretical consideration have suggested that chiral symmetry is partially restored in nuclear matter with 30% reduction of quark condensate



**light pion mass,  
mass generation etc.**

K. Suzuki et al. PRL92, 072302 (04)

Friedman et al. PRL93, 122302 (04)

Kolomeitsev, Kaiser, Weise, PRL90, 092501 (03).

DJ, Hatsuda, Kunihiro, PLB 670, 109 (08).

# Reduction of $\pi$ decay constant

enhancement of s-wave repulsive interaction

**Deeply bound pionic atom** K. Suzuki et al. PRL92, 072302 (04)  
systematic study of  $\pi^-$  bound states in Sn isotopes

$$b_1^{\text{free}}/b_1 = 0.78 \pm 0.05 \quad \rho \sim 0.6 \rho_0$$

**Elastic scattering** (Friedman et al.)

$$b_1^{\text{free}}/b_1 \sim 0.69$$

related to in-medium reduction of pion decay constant  $F_\pi$

## Weinberg-Tomozawa reation

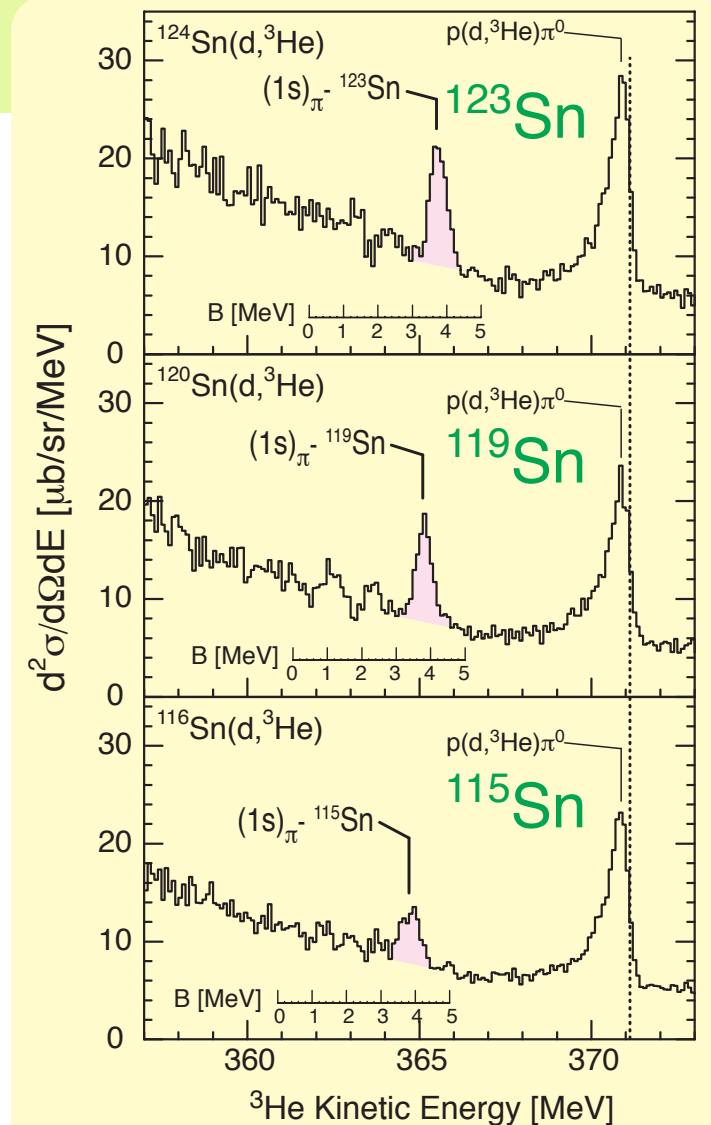
**in vacuum**  $4\pi \left(1 + \frac{m_\pi}{m_N}\right) b_1^{\text{free}} = -\frac{m_\pi}{2F^2}$

**in medium**  
**at low-density**  $4\pi \left(1 + \frac{m_\pi}{m_N}\right) b_1 = -\frac{m_\pi}{2(F_\pi^t)^2}$

$$\frac{b_1^{\text{free}}}{b_1} = \left(\frac{F_\pi^t}{F_\pi}\right)^2$$

**at low density**

DJ, Hatsuda, Kunihiro, PLB 670 (2008), 109.



# Chiral Symmetry

expectation in partial restoration of chiral symmetry in nuclear matter

- reduction of mass difference between parity partners

$\sigma$ - $\pi$     $\rho$ - $a_1$     $N$ - $N^*$    etc.

$\eta$  probes chiral symmetry for  $N$  and  $N^*(1535)$

- wave function renormalization for Nambu-Goldstone bosons

amplitudes of NG bosons have energy dependence due to chiral symmetry

$$Z = \left( 1 - \frac{\partial \Sigma}{\partial p_0^2} \right)^{-1}$$

DJ, Hatsuda, Kunihiro, PRD63, 011901(R);  
PLB 670 (2008), 109.

$K^+, \pi^0$   $K^+A$  scattering amplitude is enhanced due to  $Z$

- mass reduction of hadrons whose mass is generated by spontaneous breaking of chiral symmetry

a part of nucleon mass is generated by spontaneous breaking of chiral symmetry

effective mass of nucleon in nuclear matter is  $0.7 m_N$ .

$\eta'$  part of  $\eta'$  mass is generated by chiral symmetry breaking

$K^{\text{bar}}$  meson

# $\bar{K}$ in nuclear medium

a lots of studies on in-medium kaon  
one of the difficulties in observation

a recent review

Freedman, Gal, Phys.Rept. 425, 89 (2007)

## large in-medium absorption

kaon is strongly absorbed in nuclear medium

mesonic  $K^{\text{bar}}N$  to  $\pi Y$

nonmesonic  $K^{\text{bar}}NN$  to  $YN$       30% at  $\rho_0$

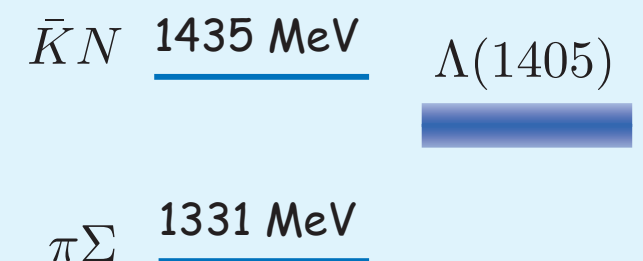
Sekihara, Yamagata-Sekihara, DJ,  
Kanada-En'yo, PRC86, 065205 (12)

hard to identify  $K^{\text{bar}}$ -nucleus bound states, even if they exist

## $K^{\text{bar}}N$ interaction as a fundamental interaction of $K^{\text{bar}}A$

$\Lambda(1405)$  is sitting 30 MeV below the  $K^{\text{bar}}N$  threshold

nature of  $\Lambda(1405)$  is extremely important to be revealed



**chiral symmetry determines low-energy  $K^{\text{bar}}N$  interaction, but it may play a minor role on the in-medium  $K^{\text{bar}}$  properties, because dynamics of  $K^{\text{bar}}N$ , or  $\Lambda(1405)$ , is more significant**



# Nature of $\Lambda(1405)$

DJ, Oller, Oset, Ramos, Meissner, NPA725, 181 ('03)

a recent review, Hyodo, DJ, Prog. Part. Nucl. Phys. 67, 55 ('12)

## - $\Lambda(1405)$ is most probably a quasi-bound state of $K^{\text{bar}}N$

low-energy theorem of chiral symmetry tells that  $K^{\text{bar}}N$  interaction is attractive  
(model independent Weinberg-Tomozawa interaction)

how strong ??

the  $l=0$  interaction is enough strong to form a bound state

dynamical calculations of the  $K^{\text{bar}}N$  system with the chiral interaction and without sources of resonances conclude a  $K^{\text{bar}}N$  bound state with 15 MeV binding energy

$\Lambda(1405)$  appears as a  $K^{\text{bar}}N$  bound state with 15 MeV binding energy

theoretically,  $K^{\text{bar}}N$  interaction is not so strong.

