

# $\eta' N$ 束縛状態の光生成

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in collaboration with

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**Shuntaro SAKAI** (Kyoto Univ.)

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**1. Introduction**

**2. Formulation of the photoproduction**

**3. Results and discussions**

**4. Summary**

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[1] T.S., D. Jido and S. Sakai, in preparation



# 1. Introduction



# 1. Introduction

## ++ The properties of the $\eta'$ meson ++

$\eta'(958)$

$$J^{PC} = 0^{+}(0^{-+})$$

$\eta'$

Mass  $m = 957.78 \pm 0.06$  MeV

Full width  $\Gamma = 0.198 \pm 0.009$  MeV

$\eta'(958)$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$p$ (MeV/c)
$\pi^+ \pi^- \eta$	(42.9 $\pm$ 0.7 ) %		232
$\rho^0 \gamma$ (including non-resonant $\pi^+ \pi^- \gamma$ )	(29.1 $\pm$ 0.5 ) %		165
$\pi^0 \pi^0 \eta$	(22.2 $\pm$ 0.8 ) %		239
$\omega \gamma$	( 2.75 $\pm$ 0.23 ) %		159
$\gamma \gamma$	( 2.20 $\pm$ 0.08 ) %		479
$3\pi^0$	( 2.14 $\pm$ 0.20 ) $\times 10^{-3}$		430

Particle Data Group.

- **Large mass** compared to the lowest pseudo-scalar meson octet, ( $\pi, K, \eta$ ).

---  **$U_A(1)$  problem:**  
Where has the 9th NG boson gone ?

Weinberg ()1975).

- The  $U_A(1)$  problem can be solved by **instantons** (non-trivial classical solutions of EOM) through the  $U_A(1)$  anomaly.

't Hooft ()1976).

- The  $\eta'$  meson has **a direct connection to the dynamics of QCD**.

# 1. Introduction

## ++ The properties of the $\eta'$ meson ++

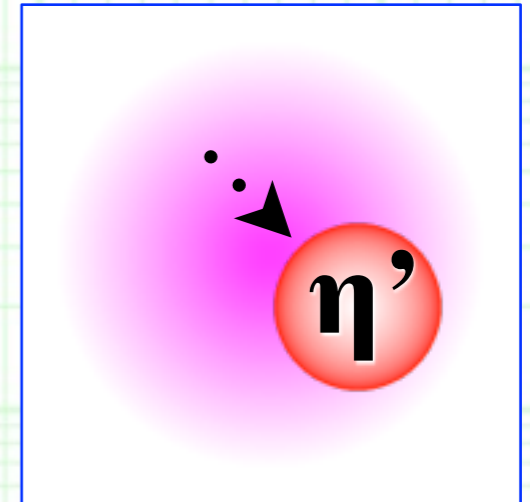
- There are **several approaches** to investigate the  $\eta'$  properties.

- Behavior of the  $\eta'$  meson in vacuum.

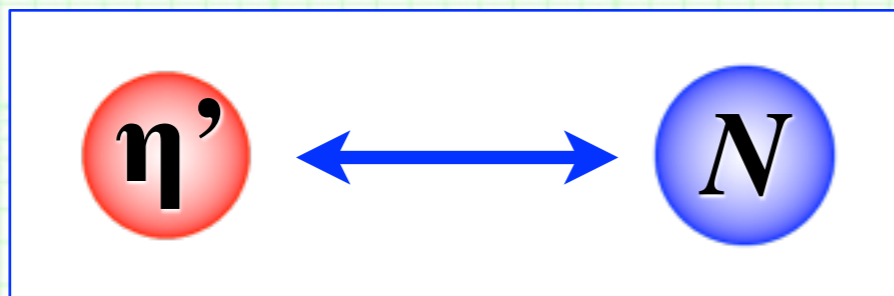
--- Decay modes, mixings, ... .

- Behavior of the  $\eta'$  meson in medium.

--- Finite temperatures, **finite nuclear densities**.



- **The interaction between  $\eta'$  and  $N$ .**



- Numerical experiments for the  $\eta'$  meson.

# 1. Introduction

## ++ The $\eta'$ $N$ interaction ++

- So far, **the interaction between  $\eta'$  and  $N$  is not well known.**
- We do not know even whether it is attractive or repulsive.
- Recently, **based on the linear sigma model**, the  $\eta'$   $N$  interaction was studied. Sakai and Jido, *Phys. Rev. C* **88** (2013) 064906.

### Lagrangian of linear sigma model

$$\mathcal{L} = \frac{1}{2} \text{tr}(\partial_\mu M \partial^\mu M^\dagger) - \frac{\mu^2}{2} \text{tr}(M M^\dagger) - \frac{\lambda}{4} \text{tr}[(M M^\dagger)^2] - \frac{\lambda'}{4} [\text{tr}(M M^\dagger)]^2 + \text{Atr}\chi M^\dagger + \sqrt{3}B \det M + \text{h.c.}$$

J.Schechter,Y.Ueda,Phys.Rev.D3,168(1971).  
J.T.Renaghan, et al. PRD62,085008(2000).

The effect from the current quark mass

$U_A(1)$  anomaly effect

$$+ \bar{N} i \not{\partial} N - g \bar{N} \left( \frac{1}{\sqrt{3}} \sigma_0 + \frac{1}{\sqrt{6}} \sigma_8 + i \gamma_5 \frac{\vec{\tau} \cdot \vec{\pi}}{\sqrt{2}} + i \gamma_5 \frac{1}{\sqrt{3}} \eta_0 + i \gamma_5 \frac{1}{\sqrt{6}} \eta_8 \right) N$$

Contribution from nucleon

$$M = \sum_{a=0}^8 \frac{\sigma_a \lambda_a}{\sqrt{2}} + i \sum_{a=0}^8 \frac{\pi_a \lambda_a}{\sqrt{2}} \quad N = \begin{pmatrix} p \\ n \end{pmatrix} \quad \chi = \sqrt{3} \begin{pmatrix} m_u & & \\ & m_d & \\ & & m_s \end{pmatrix} = \begin{pmatrix} m_q & & \\ & m_q & \\ & & m_s \end{pmatrix}$$

( $\lambda_a$ : Gell-Mann matrix,  $\tau_i$ : Pauli matrix)

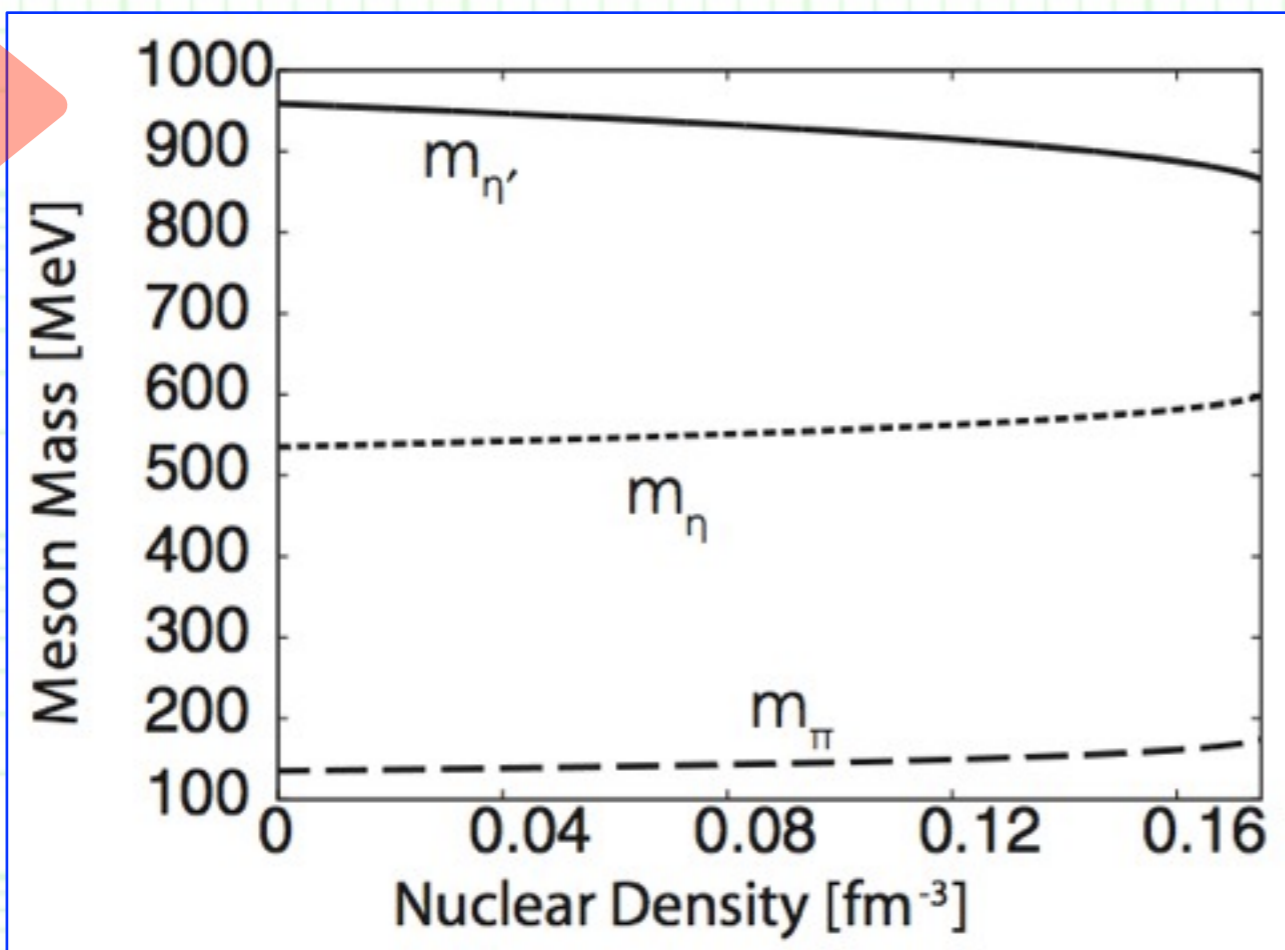
- In this model, a large part of the  $\eta'$  mass is **generated by the spontaneous breaking of chiral symmetry through the  $U_A(1)$  anomaly.**

Taken from talk in ELPH workshop C008 given by S. Sakai.

# 1. Introduction

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- So far, **the interaction between  $\eta'$  and  $N$  is not well known.**
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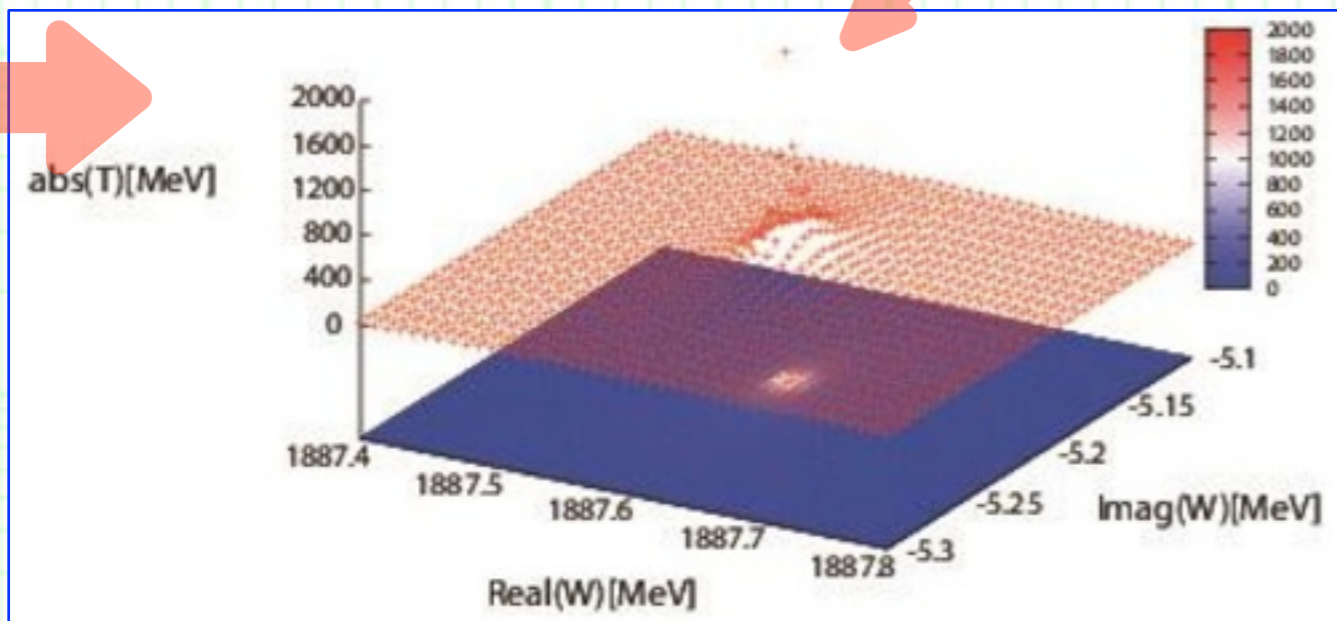
- Since the mass is generated by the spontaneous breaking of the chiral symmetry, **the mass is reduced in nuclear matter**, where **the chiral symmetry is partially restored**:

$$\Delta m_{\eta'} \sim \sim 80 \text{ MeV at } \rho = \rho_0.$$

# 1. Introduction

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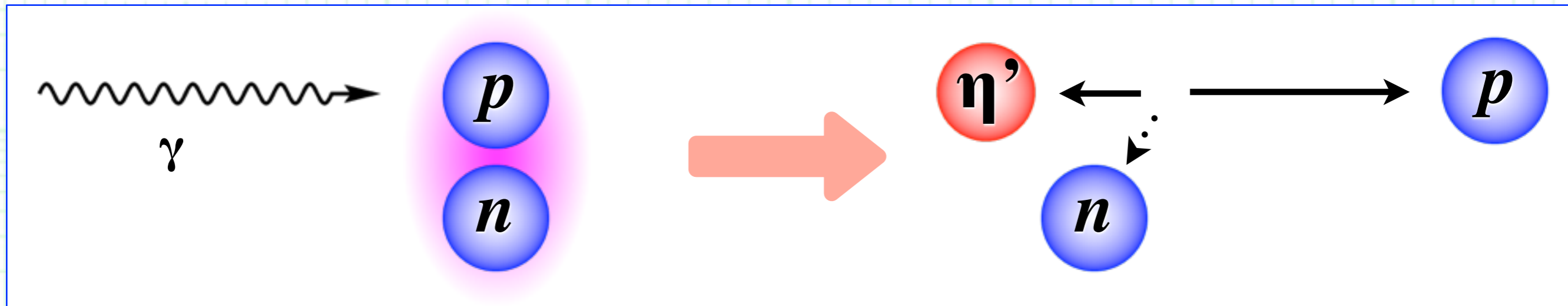
Taken from talk in ELPH workshop C008 given by S. Sakai.

- Mass modification is represented by self-energy, which can be translated into a potential between two particles.
- Indeed, in this model, **the attraction between  $\eta'$   $N$  is sufficiently attractive to generate an  $\eta'$   $N$  bound state ( $B_E \sim 10$  MeV).**

# 1. Introduction

## ++ Motivation ++

- **Such an  $\eta'$   $N$  bound state should be observed in Exps.**
- Which reactions ?
- The photoproduction of  $\eta^{(\prime)}$  on a deuteron with forward proton emission will be suited for the observation.



