

# ***J-PARC hadron physics in 2016***

## **Open charm production in exclusive reactions at PANDA-FAIR and J-PARC energy region**

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The aim of our discussion is qualitative/quantitative estimation of open charm production in  $\bar{p}p$  reactions with one flavor exchange

$$\bar{p}p \rightarrow \bar{\Lambda}\Lambda(\Sigma) \quad \text{and} \quad \bar{p}p \rightarrow \bar{\Lambda}_c\Lambda_c(\Sigma_c)\dots$$

$$\bar{p}p \rightarrow \bar{K}K \quad \text{and} \quad \bar{p}p \rightarrow D\bar{D}\dots \quad (\text{PANDA})$$

$$\bar{p}p \rightarrow \bar{K}K^* \quad \text{and} \quad \bar{p}p \rightarrow D\bar{D}^*\dots$$

and reactions with two flavor exchange

$$\bar{p}p \rightarrow \Xi\Xi \quad \text{and} \quad \bar{p}p \rightarrow \Xi_c\Xi_c$$

open charm production in  $\pi p$  reactions

$$\pi^- p \rightarrow D^{*-}\Lambda_c \quad (\text{J-PARC})$$

also in  $pp$  reactions, like

$$pp \rightarrow \Lambda_c\bar{D}^0 p \quad \text{and} \quad pp \rightarrow \Lambda_c\bar{D}^0 X$$

mainly in forward production (large  $x$ )

# Charmed and strange hadrons

$c\bar{u}$  ( $D^0$ ) (1864) or ( $D^{*0}$ )(2007)  
 $c\bar{d}$  ( $D^+$ ) (1869) or ( $D^{*+}$ )(2010)  
 $c\bar{c}$  ( $J/\psi$ ) (3096)

$\rightarrow s\bar{u}$  ( $K^-$ ) (494) or ( $K^{*-}$ )  
 $\rightarrow s\bar{d}$  ( $\bar{K}^0$ ) (498) or ( $\bar{K}^{*0}$ )  
 $\rightarrow s\bar{s}$  ( $\phi$ ) (1020)

$\bar{c}u$  ( $\bar{D}^0$ ) (1864) or ( $\bar{D}^{*0}$ )  
 $\bar{c}d$  ( $D^-$ ) (1869) or ( $D^{*-}$ )

$\rightarrow \bar{s}u$  ( $K^+$ ) (494) or ( $\bar{K}^{*+}$ )  
 $\rightarrow \bar{s}d$  ( $K^0$ ) (498) or ( $K^{*0}$ )

$cuu$  ( $\Sigma_c^{++}$ ) (2452)

$\rightarrow suu$  ( $\Sigma^+$ )

$cud$  ( $\Lambda_c^+$ ) (2286) or ( $\Sigma_c^+$ ) (2451)

$\rightarrow sud$  ( $\Lambda$ ) or ( $\Sigma^0$ )

$cdd$  ( $\Sigma_c^0$ ) (2452)

$\rightarrow sdd$  ( $\Sigma^-$ )

$csu$  ( $\Xi_c^+$ ) (2467)

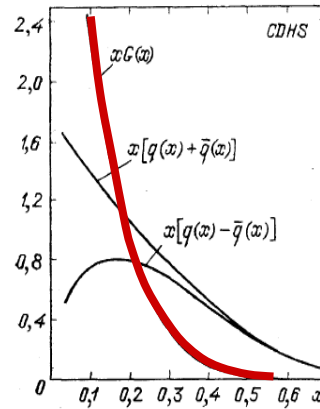
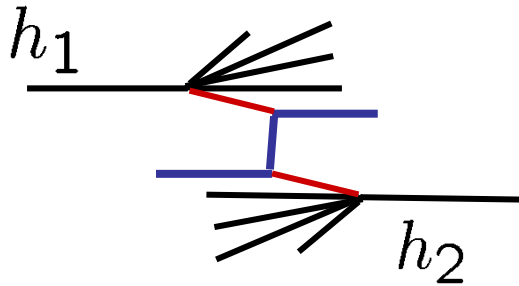
$\rightarrow ssu$  ( $\Xi^0$ ) (1315)

$csd$  ( $\Xi_c^0$ ) (2470)

$\rightarrow ssd$  ( $\Xi^-$ ) (1322)

# *Challenges of some utilized models*

# Open charm at high energy and pQCD models



$$d\sigma_{H_c} \sim xG(x)$$

$$xG(x)|_{x \rightarrow 1} \sim (1-x)^5$$

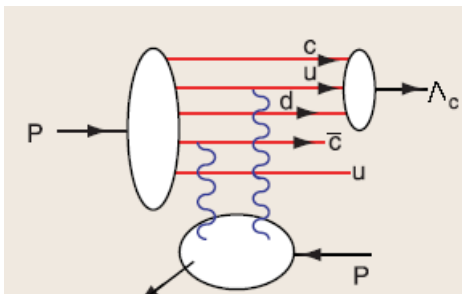
with  $x \simeq 1$

M. Basile *et al.*, Lett. Nuovo Cim. 30, 487 (1981)

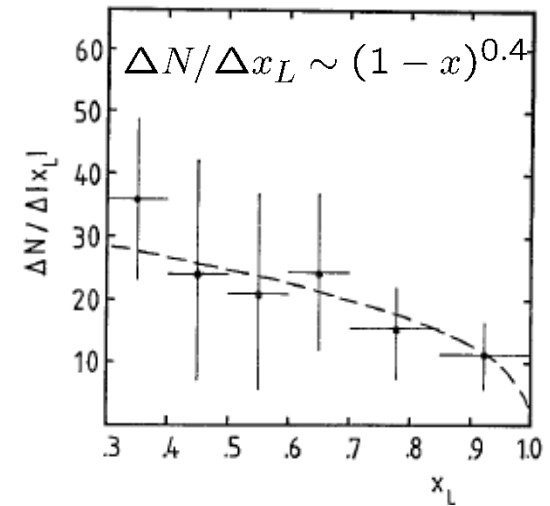
$$p + p \rightarrow \Lambda_c + X, \quad \sqrt{s} = 62 \text{ GeV}$$

“Intrinsic charm model”

Brodsky *et al*, PLB**93** (1980)



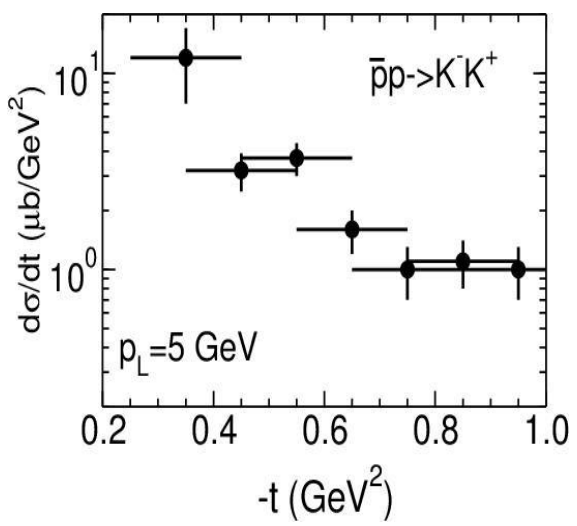
$\sim 1\% [c\bar{c}]$  in proton



# Effective Lagrangian Models

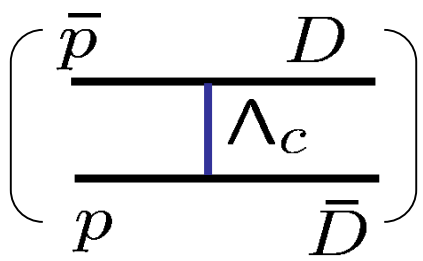
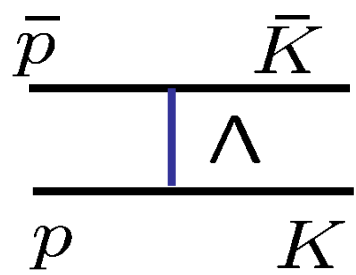
Heidenbauer, Krein et al., (1993-2015)  $\bar{p}p \rightarrow \bar{Y}Y$   
 $\vdots$   
 Shyam&Lenske,(2015)  $\bar{p}p \rightarrow \bar{M}M$   
 $\vdots$

Example:  $\bar{p}p \rightarrow K^-K^+$



A. Eide *et al.*, Nucl. Phys. **B60**,173 (1973)  
 (LEAR)

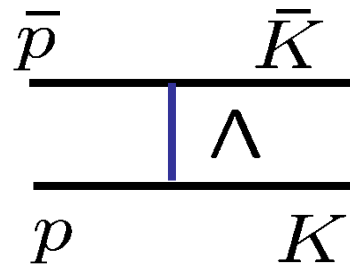
*Definite enhancement at forward production angles encourage for t-exchange channels*



$$\mathcal{L}_{NYK} = -i\bar{N} \gamma_5 Y K + \text{h.c.} ,$$

$$\mathcal{L}_{NYD} = -i\bar{N} \bar{D} \gamma_5 Y_c + \text{h.c.} ,$$

# Amplitude and cross sections



$$\mathcal{L}_{NYK} = -i g_{KNY} \bar{N} \gamma_5 Y K + \text{h.c.} ,$$

$$A_{m_i n_i}^{\bar{p} p \rightarrow \bar{K} K}(s, t) = \frac{\bar{v}_{n_i} (p_Y \cdot \gamma - M_Y) u_{m_i}}{t - M^2} g_{KNY}^2 f^2(t)$$

$f(t)$  – form factor

$$\frac{d\sigma}{dt} = \frac{1}{16\pi s(s - 4M_N^2)} \text{Tr}[AA^\dagger]; \quad \sigma_{\text{tot}} = \frac{1}{32\pi s} \frac{p_f}{p_i} \int_{-1}^1 d\cos\theta \text{Tr}[AA^\dagger]$$

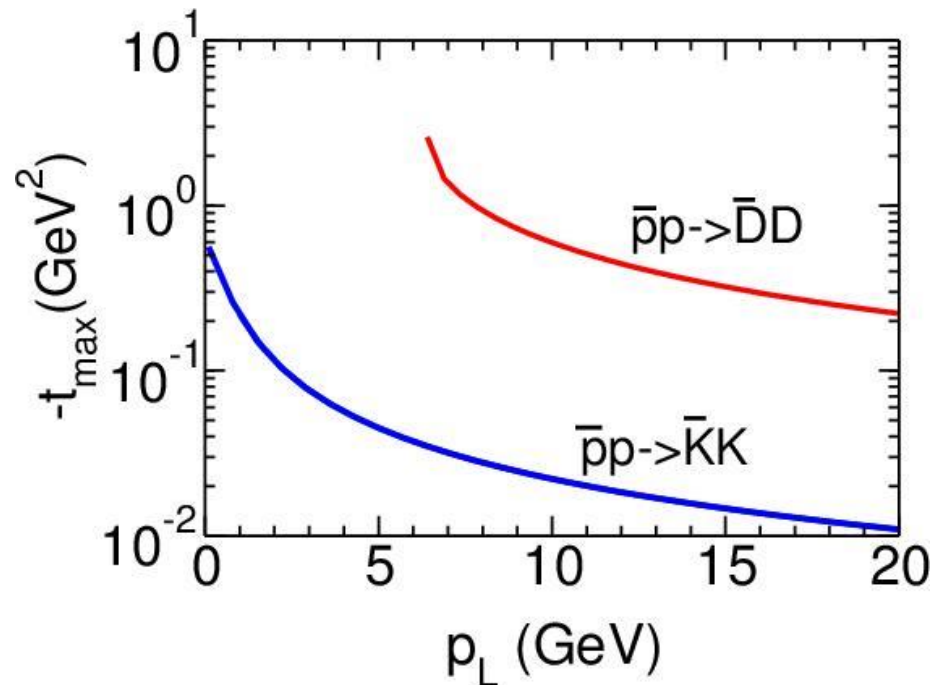
$$\text{Tr}[AA^\dagger] = \frac{g_{KNY}^4 f^4(t)}{(t - M_Y^2)^2} F^2(s, t)$$

$$F^2(s, t) = \frac{1}{2} \left( (s - 2M_N^2)(M_Y^2 - t) + 4M_N M_Y (M_N^2 + M_K^2 + t) - (M_N^2 - M_K^2 + t)^2 - M_N^2 (M_Y^2 + t) \right) ,$$

# Kinematics: momentum transfers

$$t = 2M_p^2 - 2E_p E_K + 2p_p p_K \cos \theta$$

$$-t_{\max} \equiv |-t|_{\max} = -2M_p^2 + 2E_p E_K - 2p_p p_K$$



$$\frac{d\sigma(\bar{D}D)}{dt} \ll \frac{d\sigma(\bar{K}K)}{dt}$$



$$\sigma_{\text{tot}} \propto \text{Tr}[AA^\dagger] = \frac{1}{s} \frac{g_{KNY}^4 f^4(t)}{(t - M_Y^2)^2} F^2(s, t)$$

$$F^2(s, t) = \frac{1}{2} \left( (s - 2M_N^2)(M_Y^2 - t) + 4M_N M_Y (M_N^2 + M_K^2 + t) - (M_N^2 - M_K^2 + t)^2 - M_N^2 (M_Y^2 + t) \right),$$

↙

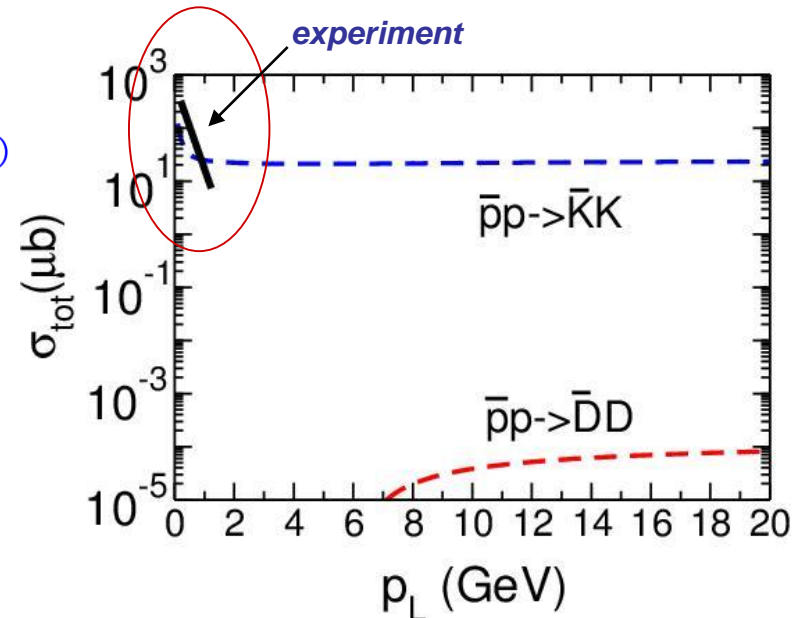
$$\sigma_{\text{tot}} \approx \text{Constant} \quad \text{at} \quad s \ll M_i^2, |t|$$

**experiment**

$$\sigma_{\text{tot}} \approx C \left( \frac{s}{s_0} \right)^{-\gamma} \quad \text{with} \quad \gamma \gg 1$$

$$\frac{\sigma_{\bar{D}D}}{\sigma_{\bar{K}K}} \leq 10^{-5}$$

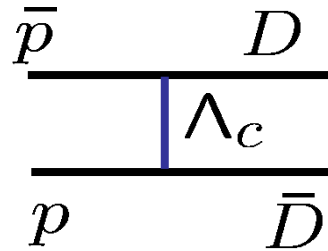
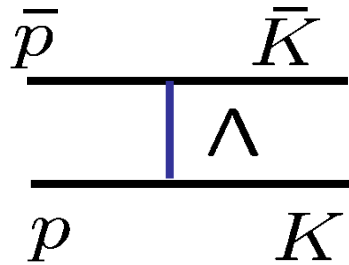
✧ **Limited region of application**



✧ **Wrong energy dependence**

Contrary to the hadron-exchange models, Regge approaches are work satisfactorily for strangeness production

*Similarity of  $\bar{p}p \rightarrow \bar{K}K$  and  $\bar{p}p \rightarrow D\bar{D}$  motivates for utilizing the Regge models for charm production*



*internal lines are associated with Regge trajectories*

$$T_{Regge} \sim \left(-\frac{s}{s_R}\right)^{\alpha_R(t) - \frac{1}{2}}$$

$$\alpha_R(t) \simeq \alpha_R(0) + \alpha'_R t \rightarrow \text{linear trajectories}$$

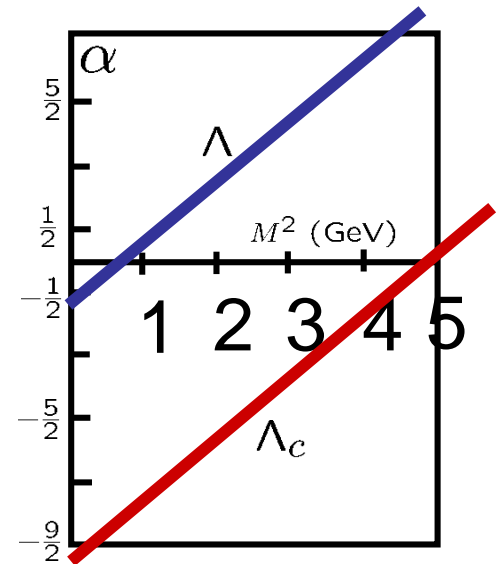
$$R = \Lambda_c, \Sigma_c, D^* \dots$$

*small yields of charm*

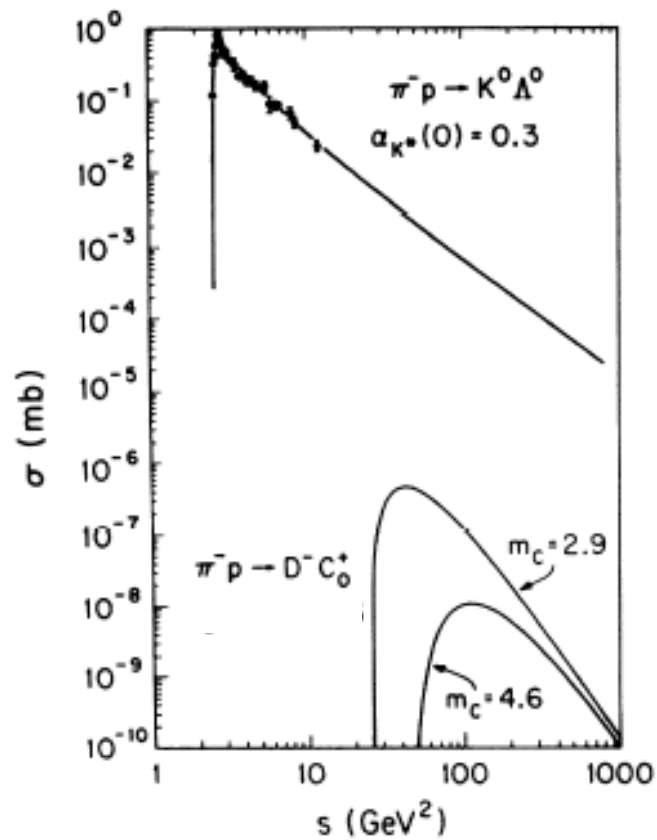
*Therefore, there are doubts:*

(1) trajectories  $\alpha(t)$  *non-linear?*

(2) what is a value of scale parameters  $s_R$



Chew-Frautschi plot



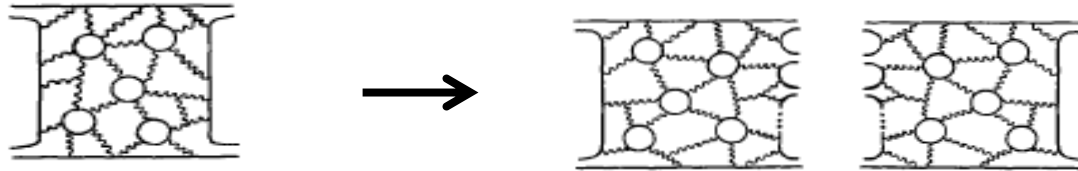
$$\frac{\text{charm}}{\text{strangeness}} < 10^{-6} \dots 10^{-7}$$