the binding energy is 15 MeV not 30 MeV

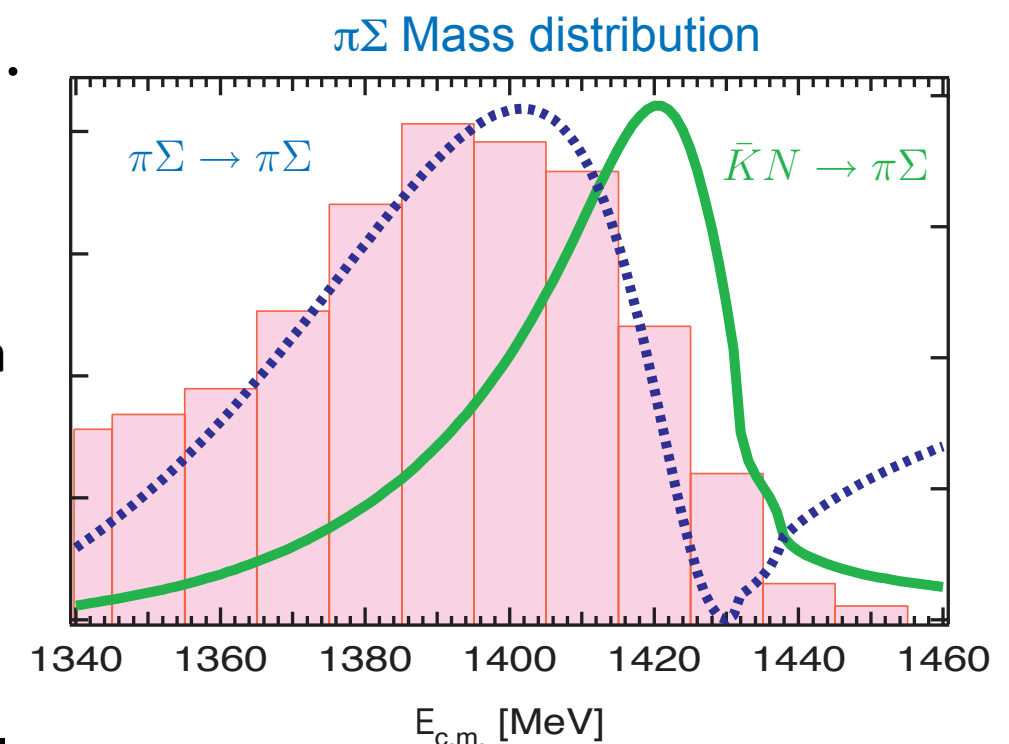
### two-pole structure

the spectrum of  $\Lambda(1405)$  is explained by interference between two components,  $K^{\text{bar}}N$  bound state and  $\pi\Sigma$  resonance.

Hyodo, Weise, PRC77, 035204 ('08)

**to confirm this scenario,**

**we observe  $\Lambda(1405)$  produced by  $K^{\text{bar}}N$  channel**



# Subthreshold amplitude of $K^{\text{bar}}N$

$\Lambda(1405)$  is located below the  $K^{\text{bar}}N$  threshold

cannot be produced by direct reaction  $\bar{K}N \rightarrow \Lambda(1405)$



## indirect reaction

use nuclear effect

to see subthreshold amplitude



nuclear effect

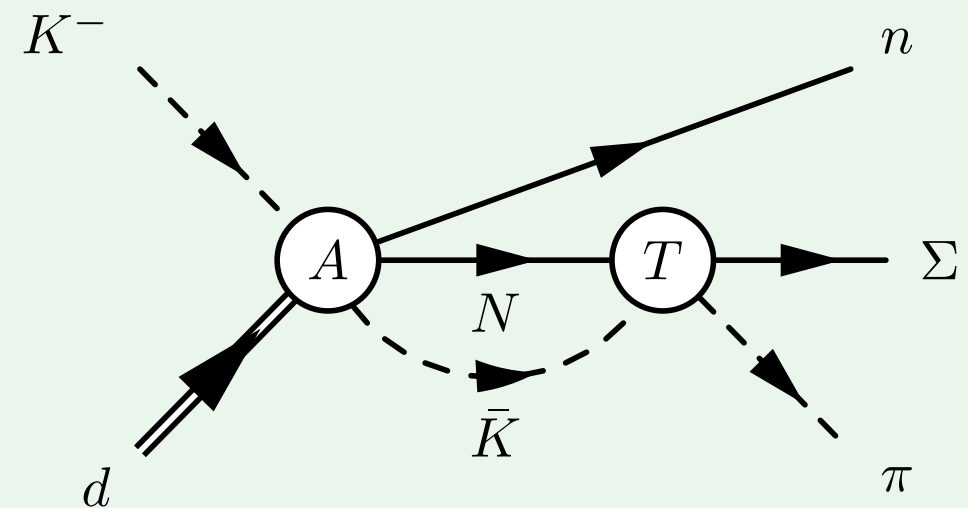
- fermi motion
- two-body effect

$K^{\text{bar}}N$  selective production

- strangeness carried by incident kaon

more sophisticated calculations given by  
Ohnishi and Miyagawa

production mechanism be under control



Want to extract T-amplitude from experiment.  
For this purpose, need to understand the  
production mechanism described by A-amplitude.

DJ, Oset, Sekihara, Eur.Phys.J.A. 42, 257 (2009).  
Yamagata-Sekihara, Sekihara, DJ, PTEP 2013, 043D02

# $\Lambda(1405)$ in $K^{\text{bar}}N$ channel

DJ, Oset, Sekihara, Eur.Phys.J.A. 42, 257 (09); ibid.A49, 95  
Yamagata-Sekihara, Sekihara, DJ, PTEP 2013, 043D02