- The forward proton emission gives **a good kinematical condition for the production of the  $\eta'$   $N$  bound system.**
  - This reaction can be observed in **LEPS(2) and ELPH experiments.**
  - It may also contain some clue to the  $\eta'$   $N$  interaction.
- > **Against the quasi-free  $\eta'$ , can we really observe the signal ?**

## **2. Formulation of the photoproduction**



## 2. Formulation

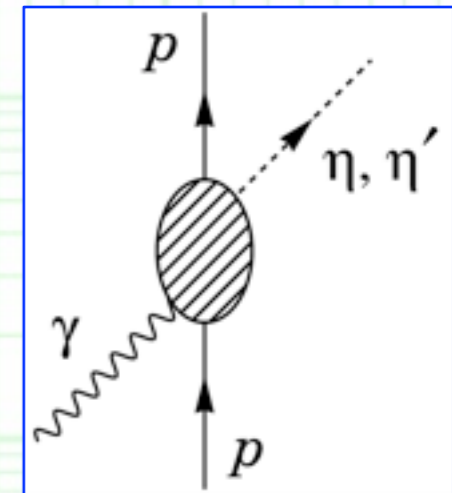
**++  $\gamma p \rightarrow \eta p$  and  $\eta' p$  reactions ++**

- We first consider **the free proton  $\gamma p \rightarrow \eta p$  and  $\eta' p$  reactions** as an elementary part of the photoproduction on a deuteron target.

- The cross section can be expressed as:

$$\frac{d\sigma_{\gamma p \rightarrow mp}}{d\Omega} = \frac{p'_{\text{cm}} M_p}{16\pi^2 E_{\gamma}^{\text{lab}} W_2} |T_{\gamma p \rightarrow mp}|^2, \quad m = \eta, \eta'$$

- $E_{\gamma}^{\text{lab}}$ : Initial photon energy in the Lab. frame,  
 $\Omega$ : CM solid angle for the final proton momentum,  
 $p'_{\text{cm}}$ : CM momentum of the final proton,  
 $W_2$ : CM energy of the system,  
 $T_{\gamma p \rightarrow mp}$ : The  $\gamma p \rightarrow m p$  ( $m = \eta, \eta'$ ) scattering amplitude.



- **Only the  $\gamma p \rightarrow m p$  scattering amplitude  $T_{\gamma p \rightarrow mp}$  is unknown.**

## 2. Formulation

**++  $\gamma p \rightarrow \eta p$  and  $\eta' p$  reactions ++**

- We first consider **the free proton  $\gamma p \rightarrow \eta p$  and  $\eta' p$  reactions** as an elementary part of the photoproduction on a deuteron target.

- In this study we are interested in **the ratio of the signal of the  $\eta' n$  bound state to the quasi-free  $\eta'$  production contribution.**

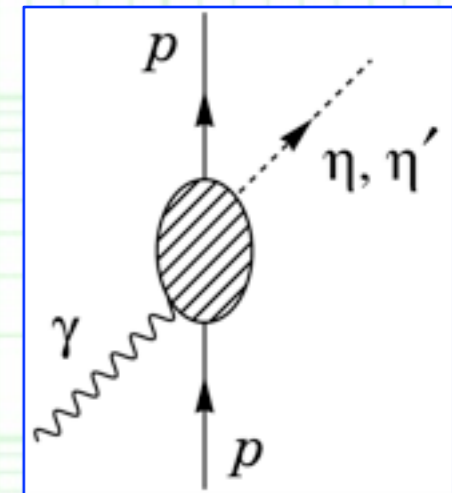
--> We need only **a “rough” scattering amplitude** for the  $\gamma p \rightarrow m p$  reaction,  $T_{\gamma p \rightarrow m p}$ , since the magnitude of the amplitude is irrelevant to the ratio of signal to quasi-free.

- We employ **the constant amplitude**

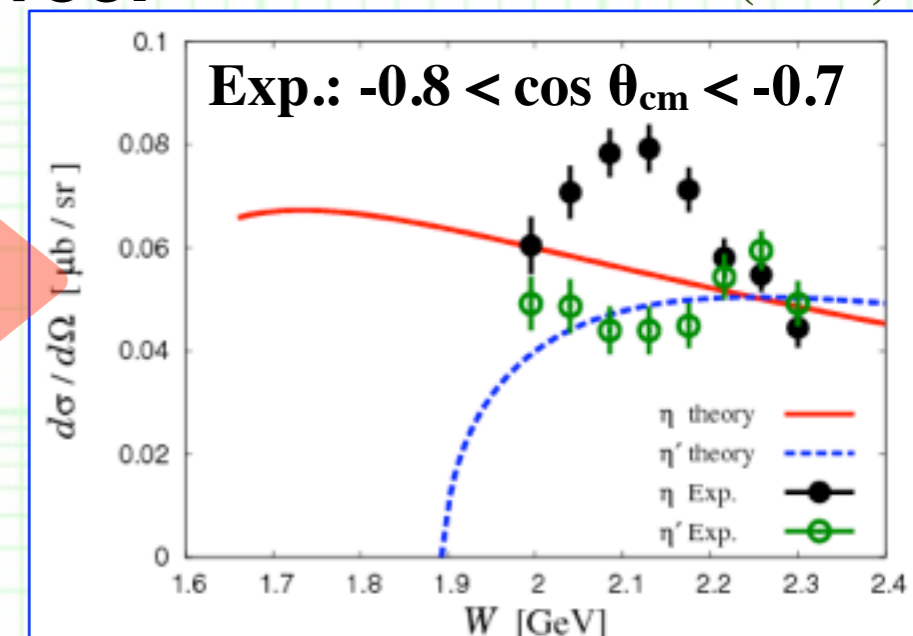
$$T_{\gamma p \rightarrow \eta p} = 0.362 \text{ GeV}^{-1}, \quad T_{\gamma p \rightarrow \eta' p} = 0.425 \text{ GeV}^{-1}$$

to reproduce roughly the LEPS data.

--- We also neglect angular dependence since we take forward proton emission.



Sumihama *et al.* (2009).



# 2. Formulation

**++  $\gamma d \rightarrow p X$  reaction with  $X = \eta n, \eta' n$  ++**

- Next we consider **the  $\gamma d \rightarrow p X$  reaction** with  **$X = \eta n, \eta' n$**  on a deuteron target.

- The cross section can be expressed as:

$$\frac{d^2\sigma_{\gamma d \rightarrow p X}}{dM_X d\Omega_p} = \frac{p_p p_m^* M_p M_n}{4E_\gamma^{\text{lab}} W_3} \frac{1}{(2\pi)^5} \int d\Omega_n^* |T_{\gamma d \rightarrow p X}|^2$$

---  **$M_X$ : Invariant mass of the final  $X = m-n$  system,**

**$\Omega_p$ : Total-CM solid angle for the final proton,**

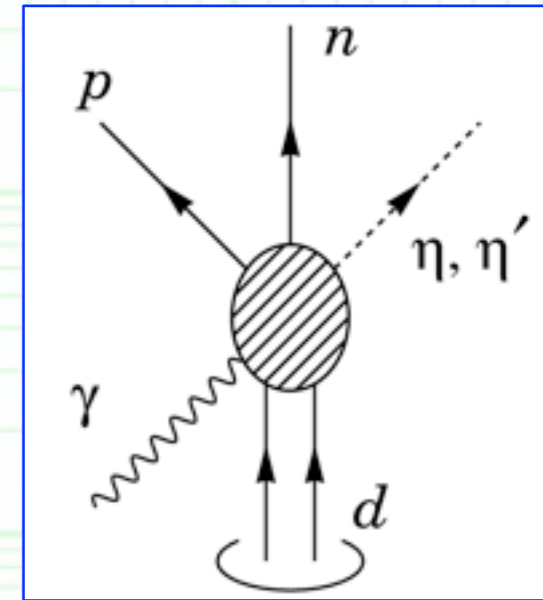
**$p_p$ : Total-CM momentum of the final proton,**

**$\Omega_n^*$ : Solid angle for the final neutron in the  $m-n$  CM frame,**

**$p_m^*$ : Momentum of the final neutron in the  $m-n$  CM frame,**

**$W_3$ : Total-CM energy of the system,**

**$T_{\gamma d \rightarrow p X}$ : the  $\gamma d \rightarrow p X$  ( $X = \eta n, \eta' n$ ) scattering amplitude.**



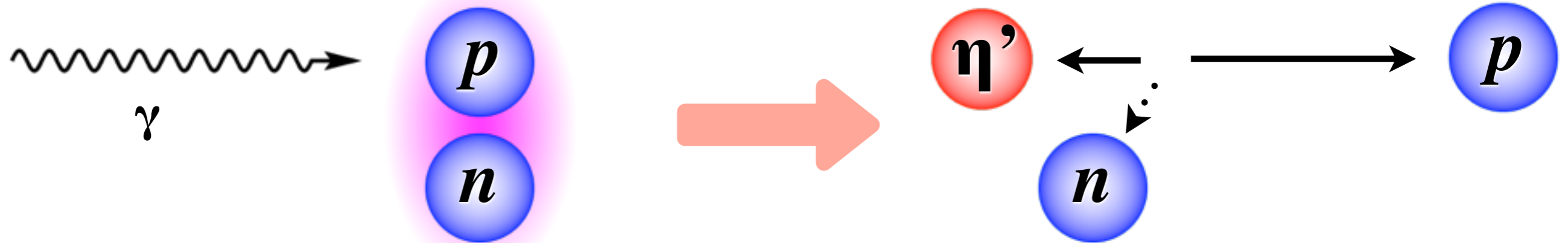
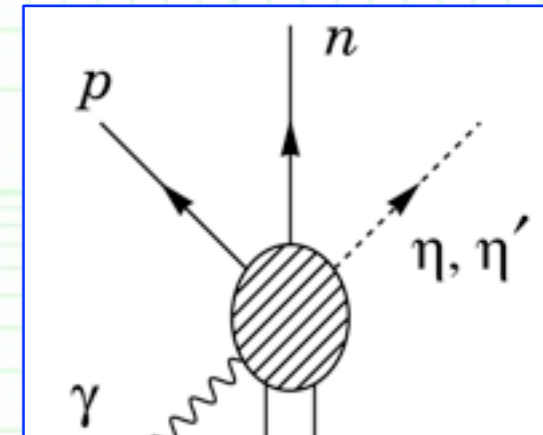
- Again **only the  $\gamma d \rightarrow p X$  scattering amp.  $T_{\gamma d \rightarrow p X}$  is unknown.**

# 2. Formulation

**++  $\gamma d \rightarrow p X$  reaction with  $X = \eta n, \eta' n$  ++**

- Next we consider **the  $\gamma d \rightarrow p X$  reaction with  $X = \eta n, \eta' n$**  on a deuteron target.

- In this study we calculate the  $\gamma d \rightarrow p X$  amp. from **diagrams favored by the kinematics** of the forward fast proton emission.



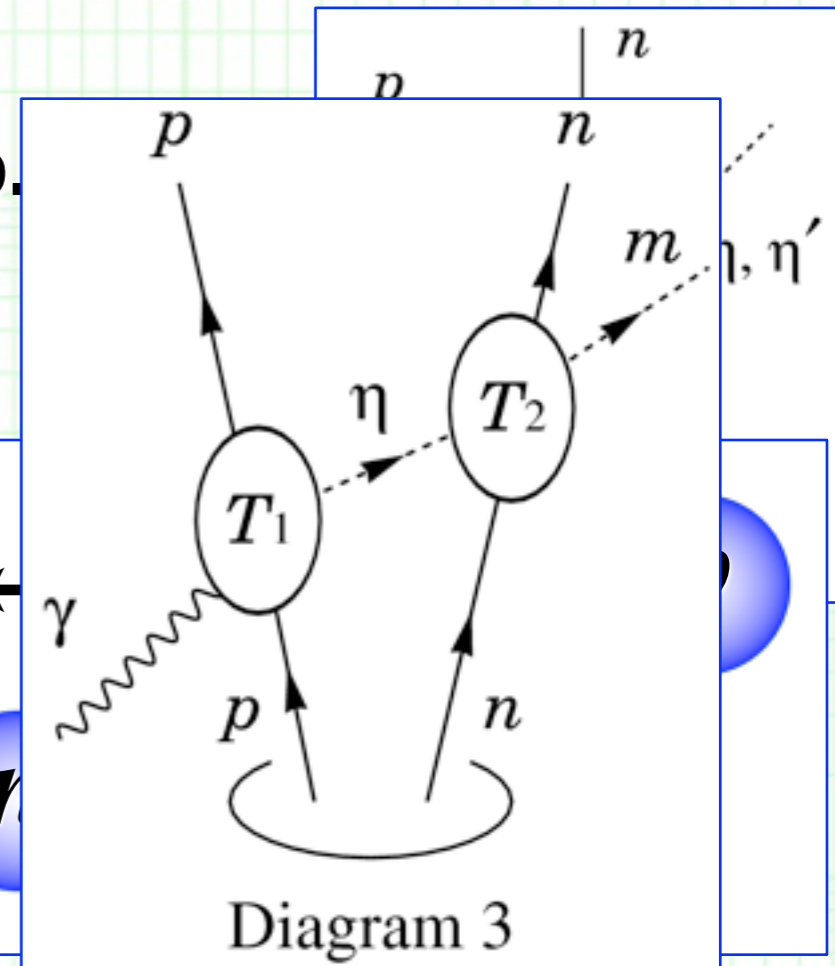
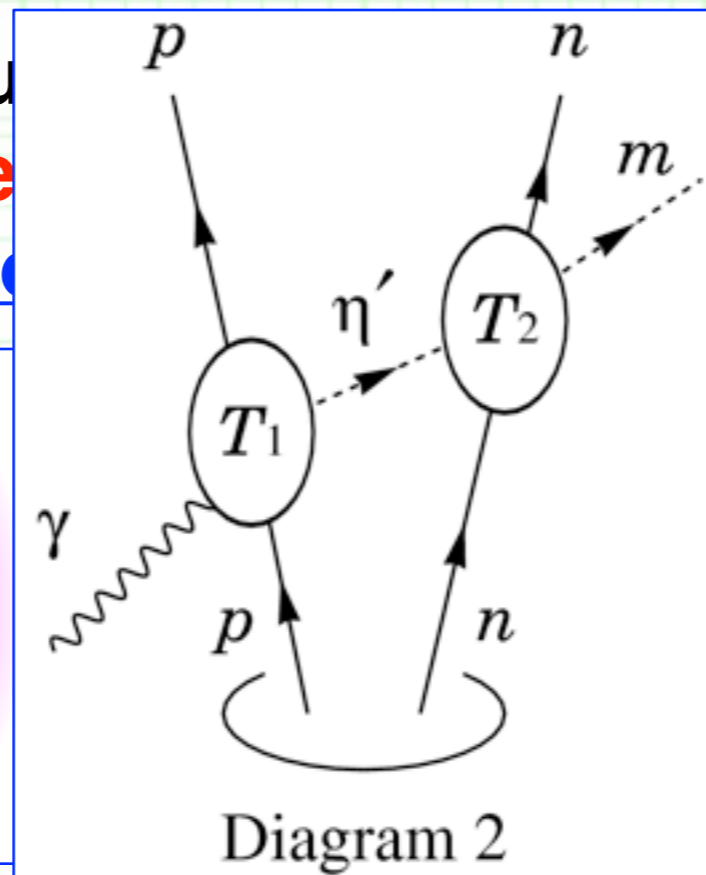
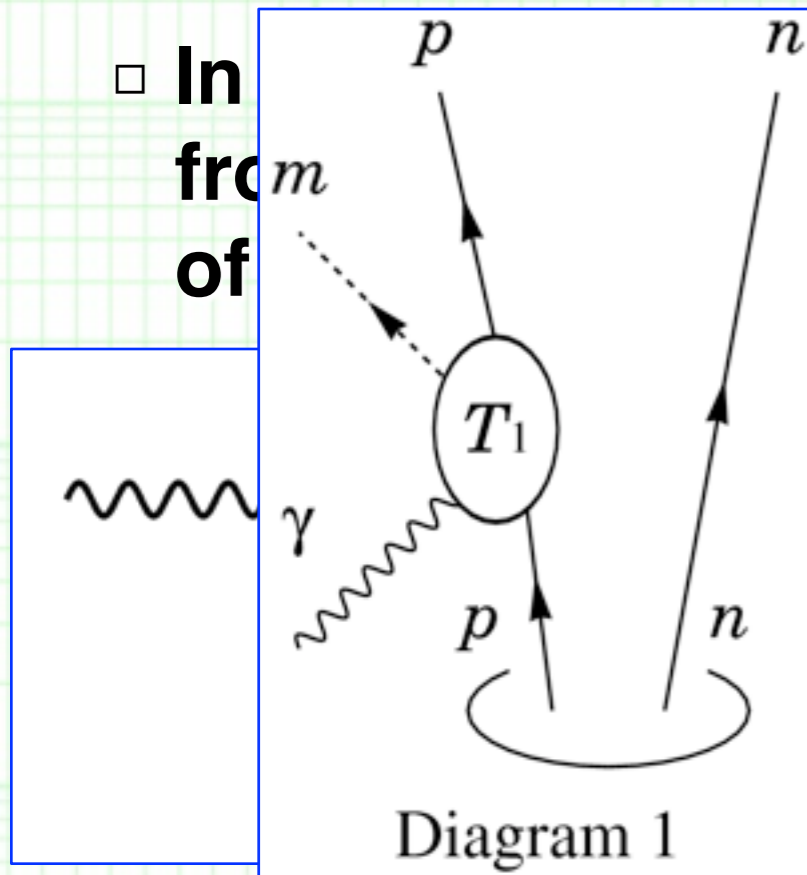
- 1. **Single scattering on a bound proton.**
- 2. **Double scattering with  $\eta' n \rightarrow X$  transition ---  $\eta'$  exchange.**
- 3. **Double scattering with  $\eta n \rightarrow X$  transition ---  $\eta$  exchange.**