V. Barger, R. Phillips, PRD 12 (1975)

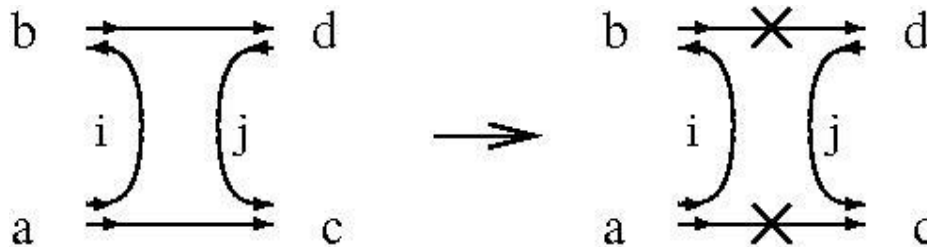
**Possible solution is an approach based on non-perturbative quark-gluon string model discussed for the first time by S.Nussinov, (PRL34(1975) and F.Low, PRD12 (1975))**  
**Essentially, they discussed formation and decay of a  $q\bar{q}$  color tube**



**with complicated intermediate (multi-particle) states**



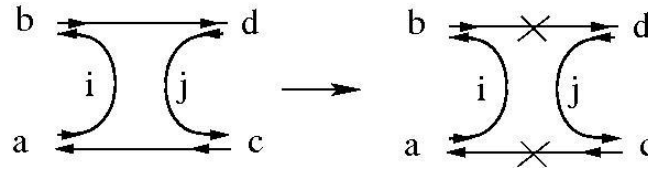
**The method of evaluation of observables based on utilizing the planar diagram for two body amplitude and it's cutting in s-channel**



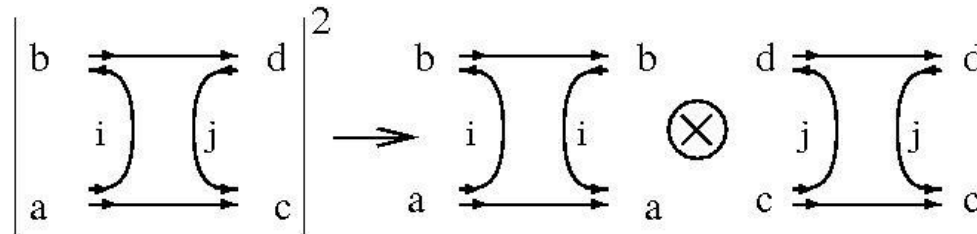
**was elaborated by Kaidalov (almost 10 years later) [Z.Phys. C 12 (1982)] and developed by Kaidalov et al. (in 1983-2005) and other groups: A.T., Kampfer(2008), A.Khojiamirian et al.(2012), G.Lykasov et al.(2010)... V. Grishina et al.(2005)(strangeness), Kim, Hosaka & et al., (2015)**

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**(In particularly for two-body exclusive processes!!)**



$$\text{Im}T_{ab \rightarrow cd} \sim \sum_X T_{ab \rightarrow X} \cdot T_{cd \rightarrow X}^\dagger$$



the use of optical theorem  $\longrightarrow$  factorization:

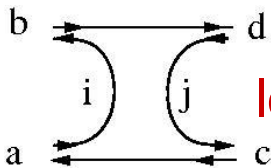
$$w_{ab \rightarrow cd}^2 \sim w_{ab \rightarrow ab} \times w_{cd \rightarrow cd}$$

$\swarrow$   
 $\searrow$

$\swarrow$   
 $\searrow$

probabilities of elastic scattering

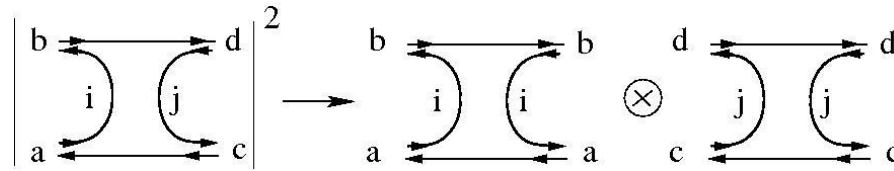
required  
diagram  
(amplitude)



looks like “Regge trajectory” with an effective “ij” Reggeon

## The main advantage of Kaidalov's approach based on

(i) factorization:



$$w_{ab \rightarrow cd}^2 \sim w_{ab \rightarrow ab} \times w_{cd \rightarrow cd}$$

(ii) Regge type of the individual and the “required amplitude”:

$$A_{ij} \sim \Gamma(1 - \alpha_{ij}(t)) \left( -\frac{s}{s_{ij}} \right)^{\alpha_{ij}(t)-1}$$

is a derivation of the consistent equations for  $\alpha_{ij}(t)$  and  $s_{ij}$ :

A.Kaidalov,  
Z.Phys.C12,  
62 (1982)

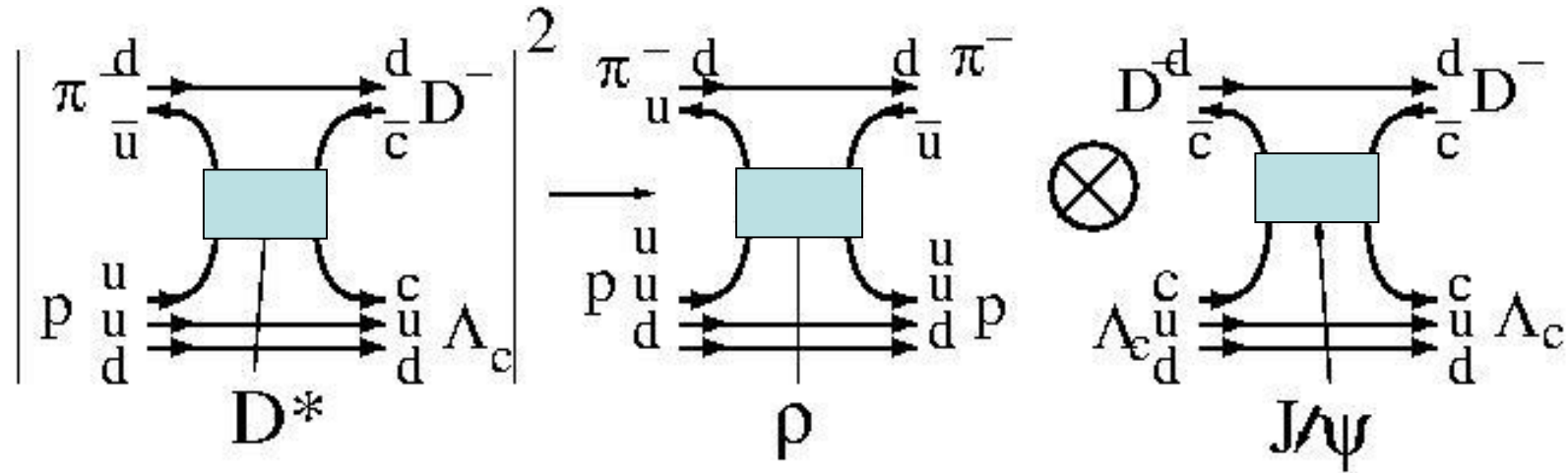
$$(1) \quad 2\alpha_{ij}^-(0) = \alpha_{ii}^-(0) + \alpha_{jj}^-(0) ,$$

$$(2) \quad 2/\alpha'_{ij} = 1/\alpha'_{ii} + 1/\alpha'_{jj} , \quad \text{and}$$

$$(3) \quad (s_{ab:cd})^{2(\alpha_{ij}-1)} = (s_{ab})^{\alpha_{ii}(0)-1} \times (s_{cd})^{\alpha_{jj}(0)-1} .$$

$$s_{ab} = \left( \sum_i^{n_a} M_{i\perp} \right) \left( \sum_j^{n_b} M_{j\perp} \right) \quad \text{with} \quad \begin{array}{l} M_{u,d\perp} \simeq 0.5 \text{ GeV}, \quad M_{s\perp} \simeq 0.6 \text{ GeV}, \\ M_{c\perp} \simeq 1.6 \text{ GeV} \end{array}$$

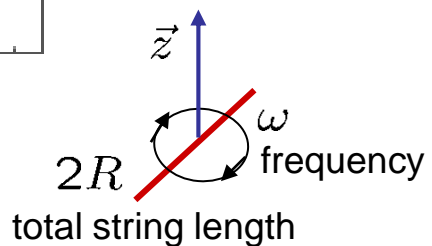
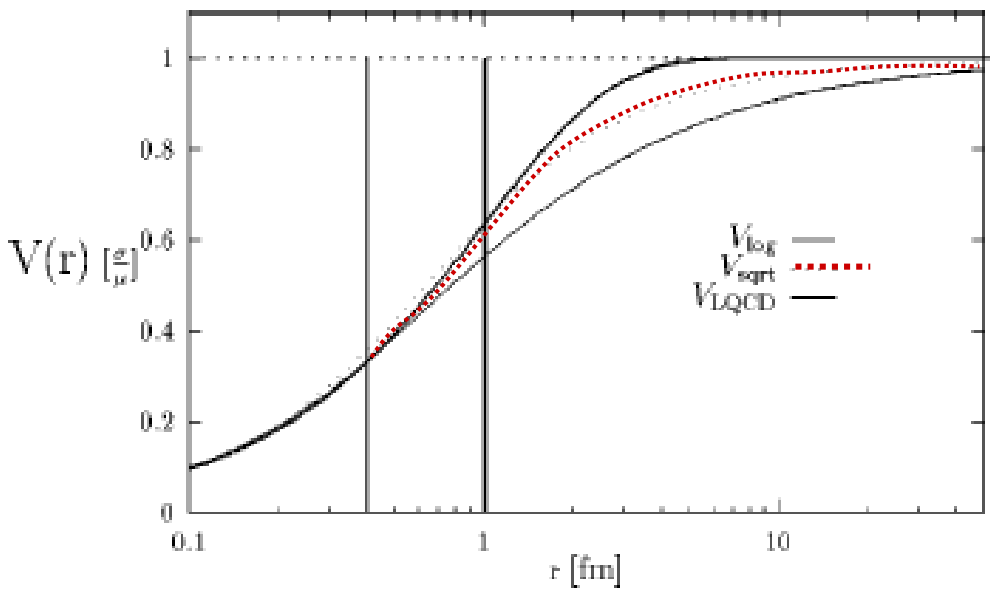
Example:  $\pi^- p \rightarrow D^- \Lambda_c$



$$w_{\pi p \rightarrow D^- \Lambda_c}^2 \sim w_{\pi^- p \rightarrow \pi^- p} \times w_{D^- \Lambda_c \rightarrow D^- \Lambda_c}$$

$[\rho (q\bar{q})$  trajectory  $J/\psi (c\bar{c})$  trajectory]

**Non-linear trajectory reflects behavior of QCD motivated  $\bar{q}q$  potential  $V(\rho)$**



string tension  $\sigma(\rho) = \frac{dV(\rho)}{d\rho}$

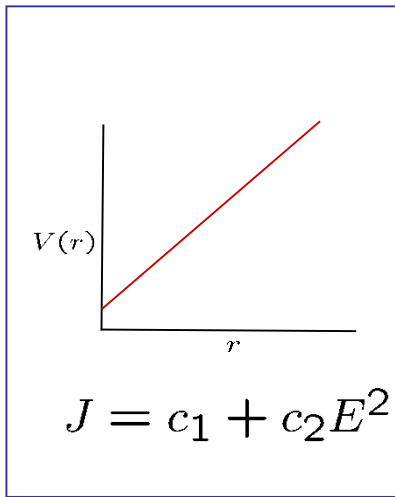
$$E = 2 \int_0^R \frac{d\rho \sigma(\rho)}{\sqrt{1-(\rho\omega)^2}};$$

string energy

$$J = 2 \int_0^R \frac{d\rho \sigma(\rho) \rho^2 \omega}{\sqrt{1-(\rho\omega)^2}},$$

string spin momentum

$$V(\rho) = \frac{a}{\pi\mu} \arctan(\pi\mu\rho) \longrightarrow J = \frac{1}{\pi\mu} (a/\sigma) - \sqrt{(a/\sigma)^2 - E^2}$$





# Non-linear Regge trajectories for diagonal channels in a square root form

Brisudova, Burakovsky, and Goldman PRD **61**, (2000).

$$\alpha(t) = \alpha(0) + \gamma(\sqrt{T} - \sqrt{T-t})$$

with  $T \gg 1\text{GeV}^2$

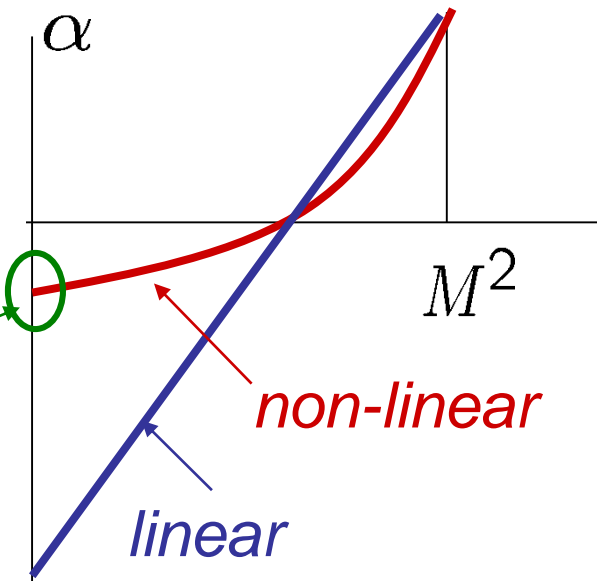
In the diffractive region with  $-t \ll T$ ,

$$\alpha(t) \simeq \alpha(0) + \frac{\gamma t}{2\sqrt{T}} \simeq \alpha(0) + \alpha' t$$

$$\alpha' = \gamma/2\sqrt{T}$$

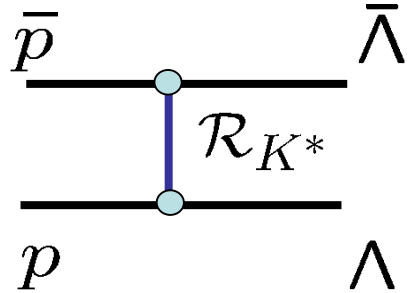
where  $\gamma = 3.65 \text{ GeV}^{-1}$   $\longleftrightarrow$  from  $\alpha_\rho(t)$   
**universal value**

$\alpha_\rho, M_{K^*}, M_{K_3^*}, M_{J/\psi}, M_{D^*}$   
are taken as input



$$\begin{aligned}
\alpha_\rho(0) &= 0.55, & \sqrt{T_\rho} &= 2.46 \text{ GeV}, & \alpha'_\rho &\simeq 0.742 \text{ GeV}^{-2}, \\
\alpha_{K^*}(0) &= 0.414, & \sqrt{T_{K^*}} &= 2.58 \text{ GeV}, & \alpha'_{K^*} &\simeq 0.71 \text{ GeV}^{-2}, \\
\alpha_\phi(0) &= 0.28, & \sqrt{T_\phi} &\simeq 2.70 \text{ GeV}, & \alpha'_\phi &\simeq 0.676 \text{ GeV}^{-2}, \\
\alpha_{D^*}(0) &= -1.02, & \sqrt{T_{D^*}} &= 3.91 \text{ GeV}, & \alpha'_{D^*} &\simeq 0.467 \text{ GeV}^{-2}, \\
\alpha_{J/\psi}(0) &= -2.60, & \sqrt{T_{J/\psi}} &\simeq 5.36 \text{ GeV}, & \alpha'_{J/\psi} &\simeq 0.34 \text{ GeV}^{-2}, \\
s_{\bar{p}p:\bar{\Lambda}_c\Lambda_c} &\simeq 5.98 \text{ GeV}^2. \\
\alpha_{dc}(0) &\simeq -2.09, & \alpha'_{dc} &\simeq 0.557 \text{ GeV}^{-2}, \\
s_{\bar{p}p:D\bar{D}} &\simeq 3.59 \text{ GeV}^2.
\end{aligned}$$

**Reaction**  $\bar{p}p \rightarrow \bar{Y}Y, Y = \Lambda, \Sigma, \Lambda_c, \Sigma_c \dots$



$$\Gamma_{\mu}^{(p)} = \bar{u}_{\Lambda} \left( (1 + \kappa_{K^* N \Lambda}) \gamma_{\mu} - \kappa_{K^* N \Lambda} \frac{(p_p + p_{\Lambda})_{\mu}}{M_N + M_{\Lambda}} \right) u_p,$$

$$\Gamma_{\mu}^{(\bar{p})} = \bar{v}_{\bar{p}} \left( (1 + \kappa_{K^* N \Lambda}) \gamma_{\mu} + \kappa_{K^* N \Lambda} \frac{(p_{\bar{p}} + p_{\bar{\Lambda}})_{\mu}}{M_N + M_{\Lambda}} \right) v_{\bar{\Lambda}}.$$

$$T_{m_f n_f; m_i, n_i}^{\bar{p}p \rightarrow \bar{\Lambda} \Lambda} = C(t) \frac{s g_{K^* N \Lambda}^2}{s_0} \Gamma(1 - \alpha_{\bar{s}q}(t)) \left( -\frac{s}{s_{\bar{p}p: \bar{\Lambda} \Lambda}} \right)^{\alpha_{\bar{s}q}(t)-1} \mathcal{M}_{m_f n_f; m_i, n_i}^{\bar{p}p \rightarrow \bar{\Lambda} \Lambda}(s, t)$$

$$\mathcal{M}_{m_f n_f; m_i, n_i}^{\bar{p}p \rightarrow \bar{\Lambda} \Lambda}(s, t) = \mathcal{N}(s, t) \Gamma_{m_f m_i}^{(p) \mu} \Gamma_{n_f n_i}^{(\bar{p}) \nu} \left( -g_{\mu\nu} + \frac{q_{\mu} q_{\nu}}{q^2} \right)$$

$$\mathcal{N}^2(s, t) = \frac{1}{F^2(s, t)},$$

$$F^2(s, t) = \text{Tr} \left( \Gamma^{(p) \mu} \Gamma^{(p) \mu' \dagger} \right) \text{Tr} \left( \Gamma^{(\bar{p}) \nu} \Gamma^{(\bar{p}) \nu' \dagger} \right) \left( g_{\mu\nu} - \frac{q_{\mu} q_{\nu}}{q^2} \right) \left( g_{\mu' \nu'} - \frac{q_{\mu'} q_{\nu'}}{q^2} \right)$$