**Experiment** bubble chamber

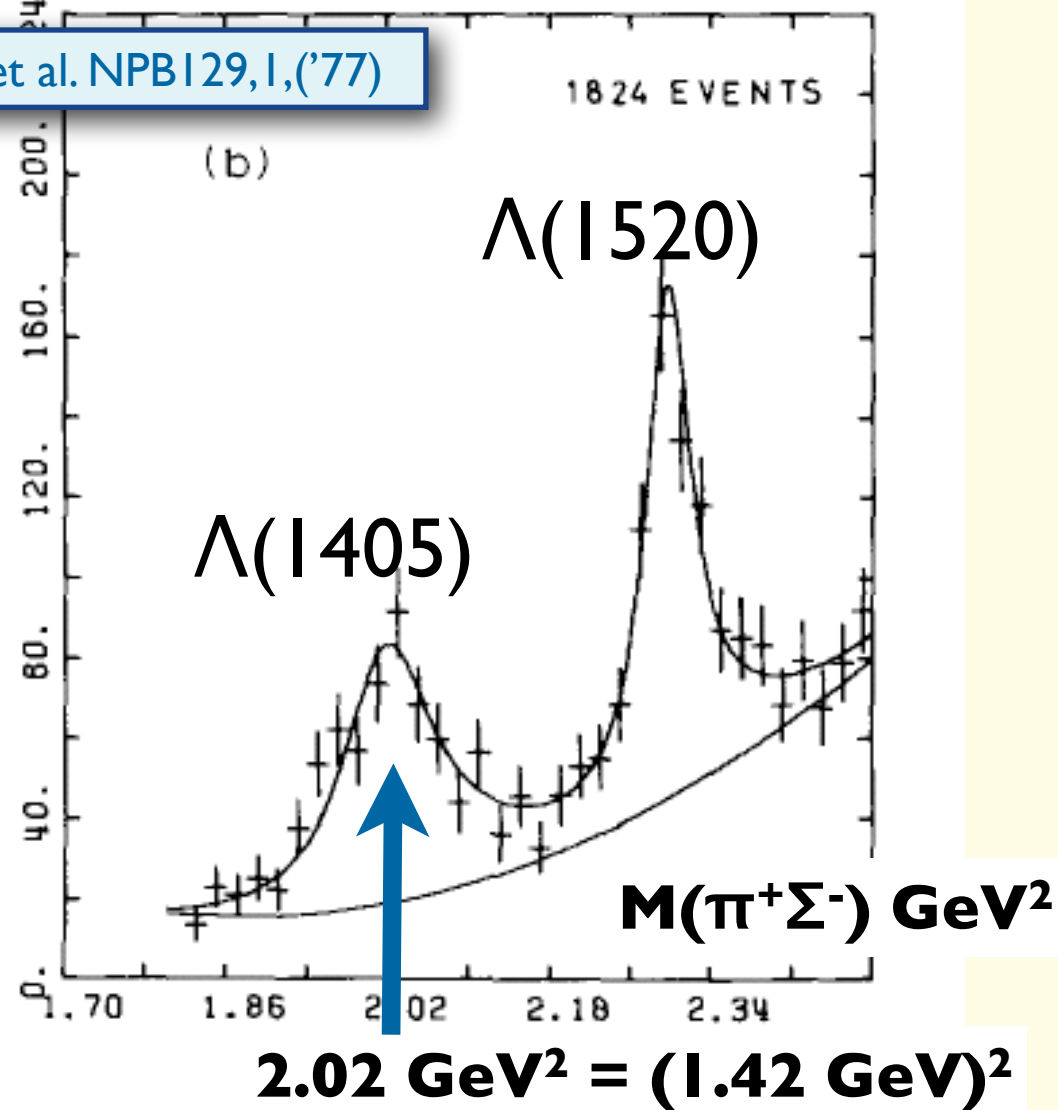
initial K momentum

686 ~ 844 MeV/c

$\pi\Sigma$  invariant mass spectrum

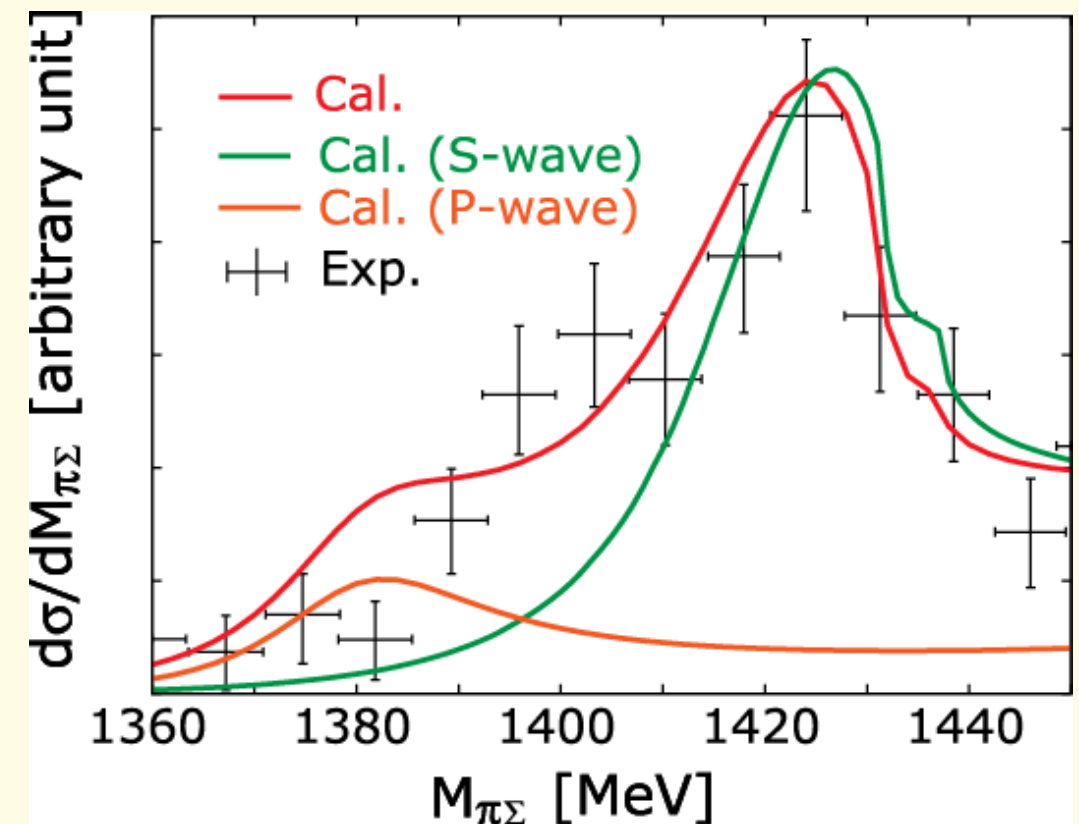
$$K^- d \rightarrow \pi^+ \Sigma^- n$$

Braun et al. NPB129,1,(77)



**peak position 1420 MeV**

**theoretical calculation in ChUM**



**production cross section of  $\Lambda(1405)$**

385  $\mu\text{b}$  @ 800 MeV/c (exp.  $410 \pm 100 \mu\text{b}$ )  
agrees with data in shape and size

inclusion of  $\Sigma^*$  does not distort the shape.

**brand-new experiment at J-PARC (E31)**

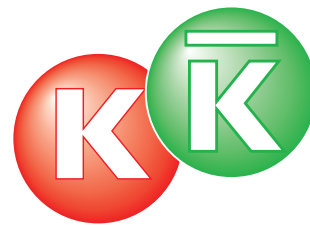
# Family of kaonic few-body systems

$\Lambda(1405)$



**BE ~10 MeV (30 MeV)**

$f_0(980), a_0(980)$



**BE ~10 MeV**

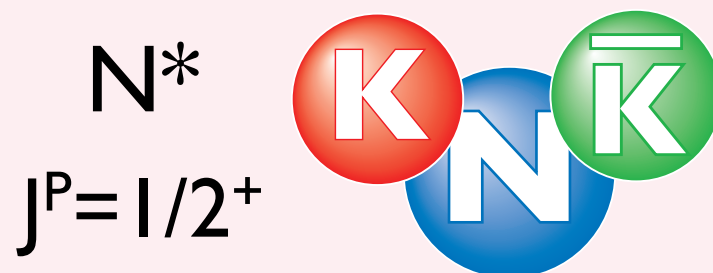
DJ, Kanada-En'yo, PRC78, 035203 (08).  
Martinez Torres, DJ, PRC82, 038202 (10).  
Martinez Torres, DJ, Kanada-En'yo, PRC83  
065205 (11).

$K^{\text{bar}}NN$



**BE ~20 MeV**  
or more

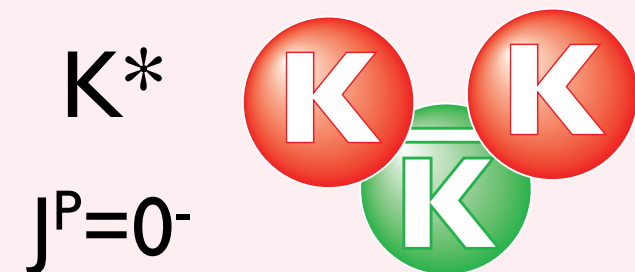
$K^{\text{bar}}KN$



a new  $N^*$  resonance  $N(1910)$

**BE ~20 MeV**

$K^{\text{bar}}KK$



1420 ~ 1465 MeV

**BE 20~60 MeV**

and more

$K^{\text{bar}}K^{\text{bar}}N$

Kanada-En'yo, DJ

$K^{\text{bar}}NNN$

Akaishi, Yamazaki, Dote,...

$K^{\text{bar}}K^{\text{bar}}NN$

Barnea, Gal, Liverts,

$K^{\text{bar}}N$  and  $K^{\text{bar}}K$  Weinberg-Tomozawa interactions are “similar” in a sense of chiral dynamics  
**pion is too light to be bound in range of strong interaction**

$K^+$  meson

# $K^+$ - nucleus scattering revisited

Aoki, DJ, on going

review articles

Dover, Walker, Phys. Rept. 89, 1 (1982)

Freedman, Gal, Phys.Rept. 425, 89 (2007)

## Kaon in nucleus

- KN interaction is repulsive, and KN cross section is small
- mean free path of K in nuclear medium is around 5 fm
- Kaon has been consider to be a clean probe to investigate nuclear matter
- no strong resonances in KN channel
- relatively easy to investigate **in-medium effects on kaon**

## breakdown of linear density approximation

thanks to large mean free path,  $K^+A$  scatting could be written well by single step

$$\sigma_{K+A} \simeq A \sigma_{K+N} \quad p_{\text{lab.}} < 800 \text{ MeV}/c$$

the ratio of the cross sections is known to be larger than unity

$$\frac{\sigma_{K+^{12}\text{C}}}{6\sigma_{K+d}} > 1.0$$

# $K^+$ - nucleus scattering revisited

Aoki, DJ, on going

## breakdown of $T\rho$ approximation

$$2m_K^+ V_{\text{opt}} \simeq -\rho T_{K+N} \quad \text{linear density approximation}$$

$p_{\text{lab}}$	$V_{\text{opt}}$	$\text{Re } b_0(\text{fm})$	$\text{Im } b_0(\text{fm})$	$T_{K+N} = -\frac{4\pi E_{\text{c.m.}}}{M_N} b_0$  <b>obtained by <math>\chi</math>sq fitting free KN</b>
488	$t\rho$ $t_{\text{free}}\rho$	$-0.203(26)$ $-0.178$	$0.172(7)$ $0.153$	

Friedman, Gal, Phys.Rept. 425, 89 (2007)

## 15% enhancement in in-medium KN scattering

### possible explanation

- nucleon-nucleon correlation
- “swelling” of nucleon
- mass reduction of vector mesons

etc.



# $K^+$ - nucleus scattering revisited

Aoki, DJ, on going

in the aspect of chiral symmetry

the 15% enhancement can be explained by wave function renormalization

**argument by Kolomeitsev et al. for pion**

Kolomeitsev, Kaiser, Weise, PRL90, 092501 (03)

when self-energy is energy-dependent,

See also, DJ, Hatsuda, Kunihiro, PRD63, 011901(R);  
PLB 670 (2008), 109.

equivalent energy-independent optical potential can be obtain as follows

- consider in-medium dispersion relation  $\omega^2 - m^2 - \Sigma(\omega) = 0$

- expanding self-energy around  $\omega = m$

$$2mV_{\text{opt}}(m^*) = \Sigma(m) + (\omega^2 - m^2) \frac{\partial \Sigma}{\partial \omega^2} + \dots$$

$$\simeq \left( 1 + \frac{\partial \Sigma}{\partial \omega^2} \right) \Sigma(m) \simeq Z \Sigma(m)$$

$$2mV_{\text{opt}} = -Z\rho T_{K^+N}$$

one of the higher order corrections

$$Z = 1 + 0.1 \frac{\rho}{\rho_0}$$

leading order chiral perturbation theory calculation



# $\pi^0 \rightarrow \gamma\gamma$ decay in nuclear medium

Goda, DJ, PTEP 2014, 033D03 (2014).  
Nebreda, DJ, in preparation.