# 2. Formulation

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□ In **from of** **calcul** **more** **st pro**



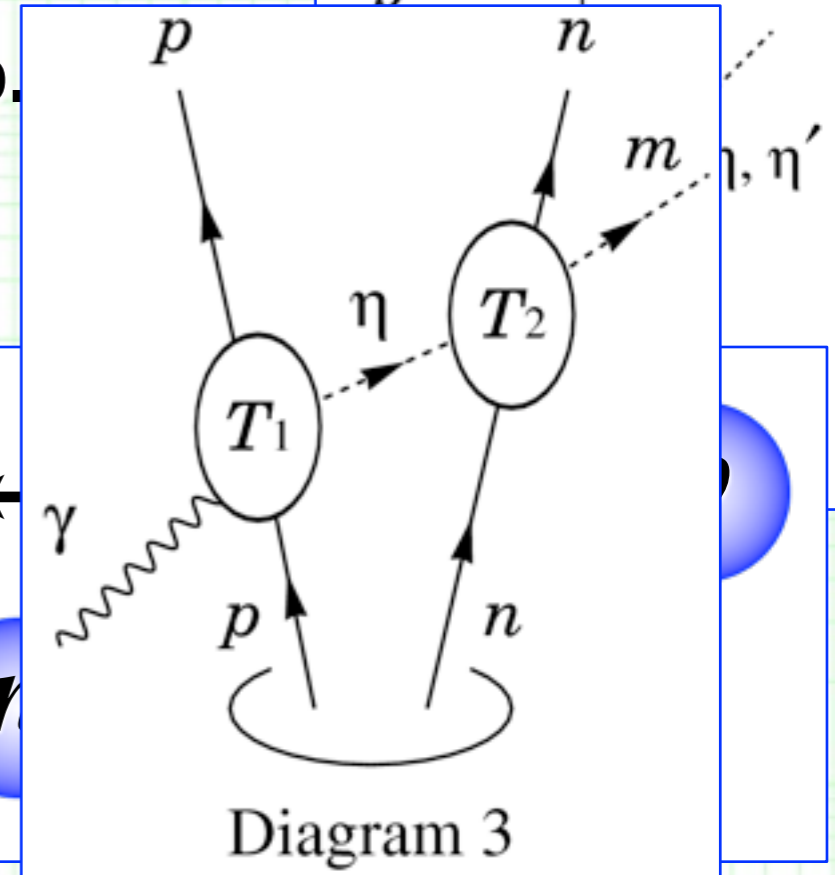
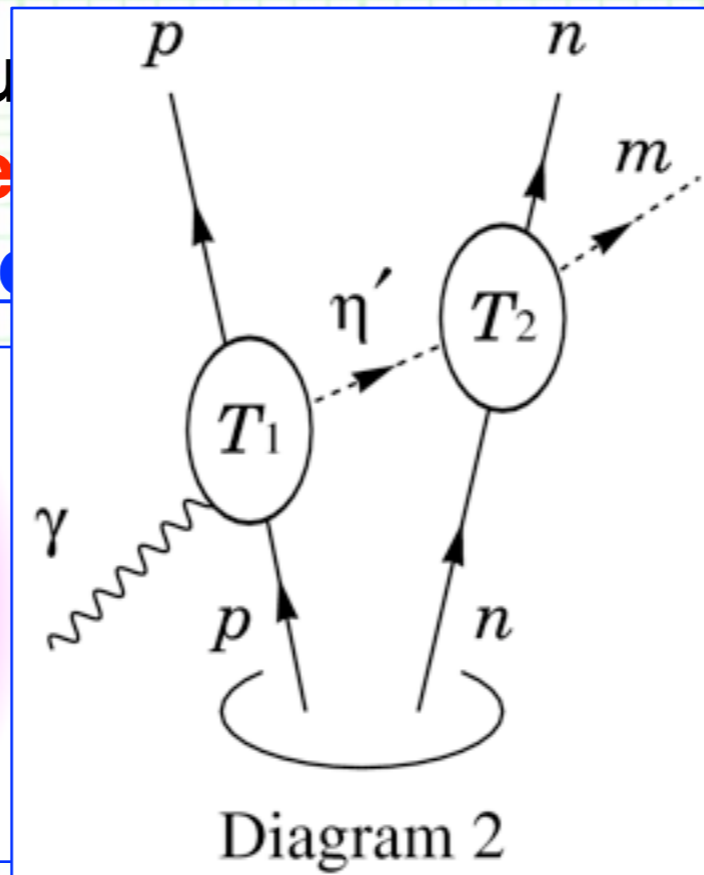
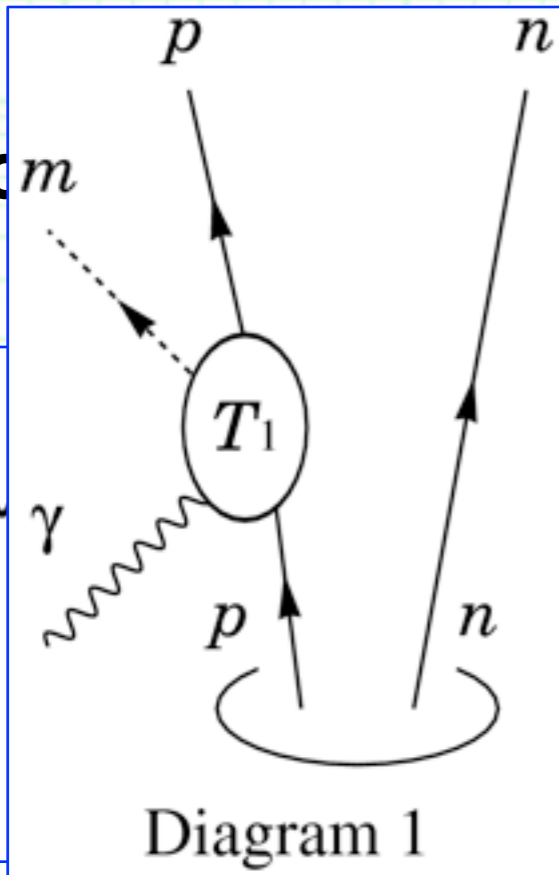
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# 2. Formulation

**++  $\gamma d \rightarrow p X$  reaction with  $X = \eta, \eta', n$  ++**

- Next we consider **the  $\gamma d \rightarrow p X$  reaction with  $X = \eta, \eta', n$**  on a deuteron target.

- In the calculation of the cross section, we have to consider the following diagrams:



- × We do **not consider scatterings on a bound neutron**, which will lead to forward fast neutron in the final state and gives only small momentum to the final proton.

# 2. Formulation

**++  $\gamma d \rightarrow p X$  reaction with  $X = \eta n, \eta' n$  ++**

- Next we consider **the  $\gamma d \rightarrow p X$  reaction with  $X = \eta n, \eta' n$**  on a deuteron target.

- **Scattering amplitudes from these diagrams** are obtained as: **D. Jido, E. Oset and T.S. (2009).**

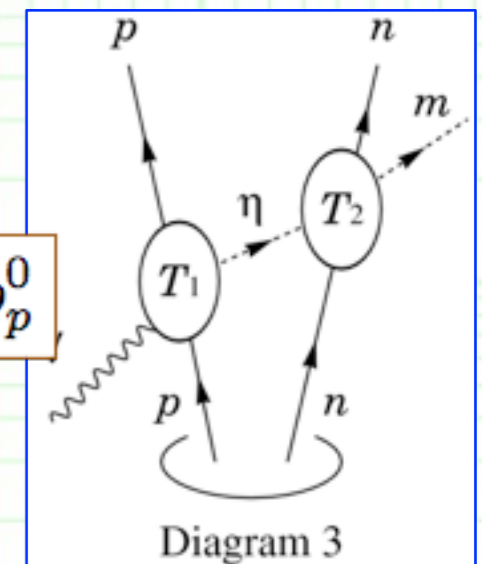
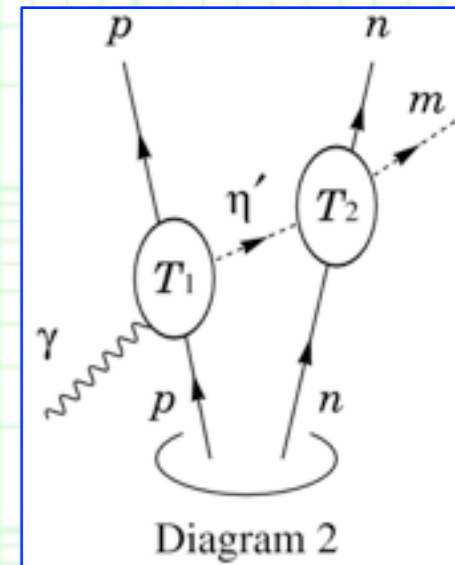
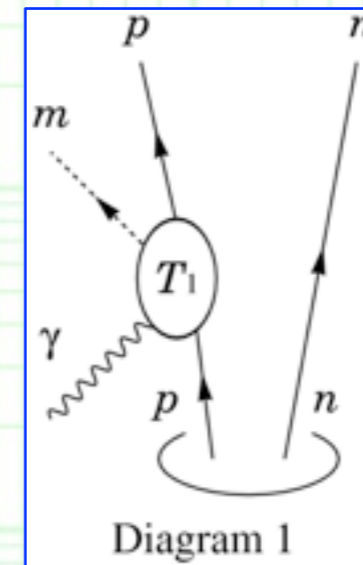
$$T_{\gamma d \rightarrow p X} = T_1^{(m)} + T_2^{(m)} + T_3^{(m)}$$

$$T_1^{(m)} = T_{\gamma p \rightarrow m p} \times \tilde{\varphi}(\vec{p}_n)$$

$$T_2^{(m)} = T_{\gamma p \rightarrow \eta' p} T_{\eta' n \rightarrow X}(M_X) \int \frac{d^3 q}{(2\pi)^3} \frac{\tilde{\varphi}(\vec{q} + \vec{p}_p - \vec{k})}{q^2 - M_{\eta'}^2 + i\epsilon}$$

$$q^0 = M_p + E_{\gamma}^{\text{lab}} - p_p^0$$

$$T_3^{(m)} = T_{\gamma p \rightarrow \eta p} T_{\eta n \rightarrow X}(M_X) \int \frac{d^3 q}{(2\pi)^3} \frac{\tilde{\varphi}(\vec{q} + \vec{p}_p - \vec{k})}{q^2 - M_{\eta}^2 + i\epsilon}$$



# 2. Formulation

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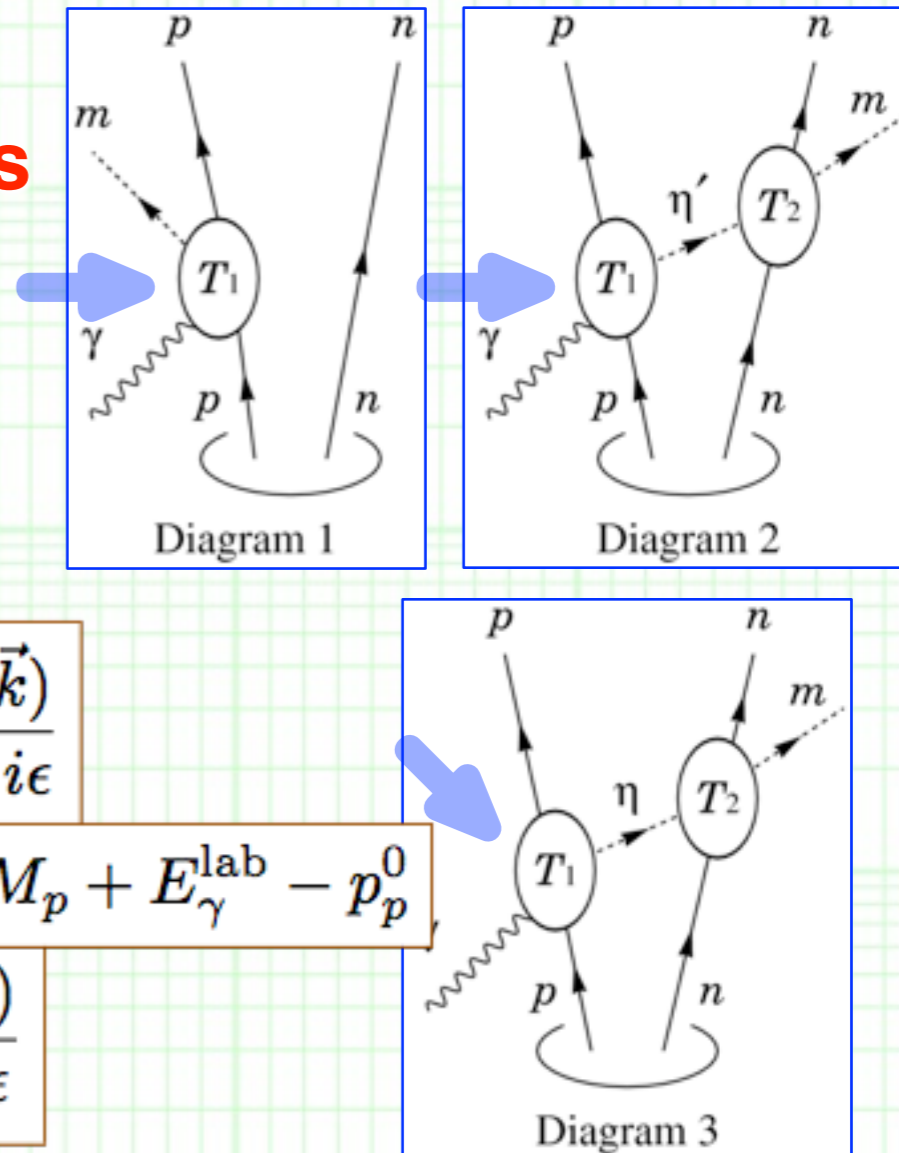
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1. The  $\gamma p \rightarrow \eta p, \eta' p$  amplitude  $T_{\gamma p \rightarrow \eta p, \eta' p}$  is **already fixed** from the free proton reaction.