$C(t)$

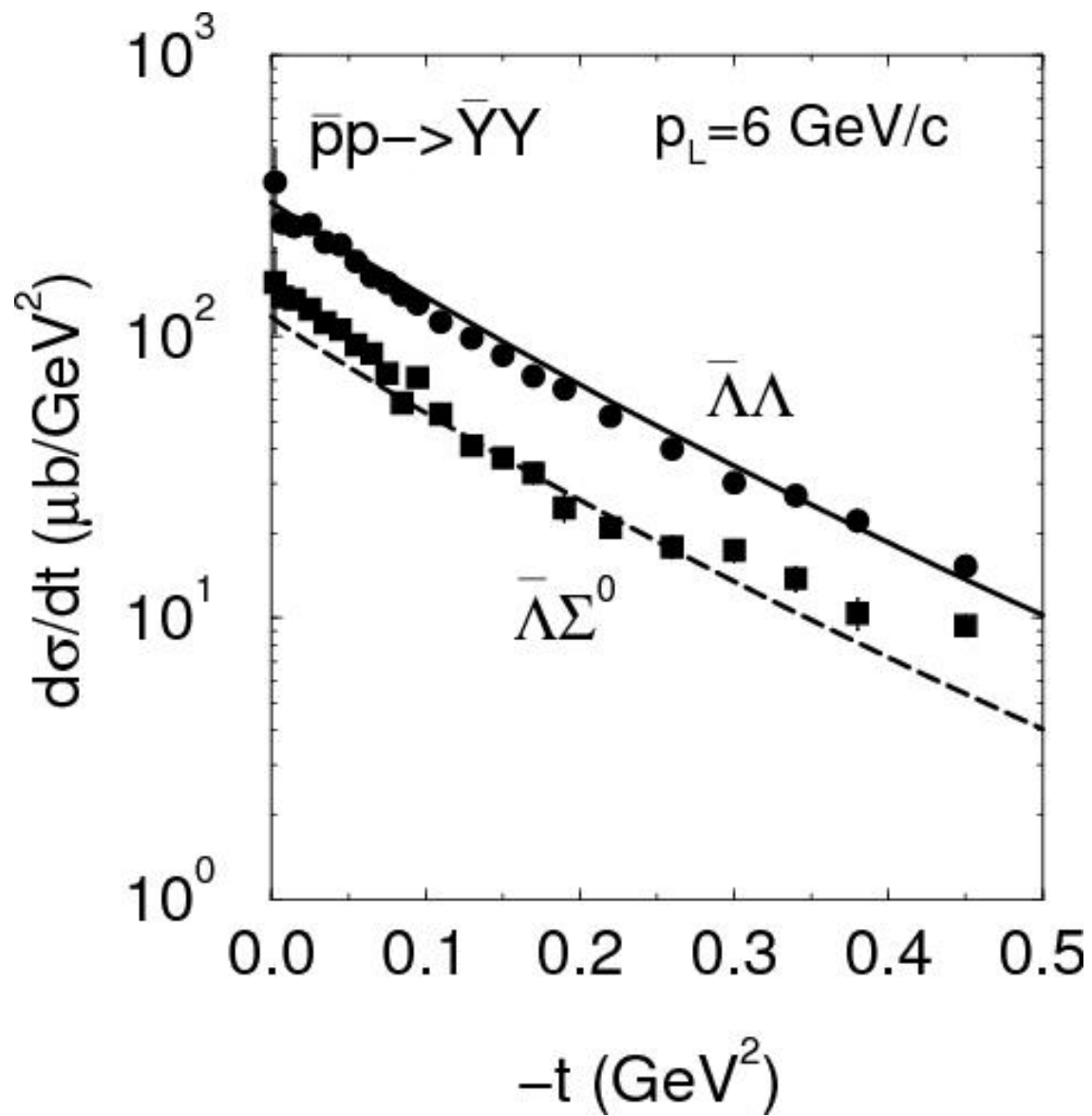
**unknown residual  
function**

$g_{KNY}, g_{K^*NY}, \kappa_{K^*NY}$  - **from hyper-nucleon physics** (Nijmegen potential)

$$\text{SU}(4) \longrightarrow g_{DNY_c}(g_{D^*NY_c}) = g_{KNY}(g_{K^*NY})$$

**Stoks & Rijken** PRC, **59**, 3009 ('99)

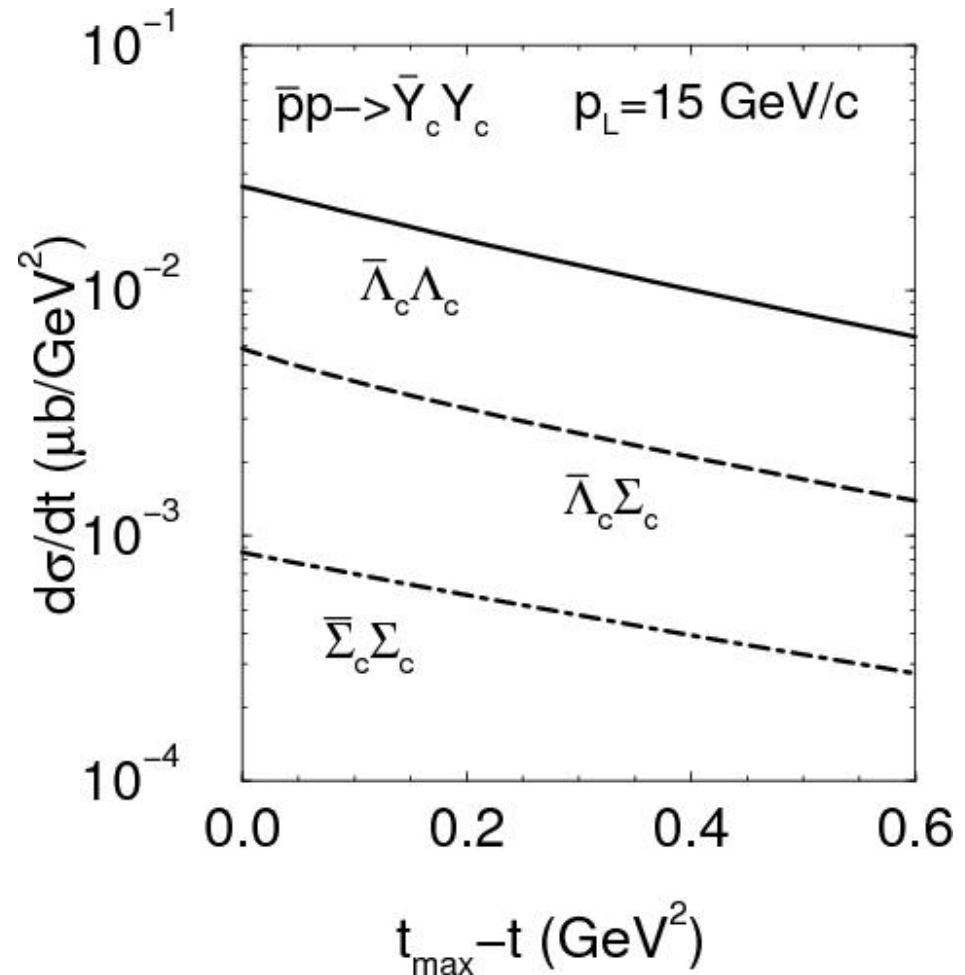
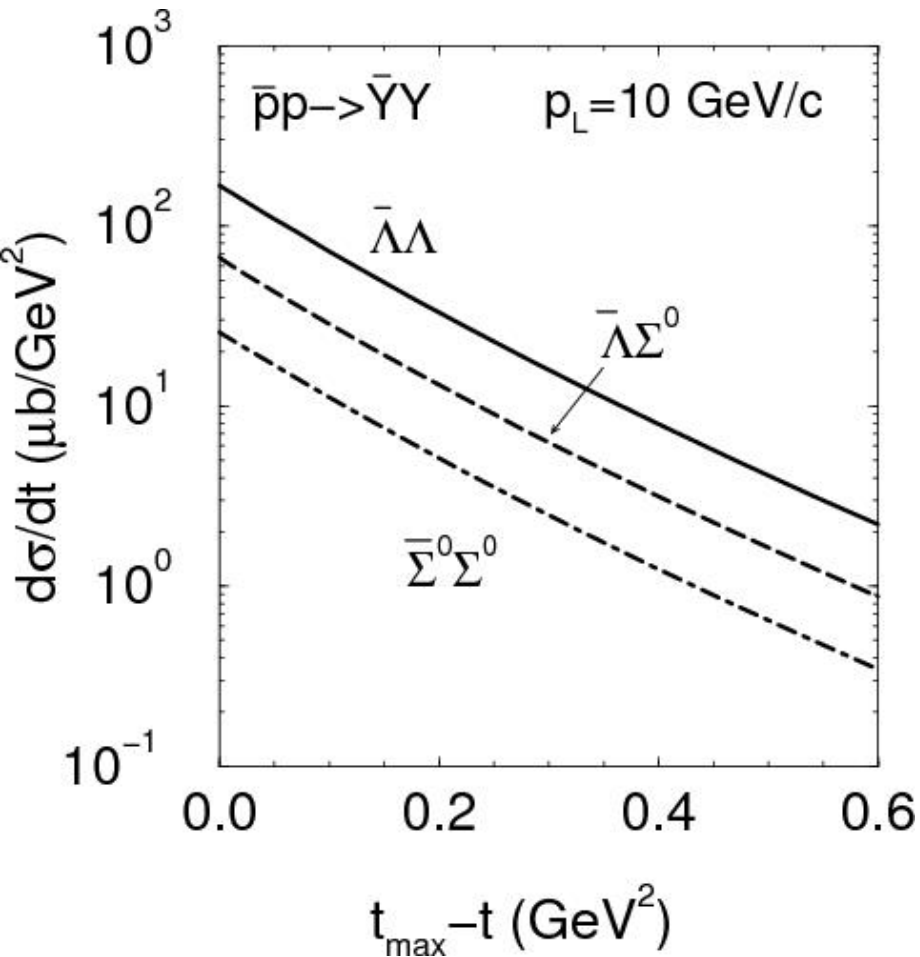
**important note: for unpolarized case**  $\sum_{\text{spins}} \mathcal{M} \mathcal{M}^{\dagger} = 1$



$$C(t) = \frac{0.54}{(1 - t/1.15)^2}$$

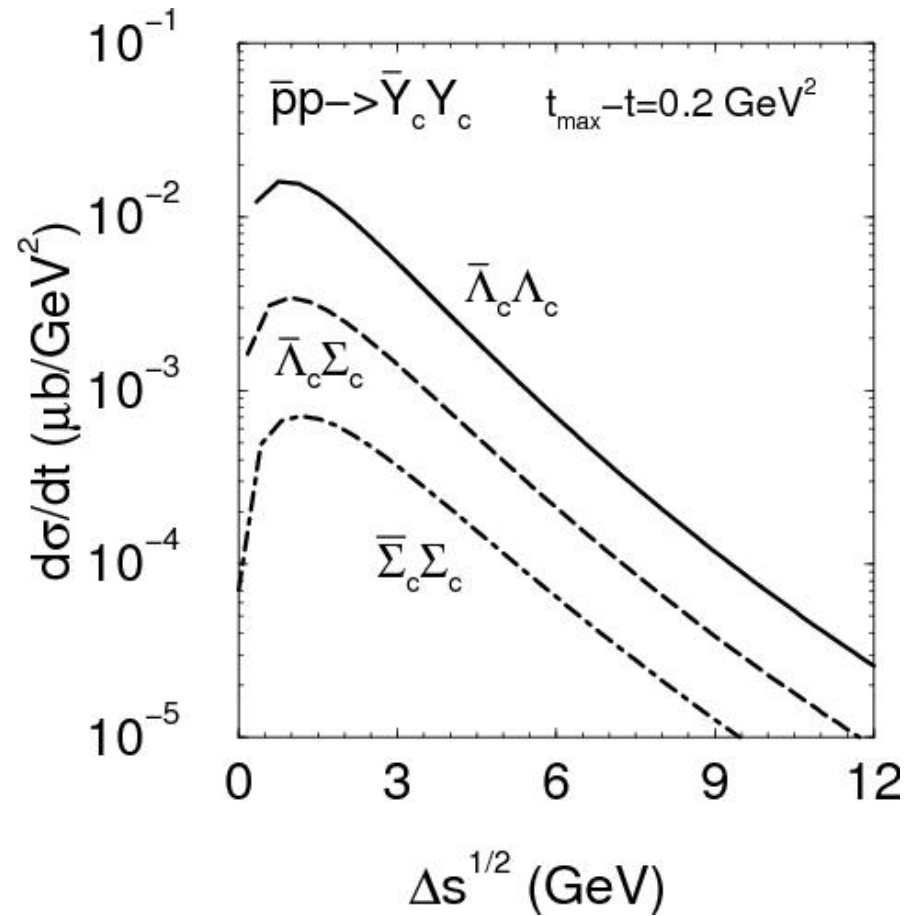
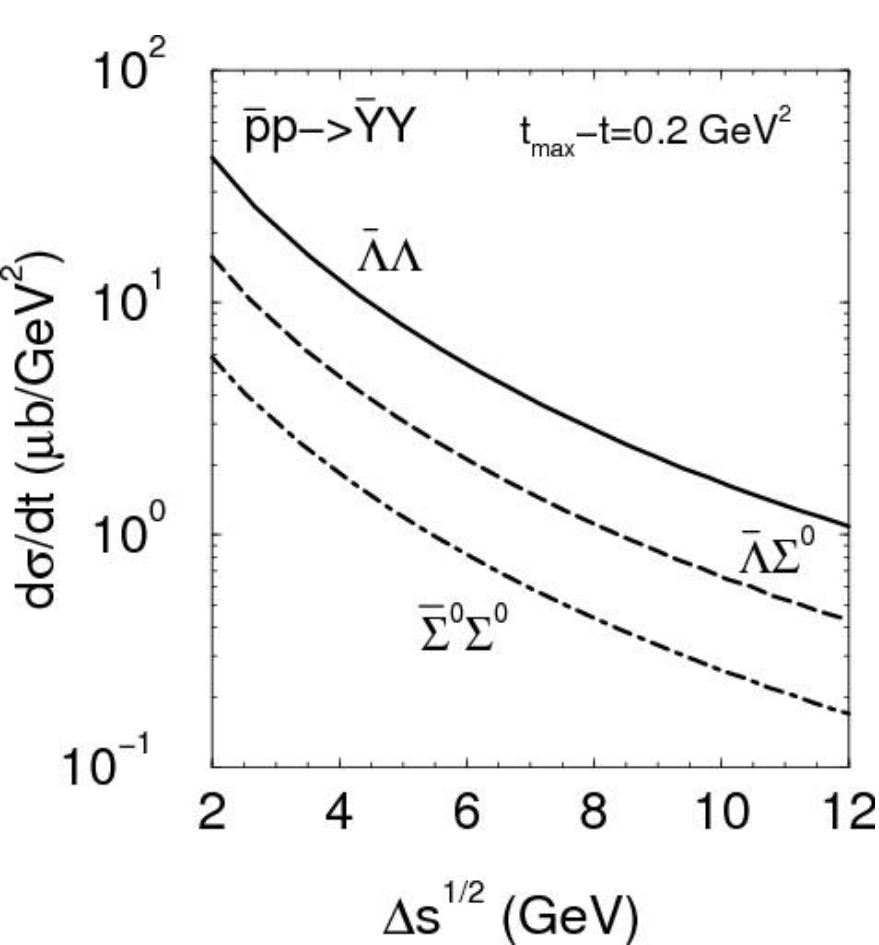
# Reactions $\bar{p}p \rightarrow \bar{Y}Y$ , $Y = \Lambda, \Sigma^0$ ( $\Lambda_c, \Sigma_c^0$ )

*t* - dependence



# Reactions $\bar{p}p \rightarrow \bar{Y}Y$ , $Y = \Lambda, \Sigma^0$ ( $\Lambda_c, \Sigma_c^0$ )

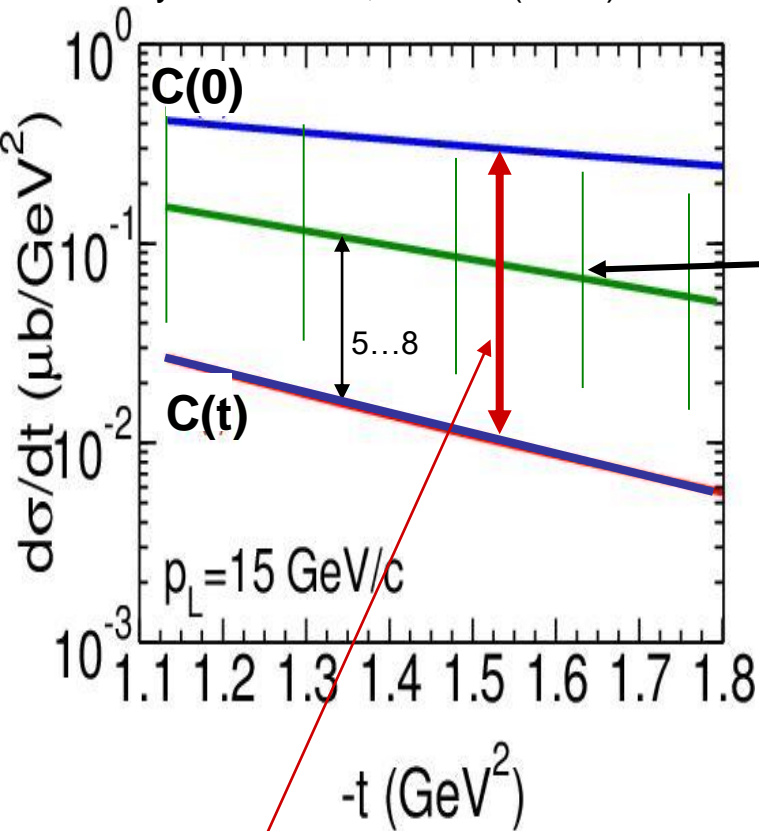
*energy dependence*



# Comparison of two realization of QGSM for $\bar{p}p \rightarrow \bar{\Lambda}_c \Lambda_c$

A.T., B. Kämpfer

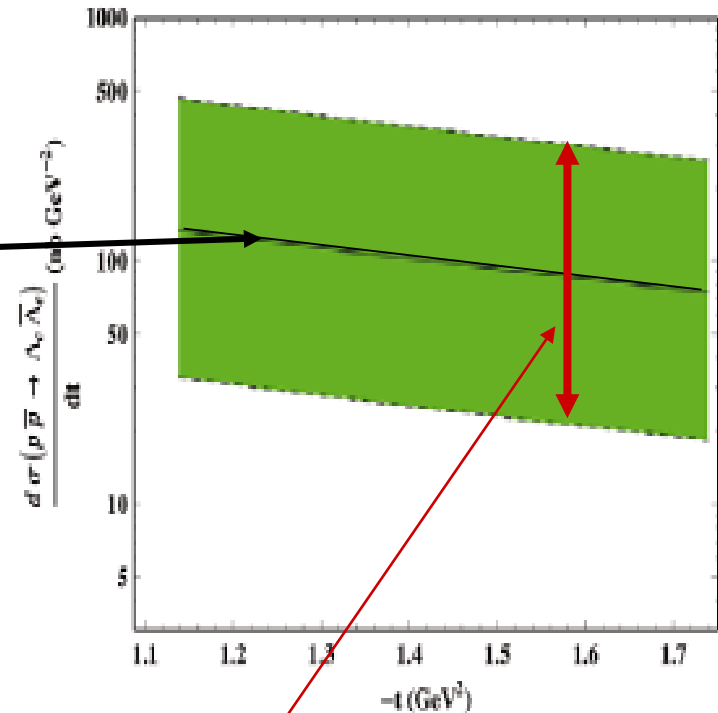
Phys. Rev. C78,025291 (2008)