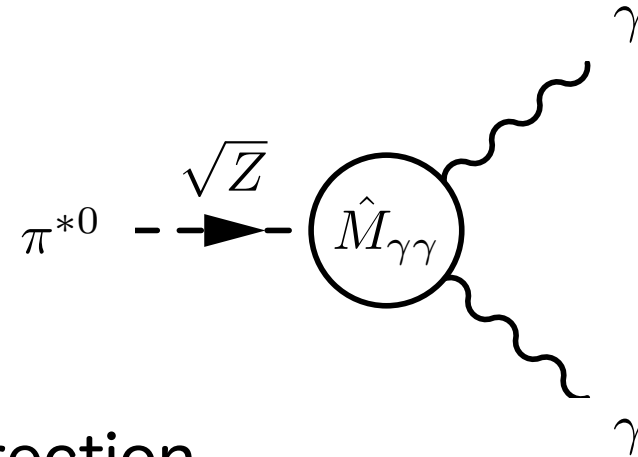
## in-medium decay amplitude

$$M_{\gamma\gamma}^* = \sqrt{Z} \hat{M}_{\gamma\gamma}$$

$Z$  wave function renormalization

$\hat{M}_{\gamma\gamma}$  1-particle irreducible vertex correction

no correction in the linear density  $\leftarrow$



Meissner, Oller, Wirzba, AnnPhys 297, 27 (02)

## in-medium change of the amplitude

$$\frac{M_{\gamma\gamma}^*}{M_{\gamma\gamma}} = \sqrt{Z}$$

$$\frac{\Gamma_{\gamma\gamma}^*}{\Gamma_{\gamma\gamma}} = Z \simeq 1 + 0.4 \frac{\rho}{\rho_0}$$

**40% enhancement in nuclear density**

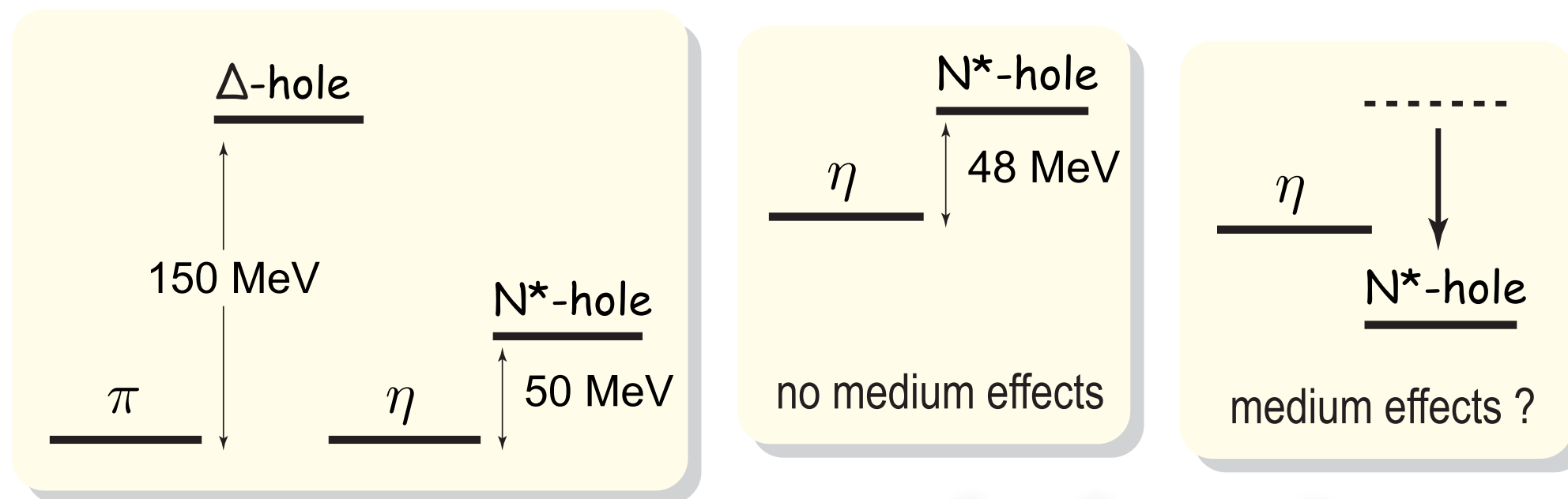
$\eta$  meson

# $\eta$ mesonic nuclei

- eta N couples strongly to  $N^*(1535)$
- $N^*(1535)$  is the first excited state with the opposite parity of nucleon
- can be a chiral partner of nucleon
- eta mesonic nuclei can prove chiral symmetry of N and  $N^*$

## chiral double picture for nucleons

- nucleon and  $N^*(1535)$  are chiral partners (**chiral doublet**)
- masses of chiral doublets tend to degenerate when ChS is being restored
- mass difference of N and  $N^*$  decreases in nuclear medium



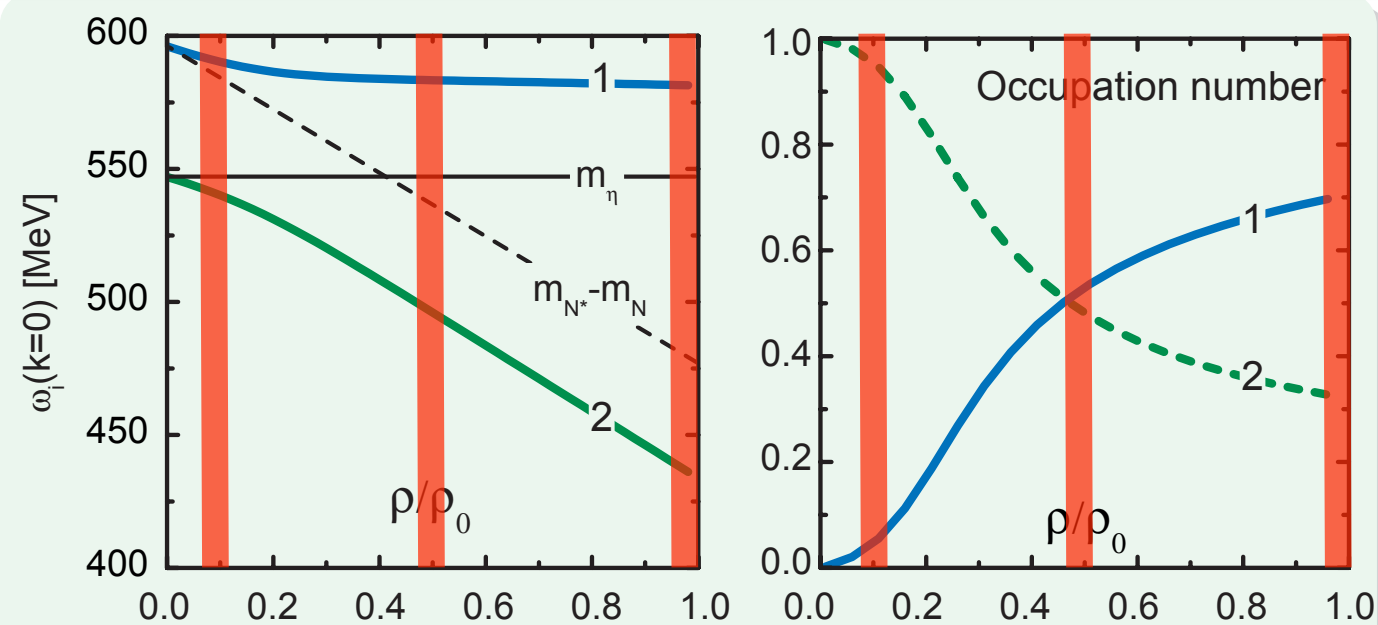
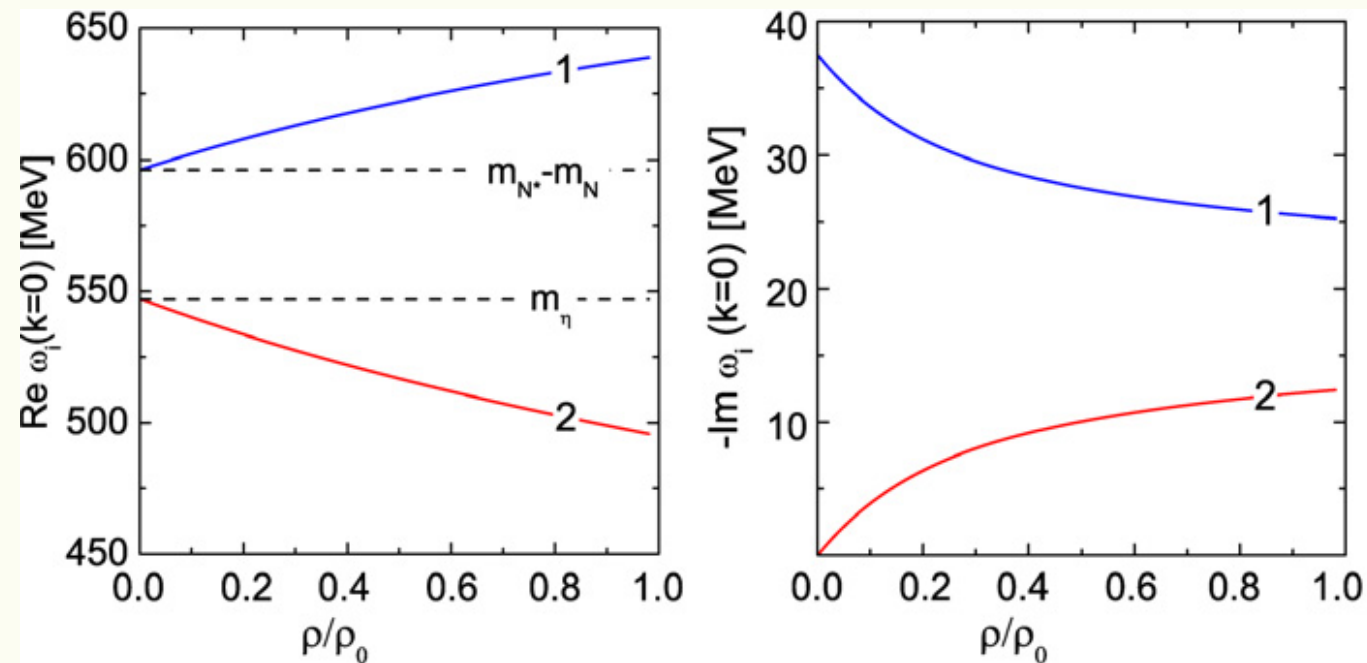
**level crossing**