# 2. Formulation

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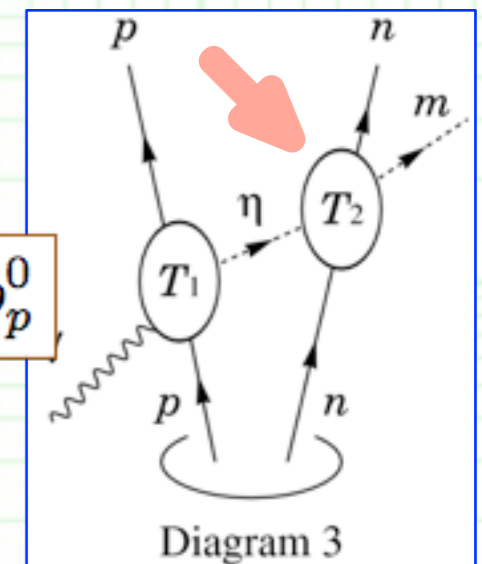
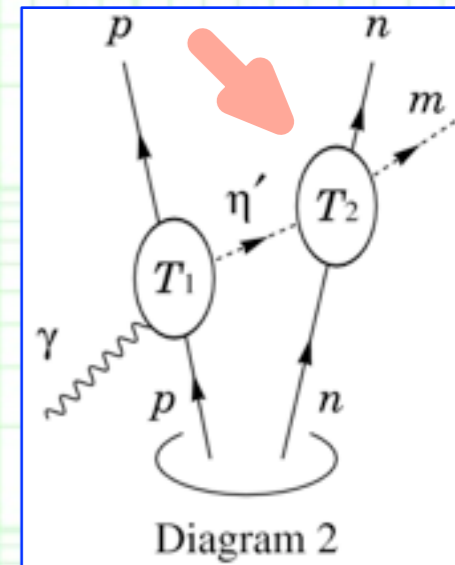
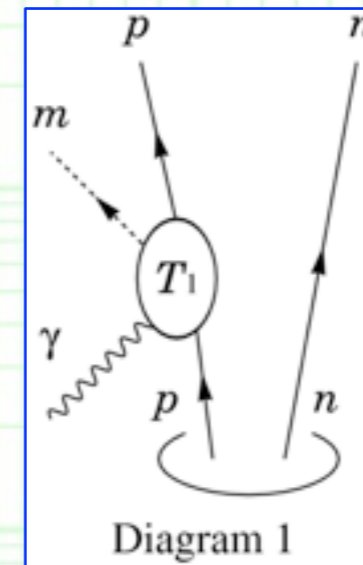
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- 2. **The  $\eta n, \eta' n \rightarrow X$  amplitude  $T_{\eta n, \eta' n \rightarrow X}$  is taken from the linear sigma model (already discussed in Intro.).**

# 2. Formulation

**++  $\gamma d \rightarrow p X$  reaction with  $X = \eta n, \eta' n$  ++**

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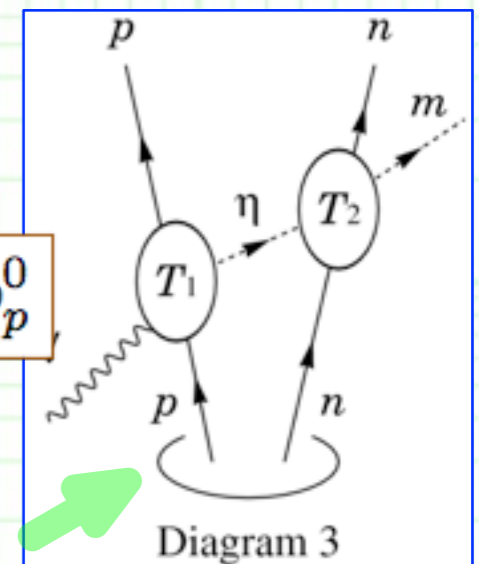
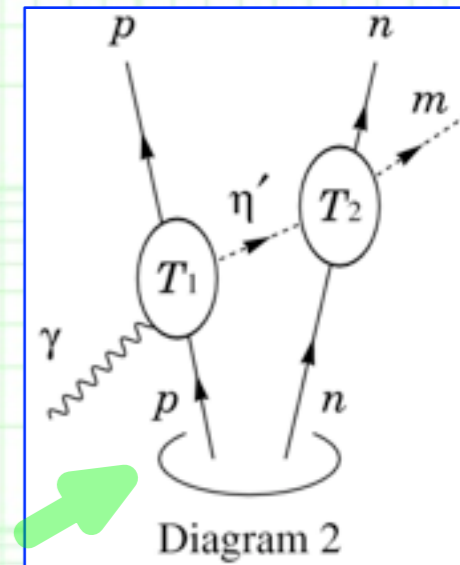
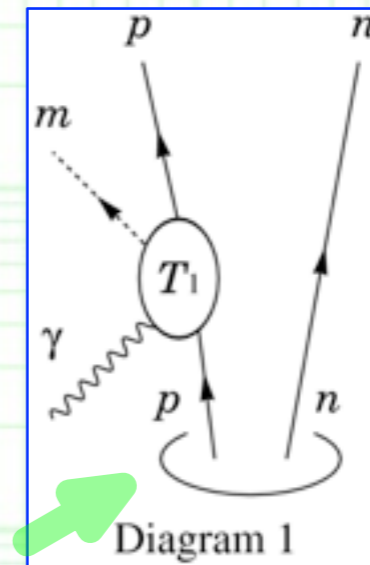
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$$T_3^{(m)} = T_{\gamma p \rightarrow \eta p} T_{\eta n \rightarrow X}(M_X) \int \frac{d^3 q}{(2\pi)^3} \frac{\tilde{\varphi}(\vec{q} + \vec{p}_p - \vec{k})}{q^2 - M_{\eta}^2 + i\epsilon}$$



**3. Deuteron wave function is **an analytic form****  
taken **from the Bonn potential with s wave only**:

Machleidt, *Phys. Rev. C* **63** (2001) 024001.

$$\tilde{\varphi}(\vec{q}) = \sum_{j=1}^{11} \frac{C_j}{\vec{q}^2 + m_j^2}$$

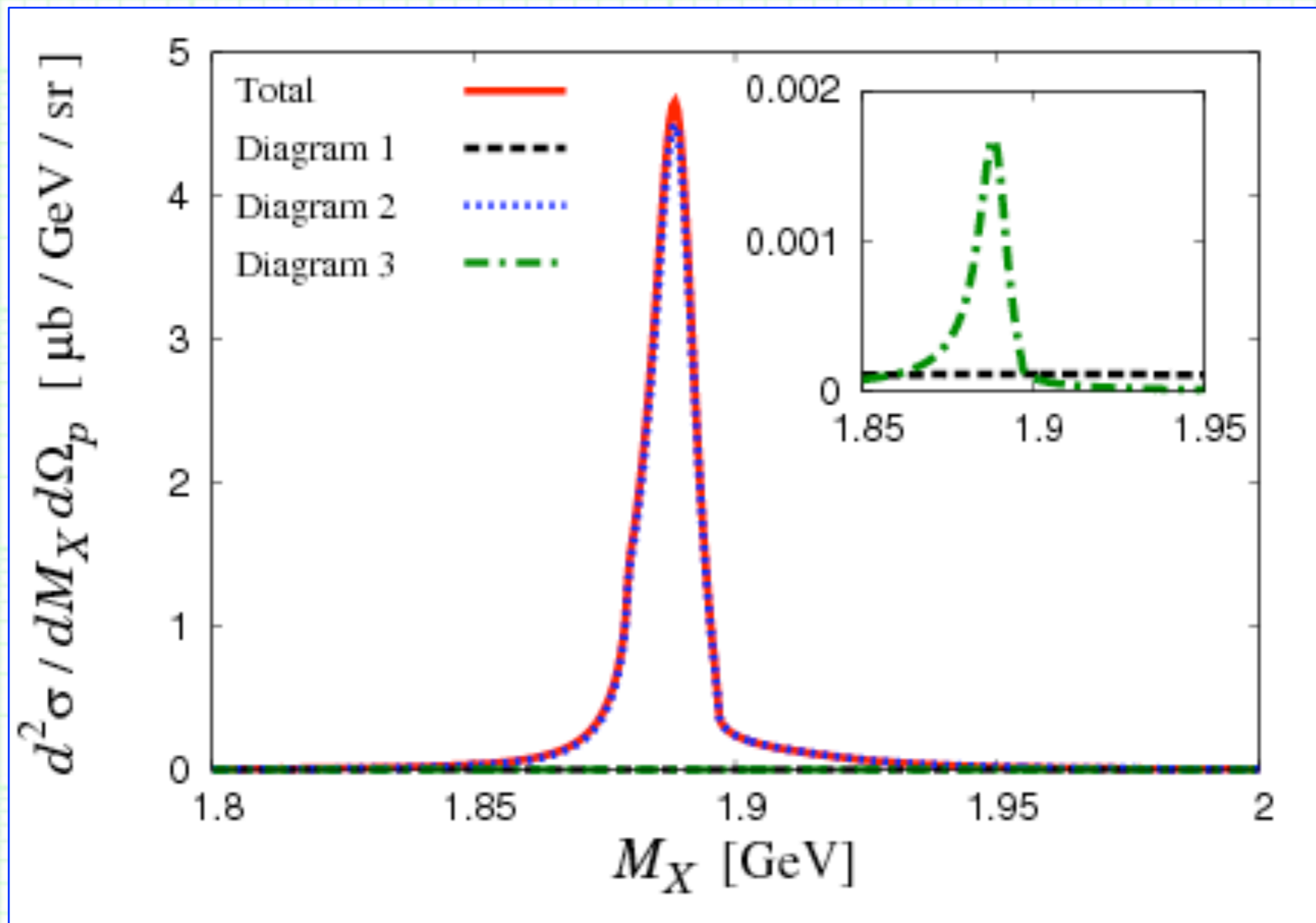
# 3. Results and discussions



# 3. Results and discussions

**$++ \gamma d \rightarrow p \eta n$  reaction  $++$**

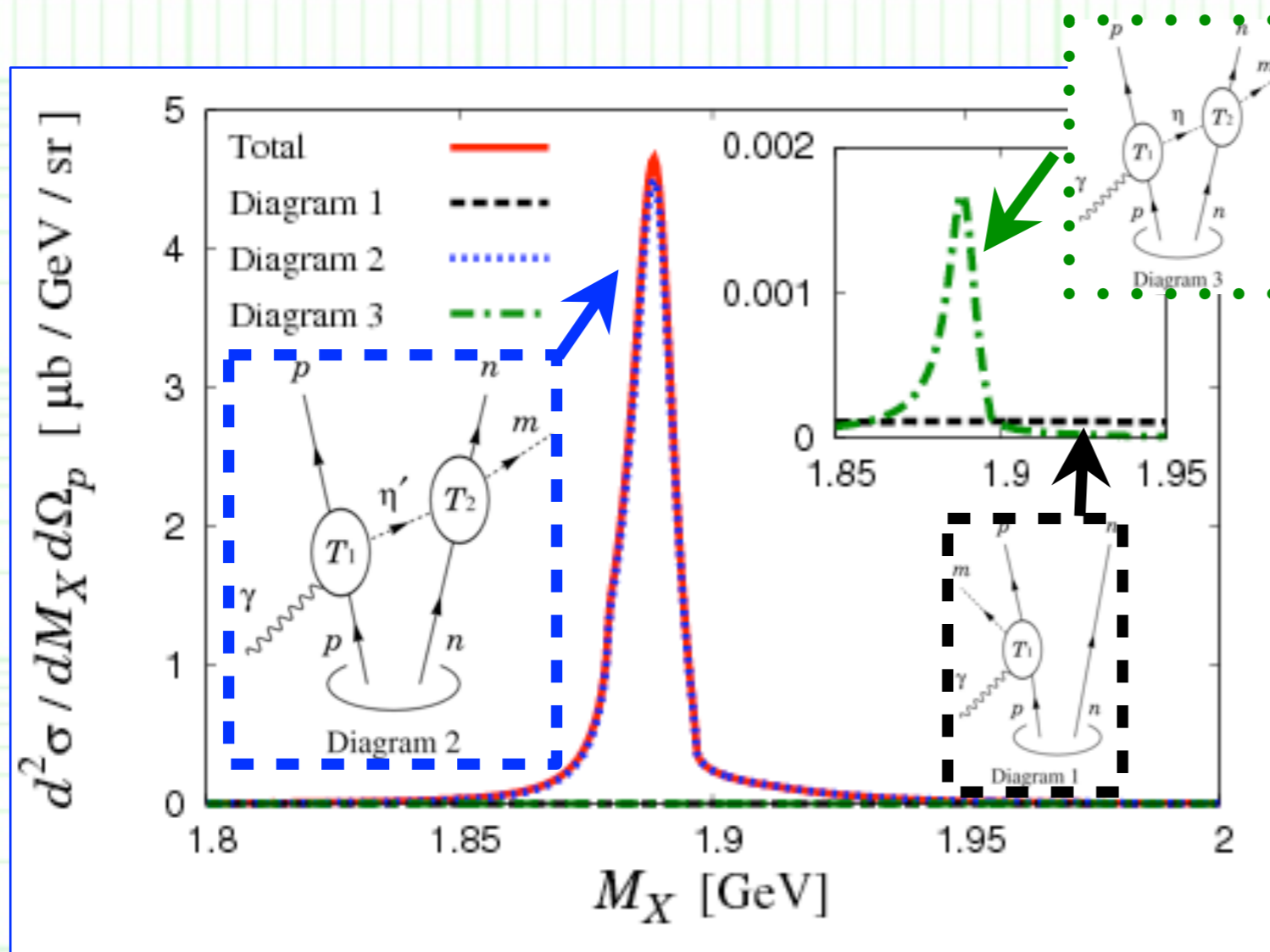
- We first consider  $\gamma d \rightarrow p \eta n$  reaction with  $E_{\gamma}^{\text{lab}} = 2.1 \text{ GeV}$ ,  $\theta_p = 0^\circ$  and calculate the differential cross section.