*the uncertainties caused  
by the residual function  $C(t)$*

A.Khodjamirian, C. Klein, T.Mannel and Y.-M. Wang

Eur.Phys.J.A.48,31(2012)



*the uncertainties caused  
by LCSR of strong couplings*

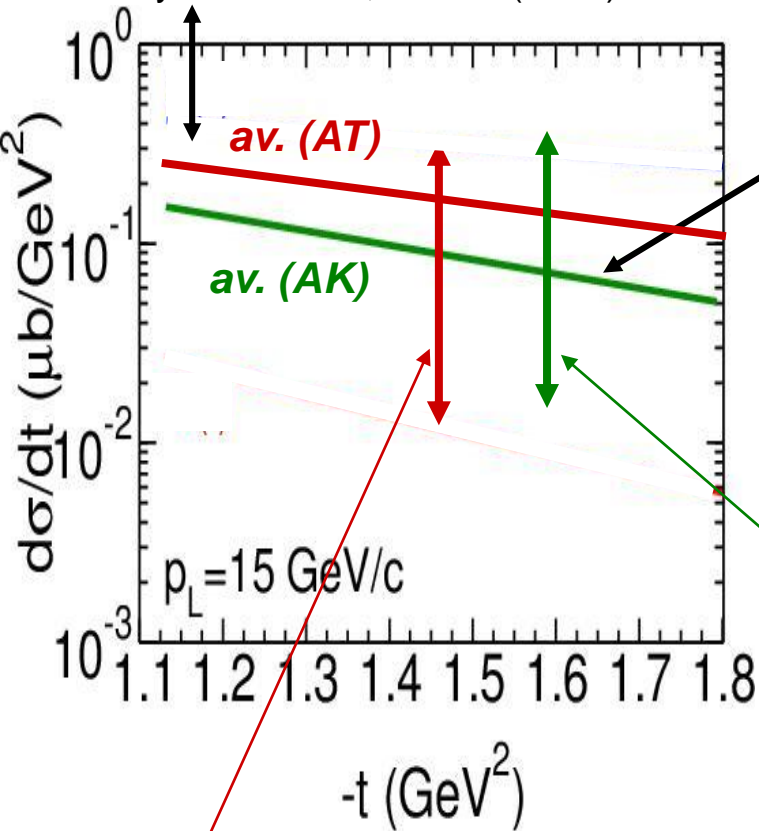
# Comparison of two realization of QGSM (average values)

A.T., B. Kämpfer

A.Khodjamirian,C. Klein, T.Mannaal and Y.-M. Wang

Phys. Rev. C78,025291 (2008)

Eur.Phys.J.A.48,31(2012)



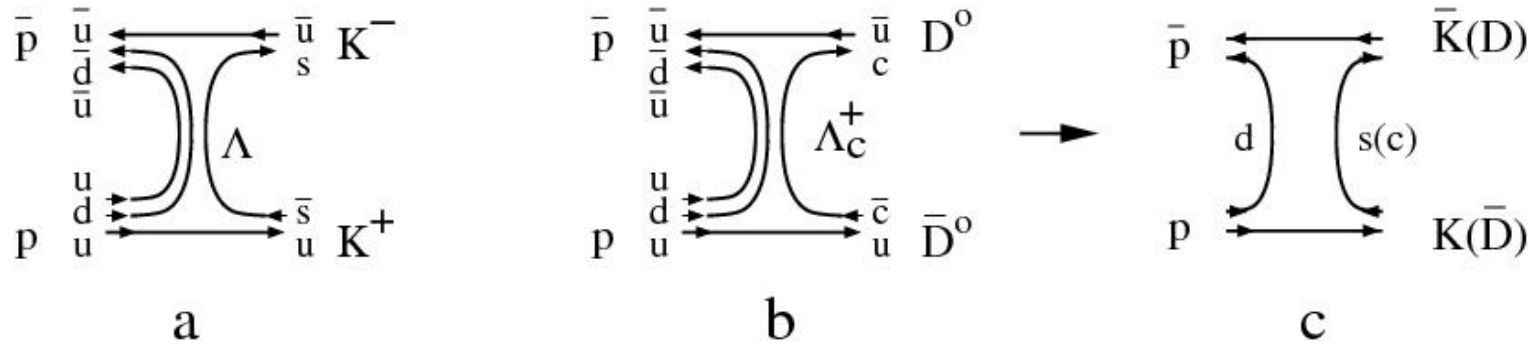
*the uncertainties caused  
by LCSR of strong couplings*

*the uncertainties caused  
by the residual function  $C(t)$*

**for the average values both predictions are consistent with each other  
within a factor of 2**



# Reaction $\bar{p}p \rightarrow \bar{K}K (D\bar{D})$



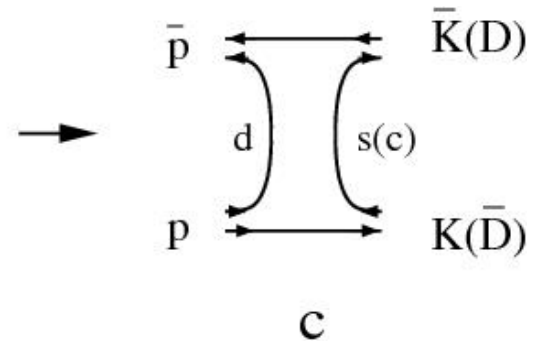
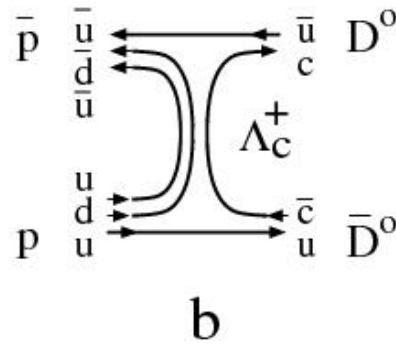
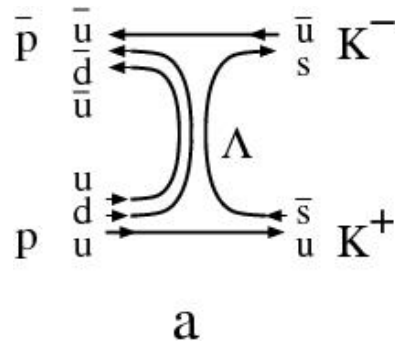
$$T_{m_i, n_i}^{\bar{p}p \rightarrow \bar{K}K} = C'(t) \frac{g_{KN\Lambda}^2 M_Y \sqrt{s}}{s_0} \Gamma\left(\frac{1}{2} - \alpha_{\bar{s}q}(t)\right) \left(-\frac{s}{s_{\bar{p}p:\bar{\Lambda}\Lambda}}\right)^{\alpha_{\bar{s}q}(t) - \frac{1}{2}} \otimes \mathcal{M}_{m_i; n_i}^{\bar{p}p \rightarrow \bar{K}K}(s, t)$$

$$\mathcal{M}_{m_i n_i}^{\bar{p}p \rightarrow \bar{K}K}(s, t) = \mathcal{N}(s, t) [\bar{v}_{n_i} (\not{p}_Y - M_Y) u_{m_i}] ,$$

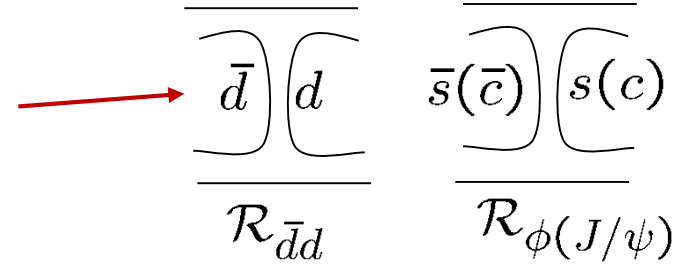
$$\mathcal{N}^2(s, t) = \frac{1}{F^2(s, t)},$$

$$F^2(s, t) = \frac{1}{2} \left( (s - 2M_N^2)(M_Y^2 - t) + 4M_N M_Y (M_N^2 + M_K^2 + t) - (M_N^2 - M_K^2 + t)^2 - 2M_N^2 (M_Y^2 + t) \right)$$

# Reaction $\bar{p}p \rightarrow \bar{K}K (D\bar{D})$



*d-diquark*



## How to evaluate the di-quark trajectory?

$$2\alpha_{sd}(0) = \alpha_{\bar{s}s}(0) + \alpha_{\bar{d}d}(0) ,$$

$$2/\alpha'_{sd} = 1/\alpha'_{\bar{s}s} + 1/\alpha'_{\bar{d}d}$$

$$\alpha_{sd}(t) \equiv \alpha_{\Lambda}(t) = -0.65 + 0.94 t$$

is taken as input [cf. K.Storror Phys. Rep. 103,135(1984)]

then

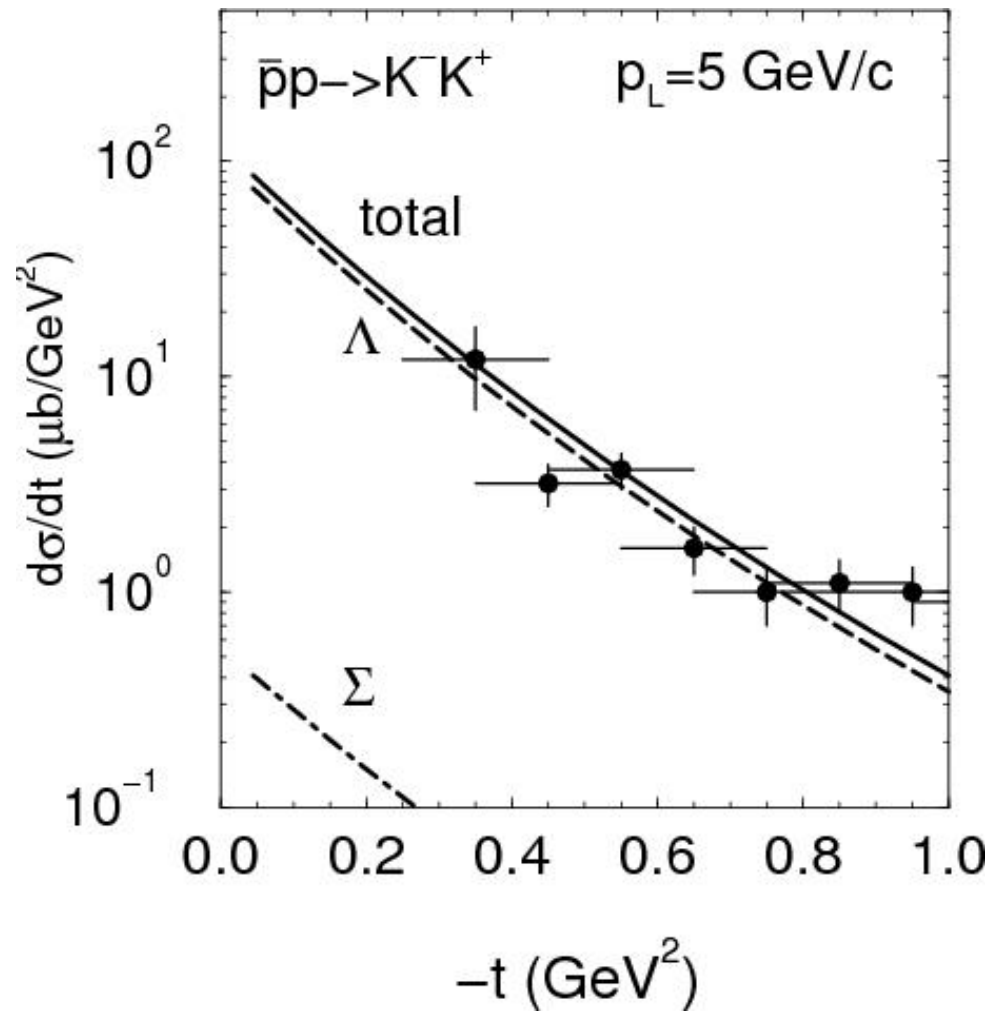
$$\alpha_{dd}(t) = -1.58 + 1.542 t$$

and allows to identify trajectory of  $\Lambda_c$

$$2\alpha_{dc}(0) = \alpha_{\bar{d}d}(0) + \alpha_{\bar{c}c}(0) ,$$

$$2/\alpha'_{dc} = 1/\alpha'_{\bar{d}d} + 1/\alpha'_{\bar{c}c}$$

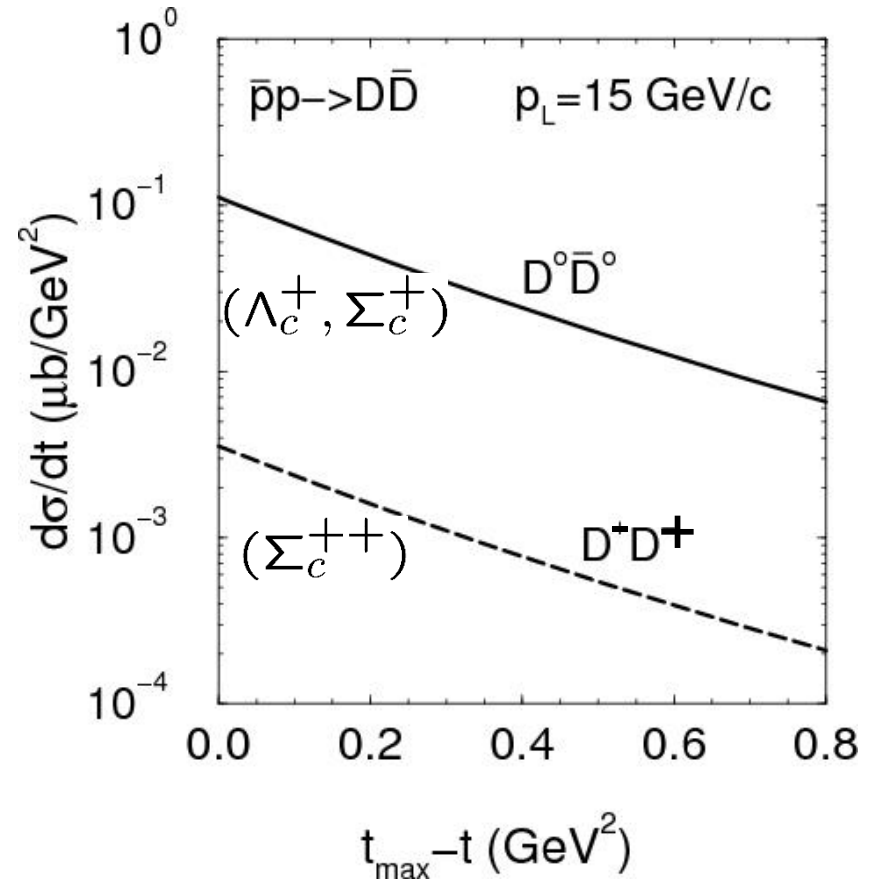
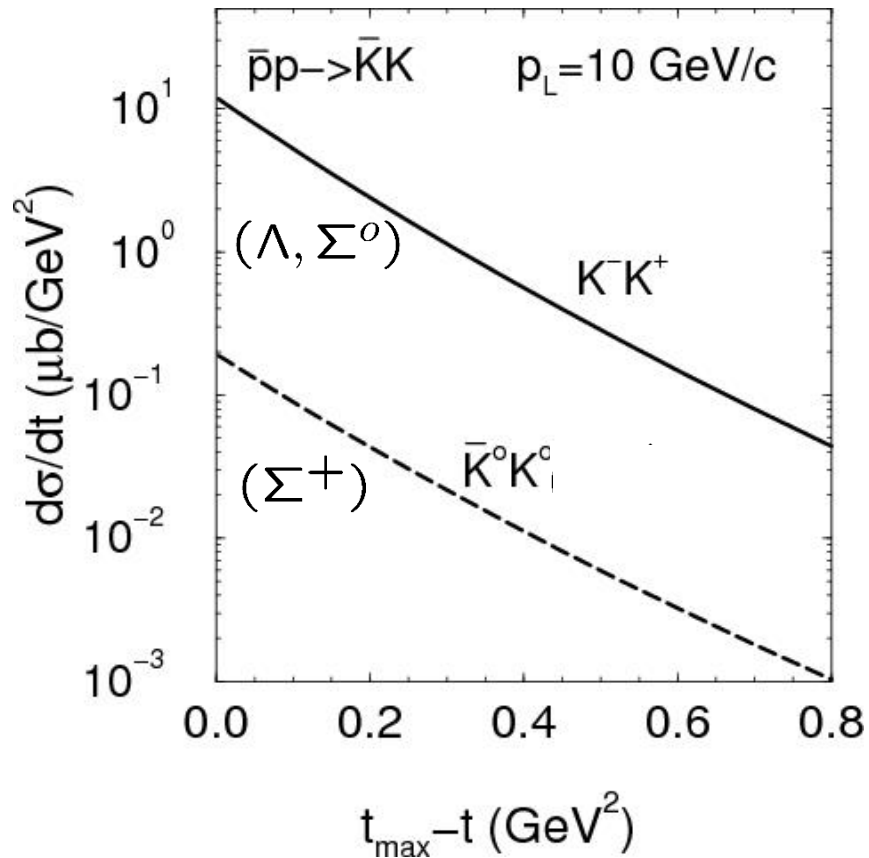
$$\alpha_{dc}(t) \equiv \alpha_{\Lambda_c}(t) = -2.09 + 0.557 t$$