# Spectral function of in-medium eta meson

## density dependence of two levels

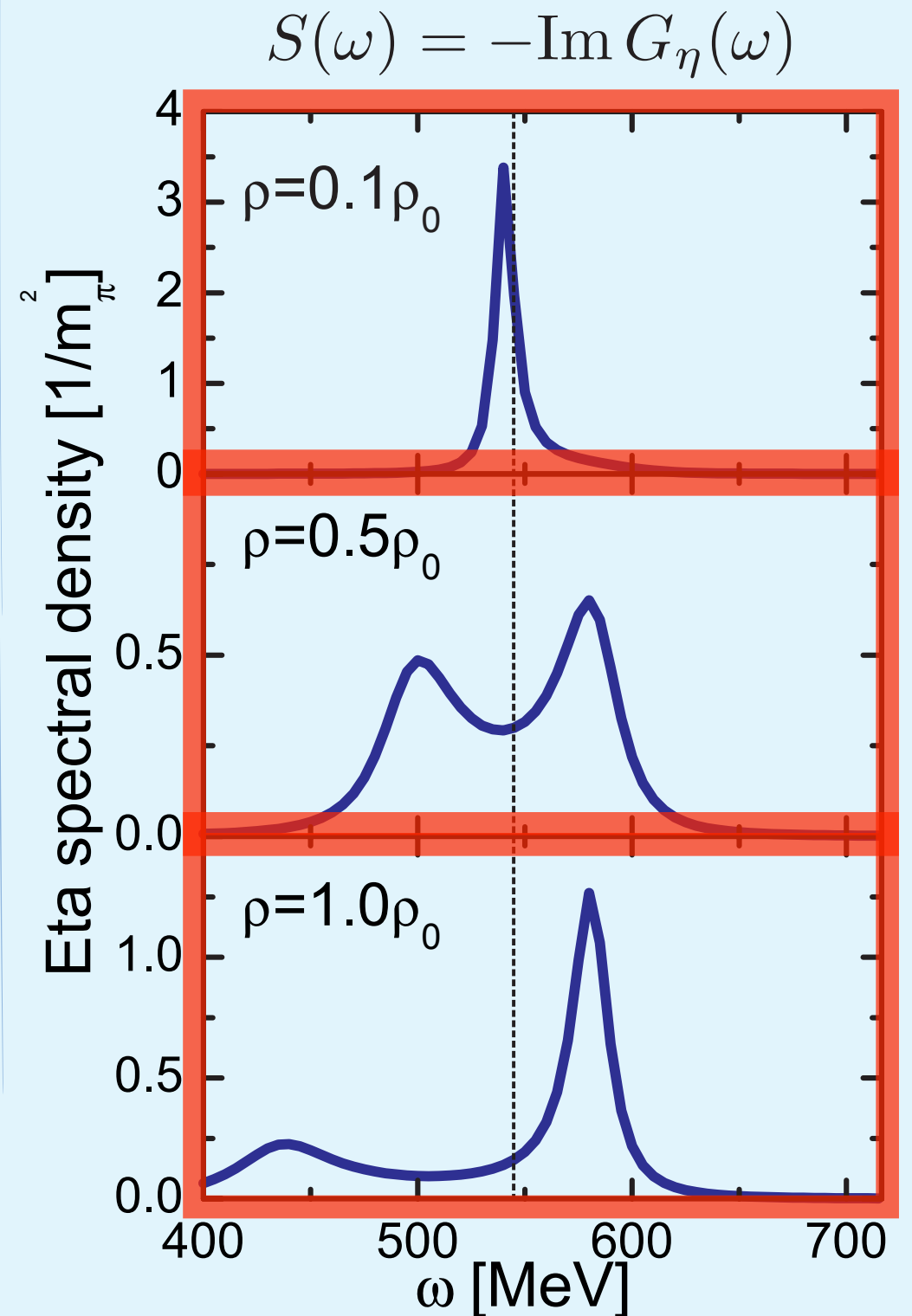
Jido, Kolomeitsev, Nagahiro, Hirenzaki, NPA811, 158 (2008)

## Spectral function



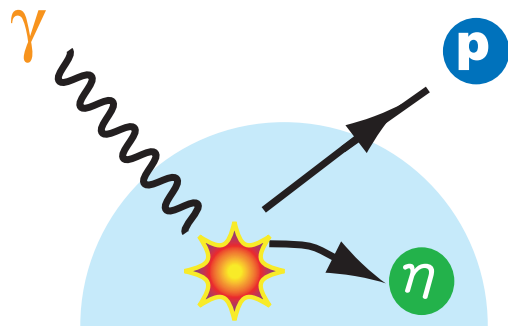
$$G_\eta(\omega) = \sum_i \frac{Z_i}{\omega - \omega_i}$$

$$Z_i = \left( 1 - \frac{\partial V_\eta(\omega)}{\partial \omega} \Big|_{\omega=\omega_i} \right)^{-1}$$



# Eta mesic nuclei

Nagahiro, Jido, Hirenzaki, PRC68, 035805 (03); NPA761, 92 (05)  
Jido, Kolomeitsev, Nagahiro, Hirenzaki, NPA811, 158 (08)



## ( $\gamma, p$ ) reaction

missing mass spectra of emitted proton

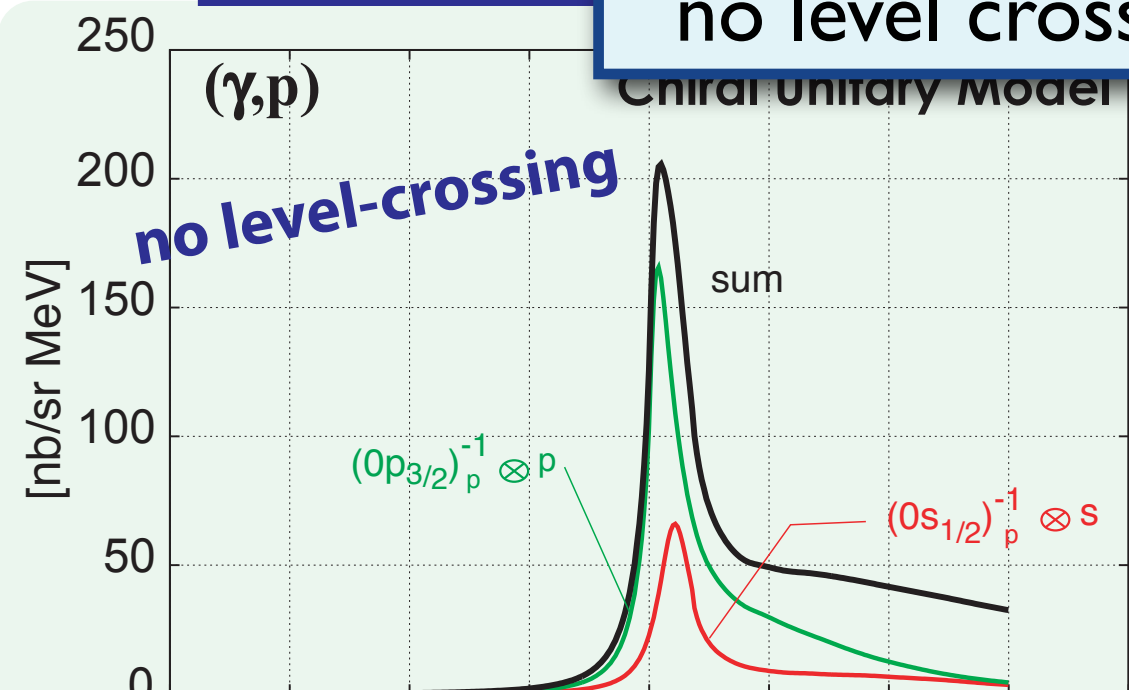
$^{12}\text{C}$  target

in recoilless condition  
(no momentum transfer)