# 3. Results and discussions

**$++ \gamma d \rightarrow p \eta n$  reaction  $++$**

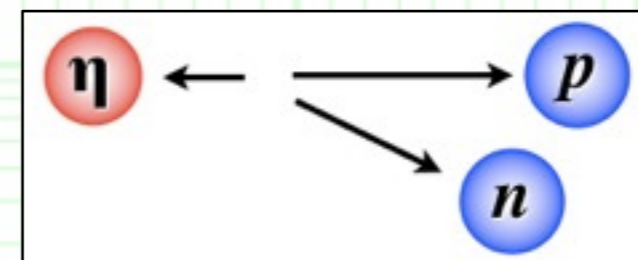
- We first consider  $\gamma d \rightarrow p \eta n$  reaction with  $E_{\gamma}^{\text{lab}} = 2.1 \text{ GeV}$ ,  $\theta_p = 0^\circ$  and calculate the differential cross section.



- The signal of the  $\eta' n$  bound state is dominated by Diag. 2 ( $\eta'$  exchange).

--- Almost on-shell  $\eta'$  and large  $\eta' n \rightarrow \eta n$  Amp.

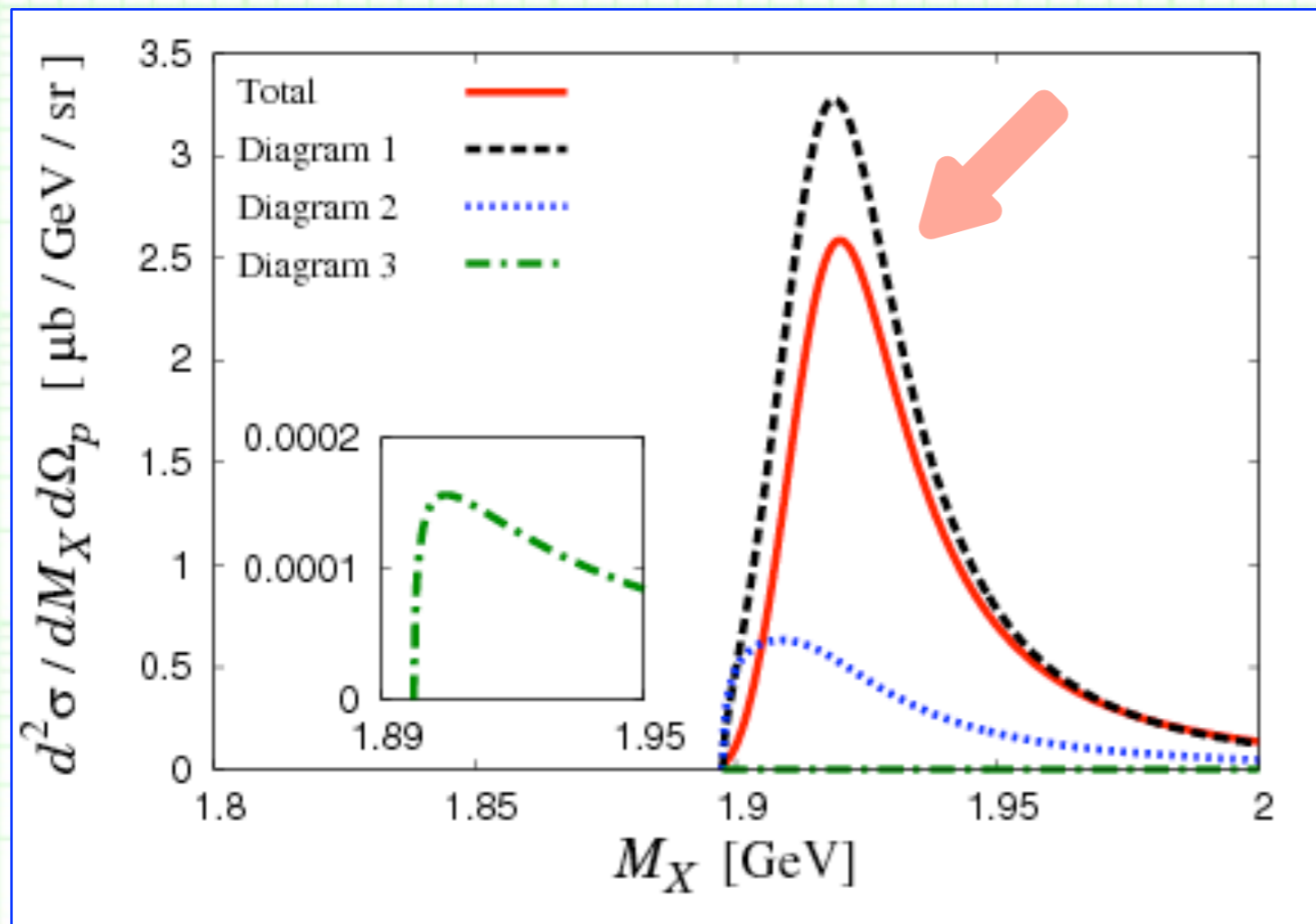
- Diag. 1 is negligible since large Fermi motion is necessary:



# 3. Results and discussions

**++  $\gamma d \rightarrow p \eta' n$  reaction ++**

- We next consider  $\gamma d \rightarrow p \eta' n$  reaction with  $E_{\gamma}^{\text{lab}} = 2.1 \text{ GeV}$ ,  $\theta_p = 0^\circ$  and calculate the differential cross section so as to compare quasi-free  $\eta'$  production with the signal of the  $\eta' n$  bound state.

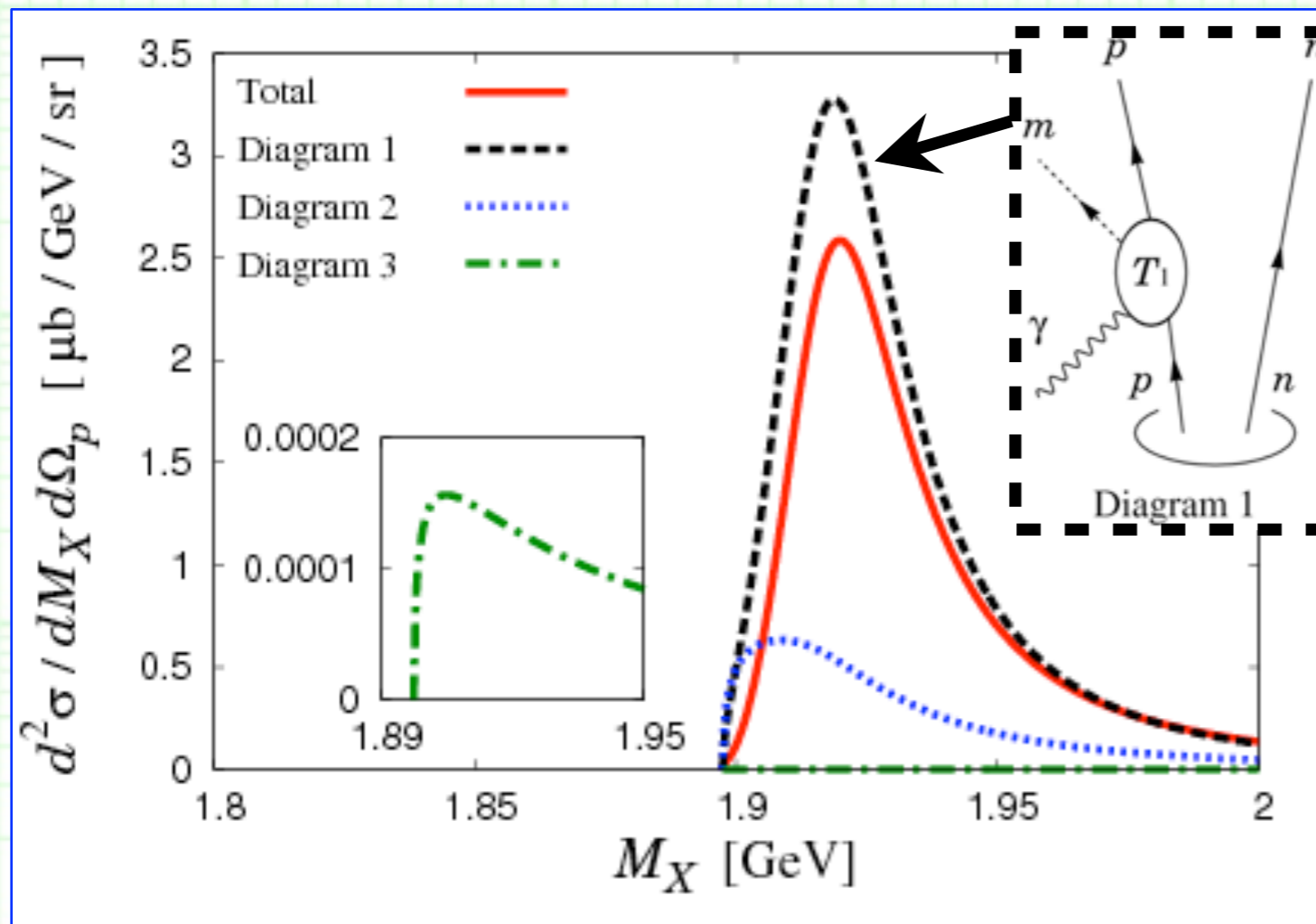


- We find **quasi-free  $\eta'$  production peak** just above the  $\eta' n$  threshold.

# 3. Results and discussions

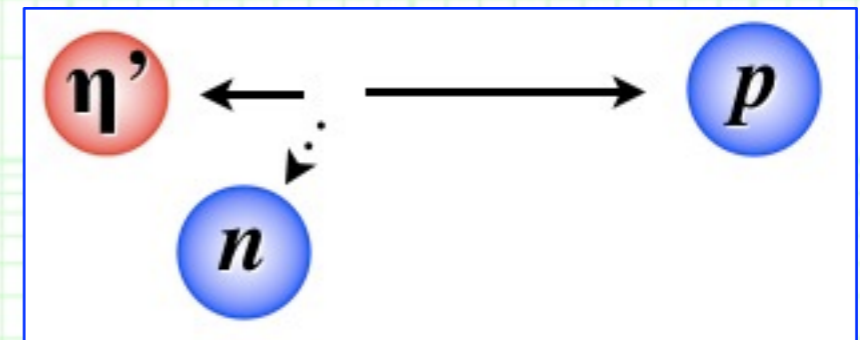
++  $\gamma d \rightarrow p \eta' n$  reaction ++

- We next consider  $\gamma d \rightarrow p \eta' n$  reaction with  $E_{\gamma}^{\text{lab}} = 2.1 \text{ GeV}$ ,  $\theta_p = 0^\circ$  and calculate the differential cross section so as to compare quasi-free  $\eta'$  production with the signal of the  $\eta' n$  bound state.



- We find **quasi-free  $\eta'$  production peak** just above the  $\eta' n$  threshold.

--- Large single-scattering  $\eta'$  production part.

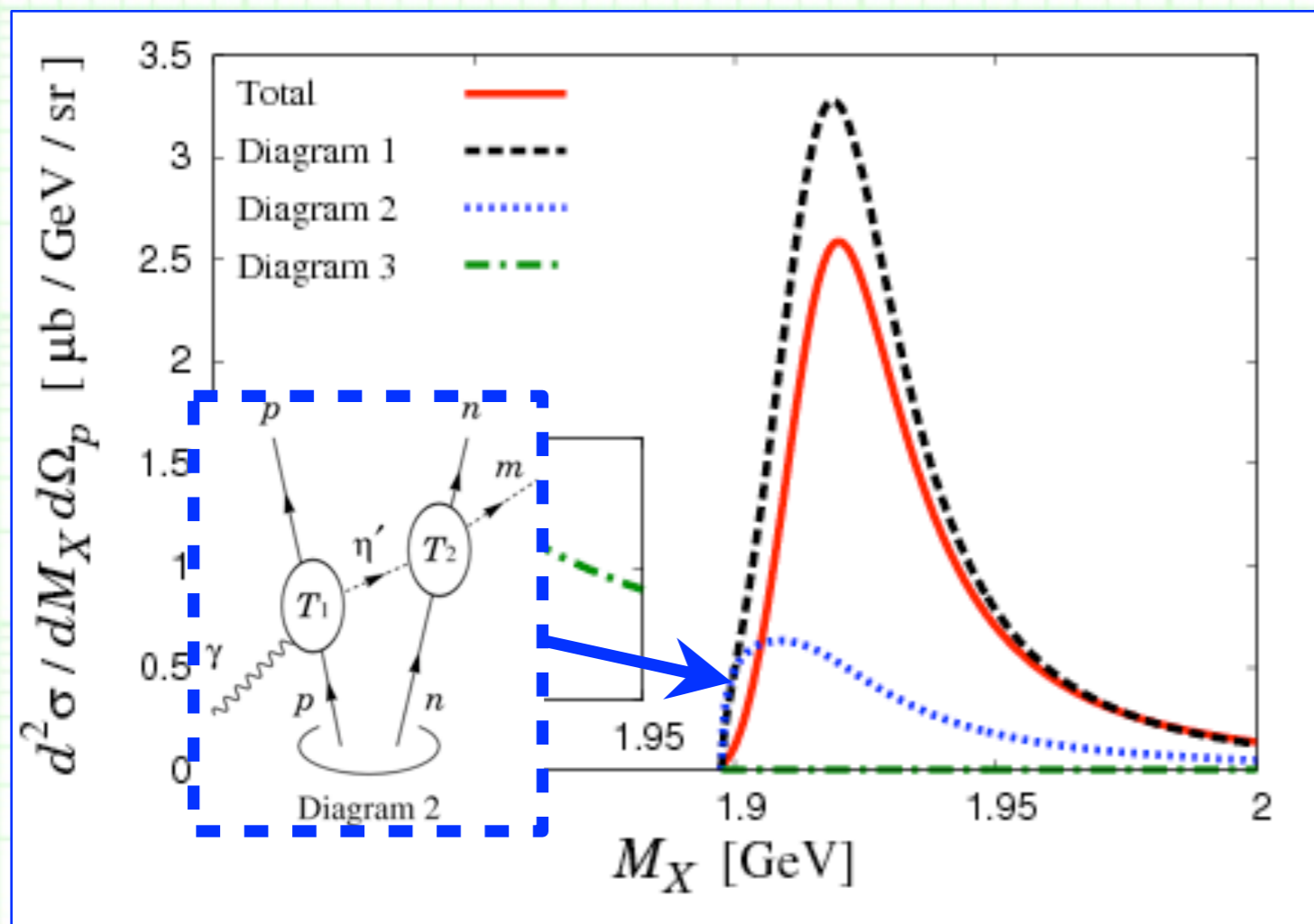


--- The invariant mass  $M_X = M_{\eta' n}$  becomes **small** for forward proton emission.