$$C'(t) = \frac{0.38}{(1-t/1.15)^2}$$

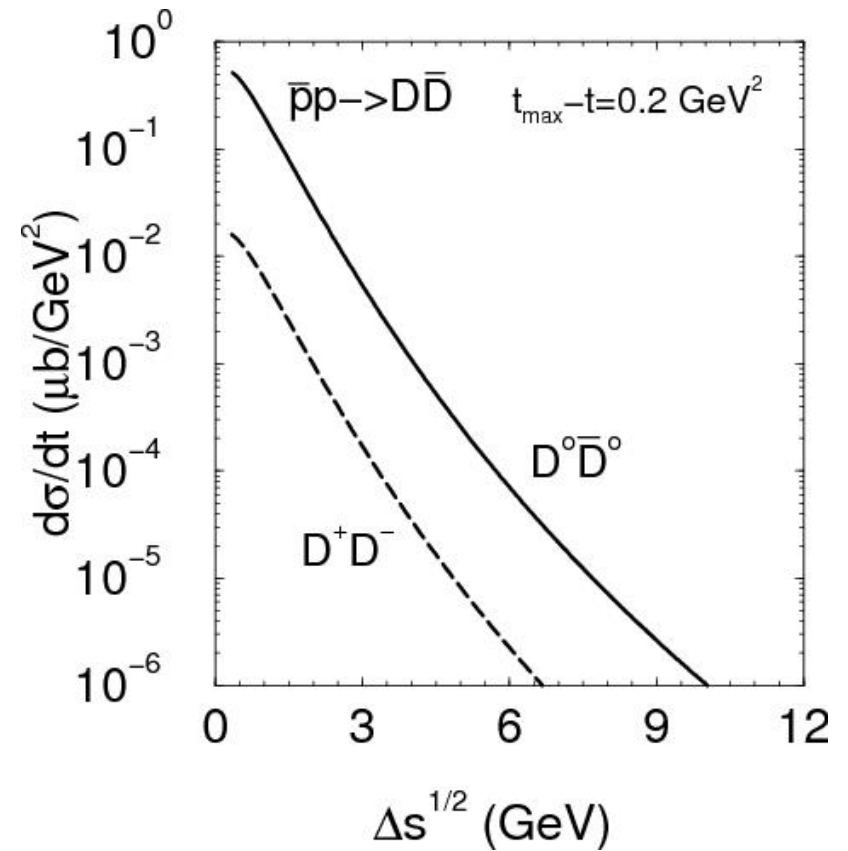
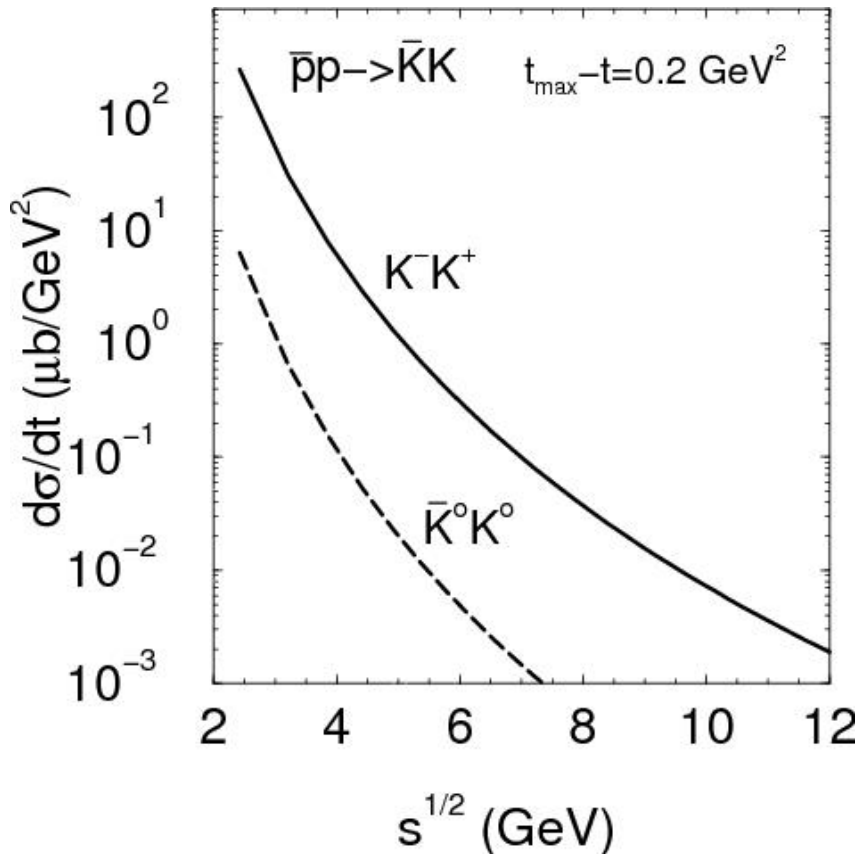
# Reactions $\bar{p}p \rightarrow \bar{K}K (D\bar{D})$

*t*-dependence



# Reactions $\bar{p}p \rightarrow \bar{K}K (D\bar{D})$

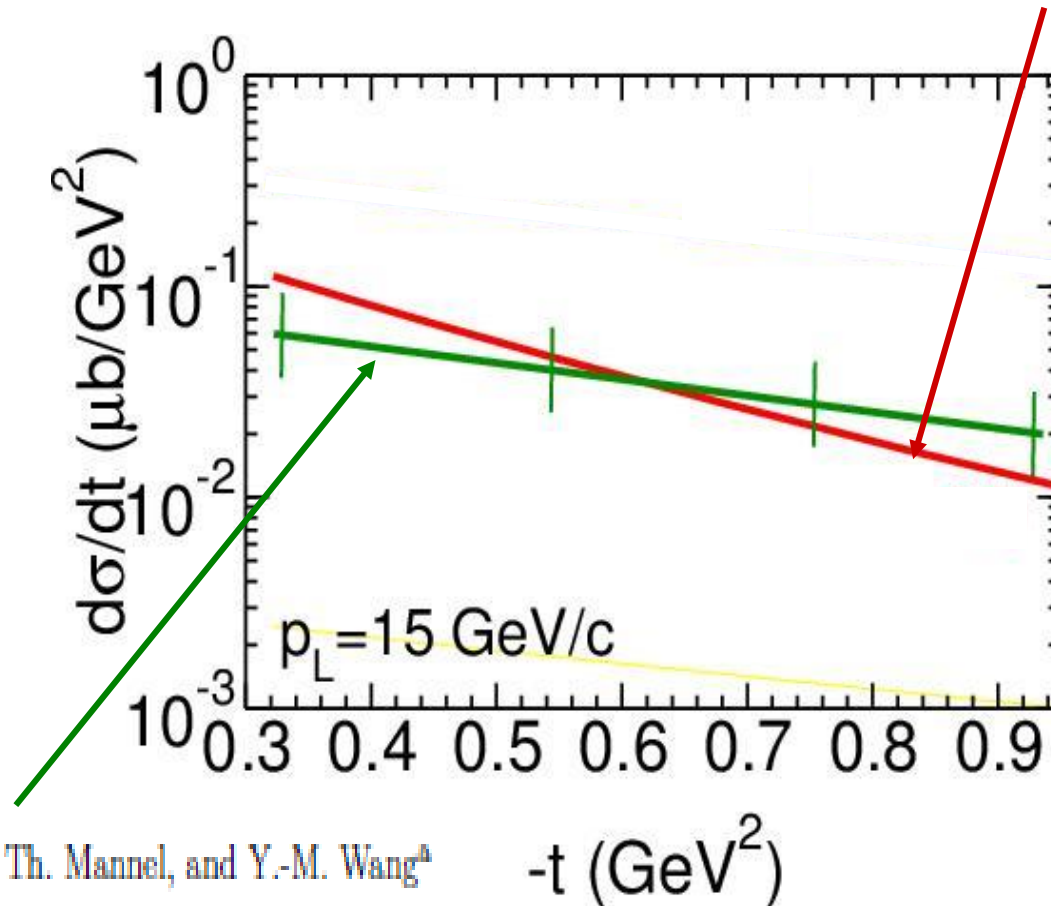
*s-dependence*



# Comparison of two realization of QGSM for $\bar{p}p \rightarrow D\bar{D}$

A.T., B. Kämpfer

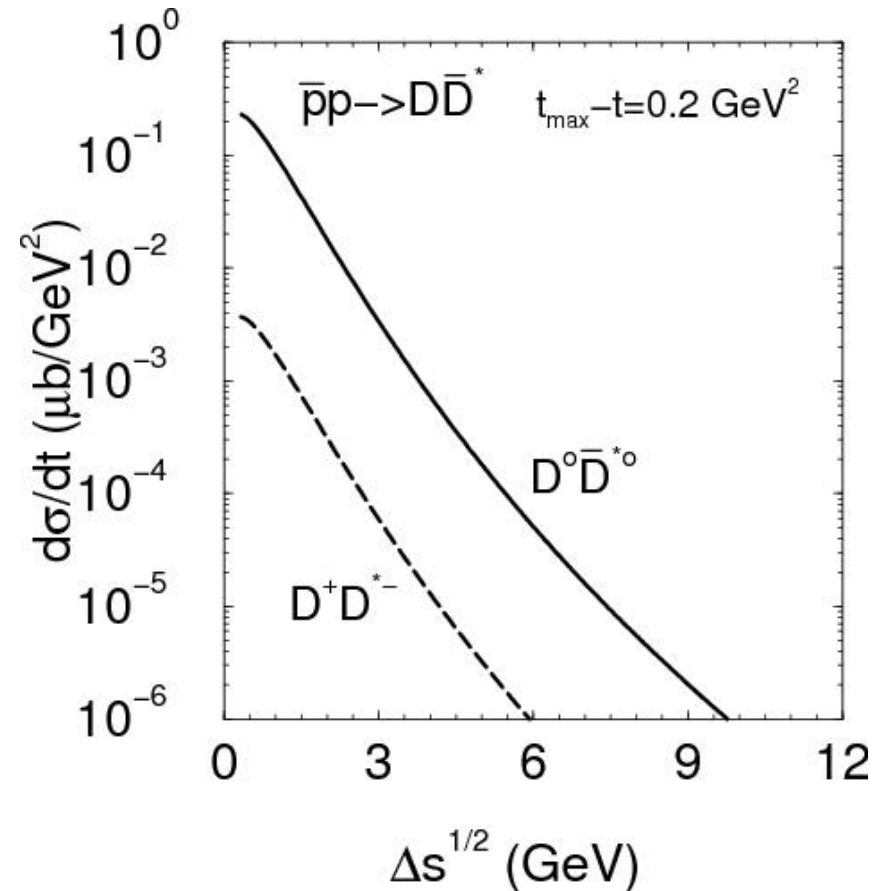
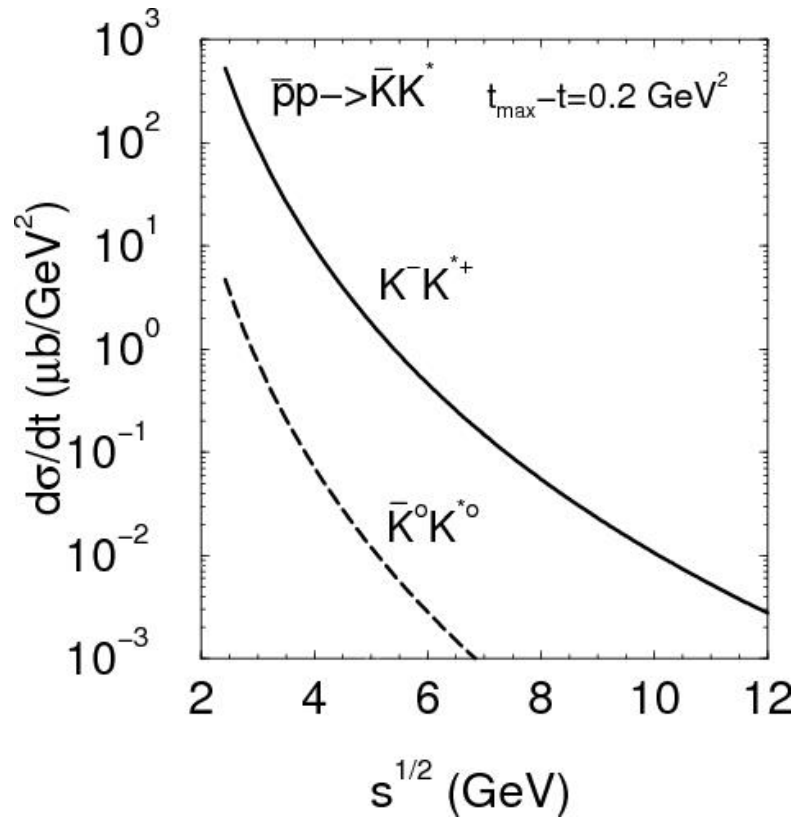
Phys. Rev. C78,025291 (2008)



A. Khodjamirian, Ch. Klein, Th. Mannel, and Y.-M. Wang<sup>a</sup>

Eur. Phys. J.A48, 31(2012)

# Reaction $\bar{p}p \rightarrow \bar{K} K^*$

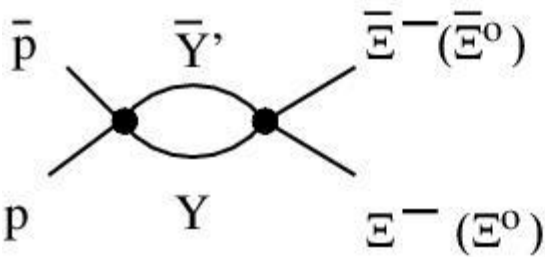


$$d\sigma^{KK^*} \simeq (2 \div 3) d\sigma^{KK}$$

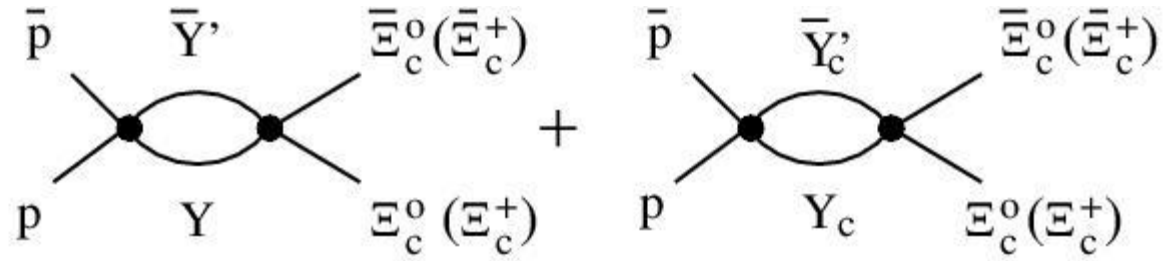
$$\frac{\text{charm}}{\text{strangeness}} \sim 10^{-3} \dots 10^{-4} \dots$$



# Double flavor exchange: $\Xi_c \Xi_c$ in $\bar{p}p$ collisions



a

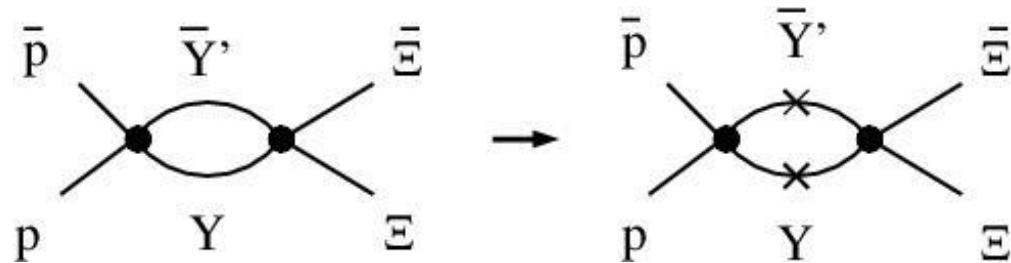


$Y = \Lambda, \Sigma^{0,+}$

b

$Y_c = \Lambda_c^+, \Sigma_c^{+,++}$

Cut (pole) diagrams

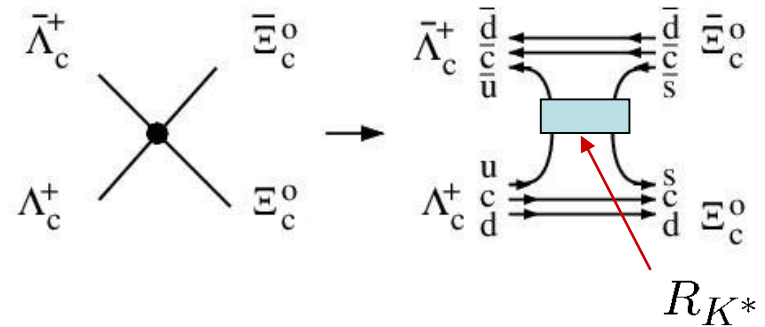
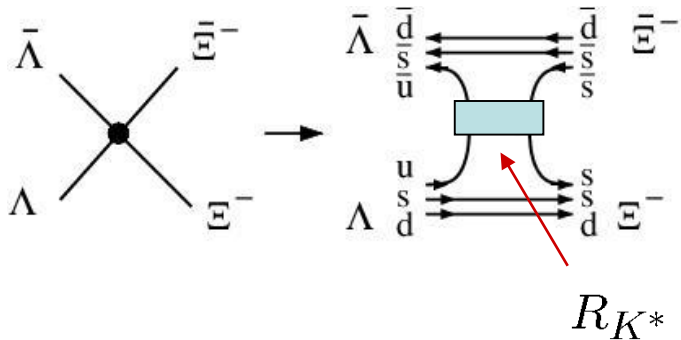


Cutkosky cutting rule

$$T^{\bar{p}p \rightarrow \Xi_c \Xi_c} \simeq T_{\text{cut}}^{\bar{p}p \rightarrow \Xi_c \Xi_c}$$

$$= -i \frac{\sqrt{1 - 4M_Y^2/s}}{16\pi} \int \frac{d\Omega_Y}{4\pi} \sum_{\text{spins } \bar{Y}'Y} T^{\bar{p}p \rightarrow \bar{Y}'Y} T^{\bar{Y}'Y \rightarrow \Xi_c \Xi_c}$$

# The vertex amplitudes: “effective region exchange”



The amplitude of  $\bar{p}p \rightarrow \bar{Y}'Y \rightarrow \Xi^0\Xi^0$  transition is a coherent sum with

$$\bar{Y}'Y = \bar{\Lambda}\Lambda, \bar{\Sigma}^0\Sigma^0, \bar{\Sigma}^+\Sigma^+, \bar{\Sigma}^0\Lambda, \bar{\Lambda}\Sigma^0$$

intermediate states

SU(3) predicts

$$g_{K^*\Lambda\Xi^0} * g_{K^*\Sigma^0\Xi^0} < 0$$

$$T^{\bar{p}p \rightarrow \Xi^0\Xi^0} = g_\Lambda^4 \left( 1 + \frac{1}{9} + \frac{4}{9} - \frac{2}{3} \right) T_0 = \frac{8}{9} g_\Lambda^4 \underline{T_0}$$

coupling constant  
independent amplitude

for  $\bar{p}p \rightarrow \bar{Y}'Y \rightarrow \Xi^-\Xi^-$ , one has  $\bar{Y}'Y = \bar{\Lambda}\Lambda, \bar{\Sigma}^0\Sigma^0, \bar{\Sigma}^0\Lambda, \bar{\Lambda}\Sigma^0$

$$[g_{K^*\Lambda\Xi^-} * g_{K^*\Sigma^0\Xi^-}] > 0$$

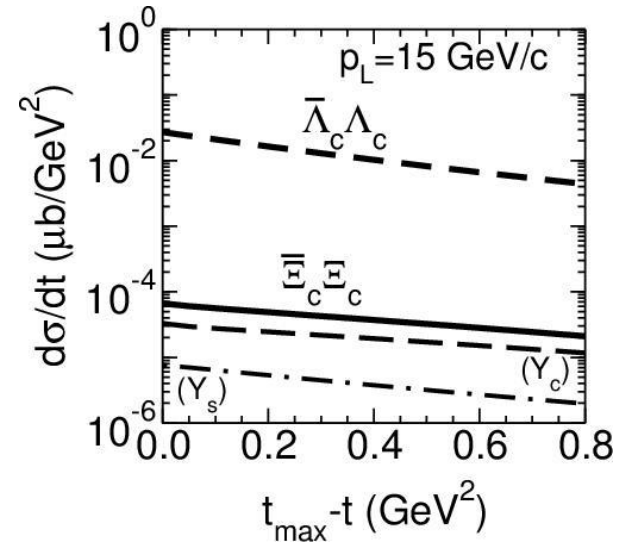
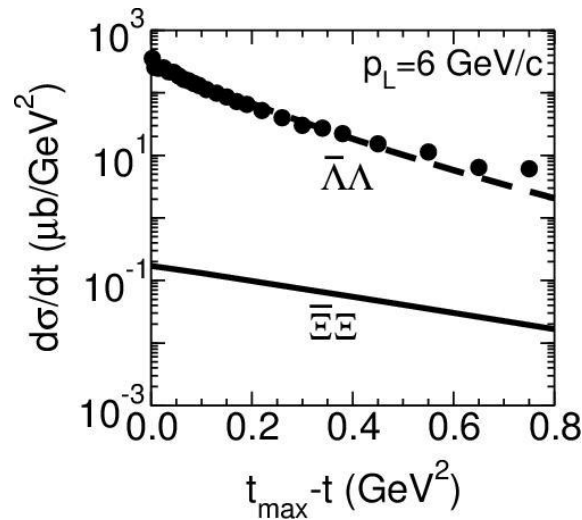
the ratio of cross sections  
looks as

$$\frac{\sigma^{\bar{p}p \rightarrow \Xi^-\Xi^-}}{\sigma^{\bar{p}p \rightarrow \Xi^0\Xi^0}} \simeq \frac{\sigma^{\bar{p}p \rightarrow \Xi_c^0\Xi_c^0}}{\sigma^{\bar{p}p \rightarrow \Xi_c^+\Xi_c^+}} \simeq 4.$$