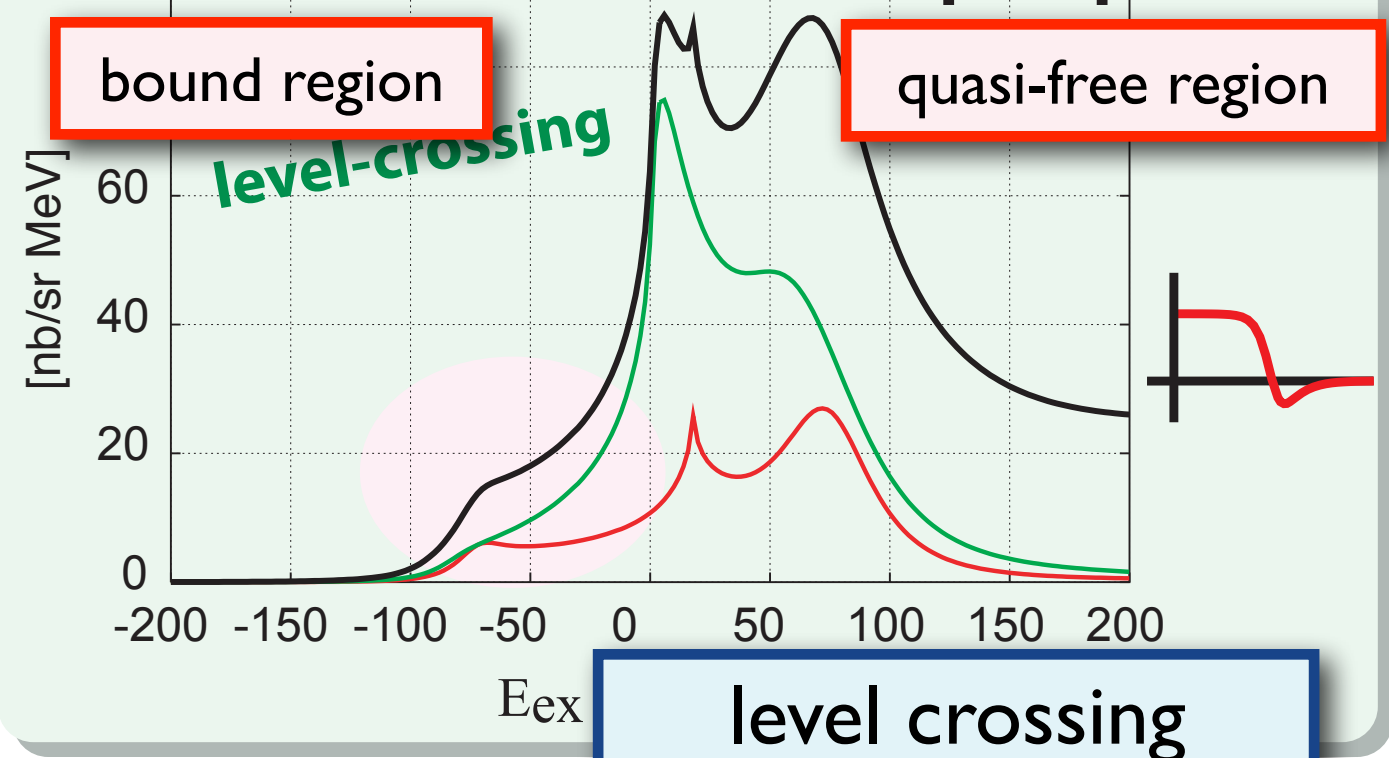
level crossing effect can be seen in  
quasi-free region as repulsive shift  
of eta meson

## Spectra of $^{12}\text{C}(\gamma, p)^{11}\text{B} @ \eta$

no level crossing



## Chiral Doublet Model [C=0.2]



level crossing

$\eta'$  meson

# $\eta'$ meson and chiral symmetry

DJ, Nagahiro, Hirenzaki,  
PRC85 (12) 032201(R)

Large eta' mass stems from quantum anomaly, which breaks axial  $U(1)$  symmetry. eta' failed to get a Nambu-Goldstone boson due to anomaly.

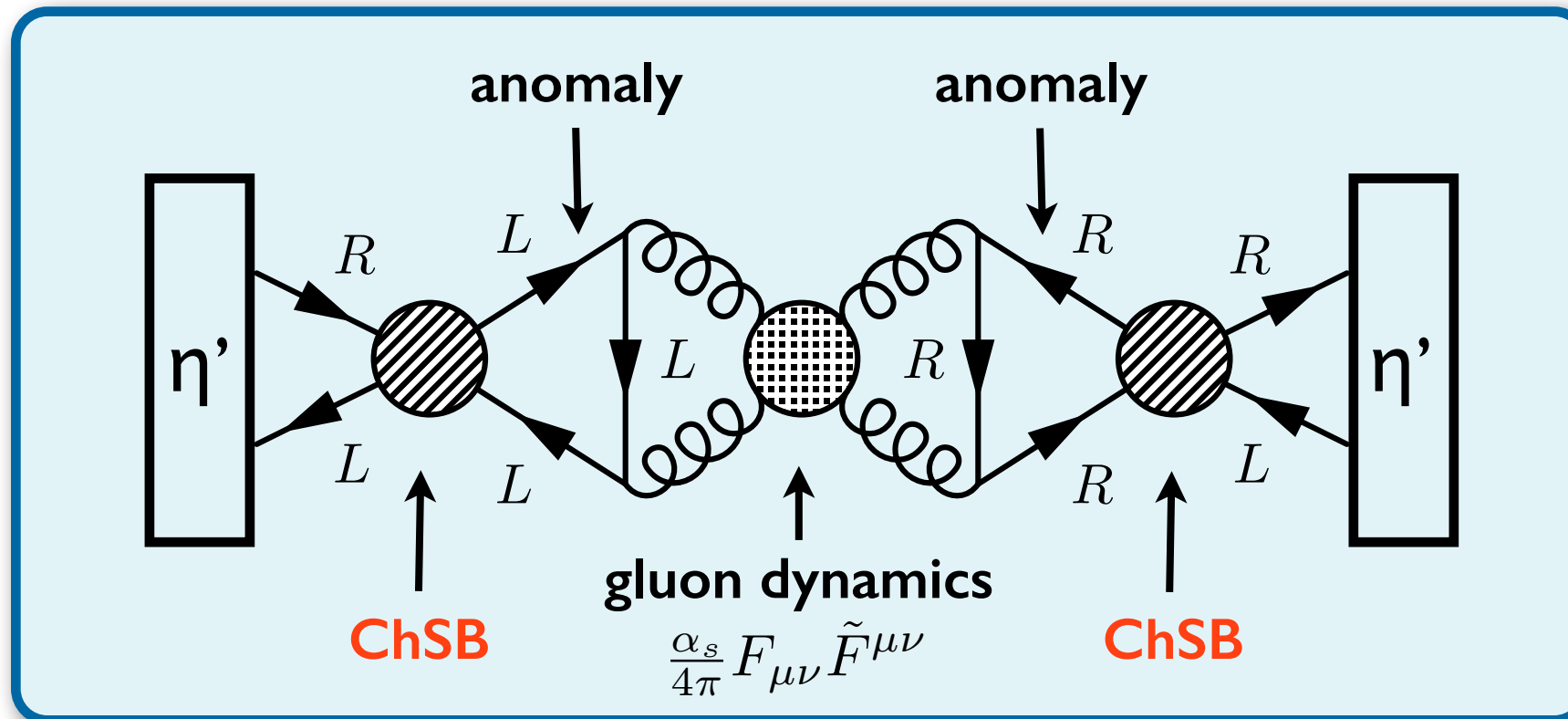
$\eta'(958)$

$$J^{PC} = 0^+(0^-+)$$

$$\text{Mass } m = 957.78 \pm 0.06 \text{ MeV}$$

$$\text{Full width } \Gamma = 0.198 \pm 0.009 \text{ MeV}$$

eta' meson has a strong connection also to chiral symmetry breaking.  
in order that  $U_A(1)$  anomaly affects the  $\eta'$  mass,  
chiral symmetry is necessarily broken spontaneously and/or explicitly.



nonchiral gluon field cannot couple to pseudoscalar states without chiral symmetry breaking.