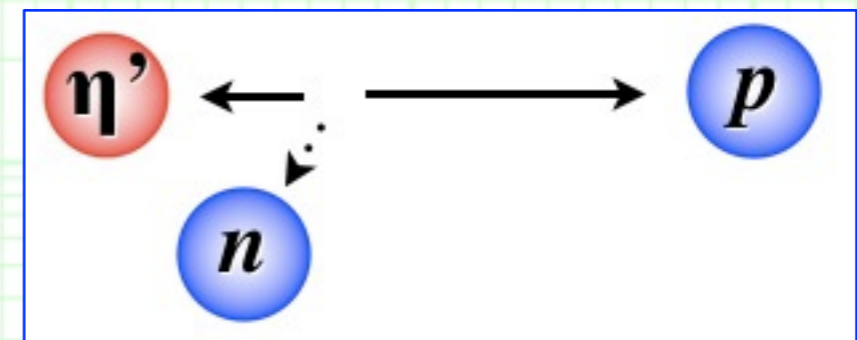
# 3. Results and discussions

++  $\gamma d \rightarrow p \eta' n$  reaction ++

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- We find **quasi-free  $\eta'$  production peak** just above the  $\eta' n$  threshold.
- Large single-scattering  $\eta'$  production part.



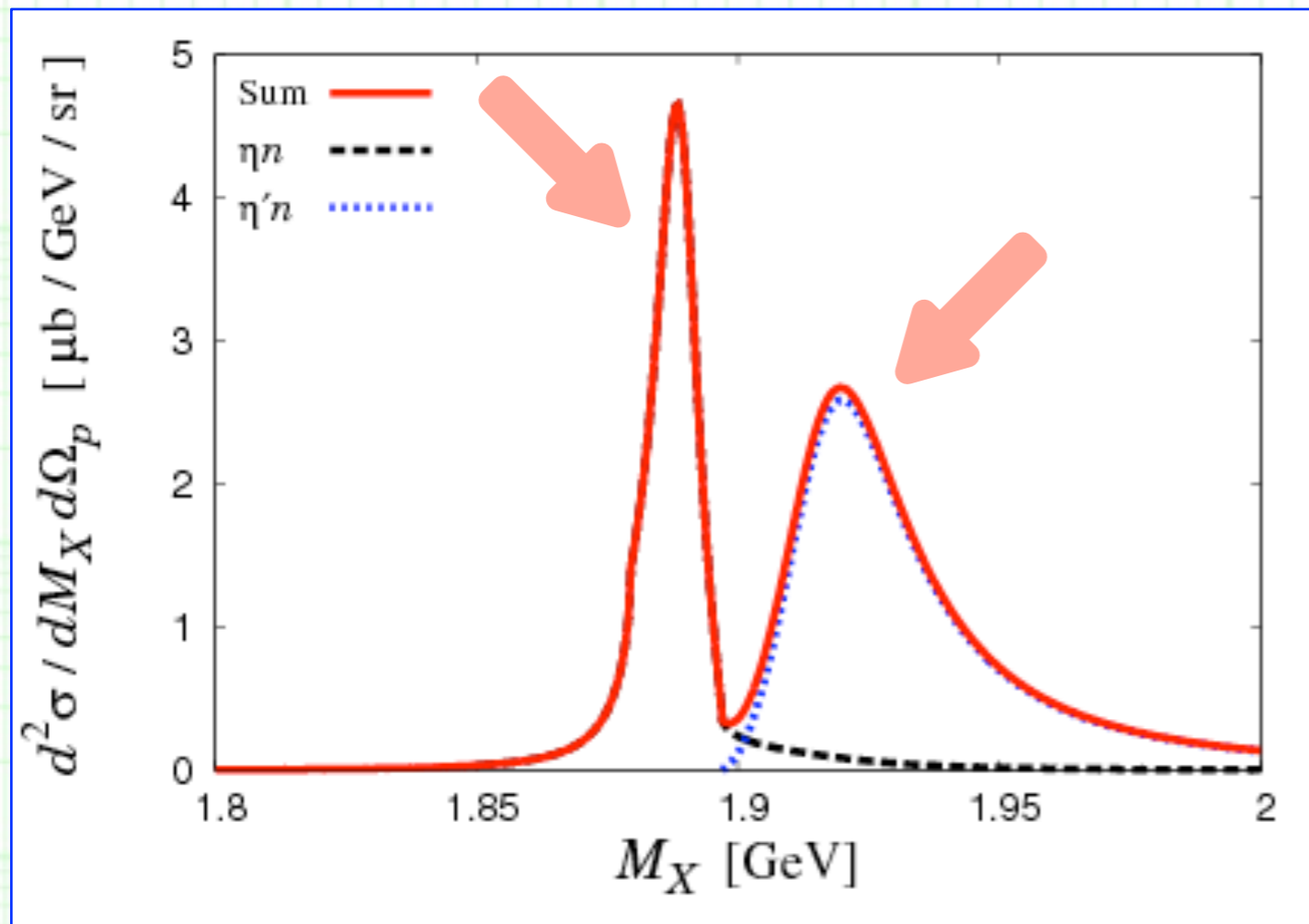
- However, the  $\eta'$ -exchange double scattering is **non-negligible**.
- Almost on-shell  $\eta'$  and large magnitude of the amplitude  $T_{\eta' n \rightarrow \eta'}$

# 3. Results and discussions

**++  $\gamma d \rightarrow p X$  ( $X = \eta n, \eta' n$ ) reaction from the sum ++**

- For **observation of the signal** of the  $\eta' n$  bound state **in real Exps.**, the signal should be comparable to the quasi-free  $\eta'$  contribution.

**--> We plot **sum of two differential cross sections** for  $\gamma d \rightarrow p \eta' n$  and  $\gamma d \rightarrow p \eta n$  reactions with  $E_{\gamma}^{\text{lab}} = 2.1 \text{ GeV}$ ,  $\theta_p = 0^\circ$ .**



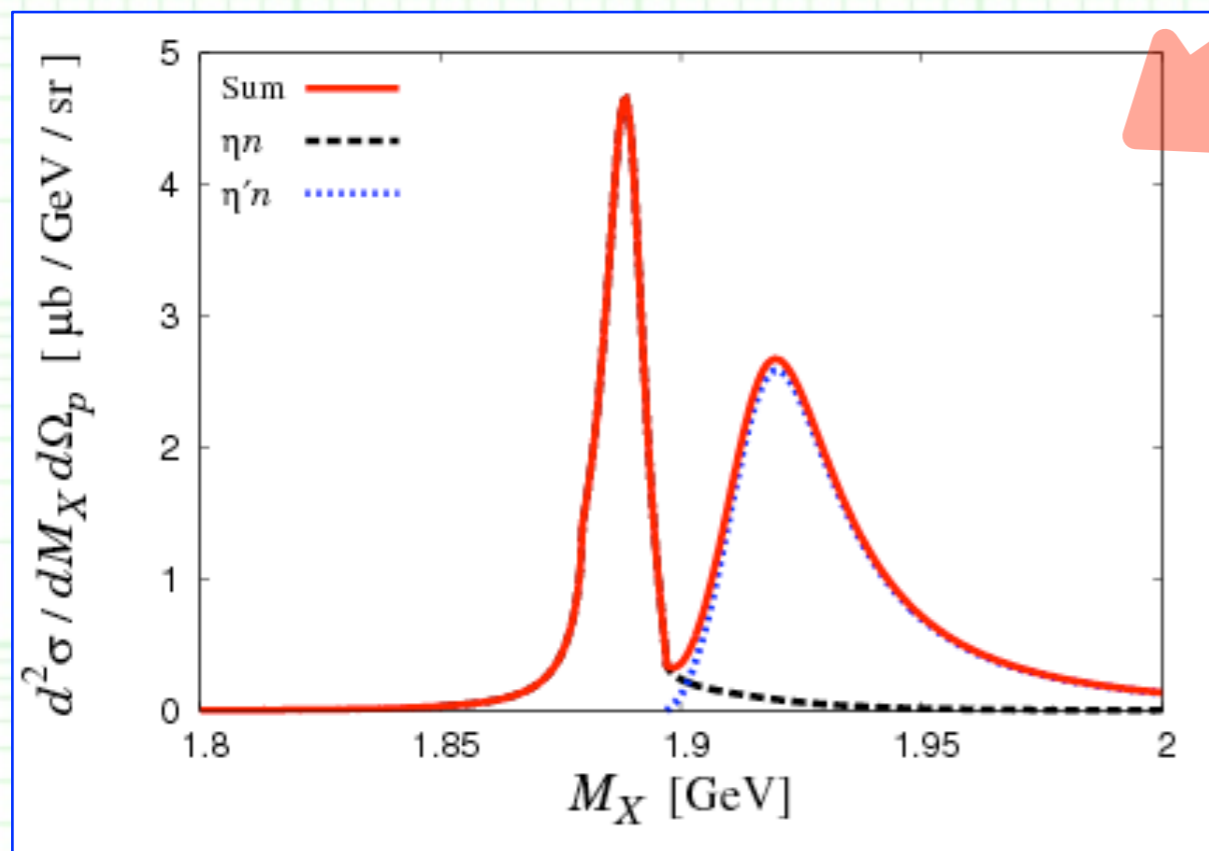
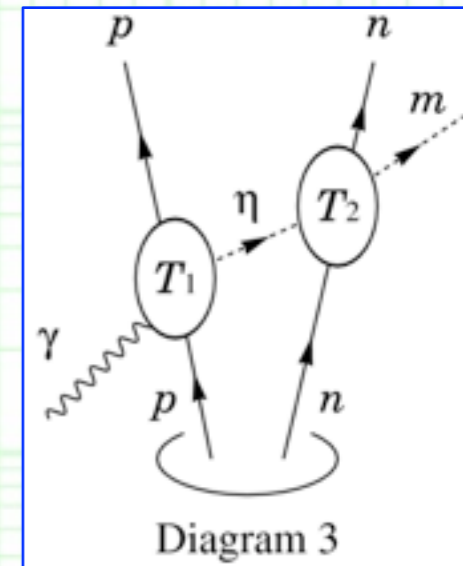
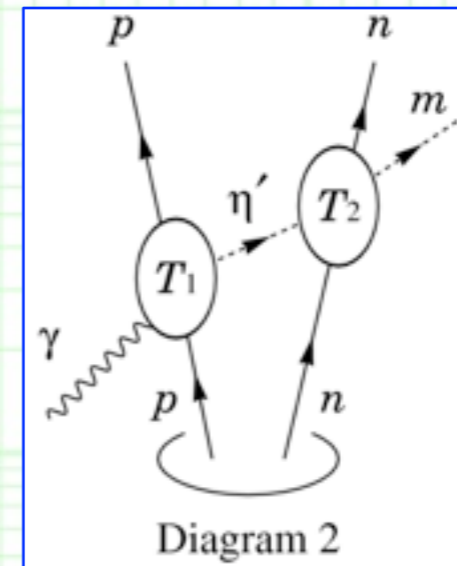
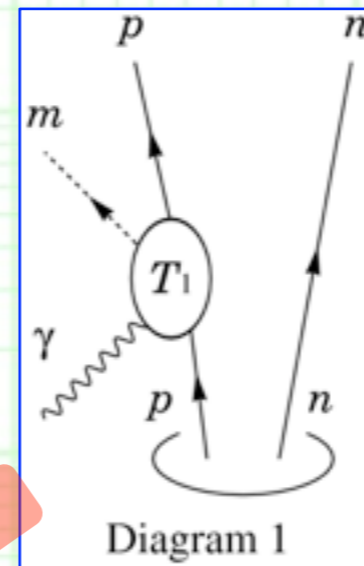
- We clearly find **two peaks** around the  $\eta' n$  threshold.
- The lower is **the bound state signal**, and the higher is the quasi-free  $\eta'$  part.
- Both the contributions are **comparable with each other**.
- > In our model we **can observe the signal** of the  $\eta' n$  bound state.

# 3. Results and discussions

++ From numerical results ... ++

- Taking into account three diagrams, which are relevant to our kinematics of the forward proton emission, we can calculate the differential cross section.

--> **The  $\eta' n$  bound state can be produced by the  $\eta'$ -exchange double scatt., and quasi-free  $\eta'$  by the single scatt.**

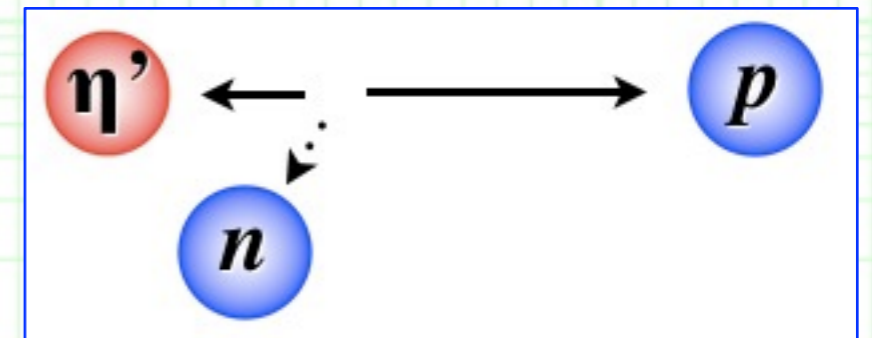
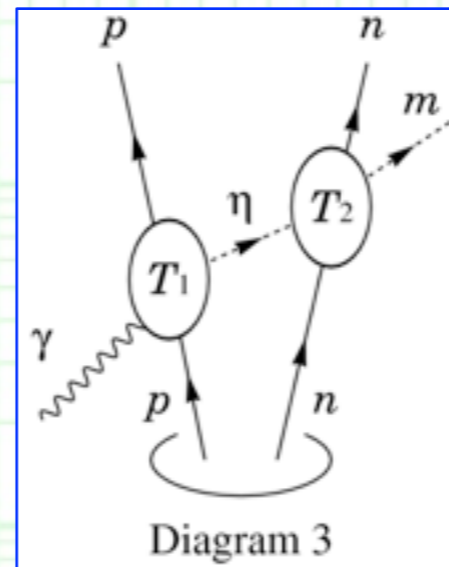
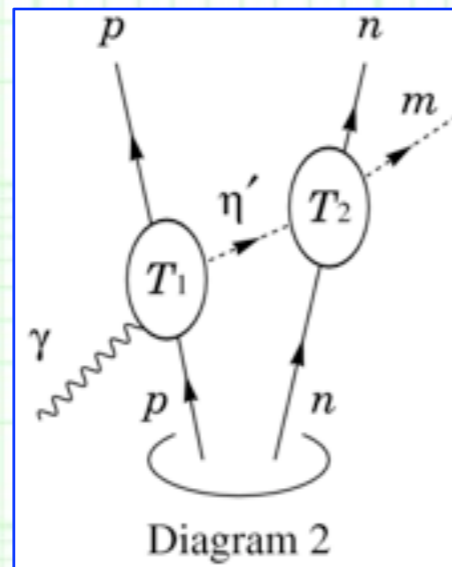
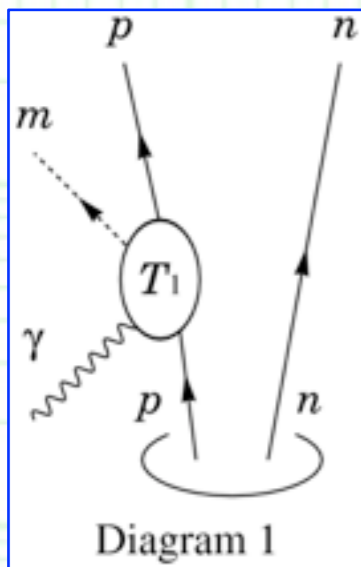


- From the numerical results of the differential cross section, **the signal of the  $\eta' n$  bound state is comparable to the quasi-free  $\eta'$ .**
- > In our model we can observe the signal of the  $\eta' n$  bound state.