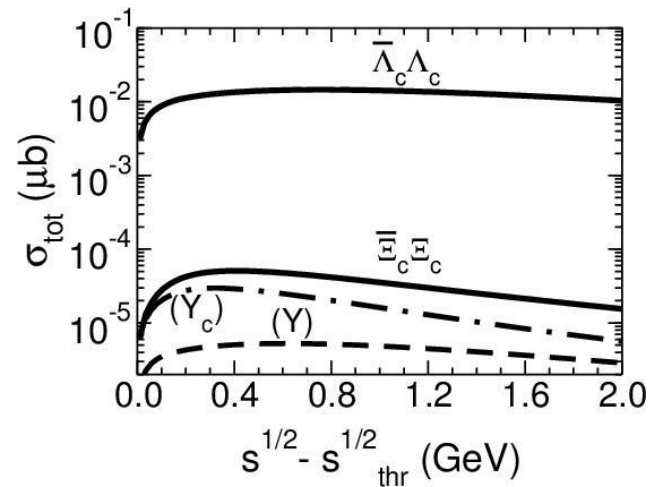
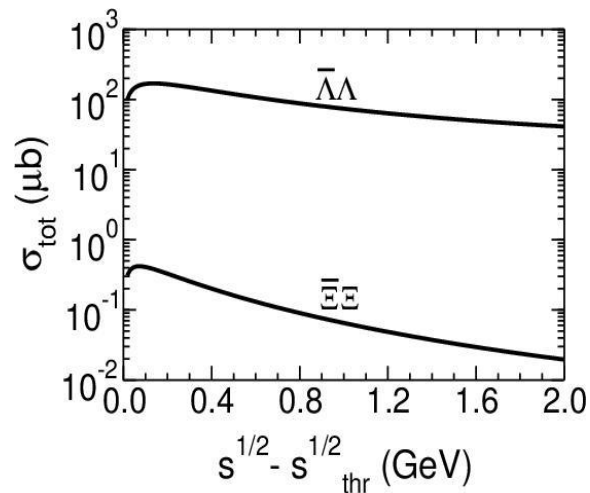
$$\Xi^- \text{ and } \Xi_c^0$$

# Cross sections

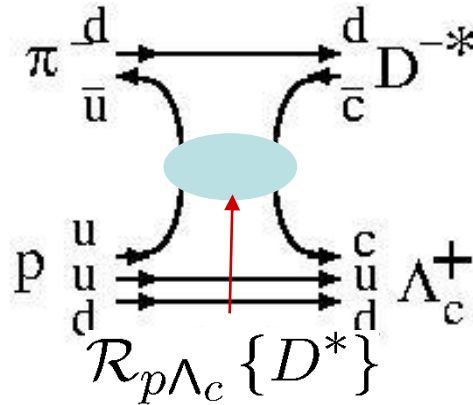
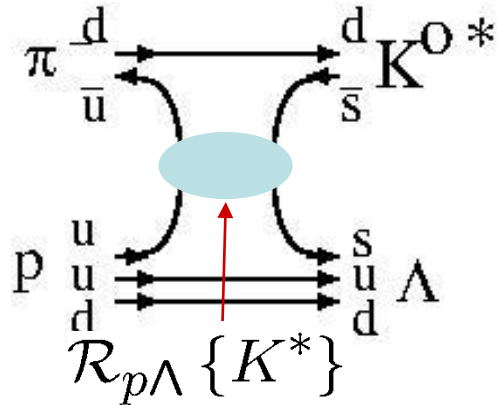
*differential*



*total*



**Exclusive**  $\pi p \rightarrow M^* \Lambda$ ;  $M^* = K^{0,*}, D^{-,*}$  **reactions**



$$T^{\pi p \rightarrow \Lambda M^*} \simeq g_0^2 \frac{s}{\bar{s}} \Gamma(1 - \alpha_{\mathcal{R}_{p\Lambda(\Lambda_c)}}(t)) \left( \frac{s}{s_0 \mathcal{R}} \right)^{2(\alpha_{\mathcal{R}_{p\Lambda(\Lambda_c)}}(t) - 1)}$$

$$\alpha_{\mathcal{R}_{p\Lambda_c}}(t) = 0.414 + 0.71t$$

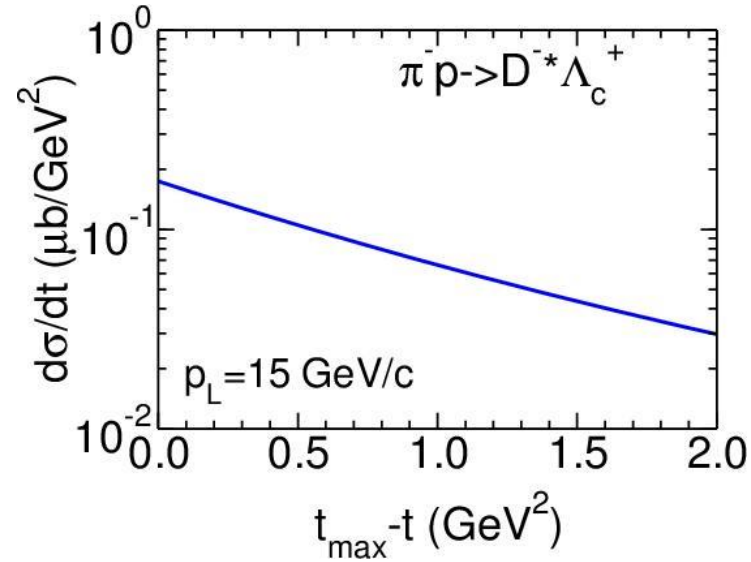
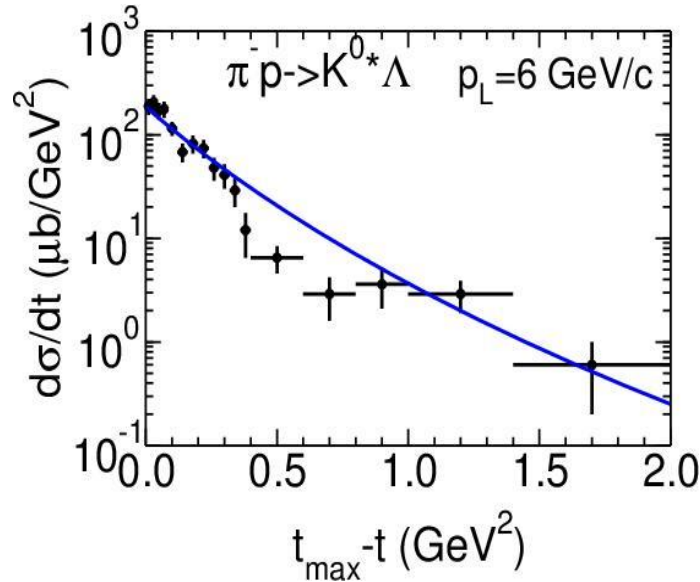
$$\alpha_{\mathcal{R}_{p\Lambda_c}}(t) = -1.02 + 0.47t$$

$$s^{\mathcal{R}_{p\Lambda}} \simeq 1.59 \text{ GeV}^2$$

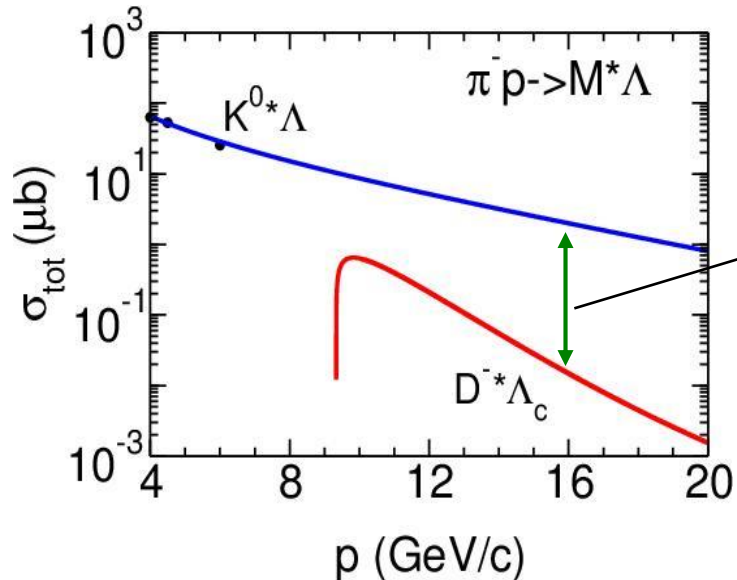
$$s^{\mathcal{R}_{p\Lambda_c}} \simeq 4.75 \text{ GeV}^2$$

$$\frac{g_0^2}{4\pi} \simeq 0.8, \quad \bar{s} \simeq 1 \text{ GeV}^2$$

## Differential cross sections



## Total cross sections

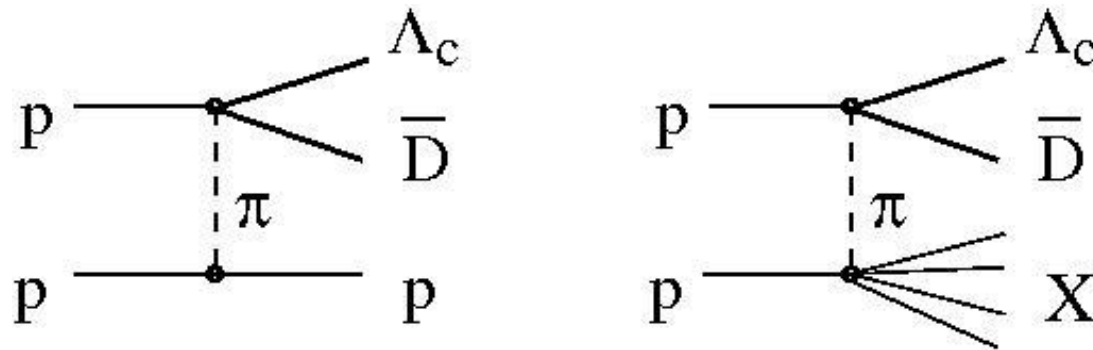


[cf. K. Boreskov, A.Kaidalov, Sov.J. Nucl.Phys. 37 (1982)]

$$\frac{c}{s} \simeq 10^{-2 \dots -3} \text{ vs. } \frac{c}{s} \simeq 10^{-6}$$

[cf. V. Barger, R.Phillips, PRD 12 (1975)]

# Reactions $pp \rightarrow \Lambda_c \bar{D} p$ and $pp \rightarrow \Lambda_c \bar{D} X$



$$d\sigma^{pp \rightarrow \Lambda_c \bar{D} p(X)} \sim \frac{d\sigma^{\pi p \rightarrow \Lambda_c \bar{D}}}{dt} \otimes \sigma_{\text{tot}}^{\pi N} d[PS]$$

For high energy cf. K. Boreskov, A.Kaidalov, Sov.J. Nucl.Phys. 37 (1982)

**For J-PARC energies our work is in a progress**

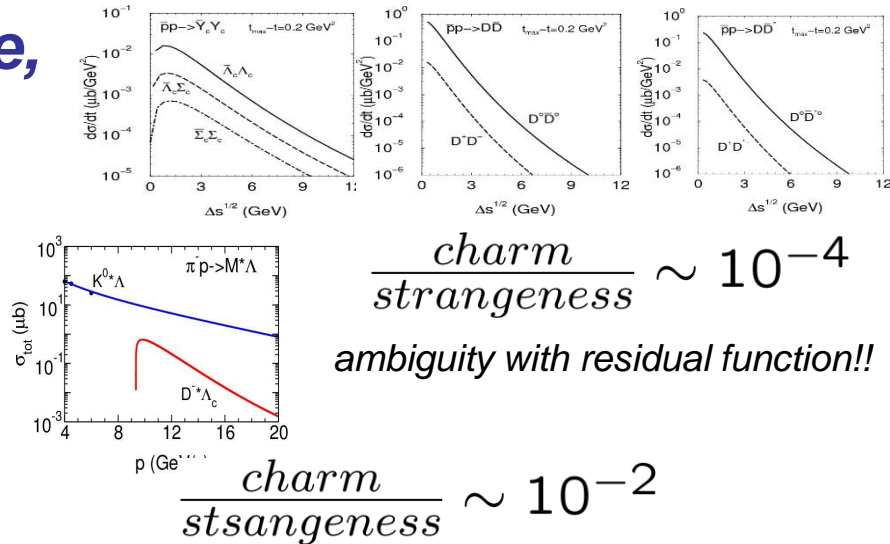
# Summary

★ We have evaluated the cross sections for  $\bar{p}p \rightarrow \bar{Y}_c Y_c, D\bar{D}, D^*\bar{D}, \dots$  reactions, including double flavor exchange,

★ and for  $\pi p \rightarrow D^* \Lambda_c$  reactions at  $E_{\text{lab}} \leq 20$  GeV

★ This result may be used for design of PANDA detector and “charm” program at JPARC

★ And for further development of the theoretical approaches in “charmed physics”





**THE END**

*Thank you very much for attention !*

# BACKUP

## Longitudinal asymmetries

$$\mathcal{A}(s, t) = \frac{d\sigma^A - d\sigma^P}{d\sigma^A + d\sigma^P},$$

*where*  $d\sigma^A \equiv d\sigma^{\leftrightarrow} \quad d\sigma^P \equiv d\sigma^{\rightarrow}$

**Polarized Antiproton EXperiment (PAX)**

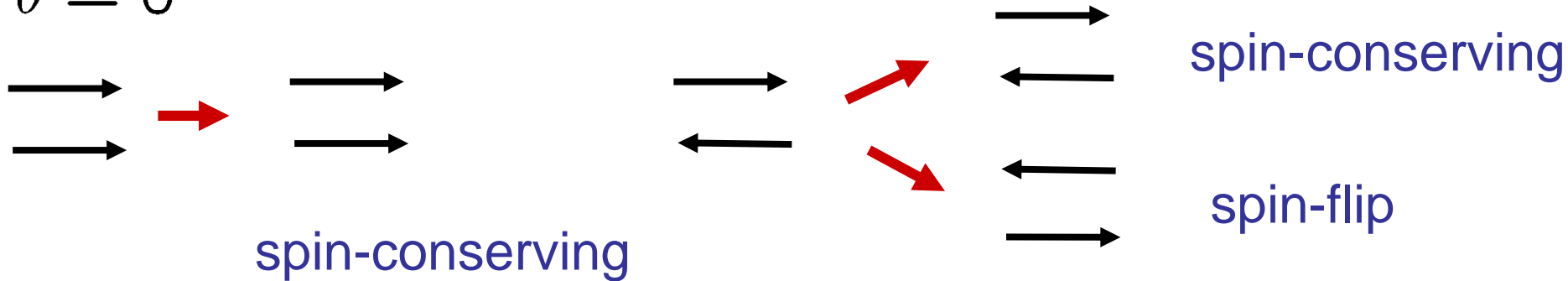
<http://www.fz-juelich.de/ikp/pax/>

# Longitudinal asymmetry

$$\mathcal{A} = \frac{d\sigma^A - d\sigma^P}{d\sigma^A + d\sigma^P},$$

$$\begin{aligned} d\sigma^A &\equiv d\sigma^{\leftrightarrow} \\ d\sigma^P &\equiv d\sigma^{\Rightarrow} \end{aligned}$$

$$\theta = 0$$



$$\begin{aligned} T_{m_f n_f; m_i, n_i} &\sim A(s) \delta_{m_i m_f} \delta_{n_i n_f} \\ &+ \frac{1}{\sqrt{2}} B(s) (1 - 4m_i m_f) \delta_{-m_i m_f} \delta_{-n_i n_f} \end{aligned}$$

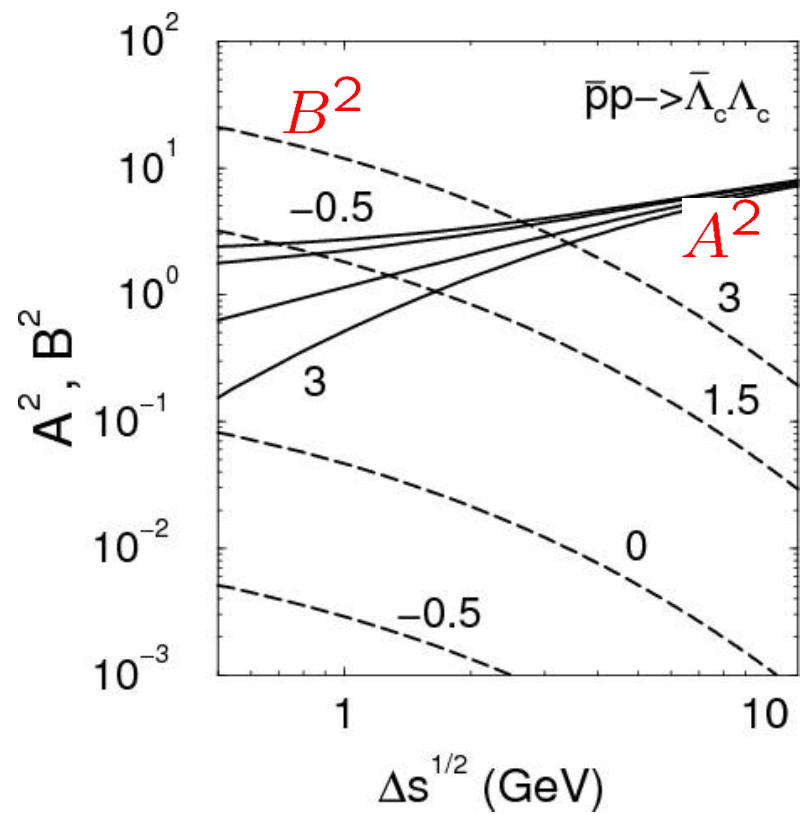
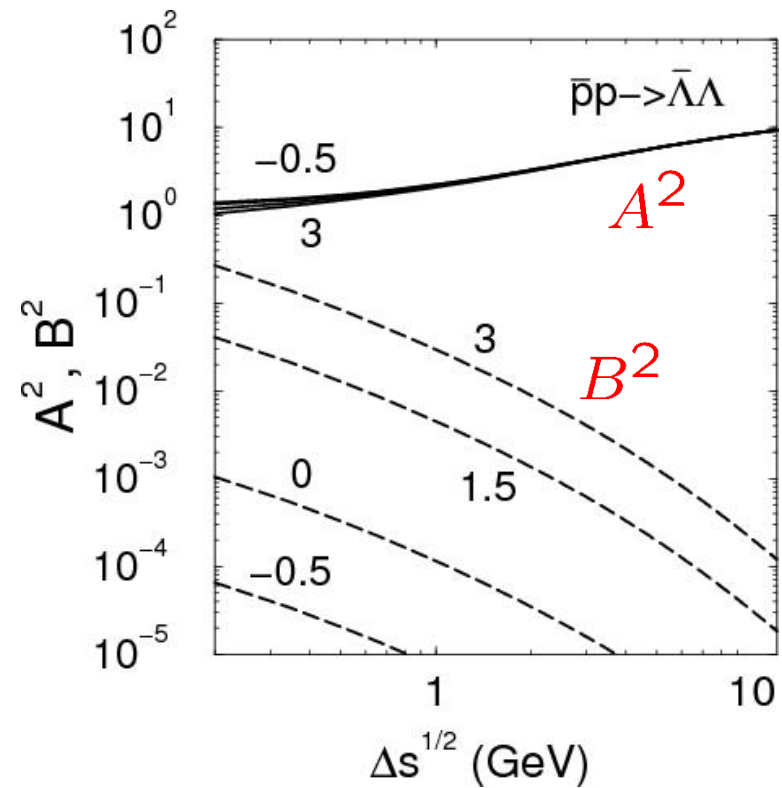
$$\mathcal{A} = \frac{B^2(s)}{A^2(s) + B^2(s)}$$