**when chiral symmetry is restored,  $\eta$  and  $\eta'$  should degenerate due to  $SU(3)$  chiral symmetry. thus,  $\eta - \eta'$  mass difference is generated by chiral symmetry breaking**

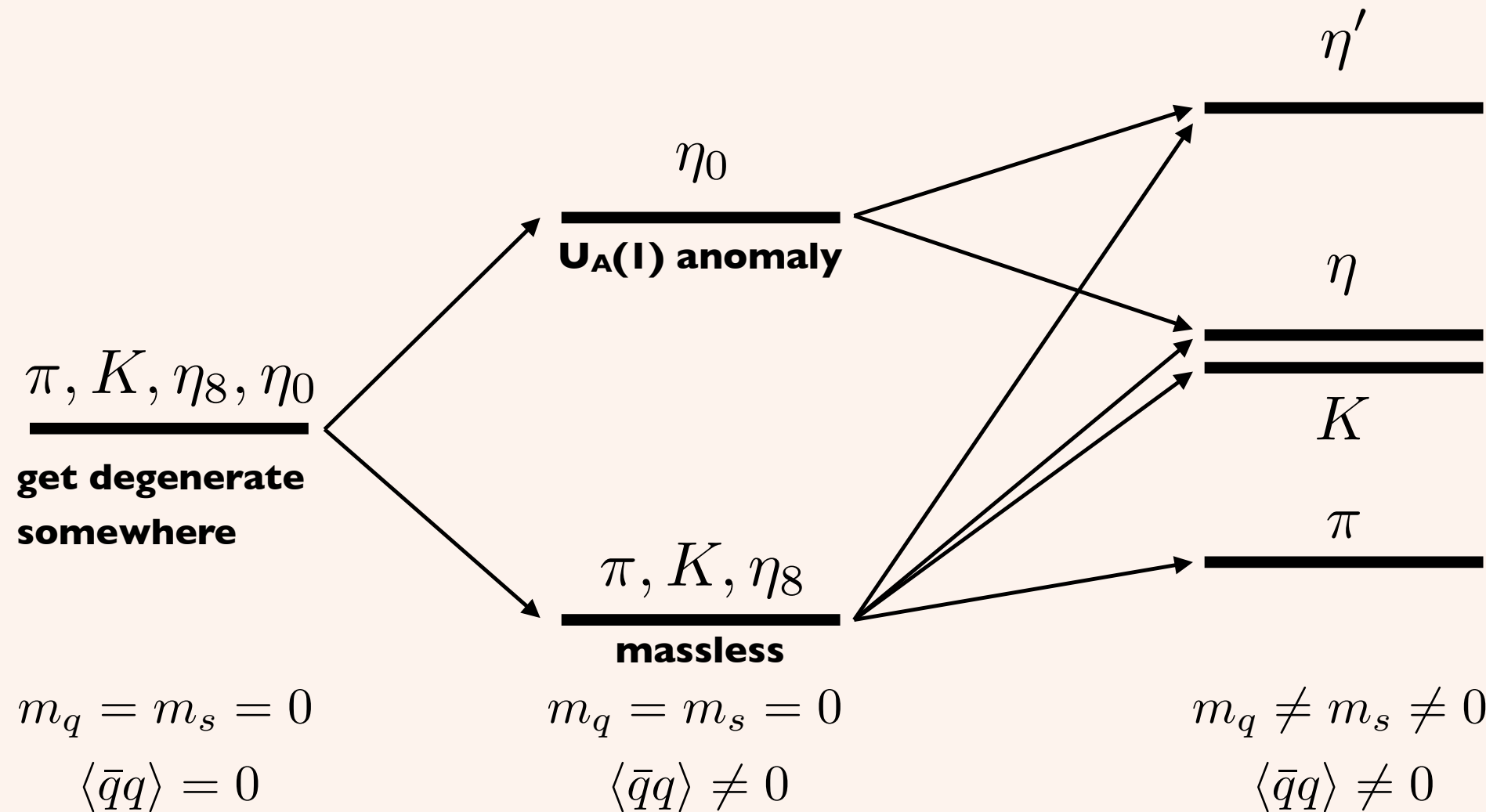
# $\eta'$ meson in chiral restoration

DJ, Nagahiro, Hirenzaki, PRC85 (12) 032201(R);  
Nagahiro, DJ, Fujioka, Itahashi, Hirenzaki,  
PRC87 (12) 045201

When chiral symmetry is restored...

as a consequence of  $SU_L(3) \otimes SU_R(3)$

9 PS  $\pi, K, \eta_8, \eta_0$  9 S  $\sigma, a_0, \kappa, f_0$  get degenerate



**ChS manifest**

**ChS broken dynamically**

**ChS broken dynamically and explicitly**

in order that  $U_A(1)$  anomaly affects the  $\eta'$  mass, chiral symmetry is necessarily broken spontaneously and/or explicitly.



# $\eta'$ meson in nuclear matter

DJ, Nagahiro, Hirenzaki,  
PRC85 (12) 032201(R)

the mass gap of  $\eta'$  and  $\eta$  is generated by chiral symmetry breaking

the  $\eta'$  mass get reduced when chiral symmetry is being restored in nuclear medium

## a simple order estimation

linear dependence of quark condensate on  $\eta'$ - $\eta$  mass difference (400 MeV)

partial restoration of ChS takes place with 35% at  $\rho_0$

we expect strong  $\eta'$  mass reduction  $\Delta m_{\eta'} \sim 100 \text{ MeV} @ \rho = \rho_0$

chiral effective theories tell similar results.

linear sigma model

Sakai, DJ, PRC88 (13) 064906

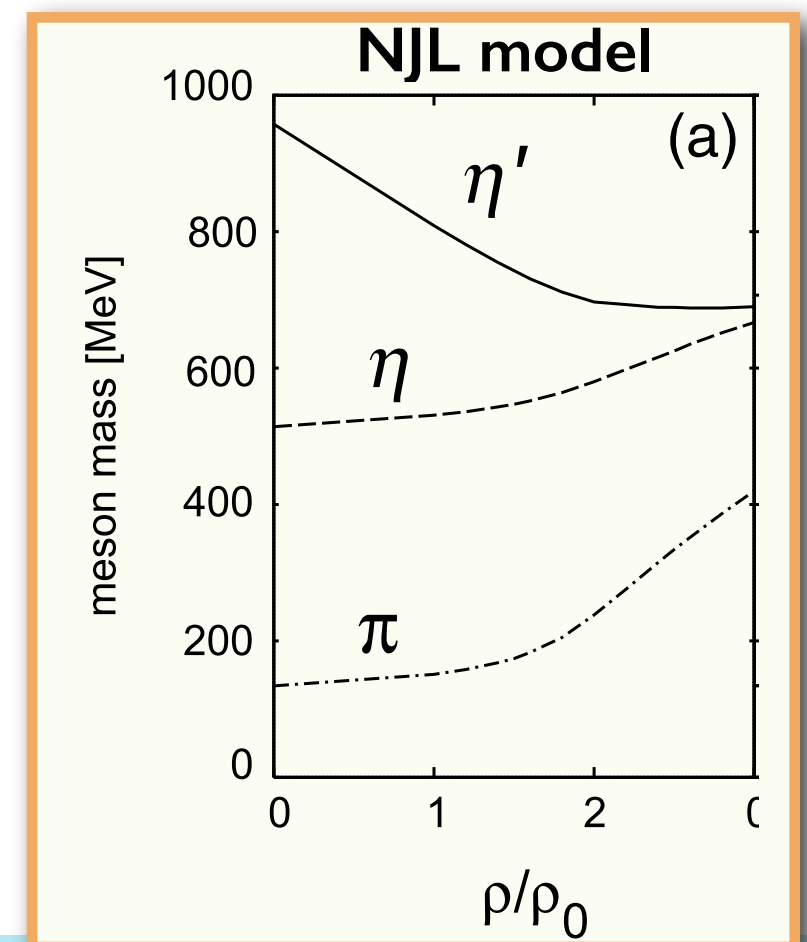
$$\Delta m_{\eta'} \sim 80 \text{ MeV} @ \rho = \rho_0$$

$$m_{\eta'} - m_{\eta} \sim 130 \text{ MeV} @ \rho = \rho_0$$

NJL model

P. Costa, M. C. Ruivo, and Y. L. Kalinovsky, PLB560, 171 (03).  
Nagahiro, Takizawa, Hirenzaki, PRC74,045203 (2006)

$$\Delta m_{\eta'} \sim 150 \text{ MeV} @ \rho = \rho_0$$



# Possible bound state spectra

DJ, Nagahiro, Hirenzaki,  
PRC85 (12) 032201(R)