# 3. Results and discussions

## ++ Model dependence ++

- We want to study **model dependence** of our results.



### □ Other diagrams ?

<-- Other diagrams will be **kinematically unfavored**, or give only background (small?). --- The forward emission of a fast proton.

□ Improvement of amplitudes  $T_{\gamma p \rightarrow \eta p, \eta' p} (T_1)$  and  $T_{\eta p, \eta' p \rightarrow X} (T_2)$ .

□ Other prescription to calculate double scattering (Diags. 2, 3) ?

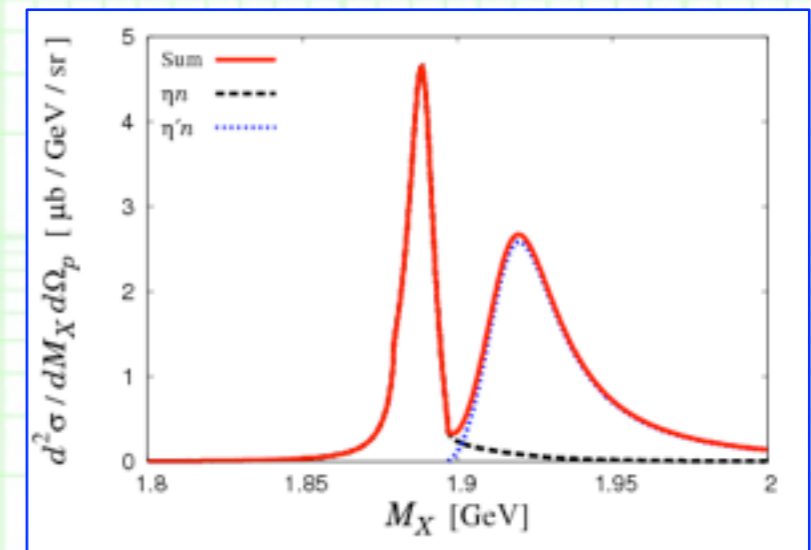
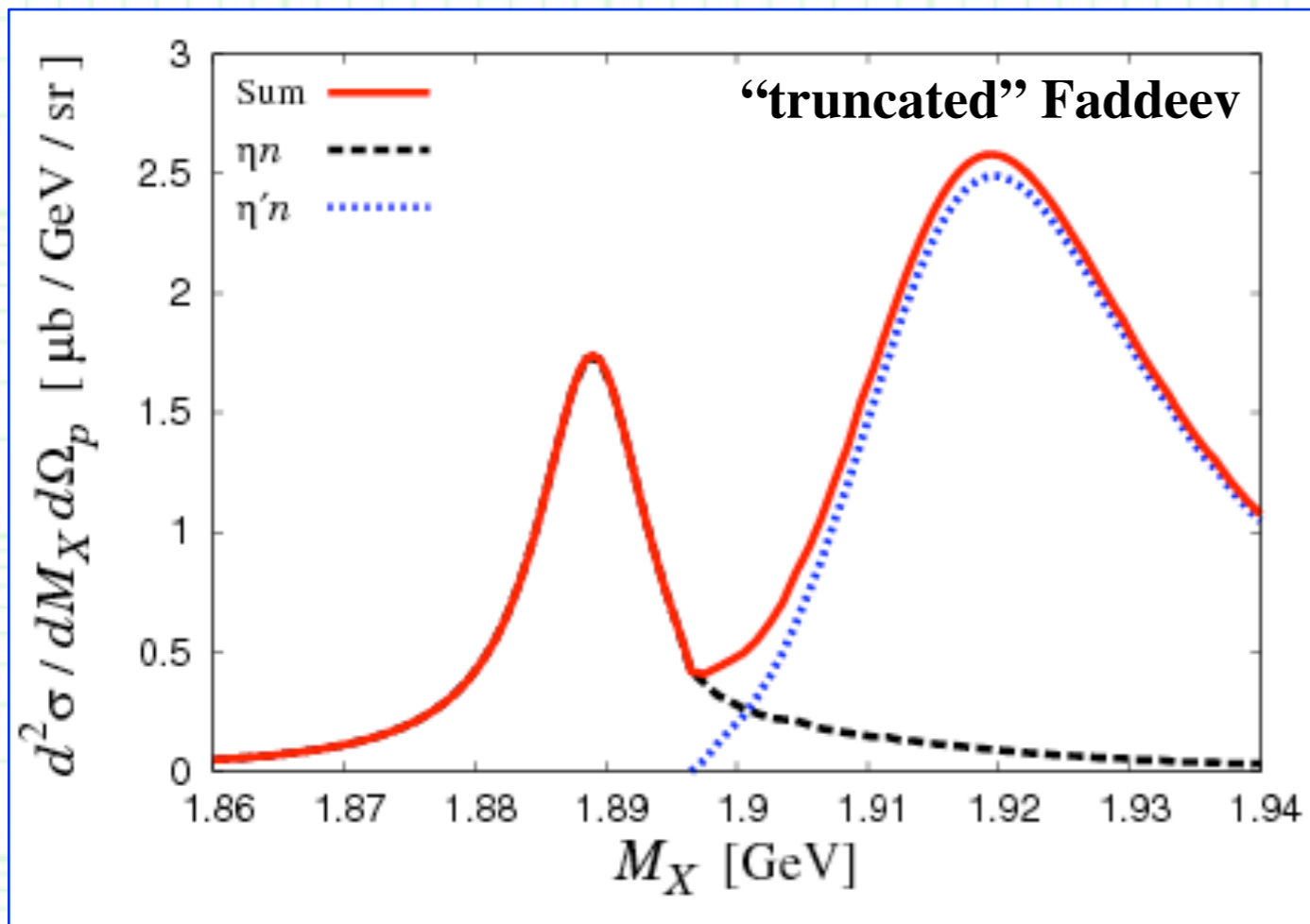
--- **Discuss the prescription dependence** in the next pages.

# 3. Results and discussions

## ++ Model dependence ++

- Calculate the differential cross section in a different prescription of double scattering (the “truncated” Faddeev approach), in which exchanged  $\eta^{(\prime)}$  energy is: Miyagawa and Haidenbauer (2012).

$$q^0 = M_d + E_{\gamma}^{\text{lab}} - p_p^0 - M_n - \frac{|\vec{q} + \vec{p}_p - \vec{k}|^2}{2M_n}$$



- We find the signal of the  $\eta' n$  bound state also in the “truncated” Faddeev approach. (But the signal becomes weak)

--> The prescription does not contaminate the bound-state signal.

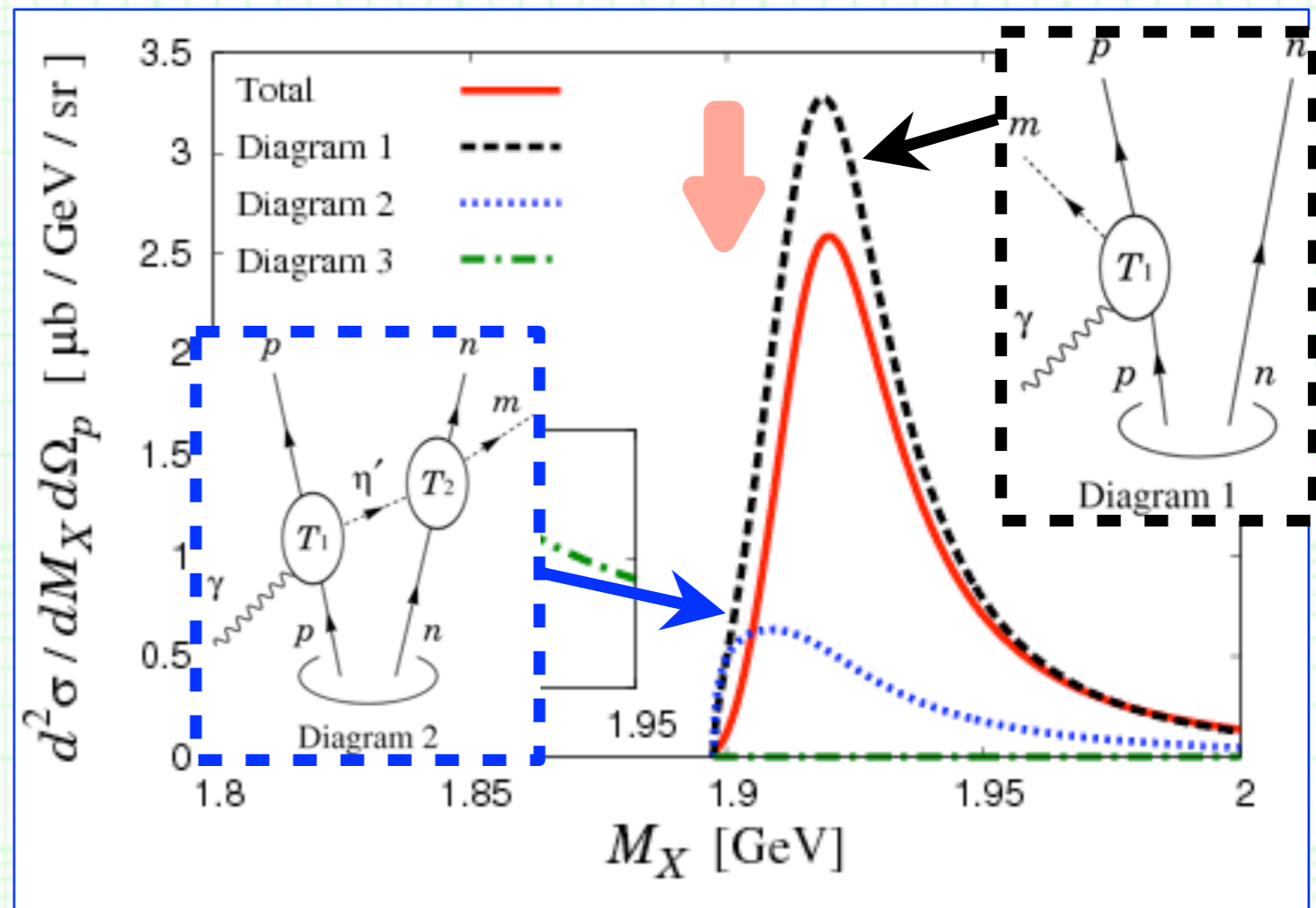
# 3. Results and discussions

## ++ Quasi-free $\eta'$ production yield ++

- We have found that in the  $\gamma d \rightarrow p \eta' n$  reaction the quasi-free  $\eta'$  production is slightly suppressed ( $\sim 80 - 90\%$ ) due to the  $\eta'$ -exchange double scattering.

--- Absorption of  $\eta'$  with large  $\text{Im}[T_{\eta' n \rightarrow \eta' n}]$ .

- Is there any possibility to observe the suppression of the production yield in Exp. ?
- Reference: Free-proton cross section.
- > Calculate the total cross section of the quasi-free  $\eta'$  production on a deuteron with forward angular cut in Lab. frame (cf. LEPS), and compare it with that on a free proton target.



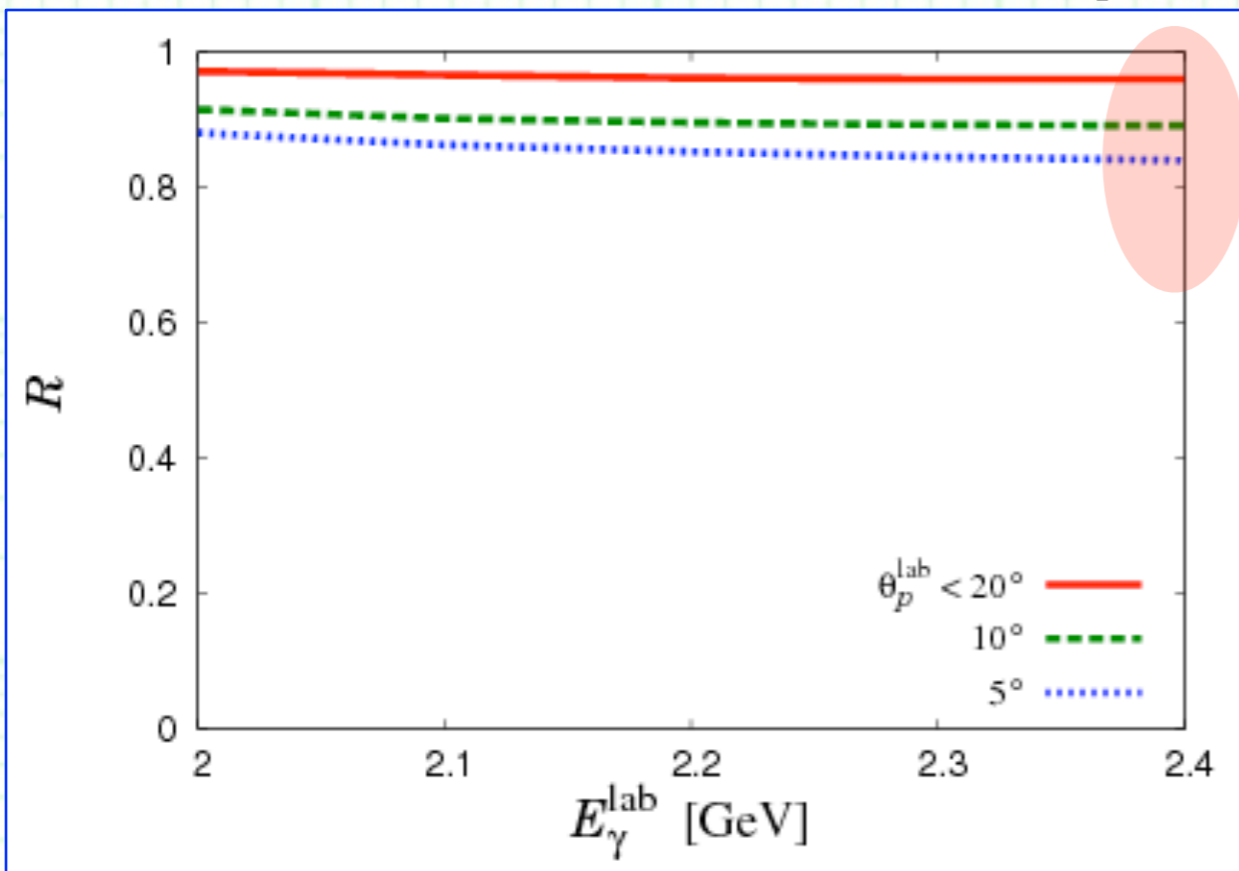
# 3. Results and discussions

## ++ Quasi-free $\eta'$ production yield ++

- We define the ratio  $R$  of the two total cross sections:

$$R \equiv \left[ \frac{\sigma_{\gamma d \rightarrow p \eta' n}}{\sigma_{\gamma p \rightarrow p \eta'}} \right]_{\theta_p^{\text{lab}} < \theta_{\text{upper limit}}}$$

- Since a bound proton is nearly on-shell and at rest in a deuteron, the ratio  $R$  is almost unity if the double scattering is negligible. (cf. similar ratio for the quasi-free  $\eta$  (not  $\eta'$ ) production is  $> 0.98$ .)