# Structure of spin-flip amplitude

$$\begin{array}{c} \bar{p} \qquad \bar{Y} \\ \hline \quad \quad \quad \text{---} K^* \text{---} \\ \hline p \qquad Y \end{array}$$

$$B(s) = -\sqrt{2} \left( (1 + \kappa) \left( \frac{\mathbf{p}_p}{E + M_N} - \frac{\mathbf{p}_Y}{E + M_Y} \right) \right)^2$$

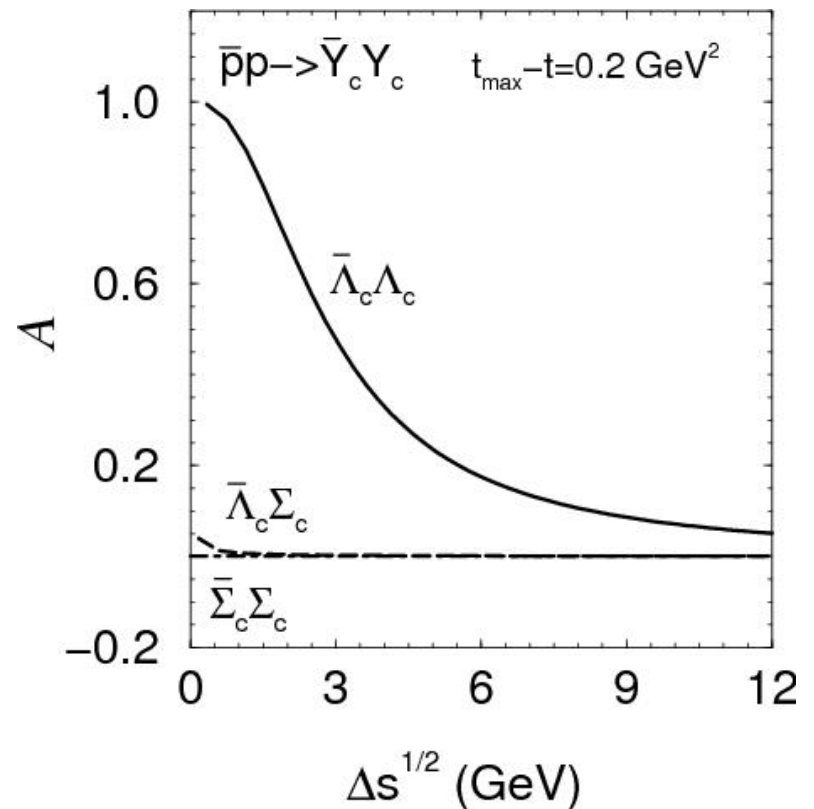
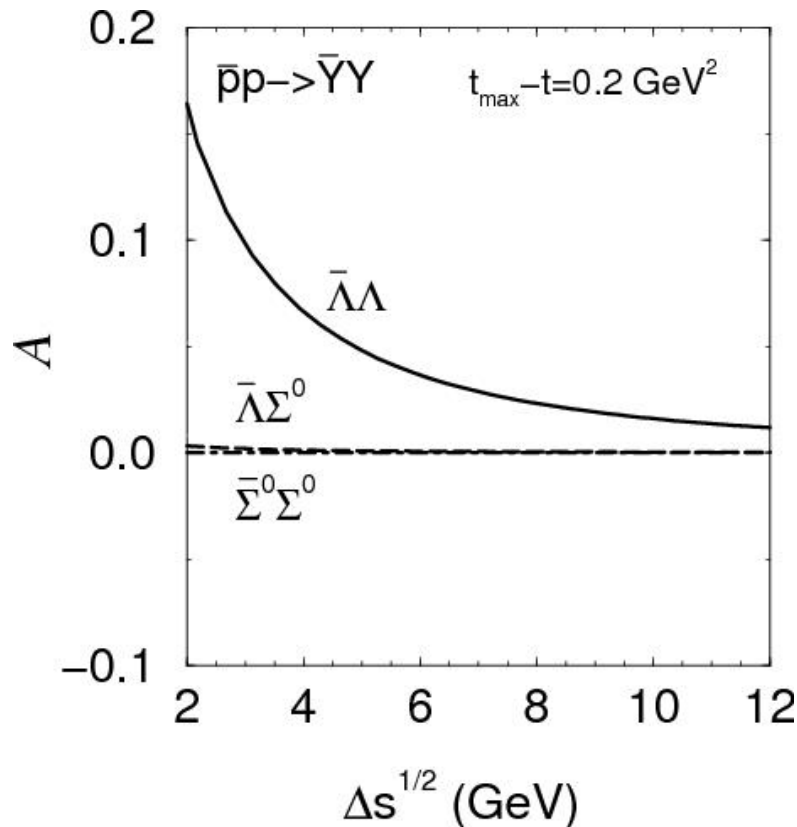
$$\mathcal{A} = \frac{B^2(s)}{A^2(s) + B^2(s)}$$



# Asymmetry

# *s*-dependence

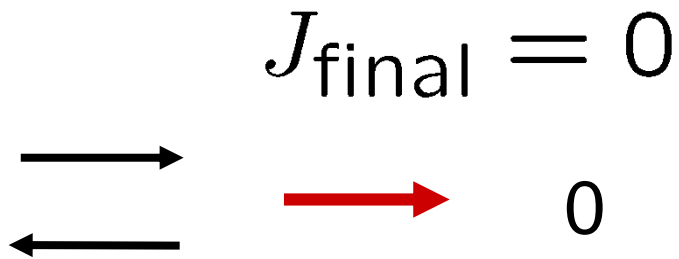
Reaction  $\bar{p}p \rightarrow \bar{Y}Y$  ,  $Y = \Lambda, \Lambda_c^+, \Sigma^0, \Sigma_c^+$



# Longitudinal asymmetry

$$\bar{p}p \rightarrow \bar{K}K (D\bar{D})$$

$$\theta = 0$$


$$J_{\text{final}} = 0$$

$$\mathcal{A} = \frac{d\sigma^A - d\sigma^P}{d\sigma^A + d\sigma^P},$$

$$d\sigma^P \equiv d\sigma^{\vec{0}} \simeq 0$$

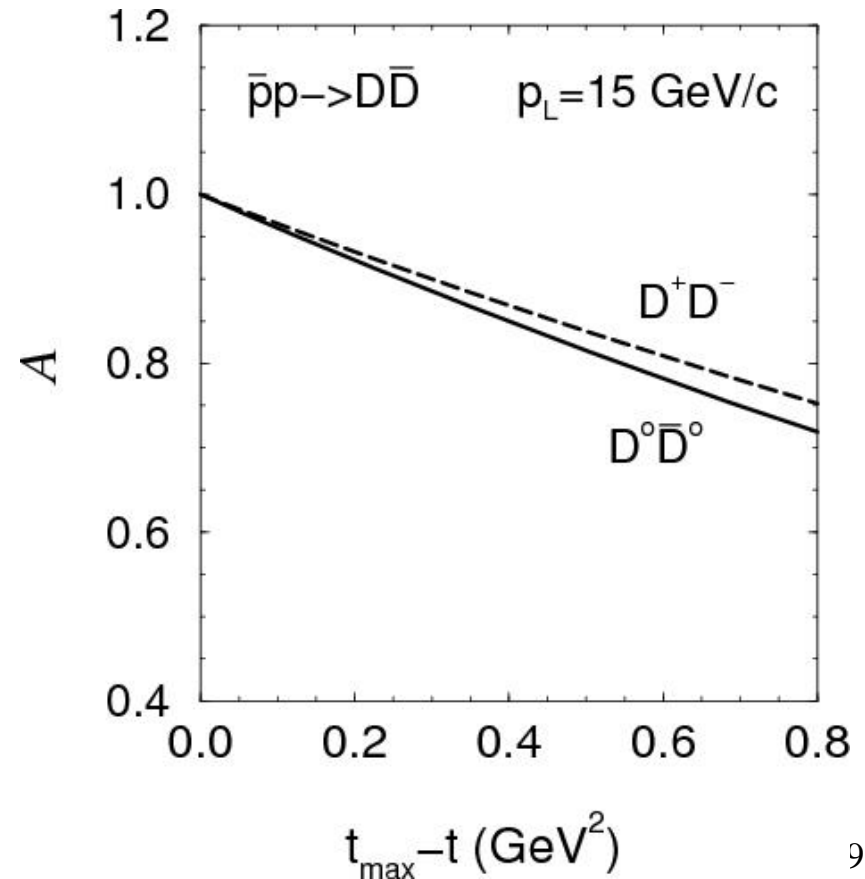
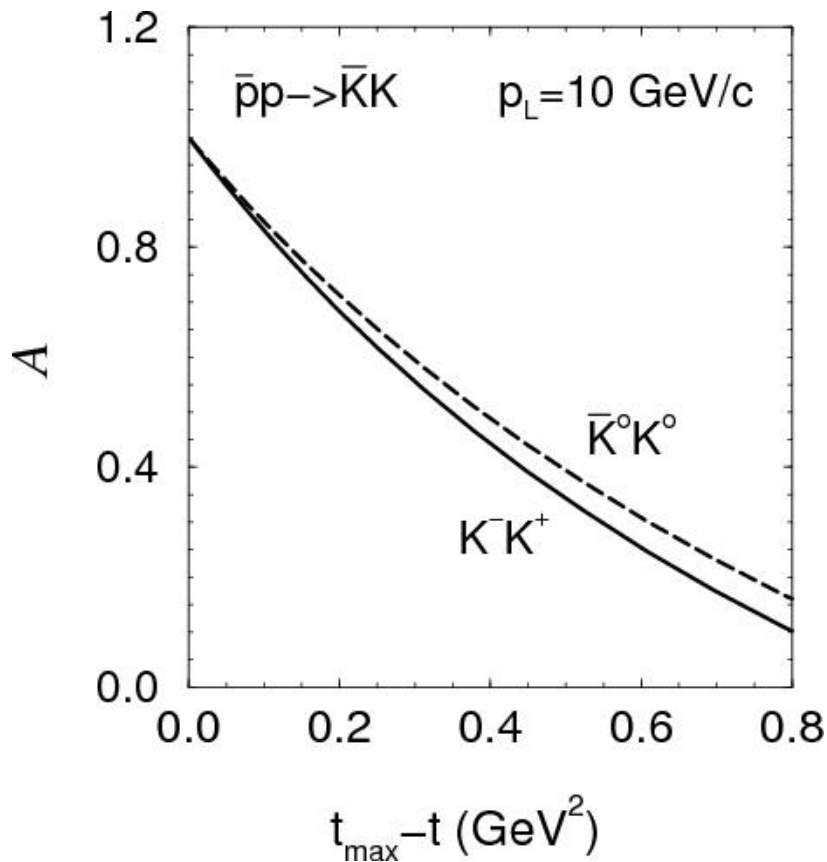
$$\mathcal{A} \simeq 1$$



# Asymmetry

# $t$ -dependence

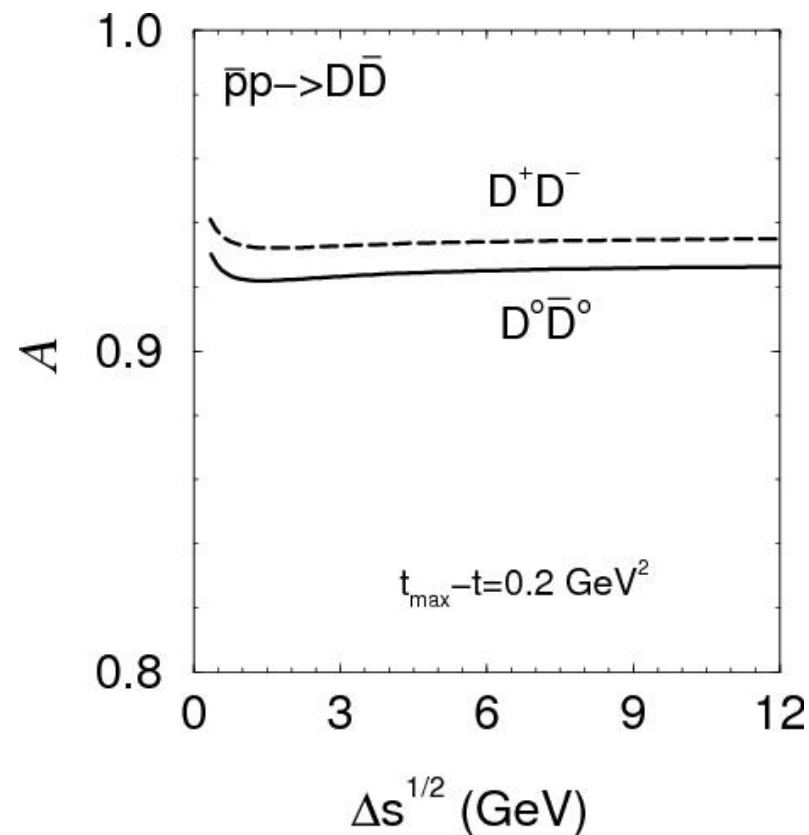
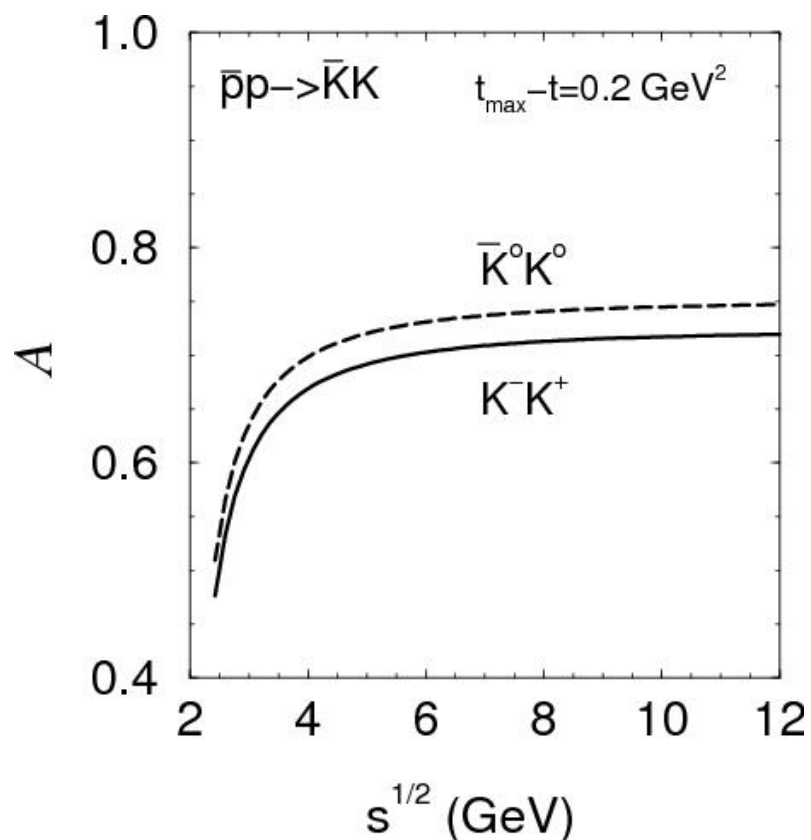
Reactions  $\bar{p}p \rightarrow \bar{K}K, D\bar{D}$