**mass reduction in nuclear matter provides a scalar potential in finite nucleus**

a simple  $\eta'$  optical potential  
(Woods-Saxon type)

proportional to nuclear density

$$V_{\eta'}(r) = V_0 \frac{\rho(r)}{\rho_0}$$

$$\Delta m = 150 \text{ MeV}$$

$$\Gamma/2 = 20 \text{ MeV}$$

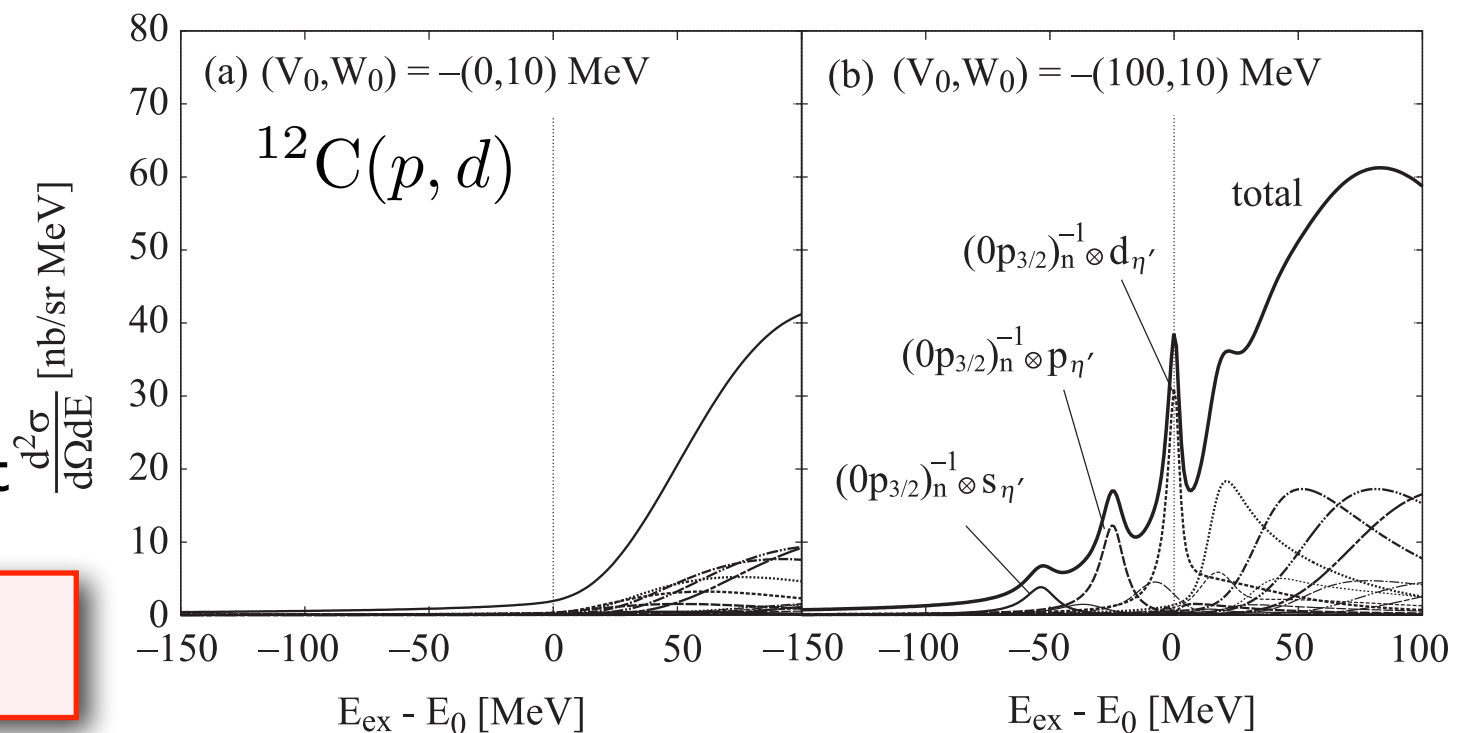
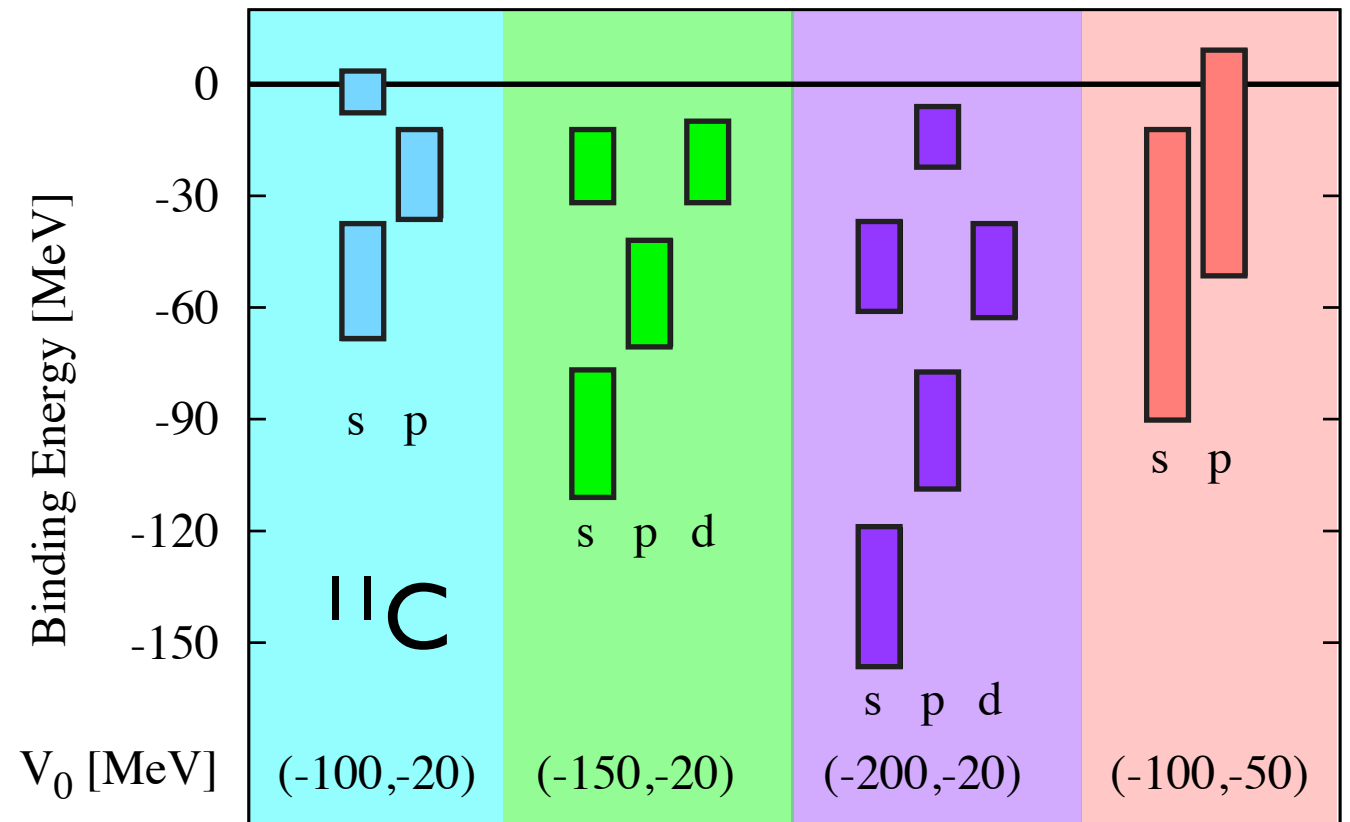
Re: theoretical expectation

Im: phenomenological observation

**well-separated bound states**

for realistic calculation

core polarization effect could be important



Nagahiro, DJ, Fujioka, Itahashi,  
Hirenzaki, PRC87 (12) 045201

# $\eta'$ -N interaction

Sakai, DJ, PRC88 (13) 064906;  
in preparation

in linear sigma model

nucleon mass is generated also by spontaneous breaking of ChS

$$m_N = g\langle\sigma_0\rangle$$

→ presence of strong coupling  $\sigma NN$

**this is the origin of the scalar attraction in NN interaction**

in the same way

chiral symmetry breaking generates a part of eta' meson with help of anomaly

$$m_{\eta_0}^2 - m_{\eta_8}^2 = 6B\langle\sigma_0\rangle$$

→ presence of strong coupling  $\sigma\eta'\eta'$

B term : anomaly effect

**we expect strong attraction in  $\eta'$ -N in scalar-isoscalar exchange**

with this attraction

two body  $\eta'$ -N bound state is expected with several MeV binding energy

**two-body bound state  $\sim 6$  MeV**

**coupled channel effect ( $\eta'$ -N,  $\eta$ -N) BE = 12 - 3i [MeV]**

calculated in the same way as  $\Lambda(1405)$  of  $K^{\text{bar}}N$  bound state

# Summary

we have discussed mesons in nuclear medium under the situation that chiral symmetry is partially (30%) restored in nuclear medium

expectations in partial restoration of chiral symmetry

- **reduction of mass difference of chiral partners**

the reduction of N-N\* mass difference could be seen in eta mesonic nuclei

- **substantial effect from wave function renormalization of NG bosons**

self-energy of NG boson has energy dependence (low energy theorem)

$$Z = \left( 1 - \frac{\partial \Sigma}{\partial p_0^2} \right)^{-1}$$

enhancement of K<sup>+</sup>A scattering is explained by K<sup>+</sup> wave function renorm.

large enhancement of  $\pi^0 \rightarrow \gamma \gamma$  in medium is expected

- **reduction of hadron mass**

a part of eta' meson mass is generated by chiral symmetry breaking

100 MeV reduction of eta' mass is expected in nuclear density

strong attraction of eta'-N int. from isoscalar-scalar  $\sigma$  exchange