- The ratio becomes smaller as the angular cut decreases, since the momentum matching between  $\eta'$  and  $n$  becomes better.
- The ratio is  $R \sim 0.84$  at  $E_\gamma^{\text{lab}} = 2.4$  GeV,  $\theta_p^{\text{lab}} < 5^\circ$ .

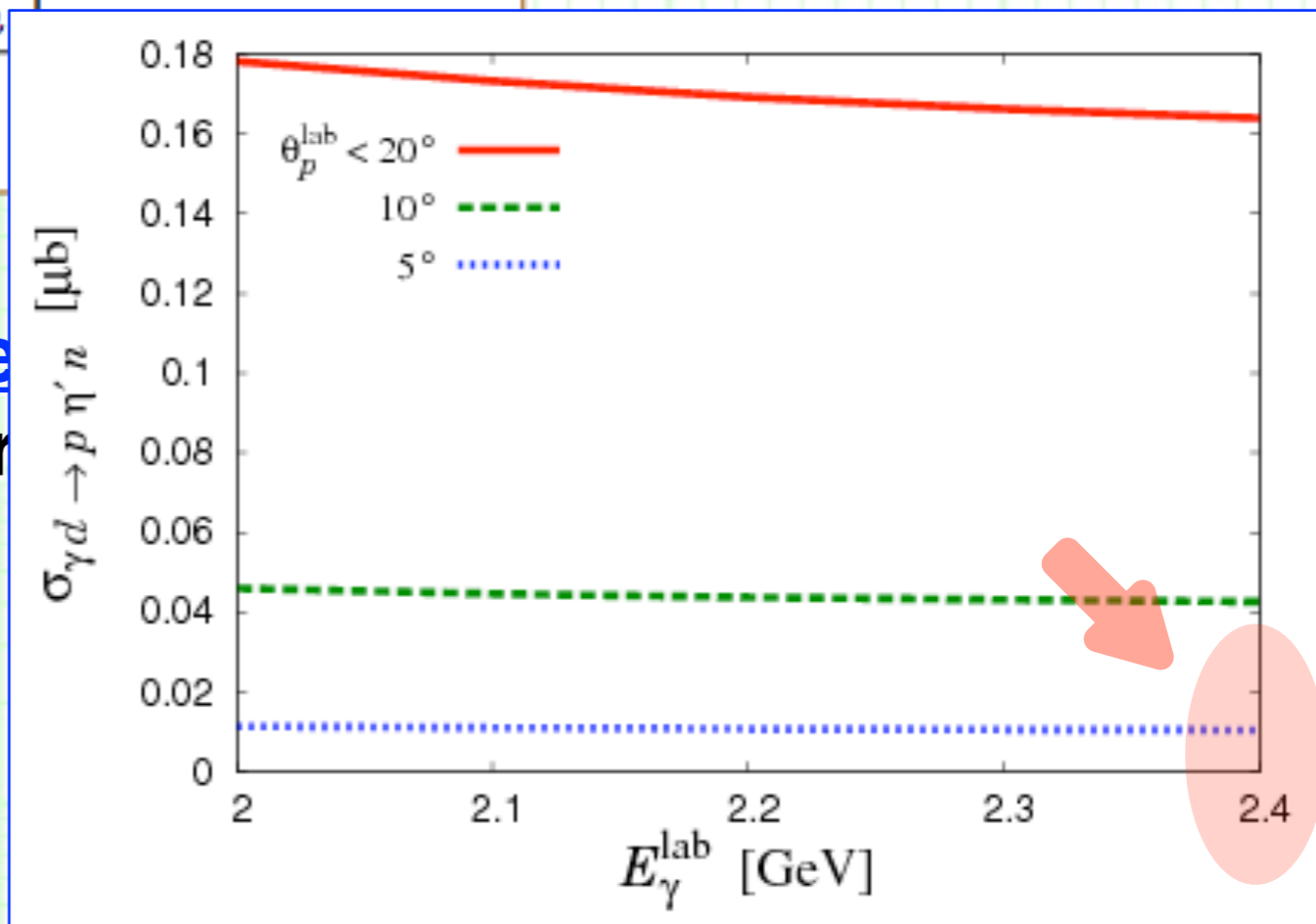
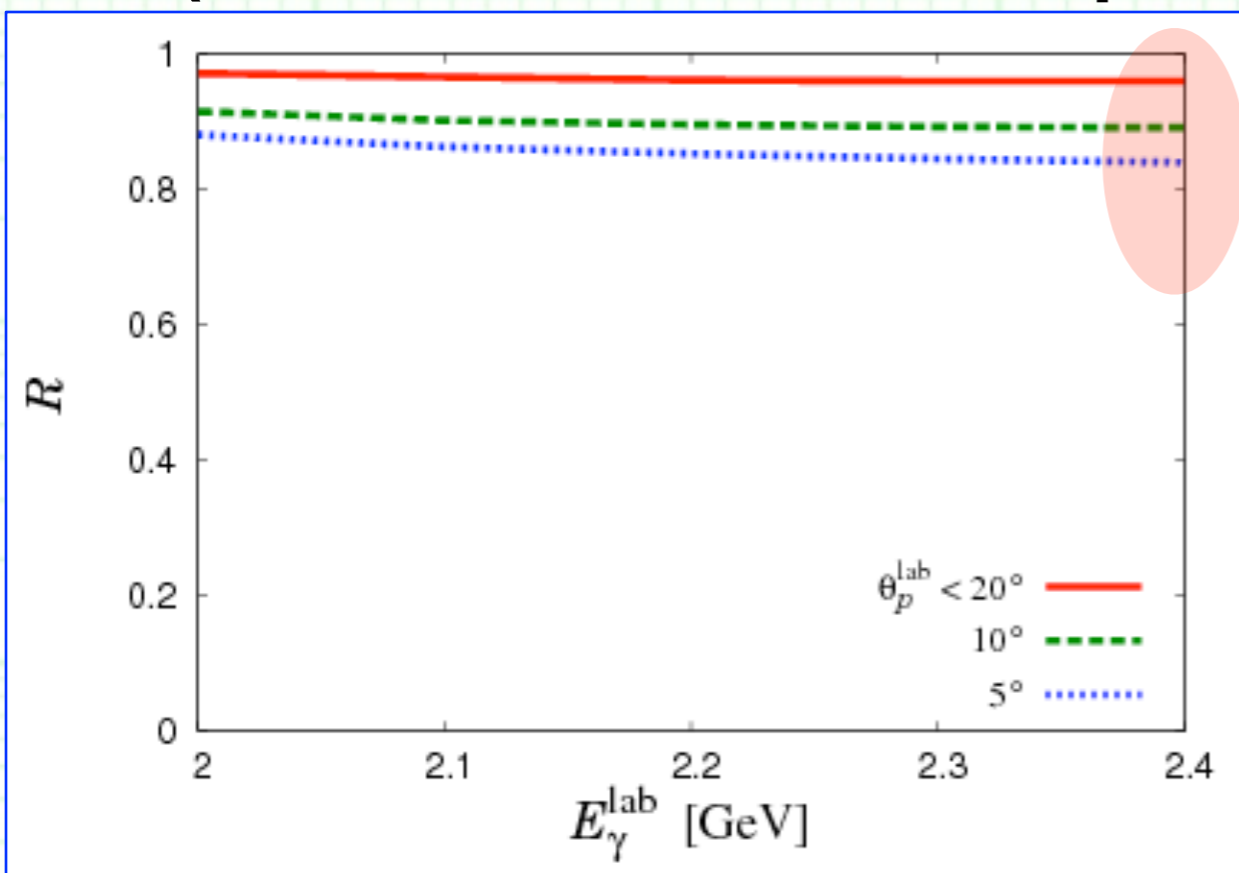
# 3. Results and discussions

## ++ Quasi-free $\eta'$ production yield ++

- We define the ratio  $R$  of the two total cross sections:

$$R \equiv \left[ \frac{\sigma_{\gamma d \rightarrow p \eta' n}}{\sigma_{\gamma p \rightarrow p \eta'}}$$

- Since a bound proton is nearly the ratio  $R$  is almost unity if the (cf. similar ratio for the quasi-fr



- However, at  $E_\gamma^{\text{lab}} = 2.4$  GeV,  $\theta_{p^{\text{lab}}} < 5^\circ$  **the total cross section is small** ( $\sim 10$  nb).

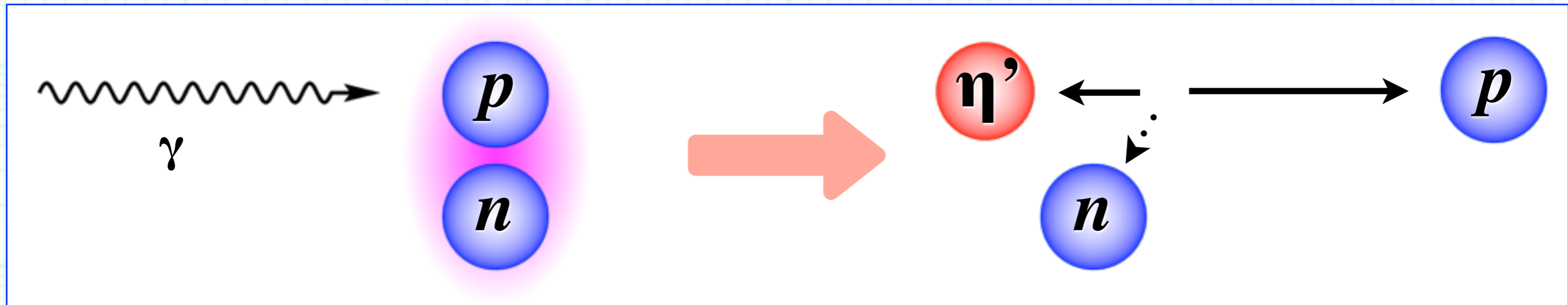
# 4. Summary



# 4. Summary

## ++ Summary ++

- We investigate **photoproduction of an  $\eta'$   $n$  bound state** in the  $\gamma d \rightarrow p X$  reaction with  $X = \eta n, \eta' n$ .



- **The forward proton emission** allows us to consider selectively the  $\eta' N$  photoproduction.
- Using the  $\eta' n$  interaction based on the linear sigma model, we **observe the bound-state signal against the quasi-free  $\eta'$** .
- The quasi-free  $\eta'$  production yield compared to free-proton case may be a clue to the  $\eta' N$  interaction.

**Thank you very much  
for your kind attention !**



# Appendix



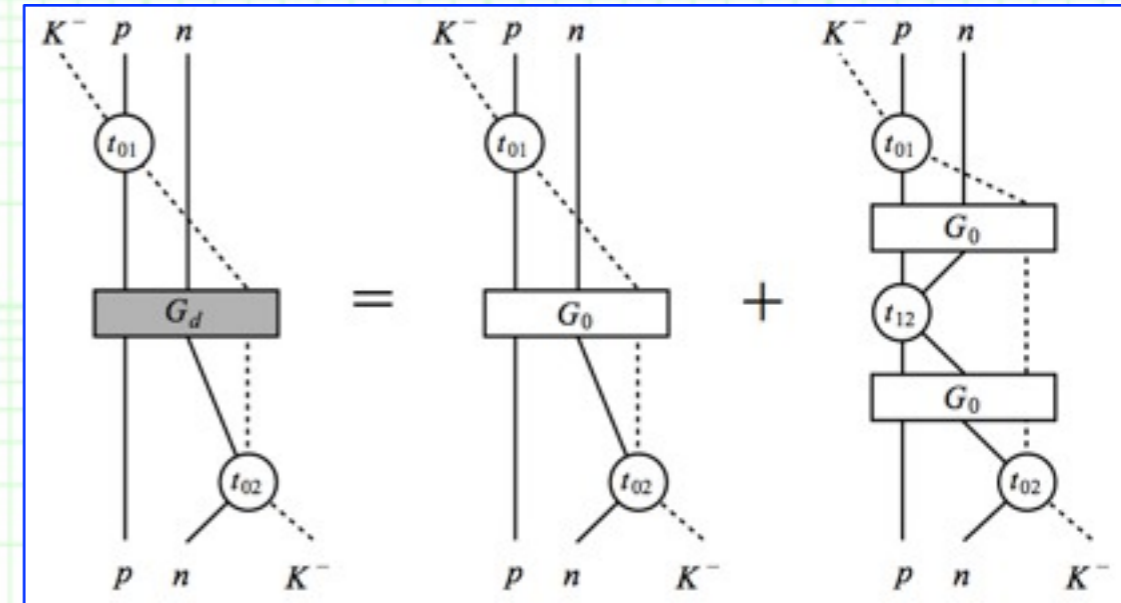
# 3. Results and discussions

## ++ Model dependence ++

- We have used the following form for the **exchanged  $\eta^{(\prime)}$  meson energy**:

$$q^0 = M_p + E_\gamma^{\text{lab}} - p_p^0$$

- Based on **the Watson formalism**, in which the Green's function contains effect of  $NN$  interaction.



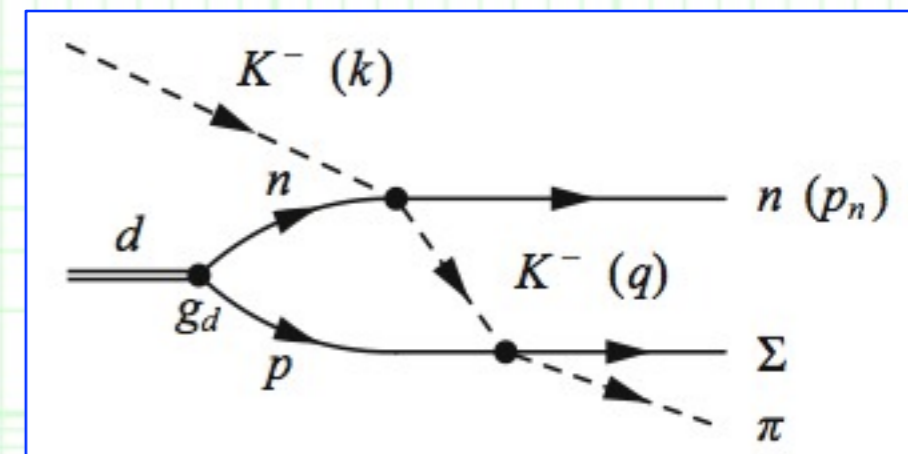
D. Jido, E. Oset and T.S. (2013).

- On the other hand, when we take **“truncated” Faddeev approach**, the energy of exchanged  $\eta^{(\prime)}$  meson is:

$$q^0 = M_d + E_\gamma^{\text{lab}} - p_p^0 - M_n - \frac{|\vec{q} + \vec{p}_p - \vec{k}|^2}{2M_n}$$

D. Jido, E. Oset and T.S. (2013).

- This contains less diagrams concerned with  $NN$  interaction, but we can calculate correct two-body threshold in loops.



--> How is **the dependence** with respect to the prescription ?