# Asymmetry

# $s$ -dependence

Reactions  $\bar{p}p \rightarrow \bar{K}K, D\bar{D}$



# Longitudinal asymmetry

$$\bar{p}p \rightarrow \bar{K} K^* \quad \text{pure vector coupling!!!}$$

$$\theta = 0 \quad s_f = 1, \lambda_V = 1, 0$$

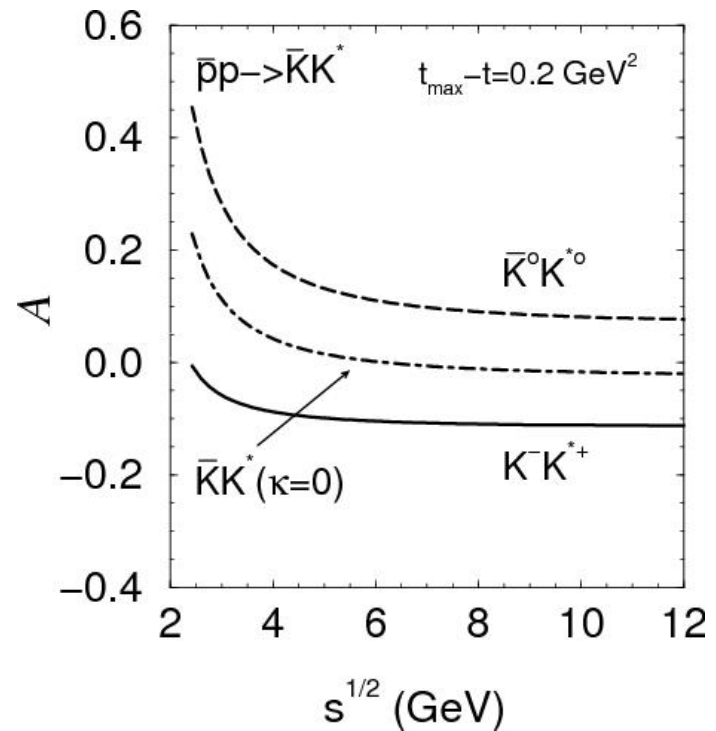
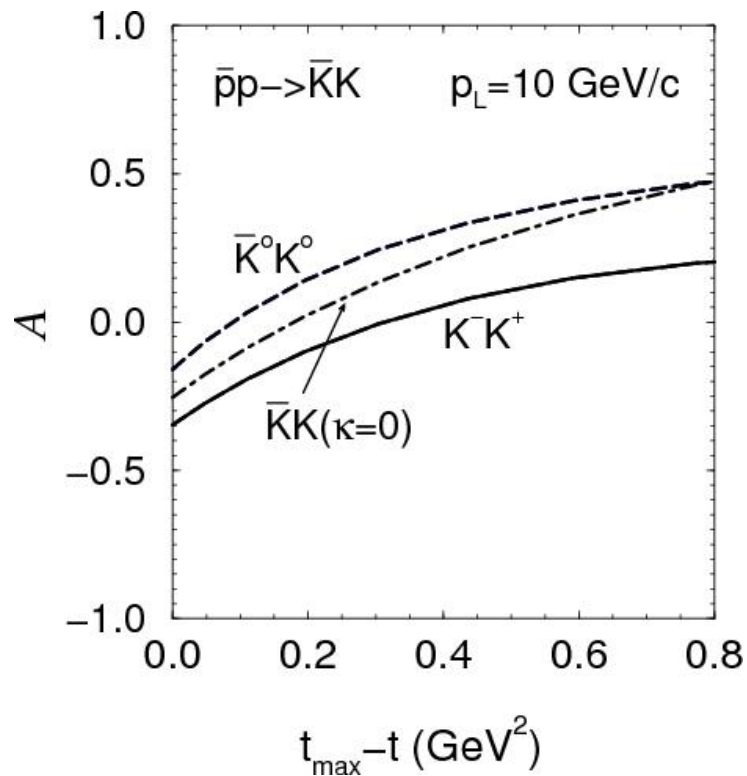
$$T_{\lambda_i; m_i, n_i} \sim \left( A \delta_{m_i n_i} + B \delta_{-m_i n_i} \right) \delta_{\lambda_i \lambda_V} ,$$

$$\lambda_i = m_i + n_i$$

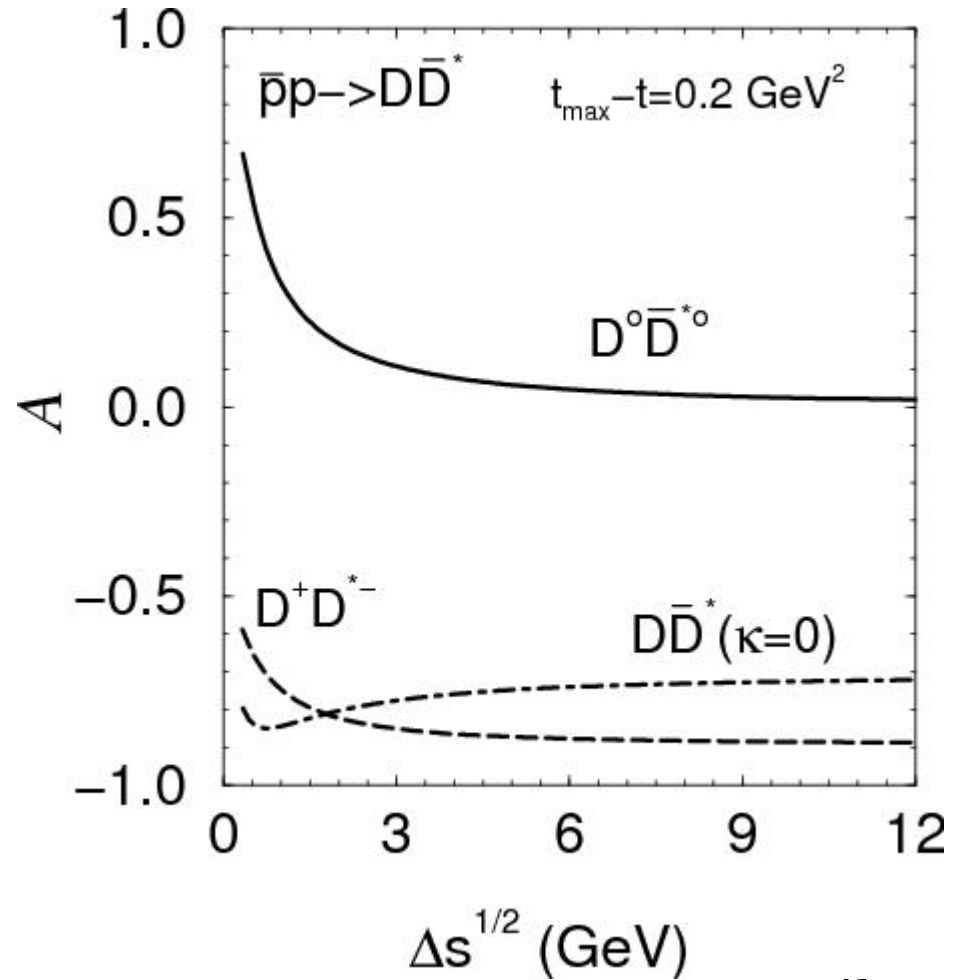
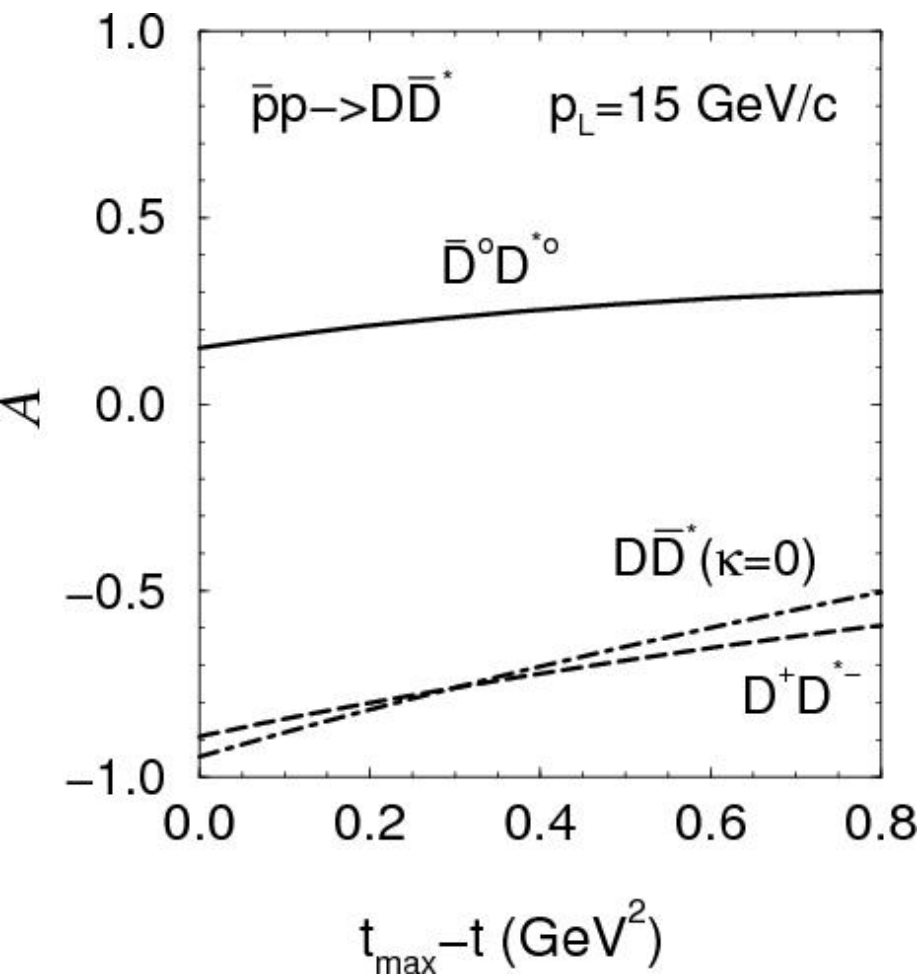
$$A \simeq \sqrt{2}, \quad B \simeq \frac{M_N}{M_V} ,$$

$$\mathcal{A} = \frac{M_N^2 - 2M_V^2}{M_N^2 + 2M_V^2} \begin{array}{l} \nearrow \sim -0.3 (\bar{K} K^*) \\ \searrow \sim -0.8 (D \bar{D}^*) \end{array}$$

# Reaction $\bar{p}p \rightarrow \bar{K}K^*$



# Reaction $\bar{p}p \rightarrow D\bar{D}^*$





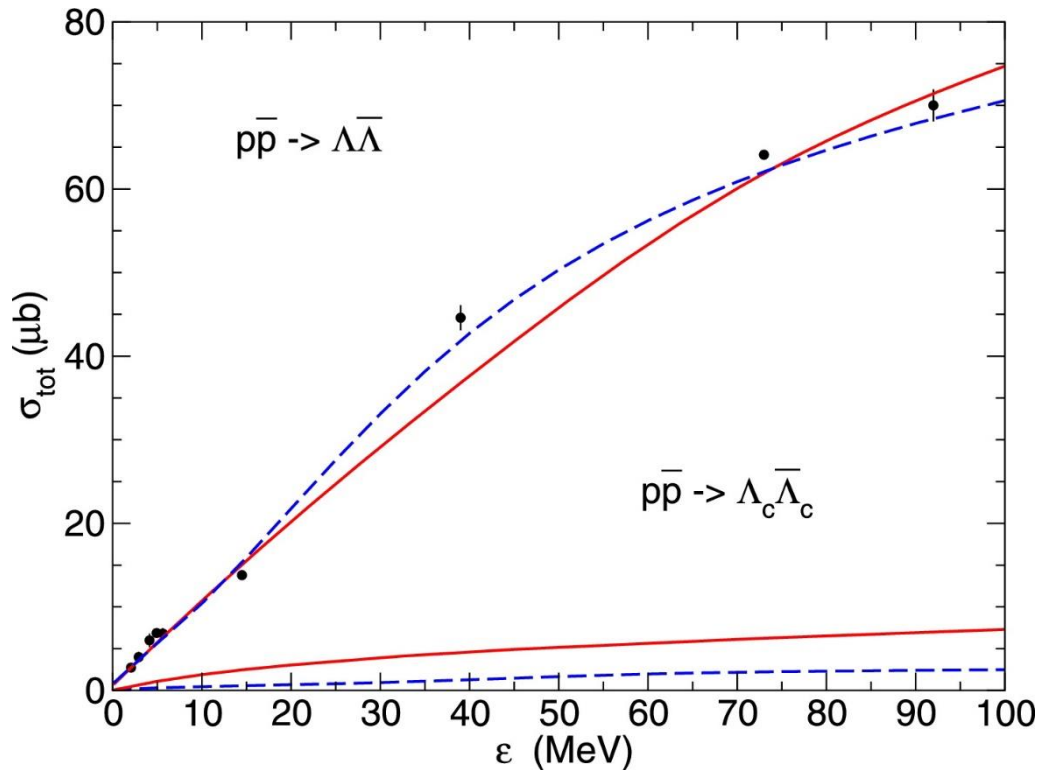


Fig. 2. Total reaction cross sections for  $\bar{p}p \rightarrow \bar{\Lambda}\Lambda$  and  $\bar{p}p \rightarrow \bar{\Lambda}_c\Lambda_c^+$  as a function of the excess energy  $\epsilon$ . The results for  $\bar{p}p \rightarrow \bar{\Lambda}\Lambda$  (upper curves) are taken from our work [7]. The solid curves are results for the meson-exchange transition potential while the dashed curves correspond to quark-gluon dynamics. The  $\bar{p}p \rightarrow \bar{\Lambda}_c\Lambda_c^+$  results are obtained with the  $\bar{p}p$  interaction C.

$$\frac{d\sigma}{d\Omega} = \frac{1}{64\pi^2} C(s, M_\Lambda) |T(s, M_\Lambda)|^2 ,$$

$$\sim |1/(t - M_V^2)|^2$$

$$-t_s = 0.22 \dots 0.50$$

$$-t_c = 3.54 \dots 5.33$$

$$\frac{d\sigma^s}{d\sigma^c} \simeq 9.8 \times 54.4 \simeq 530$$

$$\frac{\text{charm}}{\text{strangeness}} \simeq 2 \cdot 10^{-4}$$



TABLE I. Parameters of the vector meson trajectories of the form (8). The intercept of the  $\rho$  trajectory was taken as an input.

	$\rho$	$K^*$	$\phi$	
$\alpha(0)$	0.55	$0.414 \pm 0.006$	$0.27 \pm 0.01$	
$\sqrt{T}$ , GeV	$2.46 \pm 0.03$	$2.58 \pm 0.03$	$2.70 \pm 0.07$	
	$D^*$	$D_s^*$	$J/\psi$	
$\alpha(0)$	$-1.02 \pm 0.05$	$-1.16 \pm 0.05$	$-2.60 \pm 0.10$	
$\sqrt{T}$ , GeV	$3.91 \pm 0.02$	$4.03 \pm 0.04$	$5.36 \pm 0.05$	
	$B^*$	$B_s^*$	$B_c^*$	$Y$
$\alpha(0)$	$-7.13 \pm 0.17$	$-7.27 \pm 0.17$	$-8.70 \pm 0.18$	$-14.81 \pm 0.35$
$\sqrt{T}$ , GeV	$7.48 \pm 0.02$	$7.60 \pm 0.04$	$8.93 \pm 0.03$	$12.50 \pm 0.02$

TABLE V. Parameters of the pseudoscalar meson trajectories of the form (8). (The parameters for the  $\underline{K}$  trajectory were found using the mass of  $K_2$  from [29]. If we instead use a mass of the corresponding *pure ns* state as found in Ref. [46], i.e.,  $M_{K_2} = 1762 \pm 18$  GeV, the parameters change slightly: the intercept  $-0.153 \pm 0.003$ , and the threshold  $2.93 \pm 0.07$  GeV.)

	$\pi$	$K$	$\eta_s$	
$\alpha(0)$	$-0.0118 \pm 0.0001$	$-0.151 \pm 0.001$	$-0.291 \pm 0.003$	
$\sqrt{T}$ , GeV	$2.82 \pm 0.05$	$2.96 \pm 0.05$	$3.10 \pm 0.11$	
	$D$	$D_s$	$\eta_c$	
$\alpha(0)$	$-1.61105 \pm 0.00005$	$-1.751 \pm 0.001$	$-3.2103 \pm 0.0001$	
$\sqrt{T}$ , GeV	$4.16 \pm 0.03$	$4.29 \pm 0.06$	$5.49 \pm 0.02$	
	$B$	$B_s$	$B_c$	$\eta_c$
$\alpha(0)$	$-7.41 \pm 0.17$	$-7.54 \pm 0.17$	$9.00 \pm 0.17$	$-14.80 \pm 0.34$
$\sqrt{T}$ , GeV	$7.89 \pm 0.16$	$8.01 \pm 0.16$	$9.24 \pm 0.12$	$12.98 \pm 0.24$

TABLE II. Comparison of the masses of the spin-1, spin-3 and spin-5 states given by ten vector meson trajectories of the form (8) with data. All masses are in MeV.

	$J=1$		$J=3$		$J=5$	
	This work	Ref. [29]	This work	Ref. [29]	This work	Ref. [29]
$\alpha_\rho(t)$	<b>769.0<math>\pm</math>0.9</b>	769.0 $\pm$ 0.9	<b>1688.8<math>\pm</math>2.1</b>	1688.8 $\pm$ 2.1	2124 $\pm$ 19	
$\alpha_{K^*}(t)$	<b>896.1<math>\pm</math>0.3</b>	896.1 $\pm$ 0.3	<b>1776<math>\pm</math>7</b>	1776 $\pm$ 7	2215 $\pm$ 21	
$\alpha_\phi(t)$	1015 $\pm$ 17	1019.4	1863 $\pm$ 31	1854 $\pm$ 7	2305 $\pm$ 42	
$\alpha_{D^*}(t)$	<b>2006.7<math>\pm</math>0.5</b>	2006.7 $\pm$ 0.5	2721 $\pm$ 23		3191 $\pm$ 22	
$\alpha_{D_s^*}(t)$	2102 $\pm$ 29	2106.6 $\pm$ 2.1 $\pm$ 2.7	2808 $\pm$ 28		3279 $\pm$ 30	
$\alpha_{J/\psi}(t)$	<b>3096.9</b>	3096.9	3753 $\pm$ 41		4240 $\pm$ 39	
$\alpha_{B^*}(t)$	<b>5324.9<math>\pm</math>1.8</b>	5324.9 $\pm$ 1.8	5814 $\pm$ 51		6217 $\pm$ 46	
$\alpha_{B_s^*}(t)$	5411 $\pm$ 58	5416.3 $\pm$ 3.3	5901 $\pm$ 53		6306 $\pm$ 49	
$\alpha_{B_c^*}(t)$	6356 $\pm$ 80		6853 $\pm$ 72		7276 $\pm$ 65	
$\alpha_Y(t)$	<b>9460.4<math>\pm</math>0.2</b>	9460.4 $\pm$ 0.2	9906 $\pm$ 91		10304 $\pm$ 84	

TABLE VI. Comparison of the masses of the spin-0, spin-2 and spin-4 states given by ten pseudoscalar meson trajectories of the form (8) with data. (We take the error estimate on the  $\eta_b$  mass as 10% of the calculated splitting, in agreement with Fig. 2 of the second paper of Ref. [45].) All masses are in MeV.

	$J=0$		$J=2$		$J=4$	
	This work	Ref. [29]	This work	Ref. [29]	This work	Ref. [29]
$\alpha_\pi(t)$	<b>135</b>	135	<b>1677<math>\pm</math>8</b>	1677 $\pm$ 8	2237 $\pm$ 26	
$\alpha_K(t)$	<b>493.7</b>	493.7	<b>1773<math>\pm</math>8</b>	1773 $\pm$ 8	2333 $\pm$ 27	
$\alpha_{\eta_s}$	698 $\pm$ 14		1869 $\pm$ 38	1854 $\pm$ 20	2429 $\pm$ 54	
$\alpha_{D^*}(t)$	<b>1864.1<math>\pm</math>1.0</b>	1864.1 $\pm$ 1.0	2692 $\pm$ 19		3228 $\pm$ 22	
$\alpha_{D_s^*}(t)$	1971 $\pm$ 19	1969.0 $\pm$ 1.4	2786 $\pm$ 26		3323 $\pm$ 32	
$\alpha_{\eta_c}(t)$	<b>2979.8<math>\pm</math>2.1</b>	2979.8 $\pm$ 2.1	3692 $\pm$ 23		4217 $\pm$ 25	
$\alpha_B(t)$	<b>5279.8<math>\pm</math>1.6</b>	5279.8 $\pm$ 1.6	5830 $\pm$ 89		6286 $\pm$ 93	
$\alpha_{B_s}(t)$	<b>5369.6<math>\pm</math>2.4</b>	5369.6 $\pm$ 2.4	5920 $\pm$ 89		6376 $\pm$ 93	
$\alpha_{B_c}(t)$	6283 $\pm$ 79		6826 $\pm$ 79		7287 $\pm$ 80	
$\alpha_{\eta_b}(t)$	<b>9424<math>\pm</math>3.6</b>		9914 $\pm$ 148		10353 $\pm$ 150	

